-Axes labels of variance, etc

-Cite Akoglu\*\*

-if modify anomaly threshold do we need to change bayes to find it. (plot alpha bayes and theta\_anomaly\_trace). The question is the generalization of the bayes threshold.

-Definition of anomaly: review

-need definition of” anomaly”

Abstract

Process mining of unstructured, noisy environments remains an important area of process mining and graph research. This paper presents an unsupervised, threshold-based method of anomaly detection and process mining using the iterative SUBDUE graph-compression method and the Inductive Miner. We provide an overview of process mining definitions and existing approaches, then evaluate the method on synthetic data over a range of parameters. Experimental results show 96% accuracy on an anomaly detection task for reasonable synthetic parameters, as well as smoothly decaying performance metrics across a range parameters. The method generates a taxonomical representation of compressing structural features of a workflow log, a dendrogram, by which further analysis can be performed. We demonstrate one such use by performing anomaly detection with this feature representation of a process log, using a Bayesian threshold to detect unusual substructure in the context of normal behavior, thereby identifying unusual process executions. This method provides a framework for modeling and monitoring unstructured and noisy organizational, technological, and natural processes.

Introduction

As described in [1], a Process Aware Information System is, “a software system that manages and executes operational processes involving people, applications, and/or information sources on the basis of process models” (p. 5). This definition formalizes operational management systems as systems which centralize awareness of process data and the ability to prescribe tasks and activities via process models. These tasks form a loop by which processes can be defined, tracked, and evaluated using process models; likewise, process models may be derived and analyzed from process data.

However, many institutions instead rely on interwoven and non-interoperable systems to monitor and control processes, making the formal requirements of a centralized PAIS infeasible or intrusive. This paper focuses on contexts where a PAIS is instead an abstraction consuming process data derived from multiple systems. This is amenable to realistic scenarios in which processes execute within an embedded and non-stationary framework of changing people, tools, resources, and tribal knowledge, in the absence of prescribed process models. These scenarios are frequent, since modeling such environments often occurs only due to some ad hoc objective, such as an audit or root-cause analysis. In these scenarios, a PAIS is a disparate collection of operational systems and data sources by which to derive traces characterizing the underlying process-oriented view of a system.

The ability to mine and analyze normative process patterns in unstructured contexts is critical for mining regular activity and for detecting anomalous activity. The former requires prior normative activity models, thus anomaly detection and normative pattern mining are complementary tasks. For this, we present a method for mining process patterns from workflow logs with useful anomaly detection properties. We use the Inductive Miner [2] to construct a graphical process model from log data, then iteratively apply the SUBDUE [3] graph compression method to extract a hierarchical dendrogram of normative patterns executed on this model. In subsequent post-processing, anomalies and other useful features are discovered.

This hybrid approach is practical since the Inductive Miner extracts generality from process log data, outputting a graphical model *M* capable of generating all traces in a process log, including log noise. SUBDUE then extracts from *M* only its most informative components, constructing a hierarchy of sub-structures of *M* most relevant to the log as a dendrogram. Using this unsupervised method, one can mine normative process patterns, detect anomalies to those patterns, and perform other analyses.

This captures the spirit and contribution of our method, but requires a few definitions within this work. From the control-flow perspective, common process mining terms can be framed in a graph theoretic manner:

* Process model: A graph with vertices representing activities, and edges representing one-step transitions between activities. Processes can contain many constructs representing linear and non-linear constructs, and a variety of notations and languages have been defined over the space of process models. A canonical example is the Petri-Net [4] [5].
* Workflow trace: A single execution of a process as a partially-ordered sequence of activities, following any valid path from a START to an END node on a process model. These are represented as a string composed of letters representing the activities traversed.
* Workflow log: A set of workflow traces, for which various measures are taken to mitigate properties of noise or incompleteness.
* Process miner: Any algorithm for constructing a process model from a workflow log, and often incorporating criteria for model complexity, specificity, and generality. Specificity favors restrictive models including only or even less than the behavior described by the workflow log, whereas generality favors larger models describing all traces but possibly additional behavior.
* Partial-order property [18]: A property of workflow traces whereby activities may be randomly-ordered with respect to parallel sub-processes. ‘ABCD’ and ‘ACBD’ might be workflow traces from some model, where ‘C’ and ‘B’ are parallel sub-processes, and may recursively embody further parallel sub-processes, and ‘A’ always occurs before ‘D’. The primary task of process mining algorithms is disambiguating the partial-orderings, applying rules and heuristics to generate models with desired properties of complexity, specificity, and generality. The enormous search space of possible graphical models defined over a set of partially-ordered traces is the primary challenge for these algorithms.
* Process grammar: Recursively-defined constructs for common process patterns. For example, AND-SPLIT is a set of edges branching from a single node and traversing activities in parallel before synchronizing at some later activity. Other basic constructs include OR-SPLIT, XOR-SPLIT, LOOP, and JOIN [14] [15].
* Spaghetti model: A workflow defined by highly diverse, informal, and disorderly behavior, typically containing many scattered, repetitive events. These represent unstructured business processes, in contrast to orderly “lasagna” processes with prescriptive, stratified behavior.
* Inductive miner: A process mining algorithm capable of generating the most general, all-inclusive process model of the traces in some log. For our purposes, this model is used to convert a workflow log of traces into a collection of subgraphs for input to SUBDUE [2].
* SUBDUE: Short for “Substructure Discovery”, this method implements a subgraph beam search over a graph collection and, by applying the minimum-description length (mdl) heuristic, returns the top-k most compressing sub-graphs of the collection [3].
* GBAD: Acronym for “graph-based anomaly detection” [6], this method internally calls SUBDUE, then implements methods for detecting anomalies occurring in the context of discovered patterns.

An in-depth overview of process mining terms and methods can be found in [1] and [7].

Previous Work

An extensive overview of graph compression and anomaly detection is provided by Akoglu [20]. The SUBDUE graph-compression method accommodates any context of mining graph data for normative patterns, working as a graphical feature detector. It was previously used for knowledge representation systems [1], and more recently in security applications for intrusion detection [8]. Using SUBDUE as a process mining tool was successfully performed by [9] and more recently by Genga [10], whose results demonstrated the method’s utility for “spaghetti processes” describing more realistic institutional processes.

GBAD formalized SUBDUE’s anomaly-detection capabilities, particularly within the immediate proximity of normative graphical patterns. This is appropriate for safety-critical and security contexts possessing some underlying process model by which normative patterns can be assumed to have a ground-truth behavioral policy, but less so when there is no such policy or model. An application is given by Holder and Eberle, in which GBAD was used for insider threat detection by combining three anomaly detection algorithms [16].

Process-mining anomaly detection focuses primarily on the mining process itself and on trace-scoring schemes. W. van der Aalst [12] details scoring schemes, by which work traces are replayed on a discovered model, assigned a numeric fitness score, and anomalies flagged based on a discriminative threshold. Bezerra’s work [11] examined anomaly detection using several threshold-based approaches within the process mining algorithm itself. Bezerra decomposed this family of process-based anomaly detection into three groups: scoring based, iterative, and sampling. Our approach does not fit squarely into these categories since it is compression based: a generic process model is mined, graphical features detected, and anomalies are detected and reported in post-processing. Likewise, whereas previous works focused on individual traces, our feature-based approach provides structural insights into normative patterns and anomalous features. Our work replicates Bezerra’s data generation scheme, but otherwise adds a new method to this work.

The Method

Under our relaxed definition, a PAIS is a composition of process monitoring systems by which workflow traces are extracted for process mining in a standard log format, such as Extensible Event Stream (XES) [17]. Our method decomposes to three tasks: converting such a log to a collection of subgraphs via a mined process model, extracting descriptive normative graphical patterns of the log (with respect to this model) as a dendrogram, and lastly detecting outliers and anomalous behavior.



For the first task, the Inductive Miner was suitable for mining the most general graphical process model described by some log. This model is typically overly-inclusive, whereas the second and third tasks discover the patterns and features more precisely relevant to the log. For this, we use the SUBDUE graph-compression method to discover normative behavioral patterns, subsequently permitting anomaly detection.

The workflow extends the discovery of overall process characteristics irrespective of prior constraints, such as a prescribed process model. Our approach encompasses more realistic and informal “spaghetti” model scenarios in which processes are organically-defined and highly unstructured, such as enterprises, communication networks, distributed systems, software execution, or natural processes.

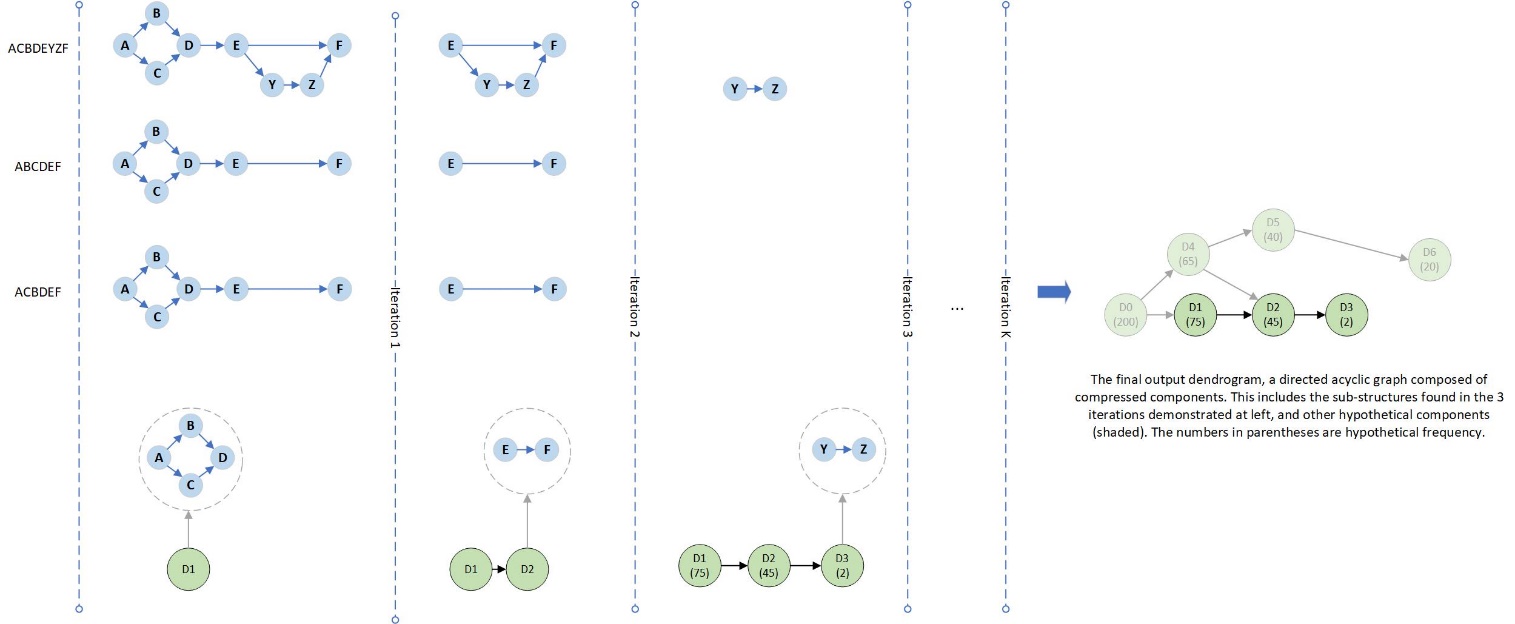
Using Graph Compression to Discover Patterns and Cluster Traces

SUBDUE discovers highly compressing patterns in graph data via the minimum description length (MDL) principle and a beam search over candidate subgraphs. This satisfies the requirement for an unsupervised method of discovering the most meaningful components of a graphical process model, since a workflow log is also a set of subgraphs generated by a process model. The Inductive Miner complements this approach by providing the super-graph for converting a log of partially-ordered traces into subgraphs; these subgraphs are passed to SUBDUE to discover meaningful graphical patterns.

Prior work showed strong anomaly-detection results when running SUBDUE iteratively on a set of graphs [8]. At each iteration, the most compressing subgraph discovered by SUBDUE was used to replace all such instances with a single node, and the method repeated until no further compression was possible. At the end, the authors obtained a recursive and hierarchical description of a set of graphs, by which they modelled their anomaly-detection activities.

We tested a similar approach using GBAD, by which workflow traces were iteratively recompressed using the most-compressing subgraph found at each iteration. The three anomaly detection methods of GBAD were used to detect anomalies at each iteration. While successful for discovering patterns, this method suffered a very high false positive rate for anomaly detection. Ultimately the issue was iterative recompression: on successive iterations, the most highly compressing subgraph was often only a small alteration (node substitution, deletion, or insertion) to a compressing subgraph found by a previous iteration. GBAD’s primary deficiency in this context is that its anomaly-detection methods apply to the local vicinity of the compressing pattern discovered by SUBDUE. Hence, the search space was highly redundant, repeatedly analyzing the same regions of the process model, progressing very slowly toward the outlying model regions where compressing structure decays, and where anomalies often lie.

Since the desire was to force SUBDUE to analyze new regions, the remedy was to simply delete all instances of the most-compressing subgraph from the traces at each iteration. This forces SUBDUE to discover regularity in new regions at each iteration, and thus to discover dissimilar graphical features. Compressing graphical features (substructures) are thus compressed away in order of higher information to lesser information, as such:



The approach loosely resembles data dimensionality reduction, in which data is compressed via an ordered set of vectors of decreasing information. Except vectors are replaced by graphical substructures forming a lossy hierarchical derivation of process substructures as a dendrogram. This representation is currently lossy, since any edges connecting to a compressing substructure are deleted with the substructure, and could not be deterministically reconstructed from the dendrogram. Otherwise the dendrogram comprises the entire behavior of the log, with the ancestral components reflecting its most relevant (most compressing) graphical features. This is amenable to anomaly detection since the less compressing a feature is, the greater its deviation from normative patterns and normal overall behavior, and hence it will be located “deeper” in the dendrogram and with lower frequency.

This gives the following process-oriented pattern-mining algorithm:

**Algorithm 1: SUBDUE-based Process Log Compression**

**Input** *miner*: A process mining algorithm (e.g., the Inductive miner)

*log*: A trace log from some process

**Output** *dendrogram*: A graphical decomposition of the log’s structural features

1. model = mine(miner, log) #mine the graphical process model
2. traceGraphs = convert(model, log) #regenerate the log traces as graphs, using model
3. dendrogram = {}
4. until empty(traceGraphs):
5. bestSubstructure = MineBestSubstructure(SUBDUE, traceGraphs)
6. dendrogram = AddSubstructure(dendrogram, bestSubstructure)
7. traceGraphs = DeleteSubstructure(traceGraphs, bestSubstructure)
8. return dendrogram

As described, the Inductive Miner takes a workflow log and returns a process model by which the traces are converted to graphs. This collection is iteratively fed to SUBDUE to discover the most compressing substructure, which is appended to the dendrogram, then deleted from all traces in which it occurs. This repeats until no further progress can be made, and all traces have been compressed to their most elementary substructures. The dendrogram is returned, whose vertices represent compressed substructures, and whose edges represent trace-ancestry between compressing substructures.

The strength of this method lies in the dendrogram as a descriptive model of the input log. The dendrogram can be analyzed in post-processing for frequent process features, redundant behavior, outliers, and anomalies. Diamintini *et al* [13] successfully implemented a variety of uses for similar SUBDUE-based dendrograms, especially in the context of spaghetti processes.

This method of frequent-subgraph mining of workflow logs belongs to the family of dendrogram- or tree-induction methods in process mining literature [19], for which anomaly detection is only one application. For instance, while the low-frequency, outlier components of the dendrogram characterize anomalies, outliers, and noise, the ancestral components encode the most relevant substructures of the log. Using this information, the process model returned by the Inductive Miner could be reduced for greater specificity. For instance, the underlying properties of an unstructured institution could be discovered, and thereby the process could be identified, measured, and improved via business-process formalisms.

In this regard, coupling SUBDUE with the generalization feature of the Inductive Miner lends an extensible framework for more concise modelling of unstructured “spaghetti” process environments. Similarly, an analyst may examine highly similar components of the dendrogram, likely indicating duplicate work or poor cohesion among business processes. In summary, the dendrogram extends to a range of pattern mining and other enterprise uses, beyond the scope of anomaly detection.

Anomaly Detection Method

Anomaly detection lends an illustrative example because of the structural characteristics of the dendrogram: given that anomalies are assumed to be infrequent events in the context of regular structure, subgraphs containing anomalies will be among its lower-frequency components. As a result, the size of the dendrogram components decreases smoothly, then drops suddenly, such that the only remaining traces/subgraphs are those representing anomalies, outliers, and noise.

This property is useful for anomaly detection objectives since many discriminating metrics could be devised to differentiate anomalies, noise, and regular patterns. Given that anomalies occur in the context of regular behavior, the anomalous structures tend to have sharply lower frequency than their parent substructures in the dendrogram. Further, they are also distinguished from noise in the input log, since noise tends to result in poorer structural decomposition of a trace, and as such, substructures characterized by noise and their parents tend to both have lower frequency. Hence, finding anomalies resolves to finding these sharp boundaries between high frequency substructures and relatively lower frequency substructures adjacent to them.

A Bayesian metric was selected to capture this property, based on the frequency of substructures and their parent (immediate ancestor) substructures in the dendrogram. This metric was chosen because it discriminatively quantifies the relationships between parent and child substructures such that unusual child substructures have very low probability. Under this model, each substructure is assigned a Bayesian probability defined as:

Where unconditional prior substructure probabilities like are defined in terms of the global probability of a substructure in any trace, or , where the ‘#’ operator returns the frequency of substructure *s*. Characterizing the numerator is trickier, since it involves defining the probability of a parent relating to one of any of its children, where parents may have multiple children, and children may have multiple parents. Hence, one must sum over all parents of a given child, a joint set of independent events (since substructures are independent), with each event weighted by its likelihood :

The repeated looks unusual, but correctly weights each summation component’s contribution as required to obtain a proper probability distribution. Substituting ‘c’ for child, ‘p’ for ‘parent’, and ‘P’ for ‘parents’, the fully-defined metric becomes:

An awkward looking probability, but nonetheless the properly weighted result from defining the Bayesian interpretation for the probability of a child given its parents. Anomalous substructures are expected to have a low value for , and a substructure is flagged as anomalous when , where is the anomaly threshold. Traces containing the anomalous substructure are then flagged, as follows:

**Algorithm 2: Dendrogram-based Anomaly Detection Using a Bayesian Threshold**

**Input** *dendrogram*: A dendrogram, as output by Algorithm 1

bayesThreshold: An anomaly detection threshold

**Output** *anomalies*: A set of trace-id’s identified as anomalous

1. anomalyIds = {}
2. for vertex in dendrogram:
3. bayesProbability = (vertex)
4. if bayesProbability < bayesThreshold:
5. traceIds = GetVertexTraceIds(vertex)
6. anomalyIds = anomalyIds traceIds
7. return anomalyIds

Algorithm Evaluation

Although real process-oriented datasets are available, they do not offer the controlled conditions sufficient to compare the characteristics of different algorithms. Instead we used a synthetic data generation algorithm as found in appendix A of [11], modified slightly to generate data directly from probability distributions embedded in the generated models. This approach generates random process models from which synthetic traces are generated, and thus the performance of an anomaly detection method can be assessed with respect to a known model and known trace-generation parameters. To cohere to a stable performance baseline, we also used the same model generation parameters as described in [11]: 60 randomly-generated process models, 1000 traces.

Data Generation Algorithm

Data generation consisted of two steps: generating process models and generating traces from them. The parameters described the probability of recursively generating various structural features, including SEQ, OR-SPLIT, AND-SPLIT, and LOOP, defined as follows.

SEQ: the appending of a single activity.

OR-SPLIT: a single activity splitting to one of two successors.

AND-SPLIT: a single activity splitting to two parallel activities, both of which are traversed.

LOOP: An activity splitting to an optional loop, then returning to the activity.

These recursive operators generate directed, potentially cyclic graphs of arbitrary complexity, with the constraint that the graph start at a single START node and all paths eventually terminate at a single END node. Additional complexity results by including the null transitions in the set of “activities”, and as such the split constructs may divert to more than two activity paths or may bypass components of a model. The parameters constrain model complexity to a probability distribution over these operators, replicated from Bezerra [CITE] and fixed throughout this work.

Since probabilistic model-generation allows for the possibility of unusual or task-trivializing models, additional basic tests were applied to ensure sufficient complexity. These included verifying the models contained a minimum START to END path length of 1, maximum of 1 anomalous structures, maximum of 4 anomalous edges within an anomaly (to constrain anomaly size), minimum of 10 unique activities, and minimum of 10 unique paths from START to END for adequate model complexity.

A second parameter set defined the trace-generation distribution constraining the graphical walks of traces, which is only defined for the choice operators OR-SPLIT and LOOP. These parameters determine trace diversity, from very uniform to very non-uniform. A value of implies the trace-generation scheme has a 0.9 probability of taking one branch and a probability of taking its alternative. Thus, by varying from very uniform (0.5) to very non-uniform, one derives a less uniform distribution of traces, making anomaly detection more difficult. To ensure maximum partial-order entropy, activities lying ambiguously within the same timestep were shuffled to achieve uniform random partial order.

Lastly, the parameters defined the probability of generating anomalies. These encompassed both the generation of anomalous model structure and their embedded traversal probability when generating traces. Anomalies in this context are defined as unusual behavior occurring in the context of regular behavior, hence in this work we desired to generate insertion, substitution, or deletion anomalies in the context of more frequent behavior. LOOP and OR constructs were marked as anomalous with fixed probability 0.3. Anomalous paths were marked with traversal probability that was experimentally varied between 0.0 and 0.2 and evaluated in increments of 0.02. This overall method generated insertion, substitution, and deletion anomalies (since OR branches may be mere null transitions). Notably, embedding anomalies probabilistically allows for generated logs to contain no anomalies. This is important to include in synthetic data, to verify that a method is not simply over-generalizing and flagging anomalies when none exist.

In this manner, the models output by this method were guaranteed to achieve sufficient complexity and to generate an exponential distribution of unique traces [COULD INSERT TRACE-DIST VISUAL].

Noise Generation [obsolete?]

The model and trace generation methods are sufficient to generate spaghetti-like process data in terms of model complexity via and activity complexity via , but remain constrained to the given model. For example, under this data generation method there will be no log ambiguity as to whether anactivity occurs before another if it always lies upstream in the paths contained in the model; hence, the underlying model strongly constrains the generated data. Although likely unusual, one might expect unstructured work environments to inevitable lead to occasional repetitions, whereby sub-components of some model are repeated or activities do not always follow one another. Such a scenario occurs, for instance, if prior to some software release a bug is detected after final testing, causing components of the testing activities to be repeated arbitrarily with respect to the software development process.

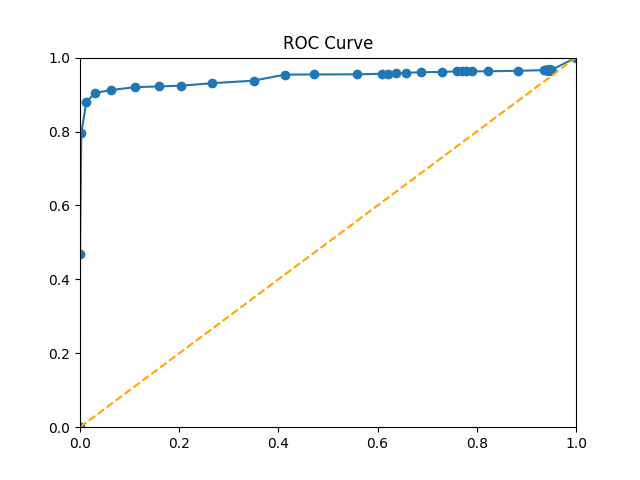
The simplest way to simulate worst-case noise is to randomly inject activities into the traces after trace generation. For every activity in each trace, with probability a random activity is inserted. The chosen activity is selected at uniform random from the set of all activities defined over the log. This method of noise addition is necessary to test our approach’s resilience to noise, and is justified since it creates many data outliers that would be too easily declared anomalous by an anomaly detection method that does not distinguish outliers from anomalies. Note that even small values of tend to create highly obfuscated partially-orderings for a process mining algorithm to mine: for a log of 1000 traces, for which the average trace length is 25, an value of 0.1 will have an expected number of “noise” activity occurrences of 0.1 \* 25 \* 1000 = 2500. This is an extreme number of random activities, since even a single misplaced activity with respect to the underlying model, breaks the logical rules and heuristics applied by process mining algorithms to mine the regular features of the underlying process model.

Experiment

To test our method, we desired datasets achieving “spaghetti” like behavior described previously. For each of 60 models generated under , 1000 traces were generated under for 0.5, 0.6, 0.7 and 0.9. For each of these, the method was run for all values of in increments of 0.02. The run-time per log was around 1 minute, and the experiment required about 6 hours total, some of which was merely result compilation. Accuracy, precision, recall, f1-measure were then averaged over the over the 60 test models for each combined value of and , giving the following plots and ROC curve:

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Notably, for all four performance curves, performance degraded only slightly along the axis for higher values, indicating the method worked well for very skewed trace distributions. Instead, impacted performance most strongly. From the top-left, accuracy maximized around , then tapered gradually as higher values decreased the true-negative rate (TN). Recall, the ability to catch all anomalies, was quickly maximized for lower values of as one might expect, for larger anomaly-detection thresholds. Precision and the f-1 score are perhaps more informative, since precision clearly influenced the f-1 score much more than recall. The plots for precision and f1-measure are nearly identical since recall quickly maximizing for **>** 0.15, and subsequently precision dominated the f1-measure. The f-1 score results are most informative in terms of selection, suggesting that one choose an value of around 0.07, with a corresponding accuracy of 96%.



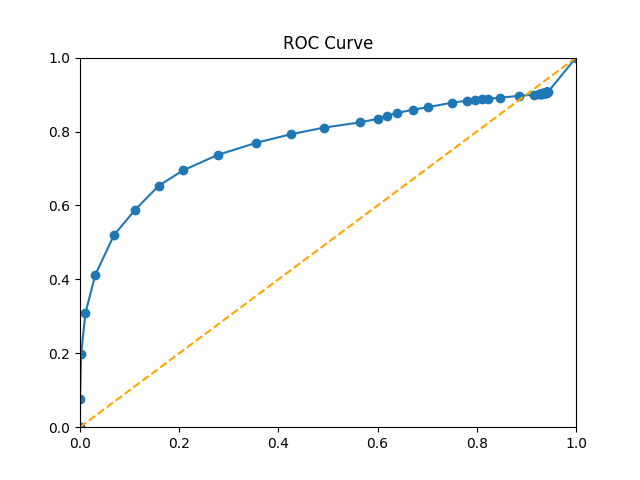
Additionally, we plotted the receiver-operator characteristic (ROC) curve TPR/FPR values for all values of in 0.02 increments, averaged over all 60 models and all values of . The area under the ROC curve is clearly very near 1.0, indicating a high true-positive rate.

The results show lower values (0.04-0.10) of are preferable, and tunable to suit recall vs. precision objectives. From a risk perspective, recall is most important in terms of capturing all anomalies, at the expense of decreasing accuracy and precision. On the other hand, precision and f1-measure provide better comparative performance metrics, and show significant room for improvement. However, the sharp maximum of the precision curve along the axis indicates the method and the Bayesian metric worked as intended, distinguishing anomalies from regular structure with a sharp boundary, for the synthetic dataset. As is often the case for anomaly detection, the test threshold is tunable for the desired performance objective in terms of either maximizing recall and tolerating false positives, or maximizing accuracy at the expense of a few false negatives.

The previous experiment analyzed performance over a range of and , but with fixed to 0.05.A second experiment analyzed the sensitivity of the result with respect to , andwith fixed. This was done to verify that the previously fixed didn’t trivialize the task of anomaly detection. In this case, , and was varied between 0.0 and 0.2 in increments of 0.02, then in increments of 0.05 between 0.25 and . A choice of yields a more uniform distribution of traces; and the low range of was expected to trivialize the discovery of anomalies due to their low frequency, whereas the high range approached , making anomalous substructures and normal substructures ambiguous.

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As expected, all four metrics performed more poorly along the axis nearer to 0.5. However the decay was smooth, showing the method works satisfactorily for a range of very rare and somewhat frequent anomaly occurrence rates, with respect to a somewhat regular process. The ROC curve bears this out, demonstrating the likely expected performance on real world data here  and are not known in advance.



Conclusions and Future Work

Overall, these results indicate this method succeeds for a range of model complexity, trace regularity, and anomaly frequencies. The expectation is that real-world data contains enough traces and sufficient regularity to discover regular graphical patterns. Additionally, the method is tunable via the parameter to suit different data sets and performance objectives.

A notable advantage of this method is that such an unsupervised approach requires no prior process model, nor exceptional tuning to derive normative patterns for a process. This makes it an extensible exploratory tool when applied to processes with no prior definition or pre-defined policy. Such processes occur often in computer networks. distributed systems, or in the context of communication protocols, for which detecting anomalies in the extrinsic process behavior of such systems is critical. A final advantage is that the method is capable not only of flagging anomalous traces, but also of causally identifying their anomalous features.

The drawback to this method is its specialized noise-tolerance, a common problem faced by mining algorithms. SUBDUE finds graphical patterns in an unsupervised way, but these become the only patterns by which the log is recompressed; such that even small deviations to a normative pattern are ignored, and may be flagged as anomalies later. This strongly discriminatory behavior is desirable for anomaly detection. However, within process mining, the goal is sometimes to mitigate such strong discrimination, balancing a noise-tolerant tradeoff between specificity and generality. Essentially, this substructure decomposition of our approach is both a strength and a potential criticism, and yields the recurring process-mining discussion on specificity-generalization tradeoffs.

Future work lies in making the approach more noise tolerant, as the GBAD system determines acceptable deviations in the local context of a normative pattern discovered by SUBDUE using graph distance metrics. Likewise, the runtime of the algorithm may be increased by specializing the complexity of the beam search over candidate compressing substructures to be more specific to process mining.

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