

MATH 242 - Quiz 10

04/25/2024

1. [4 pts] Find the general solution of the differential equation.

$$e^{-y}y' + \cos(x) = 0$$

$$\int e^{-y} dy = \int -\cos(x) dx$$

$$-e^{-y} = (-\sin(x))$$

$$e^{-y} = (+\sin(x))$$

$$-y = \ln(+\sin(x))$$

$$\boxed{\begin{aligned} y &= -\ln(+\sin(x)) \\ &= \ln\left(\frac{1}{(+\sin(x))}\right) \end{aligned}}$$

2. [6 pts] Find the general solution of the differential equation.

$$y' + \frac{xy}{2} = 2x$$

$$e^{\int P(x)} = e^{\int \frac{x}{2}} = e^{\frac{x^2}{4}}$$

$$e^{\frac{x^2}{4}} y' + \frac{x}{2} e^{\frac{x^2}{4}} y = 2x e^{\frac{x^2}{4}}$$

$$\int \frac{d}{dx} [e^{\frac{x^2}{4}} y] dx = \int 2x e^{\frac{x^2}{4}} dx$$

$$e^{\frac{x^2}{4}} y = 4e^{\frac{x^2}{4}} + C$$

$$\boxed{\begin{aligned} y &= 4 + \frac{C}{e^{\frac{x^2}{4}}} \\ &= 4 + C e^{-\frac{x^2}{4}} \end{aligned}}$$