

# EME 152 Discussion 9

November 24, 2021

# Agenda

- Derivation of slider velocity
- Input/output torque example
- Three-position synthesis example

# Derivation of Slider Velocity

# Input/output Torque Example

- Setting US/SI units is now very important!
  - Set the unit system with `uscUnit(true)` for US units and `false` for SI units.
- In the `CFourbar` class:
  - Use the function `setGravityCenter()` to set the gravity center properties (including  $r_g$  and delta) of links 2, 3, and 4.
  - Use the function `setInertia()` to set inertial properties of links 2, 3, and 4.
  - Use the function `setMass()` to set the masses of links 2, 3, and 4.
  - Use the functions `forceTorque()`, `forceTorques()`, and `plotForceTorques()` to calculate or plot forces on joints in the four bar linkage mechanism.
- Visit the Ch Mechanism Toolkit file in *C-STEM Studio > My Workspace > LearnMechanism > chmechanism.pdf* for the parameters and return value of these functions.

01\_forceTorque.ch

02\_plotForceTorques.ch

# Four Bar Linkage Position Synthesis

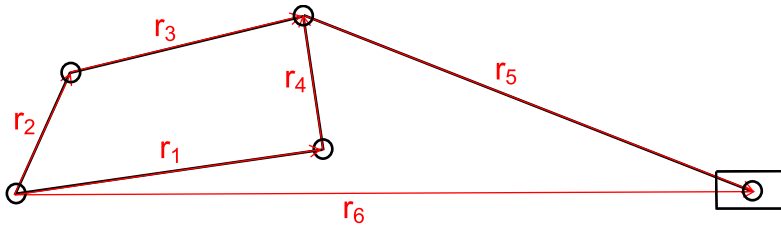
- Need to have  $\phi_1$ ,  $\phi_2$ ,  $\phi_3$  and  $\psi_1$ ,  $\psi_2$ ,  $\psi_3$  in radians.
- In the `CFourbar` class:
  - The function `synthesis()` requires an empty array for the length of links `r[1:4]`, an array of the input angles `phi[1:3]`, and an array of the output angles `psi[1:3]`. This function synthesizes the four bar linkage and generates the array `r[1:4]` which you can then use in the function `setLinks()`.
  - After using `setLinks()`, you can treat the `CFourbar` class like a normal four bar mechanism and you can call any other function (e.g. calculating forces and torques, animating, etc.)

03\_synthesis.ch



# Thank you!

Questions? Email!



# Fourbar Slider Acceleration Derivation

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## 1 Derivation

$$\vec{r}_6 = \vec{r}_2 + \vec{r}_3 + \vec{r}_5 \quad (1)$$

$$r_6 e^{i\theta_6} = r_2 e^{i\theta_2} + r_3 e^{i\theta_3} + r_5 e^{i\theta_5} \quad (2)$$

$$\dot{r}_6 = r_2 i \omega_2 e^{i\theta_2} + r_3 i \omega_3 e^{i\theta_3} + r_5 i \omega_5 e^{i\theta_5} \quad (3)$$

The unknowns in the previous equation are  $\dot{r}_6$  and  $\omega_5$ . We assume that  $\omega_3$  has already been found, since it is part of the four-bar mechanism. If we use the equality  $i = e^{i\pi/2}$  in the above equation, we may rewrite it as

$$\dot{r}_6 = r_2 \omega_2 e^{i(\theta_2 + \pi/2)} + r_3 \omega_3 e^{i(\theta_3 + \pi/2)} + r_5 \omega_5 e^{i(\theta_5 + \pi/2)} \quad (4)$$

The above equation may be readily solved with `complexsolve()`, or using analytical methods discussed in previous discussions.

Taking a derivative one more time, we get

$$\ddot{r}_6 = r_2 i e^{i\theta_2} (\alpha_2 - i \omega_2^2) + r_3 i e^{i\theta_3} (\alpha_3 - i \omega_3^2) + r_5 i e^{i\theta_5} (\alpha_5 - i \omega_5^2) \quad (5)$$

Again, we assume the only unknowns in the above equation are  $\ddot{r}_6$  and  $\alpha_5$ , since we found  $\omega_5$  in the last step. We assume all other angular velocities and accelerations have been solved for during the analysis of the fourbar part of the mechanism.