CS319: Scientific Computing

Week 10: Vector and Matrix classes

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Slides and examples: https://www.niallmadden.ie/2324-CS319

Outline

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Extras

See "extras" section of today's lectures for more examples of classes and overloading (points, dates, complex numbers); Code for these is in the Week10/extras/ folder on the repository/website.

These slides do not include all issues concerning operator overloading. Among the topics omitted are:

- overloading the unary ++ and -- operators. There are complications because they work in both prefix and postfix form.
- Overloading the ternary operator: ? :
- ▶ **Important:** overloading the [] operator.

News and Updates

- ► Lab 6: grades will be posted soon (if not already).
- Project proposals. Deadline for draft versions was 17:00, Tuesday 12 March. Check canvas for feedback. Should discuss further in labs.
- next step is to schedule presentations in Week 12. Indicate your availability here:

```
https://forms.office.com/e/bKBzktxdPs
```

Overview

- ➤ This week is all about extending the Vector class from Week 9. Since the code for the header and definition are different from last week's version, the new files have different names: Vector10.h, Vector10.cpp.
- ► I've also provided a program to test these, called O1TestVectorOperators.cpp. To run that, you'll need a project that contains all three files. If you are using an online compiler, I suggest trying online-cpp.com. For this specific example, try https://www.online-cpp.com/znZjLKN8hl
- ► An early version of the notes for Week 9 included a simple Matrix class. I've removed that, and instead developed the Vector class fully. (For reasons...)

In Week 9, was saw how, for example, the + operator was "overloaded" to allow us to "add" (i.e., concatenate) two strings. We want to see how overload operators for classes that we write so that, for example, we can use the + operator to add two vectors.

That is, we want to study **Operator Overloading**. But to get this to work, we need to study **copy constructors**.

This is a technical area of C++ programming, but is unavoidable.

As we already know, **constructor** is a method associated with a class that is called automatically whenever an object of that class is declared.

But there are time when objects are *implicitly* declared, such as when passed (by value) to a function.

Since this will happen often, we need to write special constuctors to handle it.

Last week we defined a class for vectors:

- It stores a vector of N doubles in a dynamically assigned array called entries;
- The constructor takes care of the memory allocation.

```
1 // From Vector.h (Week 9)
   class Vector {
   private:
     double *entries:
     unsigned int N;
   public:
     Vector (unsigned int Size=2);
     ~Vector(void);
     unsigned int size(void) {return N;};
11
     double geti (unsigned int i);
     void seti (unsigned int i, double x);
13
     // print(), zero() and norm() not shown
   };
   // Code for the constructor from Vector.cpp
   Vector::Vector (unsigned int Size) {
     N = Size:
19
     entries = new double[Size];
```

We then wrote some functions that manipulate vectors, such as AddVec in Week09/03TestVector.cpp

```
void VecAdd (Vector &c, Vector &a, Vector &b,
double alpha=1.0, double beta=1.0);
```

Note that the Vector arguments are passed by reference...

What would happen if we tried the following, seemingly reasonable piece of code?

```
Vector x(4);
x.zero(); // sets entries of a all to 0
Vector y=x; // should define a new vector, with a copy of x
```

This will cause problems for the following reasons:

Copy Constructors

Recall: Vector

The solve this problem, we should define our own **copy constructor**. A **copy constructor** is used to make an exact copy of an existing object. Therefore, it takes a single parameter: the address of the object to copy. For example:

See Vector10.cpp for more details

```
// copy constructor
Vector::Vector (const Vector &old_Vector)
{
    N = old_Vector.N;
    entries = new double[N];
    for (unsigned int i=0; i<N; i++)
        entries[i] = old_Vector.entries[i];
}</pre>
```

The **copy constructor** can be called two ways:

(a) explicitly, .e.g,

```
Vector V(2);
V.seti(0)=1.0; V.seti(1)=2.0;
Vector W(V); // W is a copy V
```

(b) *implicitly*, when ever an object is passed by value to a function. If we have not defined our own copy constructor, the default one is used, which usually causes trouble.

In this section, we'll study "Operator overloading".

Our main goal is to overload the addition (+) and subtraction (-) operators for vectors.

Last week, we wrote a function to add two Vectors: AddVec.

It is called as AddVec(c,a,b), and adds the contents of vectors a and b, and stores the result in c.

It would be much more natural redefine the standard **addition** and **assignment** operators so that we could just write c=a+b. This is called **operator overloading**.

To overload an operator we create an **operator function** – usually as a member of the class. (It is also possible to declare an operator function to be a **friend** of a class – it is not a member but does have access to private members of the class. More about **friends** later).

The general form of the operator function is:

return-type of a operator is usually the class for which it is defined, but it can be any type.

Note that we have a new key-word: operator.

The operator being overloaded is substituted for the # symbol

Almost all C++ operators can be overloaded:

but not . :: .*

- Operator precedence cannot be changed: * is still evaluated before +
- ► The number of arguments that the operator takes cannot be changed, e.g., the ++ operator will still take a single argument, and the / operator will still take two.
- ► The original meaning of an operator is not changed; its functionality is extended. It follows from this that operator overloading is always relative to a user-defined type (in our examples, a class), and not a built-in type such as int or char.
- Operator overloading is always relative to a user-defined type (in our examples, a class).
- ► The assignment operator, =, is automatically overloaded, but in a way that usually fails except for very simple classes.

We are free to have the overloaded operator perform any operation we wish, but it is good practice to relate it to a task based on the traditional meaning of the operator. E.g., if we wanted to use an operator to add two matrices, it makes more sense to use + as the operator rather than, say, *.

We will concentrate mainly on binary operators, but later we will also look at overloading the unary "minus" operator.

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For our first example, we'll see how to overload operator+ to add two objects from our vector class.

First we'll add the declaration of the operator to the class definition in the header file, Vector10.h:

```
vector operator+(vector b);
```

Then to Vector10.cpp, we add the code

See Vector10.cpp for more details

First thing to notice is that, although + is a binary operator, it seems to take only one argument. This is because, when we call the operator, c = a + b then a is passed **implicitly** to the function and b is passed **explicitly**.

Therefore, for example, a.N is known to the function simply as N.

The temporary object c is used inside the object to store the result. It is this object that is returned. Neither a or b are modified.

We now want to see another way of accessing the implicitly passed argument. First, though, we need to learn a little more about pointers, and introduce a new piece of C++ notation.

Recall that if, for example, x is a double and y is a pointer to double, we can set y=&x. So now y stores the memory address of x. We then access the contents of that address using *y.

Now suppose that we have an object of type Vector called v, and a pointer to vector, w. That is, we have defined

```
Vector v;
Vector *w;
```

Then we can set w=&v. Now accessing the member N using v.N, will be the same as accessing it as (*w).N.

It is important to realise that (*w). N is **not** the same as *w. N.

C++ provides a new operator for this situation: w->N, which is equivalent to (*w).N.

When writing code for functions, and especially overloaded operators, it can be useful to **explicitly** access the implicitly passed object.

That is done using the **this** pointer, which is a pointer to the object itself.

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As we've just noted, since this is a pointer, its members are accessed using either (*this).N or this->N.

We often use the **this** pointer when a function must return the address of the argument that was passed to it. This is the case of the assignment operator.

See Vector10.cpp for more details

```
// Overload the = operator.
100 Vector & Vector::operator=(const Vector &b)
102
      if (this == \&b)
        return(*this); // Taking care for self-assignment
      delete [] entries; // In case memory was already allocated
      N = b.N:
108
      entries = new double[b.N]:
      for (unsigned int i=0; i<N; i++)</pre>
110
        entries[i] = b.entries[i];
112
      return(*this);
```

Unary Operators

So far we have discussed just the **binary** operator, +. By "**binary**", we mean it takes **two** arguments.

But many C++ operators are **unary**: they take only one argument; examples include ++ and --.

For our Vector class, we want to overload the – (minus) operator. Note that this can be used in two ways:

- ightharpoonup c = -a (unary).
- ightharpoonup c = a b (binary)

In the first case here, "minus" is an example of a **prefix** operator. (See "Extras" for example of overloading **postfix** operators, like a++, which are a little more complicated).

After that we will then define the binary minus operator, by using addition and unary minus.

For the unary "minus" operator, when we write "-a" the object a is passed *implicitly*. This is a little different from previous cases, where the object passed implicitly is to the left of the operator.

See Vector10.cpp for more details

```
// Overload the unary minus (-) operator. As in b=-a;
Vector Vector::operator-(void)
{
    Vector b(N); // Make b the size of a
    for (unsigned int i=0; i<N; i++)
        b.entries[i] = -entries[i];

return(b);
}
```

And now that we have defined this operator, we can define the **binary** minus operator. Now this time when we write "a-b", it is the *left* argument that is implicit.

See Vector10.cpp for more details

friend functions

In all the examples that we have seen so far, the only functions that may access private data belonging to an object has been a member function/method of that object.

If we need a function that does not below to the class to be able to access private elements, it can be designated a friend of the class.

For non-operator functions, there is nothing that complicated about friends. However, care must be taken when overloading operators as friends.

In particular:

- All arguments are passed explicitly to friend functions/operators.
- Certain operators, particularly the insertion/put-to << and extraction/get-from >> operators can only be overloaded as friends.

In last week's version of the Vector class, we could output its elements using the print() method. E.g.:

```
Vector v;
v.zero()
std::cout << "v has values ";
v.print();
```

But it would be much more convinient just to do

```
std::cout << "v has values " << v;
```

But the insertion operator was not defined for our class.

We can fix that, by overloading it. However, the << operator belongs to std::cout, not to Vector. So it cannot access its entries member.

Here is how we resolve this...

We add the following line to the definition of the Vector class.

```
friend std::ostream &operator<<(std::ostream &, Vector &v);
```

And the we define:

```
std::ostream &operator<<(std::ostream &output, Vector &v)
{
    output << "[";
    for (unsigned int i=0; i<v.size()-1; i++)
        output << v.entries[i] << ",";
    output << v.entries[v.size()-1] << "]";
    return(output);
}</pre>
```

Now we can display a vector using std::cout directly.

Preprocessor Directives

Our next step is to define a Matrix class, and overload some of the associated operators. One of those is the multiplication ("times") operator * for matrix-vector multiplication.

With those done, we can think about overloading the multiplication operator for <u>Matrix-Vector</u> multiplication.

This introduces a few small new complications:

- the return type is different from the class type;
- ▶ if we use multiple source files, how do we know where exactly to place the #include directives?

So, before we can proceed, we need to take a short detour to consider **preprocessor** directives.

The preprocessor in C++ is a hang-over over from early versions of C. Originally, that language did not have a construct for defining constants and including header files. To get around this, an early version of C introduced the **preprocessor**. This is a program that

- reads and modifies your source code by checking for any lines that being with a hash symbol (#);
- carries out any operations required by these lines;
- forms a new source code that is then compiled.

We usually don't get to see this new file, though you can view it by compiling with certain options (with g++, this is -E).

The preprocessor is *separate* from the compiler, and has its own syntax.

The simplest preprocessor directive is **#define**. This is used for defining global constants, and doing a simple search-and-replace. For example,

```
#define SIZE 10
```

will find every instance of the word (well, token, really) *SIZE* and replaces it with 10.

In general, this use of the **#define** directive to define identifiers to be used like "global variables" is not very good practice. However, it can be very useful as a way of checking if a piece of code has already been compiled.

The most familiar preprocessor is #include, e.g.,

```
#include <iostream>
#include "Vector10.h"
```

This tells the preprocessor to take the named file(s) and insert them into the current file.

If the name is contained in angle brackets, as in **iostream**, this means the preprocessor will look in "the usual place" — where the compiler is installed on your system.

If the named file is in quotes, it looks in the current directory/folder, or in the specified location.

Finally, we have **conditional compilation**.

Suppose we want to write a member function for the *Matrix* class that involves the Vector class.

So we need to include Vector10.h in Matrix10.h. But then if our main source file includes both Matrix10.h and Vector10.h we could end up defining it twice.

To get around this we use conditional compilation.

In the files we can have such lines as the following in Vector10.h

```
#ifndef _VECTOR_H_INCLUDED
#define _VECTOR_H_INCLUDED
// stuff goes here
#endif
```

We now write a class implementation for a matrix, along with the associated functions.

We'll first consider how the matrix is data is stored. The most natural approach might seem to be to construct a two dimensional array. This can be done as follows:

```
double **entries = new double *[N];
for (int i=0; i<N; i++)
  entries[i] = new double N;</pre>
```

A simpler, faster approach is to store the N^2 entries of the matrix in a single, one-dimensional, array of length N^2 , and then take care how the access is done:

Matrix10.h

```
12 class Matrix {
   private:
14
     double *entries;
    unsigned int N;
16 public:
     Matrix (unsigned int Size=2);
18
     Matrix (const Matrix &m); // Copy constructor
     "Matrix(void);
     Matrix & operator = (const Matrix &B); // assignment operator
     unsigned int size(void) {return (N);};
24
     double getij (unsigned int i, unsigned int j);
     void setij (unsigned int i, unsigned int j, double x);
     Vector operator*(Vector u); // Define later!
28
     void print(void);
```

First we'll look at the code for the constructor, to verify that the data is stored just as an 1D array:

from Matrix10.cpp

```
// Basic constructor. See below for copy constructor.

Matrix::Matrix (unsigned int Size)
{
    N = Size;
    entries = new double [N*N];
}
```

Next we'll look at the setij() member, to see how indexing
works.

from Matrix10.cpp

```
void Matrix::setij (unsigned int i, unsigned int j, double x)
{
   if (i<N && j<N)
       entries[i*N+j]=x;
   else
   std::cerr << "Matrix::setij(): Index out of bounds.\n";
}</pre>
```

Other components of the Matrix class are similar to the corresponding functions for the Vector class, such as the assignment operator, and the copy constructor.

So, we'll just focus on overloading the operator* for multiplication of a vector by a matrix: c = A * b, where A is an $N \times N$ matrix, and c and b are vectors with N entries.

Since the left operand is a matrix, we'll make this operator a member of the Matrix class; its header has the line:

```
Vector operator*(Vector b);
```

The code from Matrix10.cpp is given below.

```
84 // Overload the operator multiplication (*) for a Matrix-Vector
    // product. Matrix is passed implicitly as "this", the Vector is
86 // passed explicitly. Will return v=(this)*u
    Vector Matrix::operator*(Vector u)
88 1
      Vector v(N); //v = A^*u, where A is the implicitly passed Matrix
90
      if (N != u.size())
         std::cerr << "Error: Matrix::operator* - dimension mismatch"
92
                     << std::endl:
      else
94
         for (unsigned int i=0; i<N; i++)</pre>
         {
96
           double x=0;
           for (unsigned int j=0; j<N; j++)</pre>
98
             x += entries[i*N+j]*u.geti(j);
           v.seti(i,x);
100
      return(v);
102 }
```

Preview of Lab 8

In Lab 7 you had to write a function that implemented the Jacobi method. For Lab 8, you'll rewrite it using the Vector and Matrix classes.

In addition, you'll implement the Gauss-Seidel method. For that, you'll have to to implement the "backslash" operator, for solving Ax = y, where A is triangular.