

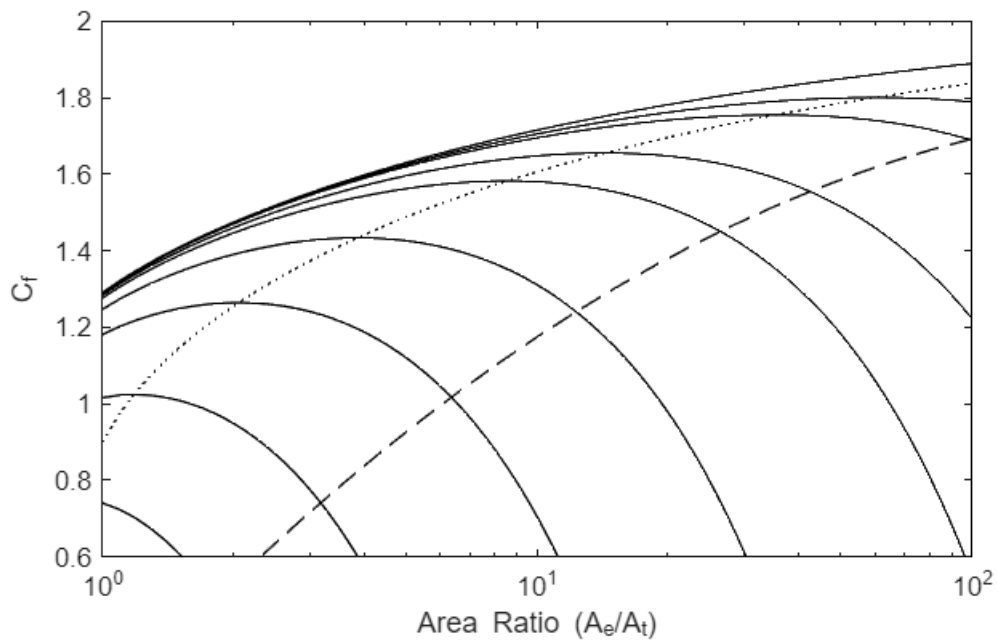
```

clear; close all; clf; clc;
AR = 0:0.1:100;
curve1 = zeros(length(AR),1);
curve2 = zeros(length(AR),1);
curve3 = zeros(length(AR),1);
curve4 = zeros(length(AR),1);
curve5 = zeros(length(AR),1);
curve6 = zeros(length(AR),1);
curve7 = zeros(length(AR),1);
curve8 = zeros(length(AR),1);
curve9 = zeros(length(AR),1);
curve10 = zeros(length(AR),1);
ratioOfTheSpecificHeats = 1.25;

for index = 1:1000
    ratio = index/10;
    curve1(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,2);
    curve2(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,4);
    curve3(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,10);
    curve4(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,25);
    curve5(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,75);
    curve6(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,150);
    curve7(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,500);
    curve8(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,1000);
    curve9(index) = thrust_coefficient(ratioOfTheSpecificHeats,ratio,100000000);
    curve10(index) = thrust_coefficient_special(ratioOfTheSpecificHeats,ratio);
end

cfmin = @(ar) -0.0445*log(ar).^2 + 0.5324.*log(ar) + 0.1843;
figure(1);
semilogx(AR,curve1,AR,curve2,AR,curve3,AR,curve4,AR,curve5,AR,curve6,AR,curve7,AR,curve8,AR,curve9,'Color','k')
hold on;
semilogx(AR,curve10,':','Color','k')
fplot(cfmin,'--','Color','k');
ylim([0.6 2])
xlim([1 100])
xlabel('Area Ratio (A_e/A_t)')
ylabel('C_f')
hold off;

```



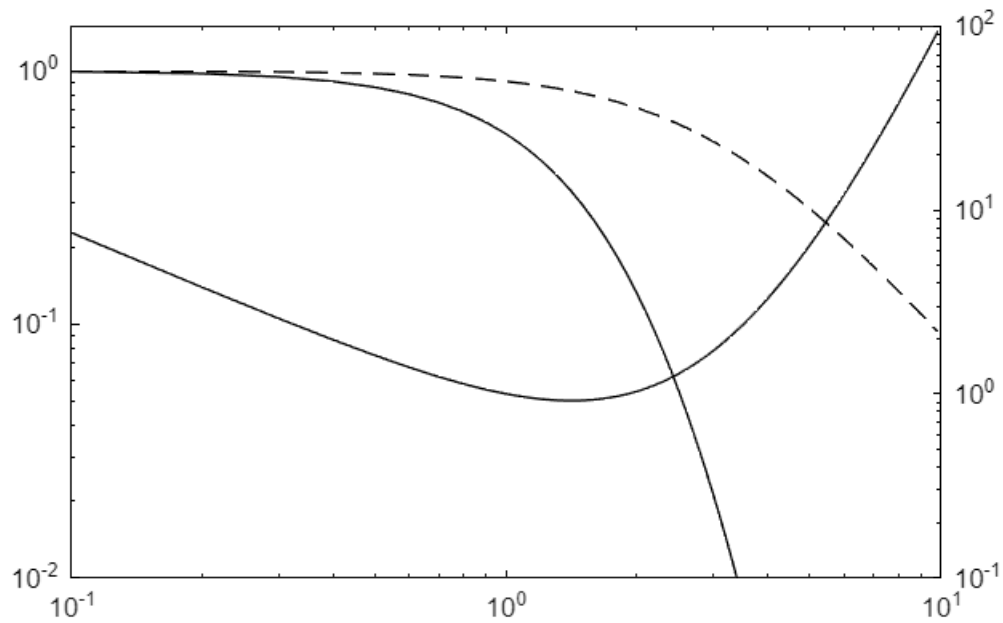
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cf_proj4a = thrust_coefficient(1.25,10,10);
fprintf('the thrust coefficient at gamma = 1.25, epsilon = 10, P_c/P_a = 10 is C_f = %f',cf_proj4a)
```

the thrust coefficient at gamma = 1.25, epsilon = 10, P\_c/P\_a = 10 is C\_f = 0.714154

```
mach = 1:100;
mach = mach./10;

for jindex = 1:100
    mach1 = jindex/10;
    [pr1(jindex),tr1(jindex),ar1(jindex)] = isentropicRatios(1.2,mach1);
    [pr2(jindex),tr2(jindex),ar2(jindex)] = isentropicRatios(1.2,mach1);
end
figure(2);
colororder({'k','k'})
yyaxis left;
loglog(mach,pr1,mach,tr1)
ylim([0.01 1.5])
yyaxis right;

loglog(mach,ar1,mach,ar2)
xlim([0 10])
```



```
function [PPc,TTc,AreaRatio] = isentropicRatios(gamma,MachNumber)
% finds the isentropic relationships pressure, temperature, and area

PPc = (1 + (gamma - 1)/2 * MachNumber * MachNumber) ^ (-gamma/(gamma-1));

TTc = (1 + (gamma - 1)/2 * MachNumber * MachNumber)^(-1);

AreaRatio = MachNumber^-1 * (( 2 + (gamma-1) * MachNumber * MachNumber)/
(gamma+1))^(gamma/(2*gamma-2));

end
```

```
function [cf] = thrust_coefficient(gamma,areaRatio,pcpa)
% Calculate the thrust coefficient using the given parameters
[~,mach] = machNumbers(areaRatio,gamma);

pcpe = (1+ (gamma-1)/2*mach^2)^(gamma/(gamma-1));

pepc = pcpe^(-1);

papc = pcpa^(-1);
```

```

    cf = (2*gamma^2/(gamma-1)*(2/(gamma+1))^(gamma/(gamma-1))*(1-
pepc^((gamma-1)/gamma)))^0.5 + (pepc - papc)*areaRatio;
end

function [cf] = thrust_coefficient_special(gamma,areaRatio)
% Calculate the thrust coefficient using the given parameters
    [~,mach] = machNumbers(areaRatio,gamma);

    pcpe = (1+ (gamma-1)/2*mach^2)^(gamma/(gamma-1));

    pepc = pcpe^(-1);

    papc = pepc;

    cf = (2*gamma^2/(gamma-1)*(2/(gamma+1))^(gamma/(gamma-1))*(1-
pepc^((gamma-1)/gamma)))^0.5 + (pepc - papc)*areaRatio;
end

function [M_sub, M_super] = machNumbers(areaRatio, gamma)
% machNumbers - Computes the subsonic and supersonic Mach numbers
% corresponding to a given area ratio A/A*

    f = @(M) (1./M) .* ( (2/(gamma+1)) .* (1 + (gamma-1)/2 .* M.^2) ) ...
        .^((gamma+1)/(2*(gamma-1))) - areaRatio;

    try
        M_sub = fzero(f, [1e-6, 0.999]);
    catch
        M_sub = NaN;
    end

    try
        M_super = fzero(f, [1.0001, 50]);
    catch
        M_super = NaN;
    end
end
end

```