

Name \_\_\_\_\_ Student ID \_\_\_\_\_ Colleges & Schools \_\_\_\_\_ Department \_\_\_\_\_

### Quiz Unit 5 Solutions

1. Simplify the following expression first by using a map and then by using Boolean algebra. Use the Karnaugh map as a guide to determine which theorems to apply to which terms for the algebraic simplification.

$$F = a'b'c' + a'c'd + bcd + abc + ab'$$

Sol.)

		a b			
		00	01	11	10
c d	00	1			1
	01	1	1		1
	11		1	1	1
	10			1	1

$$F = a'b'c' + a'c'd + bcd + abc + ab'$$

$$= (a'b'c' + ab') + a'c'd + bcd + (abc + ab')$$

$$= (a'c' + a)b' + (a'c'd + bcd) + a(bc + b') \quad \text{Elimination Theorem } (X + X'Y = X + Y)$$

$$= (c' + a)b' + (a'c'd + bcd + a'bd) + a(c + b') \quad \text{Consensus Theorem}$$

$$= (b'c' + a'bd + a'c'd) + (bcd + a'bd + ac) + ab' \quad \text{Consensus Theorem}$$

$$= (b'c' + ac + ab') + a'bd \quad \text{Consensus Theorem}$$

$$= b'c' + ac + a'bd$$