## **HW 7 Solutions**

## Problem 4

```
1 /**
* File: prob4.ch
* Author: Nicolas Ventura
* Calculate the unknowns of
  * a fourbar linkage.
6 */
7 #include <stdio.h>
8 #include <fourbar.h>
9 #include <math.h>
10
int main(void) {
      CFourbar fourbar;
12
      double theta_1[1:4], theta_2[1:4], r[1:4], rp, beta, gamma_1,
13
      gamma_2;
      double complex P_1, P_2;
15
      /* Define link lengths */
16
      r[1] = 5.0;
17
      r[2] = 2.0;
18
      r[3] = 3.0;
19
      r[4] = 4.5;
20
21
      /* Set theta1 and theta2 for both solutions */
22
      theta_1[1] = deg2rad(15.0);
23
      theta_2[1] = deg2rad(15.0);
24
      theta_1[2] = deg2rad(45.0);
25
      theta_2[2] = deg2rad(45.0);
26
27
28
      /* Set coupler point */
      rp = 2.5;
29
      beta = deg2rad(30.0);
30
31
      /* Set up the fourbar */
32
      fourbar.uscUnit(false);
33
      fourbar.setLinks(r[1], r[2], r[3], r[4], theta_1[1]);
34
35
      fourbar.setCouplerPoint(rp, beta);
      /* Part (a) */
36
      fourbar.angularPos(theta_1, theta_2, FOURBAR_LINK2);
37
38
      /* Part (b) */
      fourbar.couplerPointPos(theta_1[2], P_1, P_2);
39
      /* Part (c) */
40
      fourbar.transAngle(gamma_1, gamma_2, theta_1[2], FOURBAR_LINK2)
41
42
      /* Display solutions */
43
      printf("\nFirst Solution:\n");
44
      printf("Theta3 = %1f rad = %1f degn", theta_1[3], rad2deg(
45
      theta_1[3]));
      printf("Theta4 = %lf rad = %lf deg\n", theta_1[4], rad2deg(
46
      theta_1[4]));
      printf("P = (%lf cm, %lf cm)\n", real(P_1), imag(P_1));
      printf("Gamma = %lf rad = %lf deg\n", gamma_1, rad2deg(gamma_1)
48
      );
```

```
49
50
       printf("\nSecond Solution:\n");
       printf("Theta3 = %1f rad = %1f deg\n", theta_2[3], rad2deg(
51
       theta_2[3]));
       printf("Theta4 = %lf rad = %lf deg\n", theta_2[4], rad2deg(
       theta_2[4]));
       printf("P = (%lf cm, %lf cm)\n", real(P_2), imag(P_2));
       printf("Gamma = %lf rad = %lf deg\n", gamma_2, rad2deg(gamma_2)
54
55
56
       return 0;
57 }
First Solution:
^{2} Theta3 = 1.514694 rad = 86.785589 deg
3 Theta4 = 2.376906 rad = 136.186695 deg
_{4} P = (0.287581 cm, 3.645962 cm)
5 \text{ Gamma} = 0.862212 \text{ rad} = 49.401106 \text{ deg}
7 Second Solution:
8 Theta3 = -1.585004 rad = -90.814052 deg
9 Theta4 = -2.447216 rad = -140.215158 deg
P = (2.633327 \text{ cm}, -0.768391 \text{ cm})
11 Gamma = 0.862212 rad = 49.401106 deg
```

## Problem 7

```
1
2 /**
3 * File: prob7.ch
* Animate a quickreturn mechanism
   * with theta2=45 and in steps of
* 1 degrees.
7 * Author: Nicolas Ventura
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
13 #include <complex.h>
#include <array.h>
#include <chplot.h>
16
17 #define NUMPOINTS 361
18
19 int main(void) {
      int n1, n2;
20
       double r [1:7], theta1, rp, beta, theta6;
21
22
       complex double L [1:8];
23
24
       int i;
      double theta2[NUMPOINTS],
25
           theta3_1[NUMPOINTS], theta3_2[NUMPOINTS],
26
27
           x1, x2, x3, x4;
       array double theta4_1[NUMPOINTS], theta4_2[NUMPOINTS],
28
           theta5_1_1[NUMPOINTS], theta5_1_2[NUMPOINTS], theta5_2_1[NUMPOINTS], theta5_2_2[NUMPOINTS];
29
30
```

```
double complex z,
31
32
          P_1[NUMPOINTS], P_2[NUMPOINTS],
          B_1[NUMPOINTS], B_2[NUMPOINTS];
33
34
      array double r6_1_1[NUMPOINTS], r6_1_2[NUMPOINTS],
35
          r6_2_1[NUMPOINTS], r6_2_2[NUMPOINTS];
36
37
      class CPlot mainplot1;
      class CPlot mainplot2;
38
      class CPlot *subplot;
39
      int branches[NUMPOINTS];
40
41
      FILE *fp;
42
      double sliderWidth, sliderHeight;
43
44
45
       * Determine theta4, point B on the output link, and coupler
46
      point P *
47
      **********************
      */
48
49
      // Define the fourbar linkage
      n1 = 2;
50
      n2 = 4;
51
      r[1] = 6;
52
      r[2] = 1;
53
      r[3] = 3;
54
      r[4] = 5;
55
56
      r[5] = 4;
      r[7] = r[4] - 1; /* Length of BO - C */
57
      theta1 = deg2rad(-30);
58
      rp = 2.5;
59
      beta = deg2rad(20);
60
61
      theta6 = 0;
62
63
      // Analyze the fourbar with theta2 rotating from 0-360
      for (i = 0; i <= 360; i++) {</pre>
64
65
          theta2[i] = deg2rad(i);
66
67
          // Determine theta3 and theta4
          z = polar(r[1], theta1) - polar(r[2], theta2[i]);
68
          branches[i] = complex
solve(n1, n2, r[3], -r[4], z, x1, x2,
69
      x3, x4);
70
          // First set of solutions
71
          theta3_1[i] = x1;
72
          theta4_1[i] = x2;
73
          P_1[i] = polar(r[2], theta2[i]) + polar(rp, theta3_1[i] +
74
      beta);
          B_1[i] = polar(r[2], theta2[i]) + polar(r[3], theta3_1[i]);
75
76
          // Second set of solutions
77
          theta3_2[i] = x3;
78
          theta4_2[i] = x4;
79
          P_2[i] = polar(r[2], theta2[i]) + polar(rp, theta3_2[i] +
```

```
beta);
            B_2[i] = polar(r[2], theta2[i]) + polar(r[3], theta3_2[i]);
81
82
            // Find solutions for r5 and r6 : Circuit 1 \,
83
            complexsolve(1, 4, theta6, -r[5],
84
                           polar(r[1], theta1) + polar(r[7], theta4_1[i])
85
                           x1, x2, x3, x4);
86
            r6_1_1[i] = x1;
87
            theta5_1_1[i] = x2;
88
            r6_1_2[i] = x3;
89
90
            theta5_1_2[i] = x4;
91
92
            // Find solutions for r5 and r6 : Circuit 2
            complexsolve(1, 4, theta6, -r[5],
93
                           polar(r[1], theta1) + polar(r[7], theta4_2[i])
94
                          x1, x2, x3, x4);
95
            r6_2_1[i] = x1;
96
            theta5_2_1[i] = x2;
97
            r6_2_2[i] = x3;
98
            theta5_2_2[i] = x4;
99
        // Smooth theta4_1, theta4_2
        {\tt unwrap(theta4\_1,\ theta4\_1);}
103
        unwrap(theta4_2, theta4_2);
        unwrap(theta5_1_2, theta5_1_2);
105
        /* Part (a) */
106
        printf("At 45 degrees, \n");
108
        printf("branches = %d\n", branches[45]);
109
        printf("Circuit 1:\n");
110
        printf("theta3 = \frac{1}{n}, theta3_1[45]);
        printf("theta4 = \frac{1}{n}, theta4_1[45]);
        printf("theta5 = %lf\n", theta5_1_1[45]);
113
       printf("r6 = %lf\n", r6_1_1[45]);
114
       printf("P = %lf\n", P_1[45]);
        printf("\nCircuit 2:\n");
116
       printf("theta3 = %lf\n", theta3_2[45]);
printf("theta4 = %lf\n", theta4_2[45]);
117
118
       printf("theta5 = %lf\n", theta5_2_1[45]);
119
        printf("r6 = %lf\n", r6_2_1[45]);
120
        printf("P = 1f\n", P_2[45]);
        printf("\nCircuit 3:\n");
122
        printf("theta3 = \frac{1}{n}, theta3_1[45]);
        printf("theta4 = %lf\n", theta4_1[45]);
124
        printf("theta5 = %lf\n", theta5_1_2[45]);
125
        printf("r6 = %lf\n", r6_1_2[45]);
printf("P = %lf\n", P_1[45]);
126
127
        printf("\nCircuit 4:\n");
128
       printf("theta3 = 11 n, theta3_2[45]);
129
        printf("theta4 = \frac{1}{n}, theta4_2[45]);
130
        printf("theta5 = %lf\n", theta5_2_2[45]);
132
        printf("r6 = %1f\n", r6_2_2[45]);
       printf("P = 11 \ n", P_2[45]);
134
```

```
/* Part (b) */
135
136
        fp = fopen("partb.qnm", "w");
137
        if (fp == NULL) {
138
            printf("Could not open animation file.\n");
139
            exit(1);
140
141
142
        sliderWidth = 0.30;
143
144
        sliderHeight = 0.20;
145
146
        L[1] = complex(0, 0);
        L[2] = polar(r[2], deg2rad(45.0));
147
148
        L[3] = L[2] + polar(r[3], theta3_1[45]);
        L[4] = L[3] - polar(r[4], theta4_1[45]);
149
        L[5] = L[4] + polar(r[7], theta4_1[45]); // r4
150
        L[6] = complex(r6_1_1[45], 0);
        L[7] = P_1[45];
153
        fprintf(fp, "title \"Part B\"\n");
fprintf(fp, "fixture\n");
fprintf(fp, "groundpin 0 0\n");
154
156
        fprintf(fp, "groundpin %lf %lf\n", real(L[4]), imag(L[4]));
        fprintf(fp, "ground %lf %lf %lf %lf\n",
158
                 real(L[6]) - sliderWidth, imag(L[6]) - sliderHeight /
159
        2, real(L[6]) + sliderWidth, imag(L[6]) - sliderHeight / 2);
        fprintf(fp, "link 0 0 %lf %lf %lf %lf %lf %lf\n",
160
                 real(L[2]), imag(L[2]),
161
                 real(L[3]), imag(L[3]),
real(L[4]), imag(L[4]));
162
        fprintf(fp, "link %lf %lf %lf %lf\n",
165
                 real(L[5]), imag(L[5]),
                 real(L[6]), imag(L[6]));
166
        fprintf(fp, "rectangle %lf %lf %lf %lf\n",
167
                 real(L[6]) - sliderWidth / 2, imag(L[6]) - sliderHeight
168
         / 2, sliderWidth, sliderHeight);
        fprintf(fp, "polygon fill gray90 %lf %lf %lf %lf %lf %lf \n",
170
                 real(L[2]), imag(L[2]),
                 real(L[3]), imag(L[3]),
real(L[7]), imag(L[7]));
171
172
        fprintf(fp, "point %lf %lf \n", real(L[7]), imag(L[7]));
173
174
175
        fclose(fp);
176
        qanimate partb.qnm
177
178
        /* Part (c) */
179
180
        fp = fopen("partc.qnm", "w");
181
        if (fp == NULL) {
182
            printf("Could not open animation file.\n");
183
            exit(1);
184
185
186
187
        sliderWidth = 0.30;
        sliderHeight = 0.20;
188
189
```

```
fprintf(fp, "title \"Part C\"\n");
fprintf(fp, "fixture\n");
fprintf(fp, "groundpin 0 0\n");
190
191
        fprintf(fp, "groundpin %lf %lf\n", real(L[4]), imag(L[4]));
193
        fprintf(fp, "ground %lf %lf %lf %lf\n",
194
                 min(r6_1_1) - sliderWidth / 2, -sliderHeight / 2, max(
195
        r6_1_1) + sliderWidth / 2, -sliderHeight / 2);
        fprintf(fp, "animate restart\n\n");
196
197
        for (i = 0; i < NUMPOINTS; i++) {</pre>
198
             fprintf(fp, "# frame %d\n", i);
199
200
            L[1] = complex(0, 0);
201
            L[2] = polar(r[2], deg2rad((double)(i)));
202
            L[3] = L[2] + polar(r[3], theta3_1[i]);
203
            L[4] = L[3] - polar(r[4], theta4_1[i]);
L[5] = L[4] + polar(r[7], theta4_1[i]); // r4'
204
205
            L[6] = complex(r6_1_1[i], 0);
206
207
            L[7] = P_1[i];
208
             fprintf(fp, "link 0 0 %lf %lf %lf %lf %lf %lf\\n",
209
                      real(L[2]), imag(L[2]),
                      real(L[3]), imag(L[3]),
211
212
                      real(L[4]), imag(L[4]));
             fprintf(fp, "link %lf %lf %lf %lf \\n",
213
214
                      real(L[5]), imag(L[5]),
                      real(L[6]), imag(L[6]));
             fprintf(fp, "rectangle %lf %lf %lf %lf\\n",
216
                      real(L[6]) - sliderWidth / 2, imag(L[6]) -
217
        sliderHeight / 2, sliderWidth, sliderHeight);
             fprintf(fp, "polygon fill gray90 %lf %lf %lf %lf %lf %lf \\\
                      real(L[2]), imag(L[2]),
219
                      real(L[3]), imag(L[3]),
real(L[7]), imag(L[7]));
221
             fprintf(fp, "point trace %lf %lf\\\n", real(L[7]), imag(L
        [7]));
223
             fprintf(fp, "\n");
224
225
226
        fclose(fp);
227
228
        qanimate partc.qnm
229
        return 0;
230
231 }
```

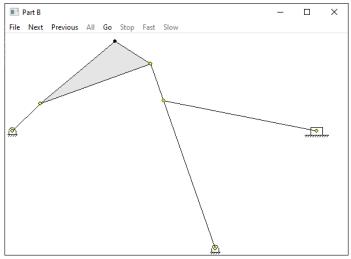


Image 1: Problem 7(b)

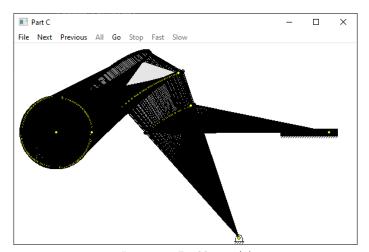


Image 2: Problem 7(c)