# 1. What is KKR? Why KKR is needed in A.I?

Knowledge Representation & reasoning is a technique for representing information about the real world so that a computer can understand and can utilize this knowledge to solve the complex real world problems.

# 2. Definition of PL (Propositional Logic), PDL(Predicate Logic), and FL(Fuzzy Logic).

**Propositional logic (PL)** is the simplest form of logic where all the statements are made by propositions. A proposition is a declarative statement that is either true or false. It is a technique of knowledge representation in logical and mathematical form.

**Predicate Logic (PDL)** deals with predicates, which are propositions, consist of variables. It is a powerful language that develops information about the objects in a more easy way and can also express the relationship between those objects.

**Fuzzy Logic** (**FL**) in artificial intelligence is a generalized form of standard logic, where any concept might have a truth degree ranging between 0.0 and 1.0.

3. What are the different types of inferences that are used on the above 3 types of knowledge representation techniques with examples?

# Propositional logic (PL)

■ Modus Ponens: One of the most important rules of inference, and it states that if
P and P → Q is true, then we can infer that Q will be true. It can be represented as:

$$P \to Q, P \qquad \{((P \to Q) \land P) \to Q\}$$

- ∴Q
- Hence, we can say that, if P → Q is true and P is true then Q will be true

# **Example:**

Statement-1: "If I am sleepy then I go to bed"  $==> P \rightarrow Q$ 

Statement-2: "I am sleepy" ==> P

Conclusion: "I go to bed." ==> Q.

Hence, we can say that, if  $P \rightarrow Q$  is true and P is true then Q will be true.

Modus Tollens: This rule state that if P → Q is true and ¬ Q is true, then ¬ P will also true. It can be represented as:

# Example:

Statement-1: "If I am sleepy then I go to bed" ==> P→ Q

Statement-2: "I do not go to the bed."==> ~Q

Statement-3: Which infers that "I am not sleepy" => ~P

- **Hypothetical Syllogism (H. S.):** This rule state that if  $P \rightarrow R$  is true whenever  $P \rightarrow Q$  is true, and  $Q \rightarrow R$  is true. It can be represented as the following notation:
- $\frac{(P \to Q) \land (Q \to R)}{\therefore P \to R}$

# ☐ Example:

Statement-1: If you have my home key then you can unlock my home.  $P \rightarrow Q$ Statement-2: If you can unlock my home then you can take my money.  $Q \rightarrow R$ Conclusion: If you have my home key then you can take my money.  $P \rightarrow R$ 

- **Disjunctive Syllogism (D. S.):** The Disjunctive syllogism rule state that if PVQ is true, and ¬P is true, then Q will be true. It can be represented as:
- <u> (PVQ) ~P</u> ∴Q

# ■ Example:

Statement-1: Today is Sunday or Monday. ==>PVQ

Statement-2: Today is not Sunday. ==> ¬P

Conclusion: Today is Monday. ==> Q

## ♦ Drawbacks of PL -

- 1. Has limited expressive power
- 2. No representation to relations like "All, some, none, etc"
  - 1. E.g All eggs are rotten, some apples are sweet, etc.
- 3. Alternate = Predicate Logic

# Predicate Logic (PDL)

# Quantifiers:

- Logical operators which assert the scope of a predicate
  - ∀ For All (universal quantifier)
  - ∃ There Exists (existential quantifier)

- ∀x LOVELY (x) Everything is lovely.
- ∃x LOVELY (x) Something is lovely.
- $\forall x$  IN  $(x, \text{garden}) \Rightarrow \text{LOVELY } (x)$  Everything in the garden is lovely.

# Fuzzy Logic (FL)

Fuzzy Inference: The process of reasoning based on Fuzzy logic.

Example:

If the power transformer is slightly overloaded, Then keep this load for a while.

**Fuzzy rule:** A conditional statement in the form:

IF x is A THEN y is B, where x and y are linguistic variables, and A and B are linguistic values determined by fuzzy sets.

- Rule 1: IF (GPA is high) and (Exam is satisfactory) and (Approach is Smart) then (Decision is Select)
- Rule 2: IF (GPA is low) and (Exam is bad) or (Approach is Stupid)
   then (Decision is Reject)
- Inputs to a fuzzy system can be:
  - fuzzy, e.g. (Score = Moderate), defined by membership functions
  - exact, e.g.: (Score = 190); (Theta = 35), defined by crisp values.
- Outputs from a fuzzy system can be:
  - fuzzy, i.e. a whole membership function, or
  - exact, i.e. a single value is produced on the output.

Four steps: fuzzification, rule evaluation, aggregation of the rules, defuzzification

Rule 1: Rule 1:

THEN z is C1 THEN risk is low

Rule 2: Rule 2:

IF x is A2 IF project\_funding is marginal AND y is B2 AND project\_staffing is large

THEN z is C2 THEN risk is normal

Rule 3: Rule 3:

THEN z is C3 THEN risk is high

- 4. <u>Symbols, quantifiers, rules of inference in different types of knowledge representation technique</u> with examples.
  - Syntax of PL:
  - symbol -> P | Q | R | S | ...
  - atomic sentence -> TRUE | FALSE
  - sentence -> atomic sentence | complex sentence
  - complex sentences -> ~ sentence | (sentence ^ sentence) | (sentence v sentence) | (sentence → sentence) | (sentence ↔ sentence)
  - Precedence relation operators: ~, ^, v, →, ↔.

# **Predicate Logic**

- ☐ Logical Connectives:
  - ➤ AND (^)
  - >OR (∀)
  - ➤ NOT (~)
  - $\triangleright$ IMPLIES ( $\rightarrow$ )

# Quantifiers:

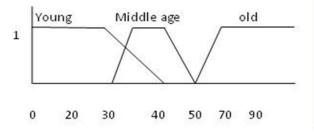
- Logical operators which assert the scope of a predicate
  - ∀ For All (universal quantifier)
  - ∃ There Exists (existential quantifier)
    Operations on Fuzzy Sets
- Operations on fuzzy sets is done by means of their membership functions. Let A and B be fuzzy sets on a mutual universe.

1. Intersection of A and B is: $A \cap B =$	= A min B, corresponding items in a and b.
2. Union of A and B is: $A \cup B =$	= A max B, corresponding items in a and b.
3. Complement of A is: A =	= 1 - A
4. Dilation (increases the degree of membership of all members by spreading out the curve) of A is:	=DIL (A) = $(u_A(x)^{1/n})$ for all x in U
5. Concentration (decreases the degree of membership of all members) of A is:	=CON (A) = $(u_A(x)^n)$ for all x in U

5. <u>Difference between Fuzzy Logic and Crisp Logic. What are fuzzy expert systems?</u>

# FUZZY SET

# Defines value between 0 or 1



# CRISP SET

# Defines either value is 0 or 1

YES or NO

Crisp logic (crisp) is the same as boolean logic(either 0 or 1). Either a statement is true(1) or it is not(0), meanwhile fuzzy logic captures the degree to which something is true.

A fuzzy expert system is an expert system that uses fuzzy logic instead of Boolean logic. In other words, a fuzzy expert system is a collection of membership functions and rules that are used to reason about data. A typical fuzzy expert system has more than one rule.

# 6. Application of PL, PDL & FL

<u>Propositional Logic</u> - Design of computing machines, artificial intelligence, the definition of data structures for programming languages, etc.

Predicate Logic - Formal notations for writing clear and concise mathematical definitions.

# Applications of Fuzzy Logic

**Control Applications:** Aircraft control, Sendai subway operation (Hitachi), Cruise control (Nissan), Automatic Transmission (Nissan, Sabaru), Self parking model car (Tokyo University), Space Shuttle docking (NASA)

# **Scheduling and Optimization:**

Elevator Scheduling (Hitachi, Fujitsu, Mitsubishi)

Stock Market Analysis: Yamichi Securities

# Signal Analysis for Tuning and Interpretation:

TV picture adjustment (Sony Corporation)

Handwriting Recognition: Sony Palmtop computer

Video Camera Autofocus: Sony and Canon Video Image Stabilizer: Matsushita, Panasonic

# **Fuzzy System Applications**

- · Pattern recognition and classification
- · Fuzzy clustering
- Image and speech processing
- Fuzzy systems for prediction
- Fuzzy control
- Monitoring
- Diagnosis
- Optimization and decision making
- Group decision making

# 7. <u>Limitations of PL, PDL & FL</u>

## **Limitations of PL** -

- 4. Has limited expressive power
- 5. No representation to relations like "All, some, none, etc"
- a. E.g All eggs are rotten, some apples are sweet, etc.

# **Limitations of PDL** -

# Limitations/Problems

- Lack of Semantics
  - No formal semantic of the relations
    - E.g. Does "IS-A" mean subclass, member, etc?
  - Possible multiple interpretations
  - Restricted expressiveness
    - E.g. can not distinguish between instance and class

# Advantages:

Easy to follow hierarchy, easy to trace association, flexible

### Disadvantages:

- Meaning attached to nodes might be ambiguous
- Exception handling is difficult
- Difficult to program

# **Disadvantages of Fuzzy Logic Systems -**

- 1. Fuzzy logic is not always accurate, so The results are perceived based on assumption, so it may not be widely accepted.
- 2. Fuzzy systems don't have the capability of machine learning as well as neural network type pattern recognition.

A major drawback of Fuzzy Logic control systems is that they are completely dependent on human knowledge and expertise.

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