

Name _____ Student ID _____ Colleges & Schools _____ Department _____

Homework Unit 1

1. (a) Show how to represent each of the numbers $(7-1)$, (7^2-1) , and (7^3-1) as base 7 numbers.
(b) Generalize your answers to part (a) and show how to represent (k^n-1) as a base k number, where k can be any integer larger than 1 and n any integer larger than 0. Give a mathematical derivation of your result.
2. (a) It is possible to have negative weights in a weighted code for the decimal digits, e.g., 8, 4, -2, and -1 can be used. Construct a table for this weighted code.
(b) If x is a decimal digit in this code, how can the code for $9-x$ be obtained?
3. An alternative algorithm for converting a base 20 integer, $d_{n-1}d_{n-2} \cdots d_1d_0$, into a base 10 integer is stated as follows: Multiply d_i by 2^i and add i 0's on the right, and then add all of the results.
(a) Use this algorithm to convert $GA7_{20}$ to base 10. (G_{20} is 16_{10} .)
(b) Prove that this algorithm is valid.
(c) Consider converting a base 20 fraction, $0.d_1d_2 \cdots d_{n+1}d_n$ into a base 10 fraction. State an algorithm to the one above for doing the conversion.
(d) Apply your algorithm of part (c) to $0.FA7_{20}$.
4. Let $B = b_{n-1}b_{n-2} \cdots b_1b_0$ be an n -bit 2's complement integer. Show that the decimal value of B is $-b_{n-1}2^{n-1} + b_{n-2}2^{n-2} + b_{n-3}2^{n-3} + \cdots + b_12 + b_0$. (Hint: Consider positive ($b_{n-1}=0$) and negative ($b_{n-1}=1$) numbers separately, and note that the magnitude of a negative number is obtained by subtracting each bit from 1 (i.e., complementing each bit) and adding 1 to the result.)