

## MA385: Assignment 1

Information on the deadline, weighting, collaboration policy, submission process, etc, is on Canvas. Direct link: <https://universityofgalway.instructure.com/courses/46941/assignments/140160>

---

- Q1. (Based on the 22/23 exam paper) Let  $\{x_0, x_1, x_2\} := \{1, 3, 5\}$  be a set of interpolation points. Write down the formulae for the associated Lagrange Polynomials,  $\{L_0, L_1, L_2\}$ , and give a rough sketch of them, clearly indicating their values at the interpolation points.

Suppose we define  $q(x) := 1 - L_0(x) + L_1(x) + L_2(x)$ . Show that, in fact,  $q(x) \equiv 0$ , for all  $x$ .

- Q2. Let  $f(x) = x^{3/2}$ . Give the Lagrange form of  $p_2$ , the polynomial interpolant to  $f$  at  $\{x_0, x_1, x_2\} = \{1, 3, 5\}$ . Use Cauchy's Theorem to give an upper bound for  $|f(4) - p_2(4)|$ . How does this compare with the actual error?

- Q3. Let  $f(x) = x^{3/2}$  again. Write down the formula for the linear spline,  $l$ , which interpolates  $f$  at  $\{x_0, x_1, x_2\} = \{1, 3, 5\}$ .

Use the relevant theorem from Section 2.1 (Linear Splines) to give an upper bound for  $|f(4) - l(4)|$ . How does this compare with the actual error?