Due April 20, 2025 (11:59pm EDT)

1. Introduction

Large Language Models (LLMs) have demonstrated remarkable improvements in mathematical and symbolical reasoning through *Chain-of-Thought* (CoT) (Kojima et al., 2023; Wei et al., 2023) prompting. Recent approaches use inference time scaling by prompting LLMs to produce long context CoT for guiding the models. For example, models like OpenAI-o1 OpenAI (2024) and DeepSeek-R1 DeepSeek-AI et al. (2025) show that reasoning quality increases significantly when intermediate thoughts are generated before making predictions.

In this homework, we investigate whether a small encoder-only classification model (BERT) Devlin et al. (2019) can benefit from such CoT supervision, even though BERT is not auto-regressive. The goal is to determine whether intermediate reasoning steps generated by another model (Flan-T5) Chung et al. (2022) can improve BERT's final predictions in multiple-choice QA tasks.

Flan-T5 is an encoder decoder model which is pre-trained in an instruction prompt fashion Ouyang et al. (2022) to support the CoT style reasoning.

Dataset: We use the MMLU Hendrycks et al. (2021) dataset, which includes multiple-choice questions across various disciplines. Each question is associated with four options (A, B, C, D), out of which only one option is the correct choice.

• Train Split:

- high_school_mathematics
- machine_learning
- high_school_computer_science

• Test Split:

college_computer_science

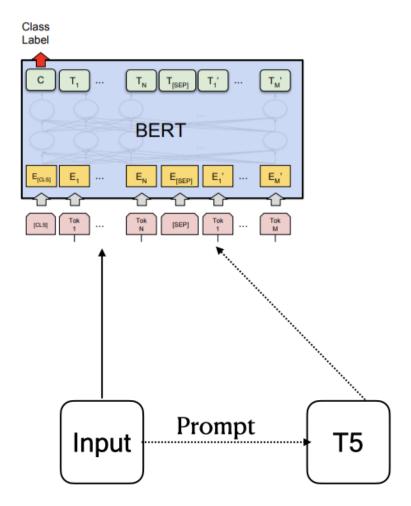


Figure 1: Pipeline overview: Input contains the QA example as input to BERT and optionally (dashed arrow) to T5 for augmenting CoT for the answer label classification

1.1. Design.

- 1.1 We evaluate the usefulness of reasoning in the form of Chain-of-Thought (CoT) to BERT using the input format shown in Fig. 1. BERT receives both the original question with options, and optionally the CoT reasoning as part of its input.
- 1.2 We use the Flan-T5 model, which is trained on CoT-style tasks, to generate the CoT reasoning for BERT input context. This model is frozen unless otherwise fine-tuned by you.
- 1.3 The next step is to fine-tune the Flan-T5 model. This allows learning from task-specific CoT style and encourages better generalization. We provide gold CoT for the train split for fine-tuning. The gold CoTs were generated using another LLM, we control for the quality but given the fact that they are generated by LLM would add some noise. However, it is a good starting point for fine-tuning.
- 1.2. (Extra Credits) Handling Longer Context BERT. BERT has a maximum context length for the input, in our design the max length is 512. However, in some cases

the input with the question + options + CoT could be longer than 512, which would be truncated, therefore throwing away some information. One technique to represent longer context is using sliding window to segment the long input into multiple sequences. You start with the first 512 tokens of the input, then slide the start to be the 256 token (512/2) and take the next 512 tokens, and continue to iterate. Basically you always take a context length of T tokens (T = 512) to form a sequence and then the next sequence starts after T/2 tokens, so that and every sequence pair overlaps T/2 tokens. Then pass all the list of sequences individually to BERT, to obtain list of [CLS] representations. You then need to pool all these [CLS] representations to obtain a final representation. This can be implemented using a BiLSTM or you may use a fixed size neural-network to compute the final embedding. The sliding window technique is discussed in this paper Sec 2.2 BERT Overlap (Joshi et al., 2019).

2. Coding

The goal is to implement the training functions for BERT and T5 within the provided codebase. You will find a starter code repository with:

- 'main.py': the main design file (with evaluation)
- 'README.md': instructions and dataset field descriptions
- 'data/': contains 'train.csv' and 'test.csv' files

You will need to implement the training methods and complete the <code>generate_CoT(...)</code> method. You have the implementation flexibility, by making design choices, helper functions, adding optional arguments to any method, but you **must not change** "the function signatures and return types of all the provided methods". **Follow** the instructions in README. Also, by default we use the small size of the LMs, please do not change them as we are constrained with the compute budget.

You are required to save and evaluate predictions for all the possible designs, i.e. the six combinations of flag settings described in the README:

- 1. No training, no CoT
- 2. No training, with CoT
- 3. Train only BERT (no CoT)
- 4. Train only BERT with CoT
- 5. Train only T5 with CoT
- 6. Train both BERT and T5 with CoT

Each run should produce a CSV file in the format:

```
test_pred_Bert_<bert_train>_CoT_<cot>_T5_<t5_train>.csv
```

Most of the logic is handled in def predict(...) and main().

GPU Access: You may use GPUs for faster training. The CS department clusters provide access to GPU nodes. Follow these instructions:

- SSH login: ssh username@data.cs.purdue.edu (works without VPN).
- From there, use ssh queue to access GPU nodes.
- Use squeue to list available GPU nodes. Jobs can be scheduled using slurm.

Coding Evaluation: We will run your code for each combination of train, no-train, and CoT, which should produce a csv and the accuracy score.

Points Breakdown:

- Coding: **75 points** + Extra Credits (10 points)
 - **50** for working code (partial credit for partial implementation)
 - -25 for max Acc > 30% (we compute the max accuracy across all the 6 settings)
 - 10 for optional extra credits
- Discussion: 25 points

Discussion Questions

(A: Abhishek will grade the question, N: Nathaniel will grade the question) Answer the following questions:

1. Compare Results Across Settings. Create a table reporting the accuracy from each of the six experiment settings. Use the *no-training*, *no-CoT* configuration as your baseline (i.e., pre-trained BERT predictions on the test set).

Then, answer the following:

- How do the other five settings compare to the baseline?
- Does adding Chain-of-Thought (CoT) help or hurt performance?
- What impact does training BERT or T5 have on accuracy?

Support your analysis with two examples from the test set:

- (a) One example where BERT alone is correct but BERT + CoT is wrong
- (b) One example where BERT + CoT is correct but BERT alone is wrong

Briefly describe what the CoT helps capture in these examples, or why it may confuse the model. (8 points; A)

- 2. Generalization and Transfer. The training data includes high school-level mathematics and computer science questions. The test set contains college-level computer science. Reflect on the following:
 - Do you believe your BERT model is learning general concepts that transfer to more difficult questions?
 - Use both your accuracy table and qualitative examples from above to support your reasoning.
 - Do you see evidence that the model is combining concepts from different subjects (e.g., math + CS)?

Now, suppose the task was much simpler — like basic grammar correction. Would your answer about the usefulness of CoT reasoning or model (any Language Model) training change? In what types of tasks does reasoning seem most beneficial, and where does it add little or no value? (6 points; A)

- 3. Applying CoT Elsewhere. Consider the task of training an autoregressive LM to find the shortest path between two vertices, given a set of labeled vertices and a set of undirected edges between them (i.e., G = (V, E)) in text form.
 - What might a CoT response look like in terms of this problem?
 - Is there a specific type of graph that would allow the model to make good use of CoT?
 - Is there a specific type of graph that the model would likely be unable to solve even with CoT?

```
(6 points; N)
```

4. Attention and CFGs Consider the following CFG from the lecture slides:

```
S → NP VP

VP → V NP

PP → P NP

NP → NP PP

NP → N

V → 'saw'

P → 'with'

N → 'binoculars' | 'Sally' | 'Alex'
```

What might one of a perfectly trained auto-regressive transformer's attention pattern (i.e., attention weights) look like if the model has perfectly learned this CFG? In other words, if given the sentence, "Sally saw Alex with binoculars", what word(s) would attend to the word "Alex" the most in an ideal attention head? How does that relate back to the original CFG rules? The transformer is decoder-only (there is a causal mask). (5 points; N)

5. Optional Extra Credit: Briefly describe your implementation for handling longer context for BERT and create another table by expanding the table from Q1 and reporting the performance with longer context, side by side for each design. (10 points; A)

Submission Instructions

• Code: Place your code in a directory called hw2_dir and submit your code using the turnin command on the CS machine (antor or data):

Verify your submission using: turnin -c cs577 -p hw2.

- Discussion Questions: Submit a typed PDF of your answers on **Gradescope**.
- If you are unable to access your account on the cs machine (only) then please email your coding submission to one of the TAs.

References

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