

Since  $n \rightarrow \infty$ , it is continuous set of random variables

As there is a uniform distribution between 0 and  $\theta$ ,

the p.d.f.  $f(x) = \text{constant}$ .

Since  $\int_0^\theta f(x) dx = 1 \Rightarrow f(x) = \frac{1}{\theta}$

$$P(a \leq X \leq b) = \int_a^b \frac{1}{\theta} dx$$

Given:  $P(X < \epsilon) \leq \frac{E(X)}{\epsilon}$

$$\left[ \begin{aligned} E(X) &= \int_0^\theta x f(x) dx \\ &= \frac{\theta}{2} \end{aligned} \right]$$

$$P(X_{n-13} < \theta + \epsilon) \leq \frac{\theta/2}{\theta - \epsilon}$$

$$P(X_{n-13} < \theta - \epsilon) \leq \frac{\theta}{\theta - \epsilon} \quad \forall \epsilon > 0$$

As  $\epsilon \rightarrow \infty$ ,  $\frac{\theta}{\theta - \epsilon} \xrightarrow{\epsilon \rightarrow \infty} 0$

Hence,  $P(X_{n-13} < \theta - \epsilon) = 0$  since inequality holds  $\forall \epsilon > 0$

Also,  $P(X_{n-13} > \theta + \epsilon) = 0$  since the distribution of  $X$  is

Hence, combining them

from  $\theta$  to  $\theta$ .  
and  $\epsilon > 0$

$$\lim_{n \rightarrow \infty} P(|X_{n-13} - \theta| \geq \epsilon) = 0 \quad (\text{Hence, } X_{n-13} \text{ converges to } \theta \text{ as } n \rightarrow \infty)$$