

## Homework 2

1.

logit func:  $P(z) = \frac{e^z}{1+e^z}$

$$\ln(P(z)) = \ln\left(\frac{e^z}{1+e^z}\right) = \ln(e^z) - \ln(1+e^z)$$

$$z = \ln(P(z)) - \ln(1+e^z)$$

$$z + \ln(1+e^z) = \ln(P(z))$$

$$z = \ln(P(z)) - \ln(1+e^z)$$

$$z = \ln\left(\frac{P(z)}{1+e^z}\right)$$

~~$$z = \ln\left(\frac{e^z}{1+e^z}\right)$$~~

$$P(z) = \frac{e^z}{1+e^z} = \frac{1}{1+e^{-z}}$$

~~$$x = \frac{e^y}{1+e^y}$$~~

~~$$x = \frac{e^y}{1+e^y} \Rightarrow x = \frac{1}{1+e^{-y}}$$~~

~~$$x = \frac{1}{1+e^{-y}}$$~~

$$P(z) = \frac{e^z}{1+e^z} \Rightarrow e^z = (1+e^z)P$$

$$\ln(P(z)) = \ln\left(\frac{e^z}{1+e^z}\right) = \ln(e^z) - \ln(1+e^z)$$

$$= (1-P)e^z = P \Rightarrow (1-P)e^z = \frac{P}{(1-P)}$$

$$= \ln(e^z) = \ln\left(\frac{P}{1-P}\right)$$

$$\Rightarrow z(p) = \ln\left(\frac{P}{1-P}\right)$$

2.

~~$$\frac{P}{1-P} \Rightarrow \frac{e^{(\beta_0 + \beta_1(x+2))}}{e^{\beta_0 + \beta_1 x}} = e^{2\beta_1}$$~~

increases by a multiplication of  $e^{2\beta_1}$

$\downarrow$  approaches 0 as  $x_1 \rightarrow \infty$  and  $x_1 \rightarrow -\infty$

$$x_1 \rightarrow -\infty$$

~~$$\frac{P}{1-P} \left(\frac{1}{1+e^{\infty}}\right) = 0$$~~

$$\left(\frac{1}{1+e^{-\infty}}\right) = 1$$

estudee



### Fundamentals of the bootstrap

1.  $(1 - 1/n)^n = P(\text{not being selected in a bootstrap sample})$
2.  $(1 - 1/1000)^{1000} \approx 0.3677$  roughly  $1/3$