16720-A F18 Hough Transform

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Total Points: 100

In this assignment you will be implementing some basic image processing algorithms and putting them together to build a Hough Transform based line detector. Your code will be able to find the start and end points of straight line segments in images. We have included a number of images for you to test your line detector code on. Like most vision algorithms, the Hough Transform uses a number of parameters whose optimal values are (unfortunately) data dependent (i.e., a set of parameter values that works really well on one image might not be best for another image). By running your code on the test images you will learn about what these parameters do and how changing their values effects performance.

Many of the algorithms you will be implementing as part of this assignment are functions in the MATLAB image processing toolbox. You are not allowed to use calls to such functions in this assignment. You may however compare your output to the output generated by the image processing toolboxes to make sure you are on the right track.

1 Instructions

- 1. **Integrity and collaboration:** Students are encouraged to work in groups but each student must submit their own work. If you work as a group, include the names of your collaborators in your write up. Code should NOT be shared or copied. Please DO NOT use external code unless permitted. Plagiarism is strongly prohibited and may lead to failure of this course.
- 2. **Start early!** Especially for those not familiar with MATLAB.
- 3. If you have any question, please look at **Piazza** first. Other students may have encountered the same problem, and it may be solved already. If not, post your question in the specified folder. TAs will respond as soon as possible.
- 4. Write-up: Your write-up should mainly consist of three parts, your answers to theory questions, the resulting images of each step (for example, the output of houghScript.m), and the discussions for experiments. Please note that we DO NOT accept handwritten scans for your write-up in this assignment. Please type your answers to theory questions and discussions for experiments electronically.
- 5. **Submission:** Your submission for this assignment should be a zip file, <andrew-id.zip>, composed of your write-up, your MATLAB implementations (including helper functions). Please make sure to remove the data/, result/ folders, and any other temporary files that you've generated. Your final upload should have files arranged in this layout:
 - <AndrewID>
 - <AndrewID>.pdf
 - matlab
 - * myImageFilter.m
 - * myEdgeFilter.m
 - * myHoughTransform.m
 - * myHoughLines.m
 - * yourHelperFunction1.m(optional)
 - * yourHelperFunction2.m(optional)

For your convenience, we have provided you with a simple script <code>checkSubmission.m</code> to check whether your submissions are in correct formats or not. The only thing your need to do is place the script at the directory where your submission, <code><your-andrew-id>.zip</code> lies and then execute it. Please make sure that you have passed the test before uploading your zip file. Assignments that do not follow this submission rule will be <code>penalized 10%</code> of the total score.

6. Please make sure that the file paths that you use are relative and not absolute. That is, it shouldn't be imread('/name/Documents/subdirectory/hw1/data/abc.jpg') but imread('../data/abc.jpg').

2 Theory Questions

(20 points)

Type down your answers for the following questions in your write-up. Each question should only take a couple of lines. In particular, the "proofs" do not require any lengthy calculations. If you are lost in many lines of complicated algebra you are doing something much too complicated (or perhaps wrong). Each question from Q2.1 to Q2.4 are worth 5 points each.

- Q2.1 Show that if you use the line equation $x\cos\theta + y\sin\theta \rho = 0$, each image point (x,y) results in a sinusoid in (ρ,θ) Hough space. Relate the amplitude and phase of the sinusoid to the point (x,y).
- Q2.2 Why do we parameterize the line in terms of ρ , θ instead of slope and intercept (m, c)? Express the slope and intercept in terms of ρ and θ .
- Q2.3 Assuming that the image points (x, y) are in an image of width W and height H (i.e., $x \in [1, W], y \in [1, H]$), what is the maximum absolute value of ρ and what is the range of θ ?
- Q2.4 For points (10, 10), (15, 15) and (30, 30) in the image, plot the corresponding sinusoid waves in Hough space (ρ, θ) and visualize how their intersection point defines the line (what is (m, c) for this line?). Please use MATLAB to plot the curves and report the result in your write-up.

3 Implementation

We have included a wrapper script named houghScript.m that takes care of reading in images from a directory, making function calls to the various steps of the Hough transform (the functions that you will be implementing) and generates images showing the output and some of the intermediate steps. You are free to modify the script as you want, but note that TAs will run the original houghScript.m while grading. Please make sure your code runs correctly with the original script and generates the required output images. Every script/function you write in this section should be included in the matlab/ directory. As for the resulting images, please include them in your write-up

3.1 Convolution (15 points)

Write a function that convolves an image with a given convolution filter

```
function [img1] = myImageFilter(img0, h)
```

As input, the function takes a greyscale image (img0) and a convolution filter stored in matrix h. The output of the function should be an image img1 of the same size as img0 which results from convolving img0 with h. You can assume that the filter h is odd sized along both dimensions. You will need to handle boundary cases on the edges of the image. For example, when you place a convolution mask on the top left corner of the image, most of the filter mask will lie outside the image. One possible solution is to pad the image such that pixels lying outside the image boundary have the same intensity value as the nearest pixel that lies inside the image.

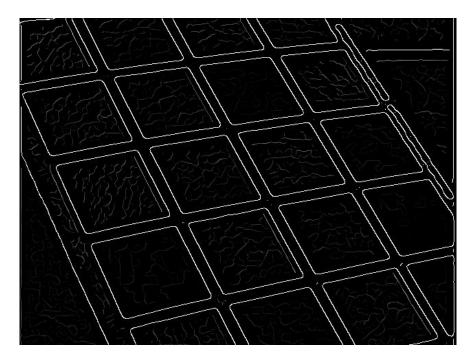


Figure 1: Example of edge intensity image

Your code cannot use MATLAB's imfilter, conv2, convn, filter2 functions or other similar functions. You may compare your output to these functions for comparison and debugging.

3.2 Edge Detection

(15 points)

Write a function that finds edge intensity and orientation in an image. Include the output of your function for one of the given images in your writeup.

```
function [Im Io Ix Iy] = myEdgeFilter(img, sigma)
```

The function will input a greyscale image (img) and sigma (scalar). sigma is the standard deviation of the Gaussian smoothing kernel to be used before edge detection. The function will output Im, the edge magnitude image; Io the edge orientation image and Ix and Iy which are the edge filter responses in the x and y directions respectively.

First, use your convolution function to smooth out the image with the specified Gaussian kernel. This helps reduce noise and spurious fine edges in the image. You may use fspecial to get the Gaussian filter. The size of the Gaussian filter should depend on sigma(e.g.,hsize=2*ceil(3*sigma)+1). To find the image gradient in the x direction Ix, convolve the smoothed image with the x oriented Sobel filter. Similarly, find Iy by convolving the smoothed image with the y oriented Sobel filter.

The edge magnitude image Im and the edge orientation image Io can be calculated from Ix and Iy.

In many cases, the high gradient magnitude region along an edge will be quite thick. For finding lines its best to have edges that are a single pixel wide. Towards this end, make your edge filter implement non maximal suppression, that is for each pixel look at the two neighboring pixels along the gradient direction and if either of those pixels has a larger gradient magnitude then set the edge magnitude at the center pixel to zero. Map the gradient angle to the closest of 4 cases, where the line is sloped at almost 0° , 45° , 90° , 135° . For eg, 20° would map to 0° and 30° would map to 45° .

For more details on non-maximum suppression, please refer to section 4 of this handout. Your code cannot

call MATLAB's edge function or other similar functions. An example of edge intensity image can be seen in Figure 1.

3.3 Hough Transform

(20 points)

Write a function that applies the Hough Transform to an edge magnitude image.

```
function [H, rhoScale, thetaScale] = myHoughTransform(Im, threshold, rhoRes, thetaRes)
```

Im is the edge magnitude image, threshold (scalar) is an edge strength threshold used to ignore pixels with a low edge filter response. rhoRes (scalar) and thetaRes (scalar) are the resolution of the Hough transform accumulator along the ρ and θ axes respectively. For example, if thetaRes = 5° and $\theta \in [0, 360^\circ]$, then number of bins along θ axis is 360/5 = 72. H is the Hough transform accumulator that contains the number of 'votes' for all the possible lines passing through the image. rhoScale and thetaScale are the arrays of ρ and θ values over which myHoughTransform generates the Hough transform matrix H. For example, if rhoScale (i) = ρ_i and thetaScale (j) = θ_j , then H (i, j) contains the votes for $\rho = \rho_i$ and $\theta = \theta_j$.

First, threshold the edge image. Each pixel (x,y) above the threshold is a possible point on a line and votes in the Hough transform for all the lines it could be a part of. Parametrize lines in terms of θ and ρ such that $\rho = x \cos\theta + y \sin\theta$. where $\theta \in [0,2\pi]$ and $\rho \in [0,M]$. M should be large enough to accommodate all lines that could lie in the image. Each line in the image corresponds to a unique pair (ρ,θ) in this range. Therefore, θ values corresponding to negative ρ are invalid, and you should not count those votes.

The accumulator resolution needs to be selected carefully. If the resolution is set too low, the estimated line parameters might be inaccurate. If resolution is too high, run time will increase and votes for one line might get split into multiple cells in the array.

Your code cannot call MATLAB's hough function or other similar functions. You may use hough for comparison and debugging. To visualize matrix H as a grayscale image, use imshow.

3.4 Finding Lines (15 points)

```
function [lineRho lineTheta] = myHoughLines(H, nLines)
```

H is the Hough transform accumulator and nLines is the number of lines to return. Outputs lineRho and lineTheta are both nLines \times 1 vectors that contain the parameters (ρ and θ respectively) of the lines found in an image.

Ideally, you would want this function to return the ρ and θ values for the nLines highest scoring cells in the Hough accumulator. But for every cell in the accumulator corresponding to a real line (likely to be a locally maximal value), there will probably be a number of cells in the neighborhood that also scored highly but shouldn't be selected. These non maximal neighbors can be removed using non maximal suppression. Note that this non maximal suppression step is different to the one performed earlier. Here you will consider all neighbors of a pixel, not just the pixels lying along the gradient direction. Implement your own non maximal suppression.

Once you have suppressed the non maximal cells in the Hough accumulator, return the line parameters corresponding to the strongest peaks in the accumulator.

Your code cannot call MATLAB's houghpeaks function or other similar functions. You may use houghpeaks for comparison and debugging.

3.5 Fitting Line Segments for Visualization

(5 points)

Now you have the parameters ρ and θ for each line in an image. However, this is not enough for visualization. We still need to prune the detected lines into line segments that do not extend beyond the objects they

belong to. This is done by houghlines and drawLine.m. See houghScript.m for more details. You can modify the parameters of houghlines and see how the visualizations change. As shown in Fig. 2, the result is not perfect, so don't worry if the performance of your implementation is not that great.

Run the houghScript.m file and include images (edge intensity image as shown in Figure 1 and line segments result as shown in Figure 2) for one example in your write-up.

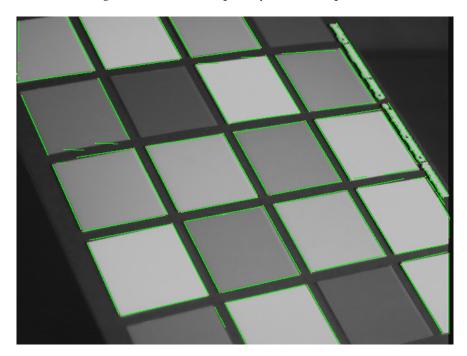


Figure 2: Line segments result

4 Experiments (10 points)

Did your code work well on all the image with a single set of parameters? How did the optimal set of parameters vary with images? Which step of the algorithm causes the most problems? Did you find any changes you could make to your code or algorithm that improved performance?

Tabulate the different experiments that you have performed with their results in your write-up. Also describe how well your code worked on different images, what effect the parameters had on any improvements that you made to your code to make it work better. If you made changes to your code that required changes to the results generation script, include your updated version in your submission.

Appendix

Non-maximum Suppression

Non-maximum suppression (NMS) is an algorithm used to find local maxima using the property that the value of a local maximum is greater than its neighbors. To implement the NMS in 2D image, one can move a 3×3 (or 7×7) filter over the image. At every pixel, it suppresses the value of the center pixel (by setting its value to 0) if its value is not greater than the value of the neighbours. To use NMS for edge thinning, one should compare the gradient magnitude of the center pixel with the neighbors along the gradient direction instead of all the neighbors. To simplify the implementation, one can quantize the gradient direction into 8 groups and compare the center pixel with two of the 8 neighbors in the 3×3 window according to the gradient direction. For example, if the gradient angle of a pixel is 30 degrees, we compare its gradient magnitude with the north east and south west neighbors and suppress its magnitude if it's not greater than the two neighbors.