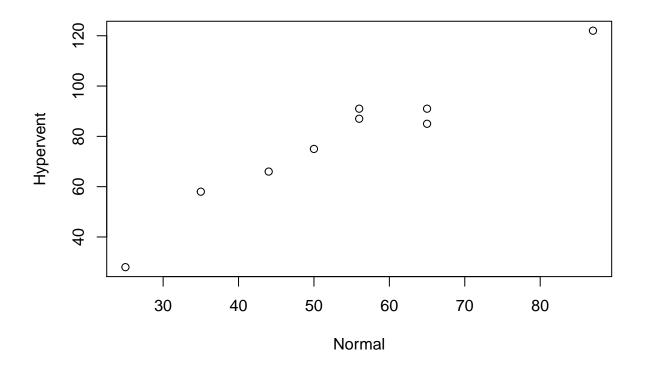
#### Statistical programming in R (part 1)

0. Summary statistics Calculate mean, median, variance, standard deviation, quantile

```
library(Stat2Data)
data(BirdNest)
mean(BirdNest$Totcare, na.rm = T)
## [1] 27.73494
median(BirdNest$Totcare, na.rm = T)
## [1] 27.5
var(BirdNest$Totcare, na.rm = T)
## [1] 23.3862
sd(BirdNest$Totcare, na.rm = T)
## [1] 4.835928
quantile(BirdNest$Totcare, probs = seq(0,
   1, 0.25), na.rm = T)
    0% 25% 50% 75% 100%
## 19.0 23.5 27.5 31.0 37.5
IQR(BirdNest$Totcare, na.rm = T)
## [1] 7.5
```

1. Pearson Correlation Pearson correlation is a statistic that measures linear correlation between two variables, given the assumption that the sample pairs are independent and follow a bivariate normal distribution.

```
# Nine students held their
# breath, once after breathing
# normally and relaxing for one
# minute, and once after
# hyperventilating for one
# minute. The table indicates
# how long (in sec) they were
```



```
cor(Normal, Hypervent, method = "pearson")

## [1] 0.9661943

cor.test(Normal, Hypervent, method = "pearson")

##

## Pearson's product-moment correlation

##

## data: Normal and Hypervent

## t = 9.9153, df = 7, p-value = 2.263e-05

## alternative hypothesis: true correlation is not equal to 0

## 95 percent confidence interval:

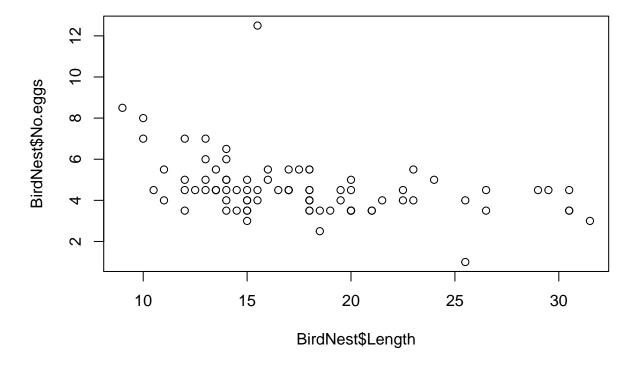
## 0.8430028 0.9930835
```

```
## sample estimates:
## cor
## 0.9661943
```

source

2. Spearman's rank correlation coefficient Spearman's rank 's correlation coefficient is a nonparametric measure of rank correlation (statistical dependence between the rankings of two variables). It assesses how well the relationship between two variables can be described using a monotonic function. (Wiki)

```
plot(BirdNest$Length, BirdNest$No.eggs)
```



```
cor(BirdNest$Length, BirdNest$No.eggs,
  method = "spearman")
```

## [1] -0.4481381

```
cor.test(BirdNest$Length, BirdNest$No.eggs,
  method = "spearman", exact = T)
```

```
## Warning in cor.test.default(BirdNest$Length, BirdNest$No.eggs, method =
## "spearman", : Cannot compute exact p-value with ties
```

```
##
## Spearman's rank correlation rho
##
## data: BirdNest$Length and BirdNest$No.eggs
## S = 143033, p-value = 1.914e-05
## alternative hypothesis: true rho is not equal to 0
## sample estimates:
## rho
## -0.4481381
```

- Read about Kendall Tau coefficient
- **3.** Cramer's V Cramer's V is a measure of association between two nominal variables, returns a value between 0 and 1.

Recall that in the BirdNest data, egg color encoded as (0=plain/solid or 1=speckled/spotted) and closed encoded as 1=closed nest (pendant, spherical, cavity, crevice, burrow) or 0=open nest (saucer, cup).

```
# install.packages('rcompanion')
library(rcompanion)
cramerV(BirdNest$Closed., BirdNest$Color)

## Cramer V
## 0.0342

cramerV(BirdNest$Closed., BirdNest$Location)

## Cramer V
## 0.5842

cramerV(BirdNest$Closed., BirdNest$Nesttype)

## Cramer V
## 1
```

**4.** Compare the means of two groups / multiple groups Two sample t-test is a parametric test for comparing the means of two groups. The null hypothesis is the mean of two groups are equal. Alternative hypothesis is that they are not equal. Significance level is set to 0.05. The process of perform a t-test in R could be found at source.

A useful source to look up statistical analysis about their assumption, interpretation and how to perform in different software is: http://rcompanion.org/rcompanion/b\_07.html You may check out more about paired or unpaired t-test, comparing the means of more than two groups using Analysis of Variance (ANOVA) or nonparametric test for comparing means of two groups (Mann-Whitney U test) etc.

• create data for t-test

```
library(dplyr)

##
## Attaching package: 'dplyr'
```

```
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
t_test_data <- BirdNest %>% filter(Location %in%
    c("ground", "decid"))
group_by(t_test_data, Location) %>%
    summarise(count = n(), mean = mean(Totcare,
       na.rm = TRUE), sd = sd(Totcare,
       na.rm = TRUE))
## # A tibble: 2 x 4
   Location count mean
    <fct> <int> <dbl> <dbl>
## 1 decid
              24 29.3 3.36
## 2 ground
              19 23.6 2.92
  • visualize data
# install.packages('ggpubr')
library(ggpubr)
## Loading required package: ggplot2
ggboxplot(t_test_data, x = "Location",
   y = "Totcare", color = "Location",
   palette = c("#00AFBB", "#E7B800"),
   ylab = "Totcare", xlab = "Location")
```

## Warning: Removed 1 rows containing non-finite values (stat\_boxplot).

#### Location $\rightleftharpoons$ decid $\rightleftharpoons$ ground

```
30-
20-
decid ground
Location
```

```
# Shapiro-Wilk normality test
# for decid's Totcare
with(t_test_data, shapiro.test(Totcare[Location ==
    "decid"])) # p = 0.5101
##
##
   Shapiro-Wilk normality test
##
## data: Totcare[Location == "decid"]
## W = 0.96224, p-value = 0.5101
# Shapiro-Wilk normality test
# for ground's Totcare
with(t_test_data, shapiro.test(Totcare[Location ==
    "ground"])) # p = 0.1502
##
##
   Shapiro-Wilk normality test
```

• check equal variances

## data: Totcare[Location == "ground"]

## W = 0.92665, p-value = 0.1502

```
# F-test to test for
# homogeneity in variances
res.ftest <- var.test(Totcare ~
    Location, data = t_test_data) # p = 0.5472
res.ftest
##
## F test to compare two variances
## data: Totcare by Location
## F = 1.3266, num df = 22, denom df = 18, p-value = 0.5472
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 0.5246666 3.2186930
## sample estimates:
## ratio of variances
##
             1.326626
  • perform t-test
# t_test
res <- t.test(Totcare ~ Location,
   data = t_test_data, var.equal = TRUE)
res # p = 7.138e-07
##
## Two Sample t-test
##
## data: Totcare by Location
## t = 5.8726, df = 40, p-value = 7.138e-07
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.786512 7.760398
## sample estimates:
## mean in group decid mean in group ground
               29.32609
                                    23.55263
##
res$conf.int
## [1] 3.786512 7.760398
## attr(,"conf.level")
## [1] 0.95
  • Mann-whitney test
# Mann-Whitney test for
# (non-parametric)
wilcox.test(Totcare ~ Location,
   data = t_test_data, exact = F)
```

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: Totcare by Location
## W = 395.5, p-value = 7.61e-06
## alternative hypothesis: true location shift is not equal to 0
```

• ANOVA

```
## Df Sum Sq Mean Sq F value Pr(>F)
## Location   2  354.6  177.31  14.82 6.82e-06 ***
## Residuals   56  669.9  11.96
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## 1 observation deleted due to missingness
```

• nonparametric Kruskal-Wallis test

```
##
## Kruskal-Wallis rank sum test
##
## data: Totcare by Location
## Kruskal-Wallis chi-squared = 22.959, df = 2, p-value = 1.034e-05
```

Nonparametric test based on resampling: permutation test Read more about it here

5. Chi-square test Chi-square test used for testing independence by evaluating the closeness between observed and expected frequencies.

Assumption: large samples and independence of individual observation.

```
##
         lung_cancer
## smoker Cases Control
##
      No
             21
                      59
##
            688
                     650
      Yes
chisq.test(ctable, correct = FALSE)
##
    Pearson's Chi-squared test
##
##
## data: ctable
## X-squared = 19.129, df = 1, p-value = 1.222e-05
```

**6. Fisher exact test** Fisher's exact test can be used for test of independence when n is small. Assumption: independence of individual observation and fixed totals. (the row and column totals are fixed, or "conditioned.") When row or column totals are unconditioned, makes this test less powerful.

```
tea <- matrix(c(3, 1, 1, 3), ncol = 2,
    byrow = TRUE)
dimnames(tea) <- list(PouringFirst = c("Milk",</pre>
    "Tea"), GuessPouredFirst = c("Milk",
    "Tea"))
tea
               GuessPouredFirst
##
## PouringFirst Milk Tea
##
           Milk
                   3
##
           Tea
                   1
                        3
fisher.test(tea, alternative = "greater") # set alternative to 'greater', 'less', 'two.sided'
##
##
    Fisher's Exact Test for Count Data
##
## data: tea
## p-value = 0.2429
## alternative hypothesis: true odds ratio is greater than 1
## 95 percent confidence interval:
   0.3135693
                    Inf
## sample estimates:
## odds ratio
##
     6.408309
```

7. Linear regression Linear regression explain the relationship between continuous response and predictors. A linear regression has an equation of the form  $Y = X\beta + \epsilon$ , where X is the explanatory matrix with the first columns of all 1s (intercept) and Y is the dependent variable. The standard multiple (linear) regression equation with p predictor variables and N observations  $y_i = b_0 + b_1 x_{i1} + b_2 x_{i2} + \ldots + b_p x_{ip} + \epsilon_i$ , where  $i=1,\ldots,N$ .

The random errors  $\epsilon$  are assumed to be independently and identically normally distributed.

Example: Hourly carbon monoxide (CO) averages were recorded on summer weekdays at a measurement station in Los Angeles. The data could be downloaded from http://www.statsci.org/data/general/cofreewy. txt There are four variables, which represents for:

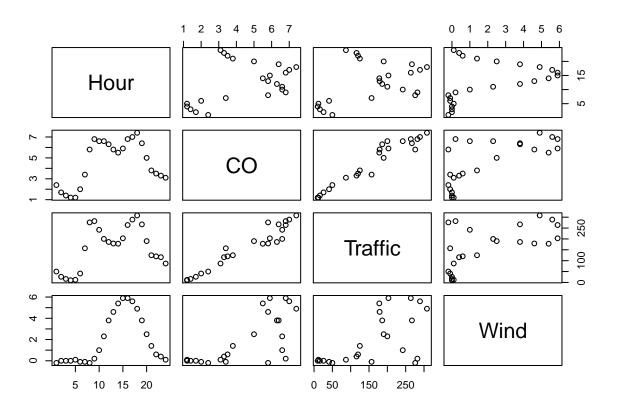
Variable	Description
Hour CO Traffic Wind	hour of the day, from midnight to midnight average summer weekday CO concentration (parts per million) average weekday traffic density (traffic count/traffic speed) average perpendicular wind-speed component, wind speed x cos(wind direction - 235 degrees)

Use CO as dependent variable, the other three variables as predictor to build a linear regression model.

```
lm_data <- read.table("http://www.statsci.org/data/general/cofreewy.txt",
    header = T)
head(lm_data)</pre>
```

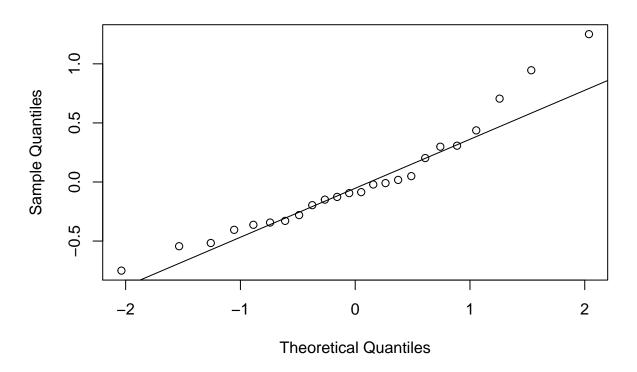
```
##
     Hour
           CO Traffic Wind
## 1
        1 2.4
                    50 -0.2
## 2
        2 1.7
                    26
                        0.0
## 3
        3 1.4
                       0.0
                    16
## 4
        4 1.2
                    10
                        0.0
        5 1.2
                    12 0.1
## 5
## 6
        6 2.0
                    41 -0.1
```

```
plot(lm_data)
```



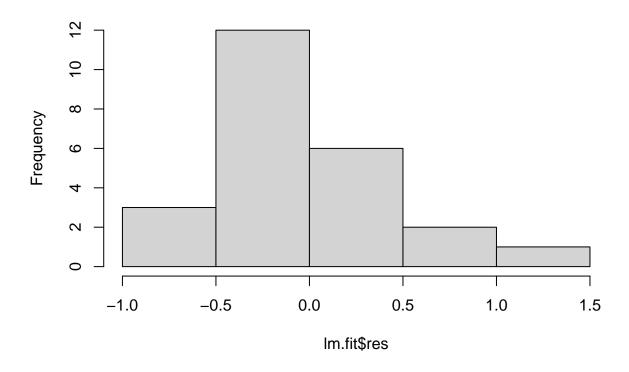
```
lm.fit \leftarrow lm(CO \sim ., lm_data)
summary(lm.fit)
##
## Call:
## lm(formula = CO ~ ., data = lm_data)
## Residuals:
                1Q Median
                                 3Q
## -0.75030 -0.33275 -0.09021 0.22653 1.25112
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.318967 0.242522 5.439 2.53e-05 ***
         -0.005689 0.017066 -0.333 0.74233
## Hour
## Traffic
             ## Wind
             0.179189 0.059517 3.011 0.00691 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.5096 on 20 degrees of freedom
## Multiple R-squared: 0.9498, Adjusted R-squared: 0.9423
## F-statistic: 126.1 on 3 and 20 DF, p-value: 3.682e-13
shapiro.test(lm.fit$res)
##
## Shapiro-Wilk normality test
## data: lm.fit$res
## W = 0.93027, p-value = 0.09885
qqnorm(lm.fit$res)
qqline(lm.fit$res)
```

### Normal Q-Q Plot

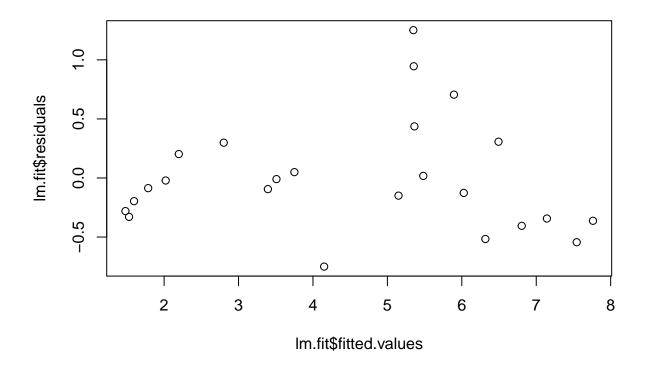


hist(lm.fit\$res) # residual

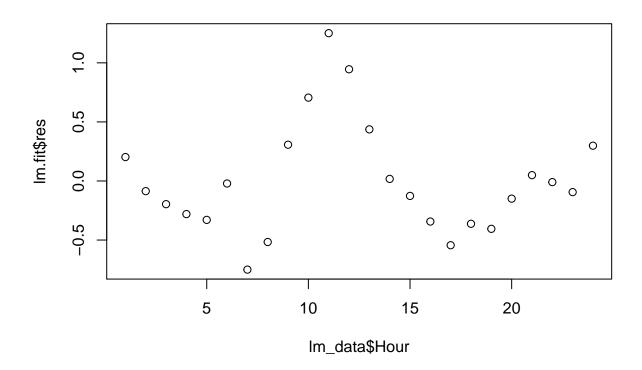
# Histogram of Im.fit\$res



plot(lm.fit\$fitted.values, lm.fit\$residuals) # residual vs fitted value



plot(lm\_data\$Hour, lm.fit\$res) # residuals vs time order



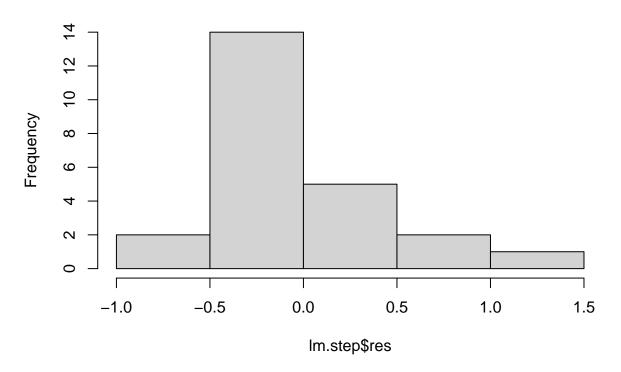
• stepwise model

```
lm.step <- step(lm.fit, direction = "backward")</pre>
## Start: AIC=-28.73
## CO ~ Hour + Traffic + Wind
##
             Df Sum of Sq
##
                             RSS
## - Hour
                    0.029 5.224 -30.597
## <none>
                           5.195 -28.730
                    2.354 7.549 -21.759
## - Wind
              1
## - Traffic 1
                   44.070 49.265 23.260
##
## Step: AIC=-30.6
## CO ~ Traffic + Wind
##
##
             Df Sum of Sq
                             RSS
                                     AIC
## <none>
                           5.224 -30.597
                    2.357 7.581 -23.659
## - Wind
                   46.117 51.341 22.250
## - Traffic 1
summary(lm.step)
```

##

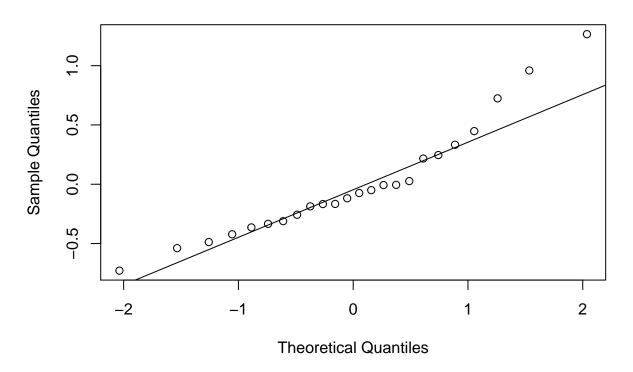
```
## Call:
## lm(formula = CO ~ Traffic + Wind, data = lm_data)
## Residuals:
                1Q Median
                                  3Q
## -0.72858 -0.31710 -0.09629 0.22409 1.26554
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.274461 0.198137 6.432 2.25e-06 ***
## Traffic 0.018290 0.001343 13.616 6.85e-12 ***
## Wind
             0.174747 0.056765 3.078 0.0057 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.4987 on 21 degrees of freedom
## Multiple R-squared: 0.9495, Adjusted R-squared: 0.9447
## F-statistic: 197.5 on 2 and 21 DF, p-value: 2.419e-14
shapiro.test(lm.step$res)
##
## Shapiro-Wilk normality test
##
## data: lm.step$res
## W = 0.91918, p-value = 0.05601
hist(lm.step$res)
```

# Histogram of Im.step\$res

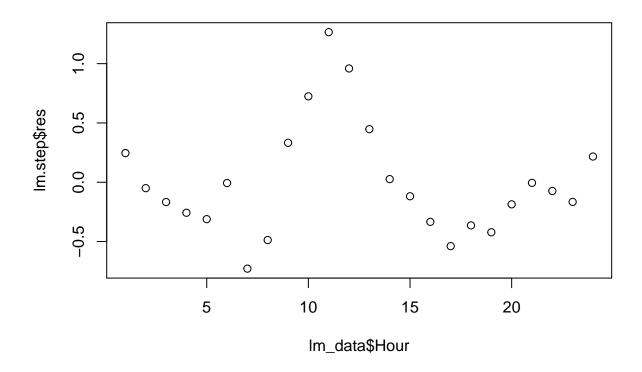


```
qqnorm(lm.step$res)
qqline(lm.step$res)
```

### Normal Q-Q Plot



plot(lm\_data\$Hour, lm.step\$res)



```
lm.co <- step(lm(CO ~ Traffic +</pre>
              Wind + Wind^2 + sin((2 * pi)/24 *
              Hour) + \cos((2 * pi)/24 * Hour) +
              \sin((4 * pi)/24 * Hour) + \cos((4 *
              pi)/24 * Hour), lm_data), direction = "backward")
## Start: AIC=-56.26
## CO ~ Traffic + Wind + Wind^2 + \sin((2 * pi)/24 * Hour) + \cos((2 * pi)/24 * Hour) + \cos((2 * pi)/24 * Hour) + cos((2 * pi)/2
                        pi)/24 * Hour) + sin((4 * pi)/24 * Hour) + cos((4 * pi)/24 *
##
##
                         Hour)
##
                                                                                                      Df Sum of Sq
##
                                                                                                                                                                   RSS
                                                                                                                                                                                                AIC
## - cos((2 * pi)/24 * Hour)
                                                                                                                            0.0038
                                                                                                                                                        1.2886 -58.188
                                                                                                         1
## - \sin((2 * pi)/24 * Hour)
                                                                                                          1
                                                                                                                            0.0063
                                                                                                                                                        1.2910 -58.142
## - Wind
                                                                                                                            0.0457
                                                                                                                                                        1.3305 -57.421
## - \sin((4 * pi)/24 * Hour)
                                                                                                                            0.0512
                                                                                                                                                     1.3360 -57.322
                                                                                                          1
                                                                                                                                                         1.2848 -56.259
## <none>
## - cos((4 * pi)/24 * Hour)
                                                                                                          1
                                                                                                                            0.6820 1.9668 -48.040
## - Traffic
                                                                                                          1
                                                                                                                         10.2379 11.5227 -5.610
##
## Step: AIC=-58.19
## CO ~ Traffic + Wind + sin((2 * pi)/24 * Hour) + sin((4 * pi)/24 *
                        Hour) + cos((4 * pi)/24 * Hour)
```

RSS

AIC

Df Sum of Sq

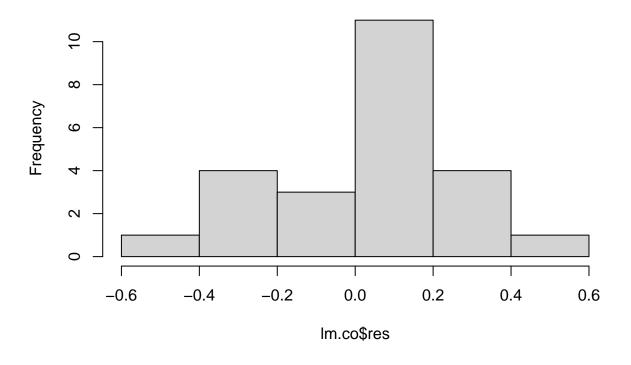
## ##

```
## <none>
                                     1.2886 -58.188
## - \sin((4 * pi)/24 * Hour) 1 0.5949 1.8835 -51.078
## - \sin((2 * pi)/24 * Hour) 1 0.9582 2.2467 -46.846
## - Wind
                             2.2561 3.5447 -35.902
                          1
## - cos((4 * pi)/24 * Hour) 1
                              2.8122 4.1008 -32.405
## - Traffic
                          1
                            12.6457 13.9343 -3.049
summary(lm.co)
##
## Call:
## lm(formula = CO \sim Traffic + Wind + sin((2 * pi)/24 * Hour) +
      \sin((4 * pi)/24 * Hour) + \cos((4 * pi)/24 * Hour), data = lm_data)
##
##
## Residuals:
      Min
               1Q
                  Median
                               3Q
## -0.54297 -0.15049 0.03351 0.11670 0.47671
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        ## Traffic
                        ## Wind
## sin((2 * pi)/24 * Hour) 0.539048 0.147342 3.658 0.00180 **
## sin((4 * pi)/24 * Hour) -0.437784   0.151861 -2.883   0.00991 **
## cos((4 * pi)/24 * Hour) 0.501101 0.079950 6.268 6.54e-06 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2676 on 18 degrees of freedom
## Multiple R-squared: 0.9875, Adjusted R-squared: 0.9841
```

hist(lm.co\$res) # residual

## F-statistic: 285.4 on 5 and 18 DF, p-value: < 2.2e-16

### Histogram of Im.co\$res

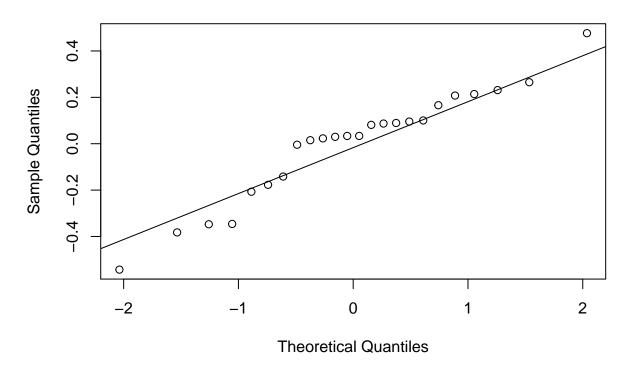


```
shapiro.test(lm.co$res)
```

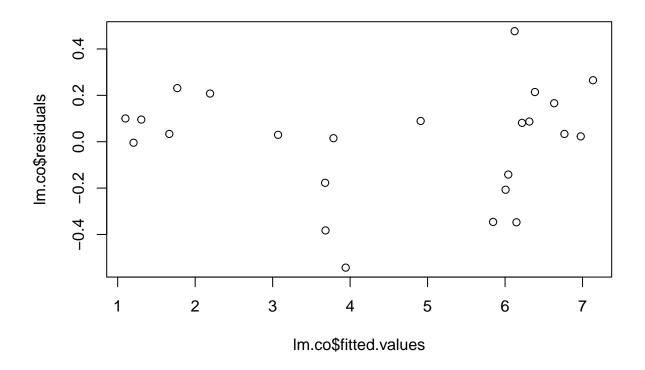
```
##
## Shapiro-Wilk normality test
##
## data: lm.co$res
## W = 0.94628, p-value = 0.2247

qqnorm(lm.co$res)
qqline(lm.co$res)
```

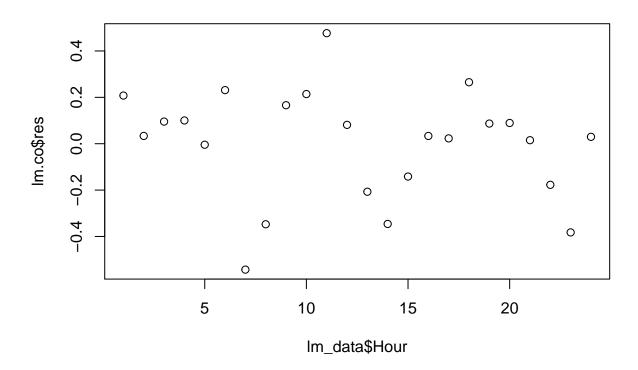
#### Normal Q-Q Plot



plot(lm.co\$fitted.values, lm.co\$residuals) # residual vs fitted value



plot(lm\_data\$Hour, lm.co\$res) # residuals vs time order



If you are interested in the linear regression example, read more about this analysis from the source.

**8. Format data** Use "table1" package to generate summary statistics. See other options in Easily create descriptive summary statistics.

```
# install.packages('table1')
library(table1)

##
## Attaching package: 'table1'

## The following objects are masked from 'package:base':
##
## units, units<-

table <- table1(~Totcare + factor(Nesttype) |
    Location, data = t_test_data)
table</pre>
```

## [1] "\nad>\n\n\n<th class

Use "finalfit" package to generate summary statistics with association between dependent and independent variables.

## Note: dependent includes missing data. These are dropped.

##	label		levels		Well	Moderate	Poor
##	Age (years)		Mean (SD)	60.2	(12.8)	59.9 (11.7)	59.0 (12.8)
##	Sex		Female	51	(54.8)	314 (47.4)	73 (48.7)
##			Male	42	(45.2)	349 (52.6)	77 (51.3)
##	Extent of spread		Submucosa	5	(5.4)	12 (1.8)	3 (2.0)
##			Muscle	12	(12.9)	78 (11.8)	12 (8.0)
##			Serosa	76	(81.7)	542 (81.7)	127 (84.7)
##		Adjacent	structures	(	(0.0)	31 (4.7)	8 (5.3)
##	Obstruction		No		(74.2)		
##			Yes		(20.4)		
##			(Missing)		5 (5.4)		
##	nodes		Mean (SD)	2.7	(2.2)	3.6 (3.4)	4.7 (4.4)
##	р						
##	0.644						
##	0.400						
##							
##	0.081						
##							
##							
##	0.055						
##	0.655						
##							
##	40.004						
##	<0.001						

Reference: Exporting tables and plots

Other sources for formatting statistical results: apa and apa Tables