## MASx52: Assignment 3

- 1. Consider the binomial model with  $r = \frac{1}{11}$ , d = 0.9, u = 1.2, s = 100 and time steps t = 0, 1, 2.
  - (a) Draw a recombining tree of the stock price process, for time t = 0, 1, 2.
  - (b) Find the value, at time t = 0, of a European call option that gives its holder the option to purchase one unit of stock at time t = 2 for a strike price K = 90. Write down the hedging strategy that replicates the value of this contract, at all nodes of your tree.

You may annotate your tree from (a) to answer (b).

- 2. Let  $S_n = \sum_{i=1}^n X_i$ , be a random walk, in which  $(X_i)_{i \in \mathbb{N}}$  is a sequence of i.i.d. random variables with common distribution  $\mathbb{P}[X_i = \frac{1}{i^2}] = \mathbb{P}[X_i = -\frac{1}{i^2}] = \frac{1}{2}$ .
  - (a) Show that  $(M_n)$  is a martingale.
  - (b) Show that  $\sup_n \mathbb{E}[|S_n|] < \infty$ .
  - (c) Determine if  $\sup_n \mathbb{E}[|S_n|^2]$  is finite or infinite.