

Pre-Calculus in Brief with Python, Colab, GitHub, and L^AT_EX PCiB - Version 0.3

November 9, 2023

MIT License

Available on GitHub at:

<https://GitHub.com/nicholaskarlson/PCiB>

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Preface

This text, *Pre-Calculus in Brief - PCiB* aspires to be more than just another math book. This book strives to foster collaborative math writing. Note that this book has very few references. The reader is encouraged to use resources available on the Web to fact-check. This book’s view on “causation” and facts is heavily influenced by Mosteller and Tukey [MT77].

Redefining the Role of the Reader

Pre-Calculus in Brief (PCiB) is an endeavor to reshape how math is written, understood, and studied. It’s not just a passive read but an open-source approach to math, aiming to encourage students to become proactive learners.

This project strives to break the traditional mold of math education and invites readers and professional mathematicians to participate actively.

A Dynamic Relationship with Math

Pre-Calculus in Brief is not just a book but a movement and methodology, heralding a new era in how we approach, consume, and interact with math. By positioning the reader as an integral part of the math-book process, PCiB fosters a dynamic relationship with math, making mathematics more accessible, proactive, and relevant. In this shifting paradigm, we are all potential mathematicians, creators of interesting and relevant ways to learn and study math.

Please fork the LaTeX source code for PCiB (available on GitHub) and create your own book that chooses the facts and exercises most relevant to you! Also, starring the PCiB project on GitHub would be greatly appreciated! Thanks for reading PCiB!

Chapter 1

Introduction to PCiB

Welcome to PCiB on GitHub

Pre-Calculus in Brief, abbreviated PCiB, isn't merely a passive read. It's an endeavor to reshape how math is written, studied, and taught. By presenting an open-source approach to math, the goal is to encourage everyone to become proactive readers and writers of math.

Fostering a Proactive Engagement with Math

Pre-Calculus in Brief is a call for a renewed engagement with mathematics. PCiB is an endeavor to reshape how math is written, understood, and studied. It's not just a passive read but an open-source approach to math, aiming to encourage students to become proactive learners.

This project strives to break the traditional mold of math education and encourages readers and professional mathematicians to participate actively.

Please fork the L^AT_EX source code for PCiB (available on GitHub) and create your own book on Pre-Calculus that chooses the content most relevant to you! Also, starring the PCiB project on GitHub would be greatly appreciated! Thanks for reading PCiB!

Chapter 2

Open-Source Ethos

The Spirit of Shared Knowledge and Collaboration

Math, like software, is better when it's open. PCiB draws inspiration from the open-source software movement; this section elucidates how a collaborative, transparent, and shared approach can enhance our understanding of math. Here, we look at the philosophy behind open-source and how it beautifully combines with the study of mathematics.

Open-Source Math: Preserving Tradition Through Collaborative Exploration

Mathematics, like software, thrives when it embraces openness and transparency. PCiB takes a leaf from the proven benefits of the open-source software model; this section highlights how a collaborative and transparent method can improve and deepen our grasp of math and its texts. Here, we explore the principles of open source and how these principles align with the development of mathematics and its texts.

Understanding the Open-Source Ethos

The open-source paradigm revolves around shared ownership, collaboration, and the free exchange of knowledge. In the software realm, this approach has led to groundbreaking innovations built and enhanced by a global community of skilled contributors. United by a mutual objective, these individuals pool their diverse talents and insights to improve and share software solutions for broader public benefit.

Advantages of the Open-Source Framework in Math

Collective Insight

Mirroring the collaborative essence of open-source software, many individuals can offer their perspectives and knowledge, making math texts more robust and varied.

Enhancement and Accuracy

Open platforms foster an environment of constructive criticism, ensuring prompt identification and correction of inaccuracies. This meticulous peer review can help provide a credible and current mathematical text.

Universal Access

Much as open-source software promotes free access and modification, open-source math prioritizes universal accessibility. This ensures mathematics knowledge isn't restricted to a select few but is available to all curious minds.

Potential Challenges

Despite its advantages, melding open-source with math has potential pitfalls. The volume of contributions can complicate accuracy verification processes.

However, the very community championing this open-source approach to math can serve as its vigilant protector. They can ensure that contributions undergo rigorous evaluation and referencing, akin to the meticulous checks within the open-source software community.

Conclusion: Reinvigorating Our Experience with Math

Adopting an open-source perspective to the approach of math signifies a refreshed approach. It beckons a worldwide community to collaborate and forge a comprehensive and exciting math text. In this refreshed approach, every individual can play a part, both as a contributor and a learner. Math texts, through this lens, evolve and flourish, reflecting the collective input of active participants.

Chapter 3

Introduction to GitHub

The Hub for Modern Collaboration

Harnessing GitHub: A New Frontier in Collaborative Math Writing

At the heart of our collaborative math endeavor lies GitHub, a platform traditionally associated with code but now repurposed for our endeavor. This section provides a primer on GitHub, laying the foundation for those unfamiliar and offering insights into its transformative potential for collective math writing, learning, and teaching.

A Brief Introduction to GitHub

Originally conceptualized as a platform for developers, GitHub is a repository hosting service that facilitates version control using Git. At its core, it allows multiple users to work on a project simultaneously, tracking changes and ensuring that the latest version of a project is always accessible. Over the years, GitHub has grown beyond its initial software-centric confines, becoming a hub for all kinds of collaborative projects, from writing to data science and now to math.

Repurposing GitHub for Math Texts

Version Control

Math writing, like software, is dynamic and constantly evolving. As new sources or perspectives emerge, math texts may need revisions. GitHub's

version control ensures that every change made to a document is tracked, enabling mathematicians to see how math texts evolve over time.

Collaborative Writing

Multiple contributors can work on a single math text simultaneously. This multi-user capability ensures diverse viewpoints can be seamlessly integrated, making the math text richer and more comprehensive.

Review and Feedback

Just as developers review and comment on code, mathematicians can provide feedback on written content. This feature encourages rigorous peer review, ensuring accuracy and credibility.

Open Access

Math texts on GitHub can be made public, granting anyone access to read, contribute, or fork the text into their own versions. This workflow democratizes math texts, making the creation process a collective endeavor rather than the domain of a select few.

Transparency

All changes and contributions are logged, providing a clear trail of the evolution of a mathematical text. This transparency bolsters the credibility of the text hosted on the platform.

Community Building

Beyond just writing, GitHub fosters a community of mathematicians, enthusiasts, and readers who can discuss, debate, and engage in meaningful dialogues about math and available math texts on GitHub.

Conclusion: Envisioning a Collaborative Mathematical Landscape

Embracing GitHub as a tool for collaborative math signifies more than just a shift in approach; it heralds a new era of inclusivity, transparency, and dynamism in writing, learning, and math teaching.

Chapter 4

Encouragement to Fork

Invitation to Dive Deep and Make It Your Own

PCiB isn't a static entity. It thrives on evolution, adaptation, and diversification, much like math itself. We encourage readers to "fork" (a term soon to be discussed) and create their own versions of this book. Read this section to understand the essence of "forking" and how it can be the starting point of your unique math journey.

The Concept of Forking: A Brief Overview

In the realm of software development, particularly in platforms like GitHub, "forking" refers to the act of creating a copy of a project, allowing one to make changes independently of the original. In this context, forking PCiB enables readers to take the base content and adapt, modify, and expand upon it, tailoring the narrative to resonate with their perspectives, insights, and understanding.

How to Begin Your Forking Journey

Start Small: You don't need to rewrite entire chapters. Begin by adding annotations, insights, or even footnotes to existing content. As you grow more confident, you can expand and modify larger sections.

Engage with the Community: Share your forked version with other readers. This encourages discourse, debate, and constructive feedback, allowing your text to be refined and enhanced.

Celebrate input: Encourage others around you to fork and create their own versions. The more in-depth the input, the deeper our collective understanding of math potentially becomes.

Conclusion: The Power of Collective Math

The invitation to fork PCiB isn't just about creating different versions of a book. It's a call to embrace collective writing, learning, and teaching. By embracing the essence of forking, math is not just something we read but something we actively shape, share, and pass on.

Chapter 5

More About GitHub

Discovering the Power of Collaborative Tools

Diving deeper into the world of GitHub, this chapter provides a comprehensive overview. Beyond its technicalities, we explore how GitHub emerged as a revolutionary platform for collaboration and how it can be leveraged for those interested in writing, teaching, and learning about math.

The Genesis of GitHub

GitHub began as a platform designed for software developers to manage and track changes to their codebase. Launched in 2008, it swiftly gained traction due to its user-friendly interface and efficient version control system powered by Git. Over the years, it evolved from a mere repository hosting service to a dynamic hub of collaboration, housing millions of projects and engaging tens of millions of users worldwide.

GitHub: More than Just Code

While GitHub's origins are rooted in code collaboration, its adaptable nature has made it a favored platform for various non-code projects. Writers, designers, educators, and researchers have discovered the potential of GitHub as a tool for:

Document Collaboration

With its built-in version control, contributors can track changes, revert to previous versions, and seamlessly merge updates.

Project Management

With features like "issues" and "milestones," teams can organize tasks, set goals, and monitor progress.

Open Access & Transparency

Public repositories allow for open contributions, ensuring transparency and fostering a sense of collective ownership.

Collaborative Writing

Multiple contributors can simultaneously work on a single document, with every change being tracked and attributed, facilitating teamwork on extensive projects like books or research papers.

Engaging the Public

With the platform's inherent transparency, researchers can make their work-in-progress accessible to the public, inviting insights, corrections, and contributions.

Case Study: PCiB's Use of GitHub

PCiB's journey on GitHub is a testament to the platform's potential in mathematical endeavors. By hosting the book on GitHub, the following is possible:

Feedback Loop

Readers can raise "issues," pointing out inaccuracies, suggesting enhancements, or even recommending new sections or topics.

Forking

As previously discussed, readers can "fork" the repository, creating their unique versions of the book while staying connected to the original.

Regular Updates

With math being dynamic, the book can be regularly updated, with new versions being released as and when significant changes are incorporated.

Challenges and Considerations

While GitHub offers many advantages, it's essential to understand its limitations:

Learning Curve

For those unfamiliar with Git or version control, there can be an initial learning curve.

Data Overwhelm

With vast amounts of data and contributions, ensuring quality and accuracy can be challenging.

Diverse Audience Management

Catering to both tech-savvy and non-tech audiences might require creating additional resources or tutorials to ensure inclusivity.

Conclusion: GitHub – A Paradigm Shift in Collaboration

The rise of GitHub marks a significant shift in how we perceive and participate in collaborative projects. Its adaptability, transparency, and user-centric design make it a powerful tool, not just for coders but for anyone passionate about collective endeavors. In the realm of mathematics, GitHub promises a future where texts are continually refined, expanded, and enriched by a global community.

Chapter 6

Forking Process

The Heart of Collaboration on GitHub

The beauty of open-source lies in its democratization of content creation. In this section, we demystify the process of "forking" on GitHub, guiding you step-by-step on how to take PCiB and create a version uniquely yours.

Understanding Forking

Before diving into the specifics, it's crucial to understand what "forking" means in the context of GitHub. In the simplest terms, to "fork" a project means to create a personal copy of someone else's project. Forking allows you to freely experiment with changes without affecting the original project. Forking is akin to taking a book you admire and making a copy to write your notes, edits, or additional chapters without altering the original book.

Why Fork?

Experimentation

It provides a safe space where you can test out ideas, make changes, or introduce new content.

Personalization

For projects like PCiB, it allows readers to customize the content, tailor it to their perspectives, or even localize it for specific audiences.

Collaboration

If you believe your changes have broad appeal, you can propose that they be incorporated back into the original project, enriching it with your unique contributions.

Step-by-Step Forking Guide

Set Up Your GitHub Account

If you don't have an account on GitHub, you'll need to create one. Visit GitHub's official site and sign up.

Navigate to the PCiB Repository

Once logged in, search for the PCiB project or navigate to its URL directly.

Click the 'Fork' Button

The fork button is located at the top right corner of the repository page; this button will create a copy of PCiB in your account.

Clone Your Forked Repository

Forking allows you to have a local copy on your computer, making editing and experimentation easier. Use the command: `git clone [URL of your forked repo]`.

Make Your Changes

Using your preferred tools, introduce the edits, additions, or modifications you desire.

Commit and Push Changes

Once satisfied, save these changes (known as a "commit") and then "push" them to your forked repository on GitHub.

Optional – Create a Pull Request

If you believe your changes should be incorporated into the original PCiB repository, you can create a "pull request." A pull request notifies the original authors of your suggestions.

Things to Keep in Mind

Stay Updated

The original PCiB project may undergo updates. It's a good practice to regularly "pull" from the original repo to keep your fork up-to-date.

Engage with the Community

Open-source thrives on community interactions. Engage in discussions, seek feedback, and please remain open to constructive criticism.

Conclusion: Embracing the Forking Culture

Forking is more than just a technical process; it symbolizes the ethos of open-source — a world where knowledge is not hoarded but shared, refined, and built upon collectively. By forking PCiB or any other project, you're not just creating a personal copy; you're becoming a part of a global movement that values collaboration, innovation, and the shared pursuit of knowledge. So, embark on this journey, make your unique mark, and contribute to the ever-evolving corpus of collective wisdom.

Chapter 7

Editing and Customizing

Tailoring Repositories to Suit Your Needs

Now, let's build upon the forking process; this segment delves into the next steps. How can you edit and customize your version of PCiB? What tools and techniques are available at your disposal? Embark on this informative journey as we guide you through the intricacies of editing on GitHub.

Understanding the GitHub Workspace

Before diving into the specifics of editing, it's essential to familiarize yourself with the GitHub workspace. Think of it as a digital toolshed where each tool serves a unique function:

- **Repository (Repo):** This is the project's main folder where all your project's files are stored and where you track all changes.
- **Branches:** These are parallel versions of a repository, allowing you to work on features or edits without altering the main project.
- **Commits:** This is a saved change in the repository, akin to saving a file after making edits.
- **Pull Requests:** This is how you notify the main project of desired changes, proposing that your edits be merged with the original.

Editing Files Directly on GitHub

For minor changes, you might opt to edit directly on GitHub:

1. **Navigate to the File:** Within your forked PCiB repository, find the file you want to edit.
2. **Click the Pencil Icon:** This button allows you to edit the file.
3. **Make Your Edits:** Modify the content as needed.
4. **Save and Commit:** Below the editing pane, you'll see a "commit changes" section. Add a brief note summarizing your changes and click 'Commit.'

Editing Files Locally

For extensive customization:

1. **Clone Your Repository:** Use a tool like Git to clone (download) your forked repo to your local computer.
2. **Edit Using Your Preferred Tools:** This could range from text editors to specialized software, depending on the file type.
3. **Commit and Push:** After making your changes, save them (commit) and then upload (push) them to your GitHub repository.

Utilizing Branches for Extensive Customization

Branches are especially useful for significant overhauls or when working on different versions:

1. **Create a New Branch:** From your main project page, use the branch dropdown to type in a new branch name and create it.
2. **Switch to Your Branch:** Ensure you're working in this new parallel environment.
3. **Make and Commit Changes:** As you would in the main project.
4. **Merging:** Once satisfied with your edits in the branch, you can merge these changes back into the main project or keep them separate as a different version.

Exploring Additional Tools and Extensions

GitHub's ecosystem is rich with tools and extensions to enhance your editing experience:

- **GitHub Desktop:** An application that simplifies the process of managing your repositories without using command-line tools.
- **Markdown Editors:** Since many GitHub files (like READMEs) are written in Markdown, tools like StackEdit or Dillinger can be invaluable.
- **Extensions for Browsers:** Tools like Octotree can help in navigating repositories more effortlessly.

Conclusion: The Art of Tailored Content

Editing and customizing on GitHub might seem daunting initially, but with practice, it transforms into a manageable workflow. Many people find that the ability to take a project like PCiB and mold it into something uniquely theirs is empowering. It's a testament to the open-source community's ethos, where shared knowledge becomes the canvas and our collective edits, the brushstrokes, crafting an ever-evolving masterpiece. As you embark on your customization journey, remember that every edit, no matter how small, contributes to the project potentially in significant ways.

Chapter 8

Engaging with the Community

Joining the Global Conversation

The Significance of the GitHub Community

The digital age has bestowed upon us the gift of connectivity. On platforms like GitHub, this connectivity transcends borders, disciplines, and ideologies, culminating in a melting pot of diverse ideas and knowledge. For mathematicians and math enthusiasts, GitHub offers a space not only to store and manage content but also to engage with an audience that is passionate, informed, and eager to contribute.

1. Discussions and Debates

One of the most enriching aspects of the GitHub community is the plethora of discussions that unfold:

- **Issues:** A core feature of GitHub, "issues" allow users to raise questions, report problems, or propose enhancements.
- **GitHub Discussions:** A newer feature, Discussions, acts like a community forum. It's an excellent place for extended conversations, brainstorming, and sharing ideas or resources.

2. Collaborative Content Creation

Beyond solitary endeavors, GitHub shines in its collaborative capabilities:

- **Pull Requests:** If you have made an alteration to a math text or added a new perspective, pull requests are the way to propose these changes to

the original repository owner. Pull requests foster a collaborative spirit, where content isn't static but continually evolving with community input.

- **Fork and Merge:** As you've learned, forking allows you to create your version of a repository. Engaging with the Community means you can merge changes from others into your fork, blending a mixture of diverse insights.

3. Building and Nurturing Networks

Connections made on GitHub often spill over into lasting professional relationships:

- **Following and Followers:** Like on social media platforms, you can follow contributors whose work resonates with you. Following contributors creates a curated feed of updates and also allows you to be part of a more extensive network.
- **GitHub Stars:** If a particular project or repository impresses you, give it a star! Starring not only bookmarks the project for you but also shows appreciation to the creator.

4. Learning and Growing Through Feedback

The Community's feedback is an invaluable asset:

- **Code Reviews:** Although traditionally for software, text writers can use this feature to receive feedback on their methodologies or approaches, refining their work.
- **Community Insights:** The "insights" tab on a repository provides analytics. For text writers, this can give a sense of which topics garner more attention and interest.

5. Participating in Community Events

GitHub often hosts and sponsors events:

- **Hackathons:** While traditionally for coders, these events can be repurposed for text writer content creation, where participants collaboratively tackle projects or themes.
- **Webinars and Workshops:** These events can range from mastering GitHub's technical side to thematic discussions on math topics.

A Project of Collective Wisdom

Math, in many ways, is a collective endeavor. GitHub can provide a dynamic Community. By engaging with this Community you can become an active participant in the creation of mathematical texts.

Chapter 9

Pre-Calculus Basic Topics

Introduction

In this chapter, we start talking about actual pre-calculus topics. Here we will introduce geometry, algebra, and trigonometry, with details provided in later chapters.

Chapter 10

Topics in Geometry

Understanding Angles and Triangles

Introduction

Geometry is important in pre-calculus studies.

Conclusion

This chapter surveys important topics in geometry relevant to the study of calculus. Please fork the LaTeX source code for PCiB (available on GitHub) and create your own book that chooses the facts and exercises most relevant to you! Also, starring the PCiB project on GitHub would be greatly appreciated! Thanks for reading PCiB!

Chapter 11

Topics in Algebra

Basic Ideas Regarding Numbers

Introduction

Algebra is important in pre-calculus studies.

Conclusion

This chapter surveys important topics in algebra relevant to the study of calculus. Please fork the LaTeX source code for PCiB (available on GitHub) and create your own book that chooses the facts and exercises most relevant to you! Also, starring the PCiB project on GitHub would be greatly appreciated! Thanks for reading PCiB!

Chapter 12

Topics in Trigonometry

Understanding the Basic Trig Functions

Introduction

Trigonometry is important in pre-calculus studies.

12.1 The Unit Circle

The unit circle is a fundamental concept in trigonometry. It is a circle with a radius of one unit, centered at the origin $(0,0)$ of the coordinate plane. The unit circle allows us to define all trigonometric functions for any angle, including those greater than 90 degrees.

12.1.1 Definition of the Unit Circle

The unit circle is defined as the set of all points (x, y) that satisfy the equation $x^2 + y^2 = 1$. This circle intersects the x-axis at the points $(1, 0)$ and $(-1, 0)$, and the y-axis at the points $(0, 1)$ and $(0, -1)$.

12.1.2 Angles and the Unit Circle

In the context of the unit circle, an angle θ is defined starting from the positive x-axis and rotating counter-clockwise for positive angles and clockwise for negative angles. This rotation creates an arc on the circle, and the length of this arc is the measure of the angle in radians.

12.1.3 Radians and Degrees

A radian is the measure of an angle corresponding to an arc length equal to the radius of the circle. Since the circumference of the unit circle is 2π , there are 2π radians in a full rotation. To convert radians to degrees, we use the fact that 360 degrees is equivalent to 2π radians. Therefore, to convert an angle from radians to degrees, we multiply by $\frac{180}{\pi}$.

$$\text{degrees} = \text{radians} \times \frac{180}{\pi}$$

Conversely, to convert from degrees to radians, we multiply by $\frac{\pi}{180}$.

$$\text{radians} = \text{degrees} \times \frac{\pi}{180}$$

12.1.4 Graphing the Unit Circle

Let's graph the unit circle with the point $(0, 1)$ marked:

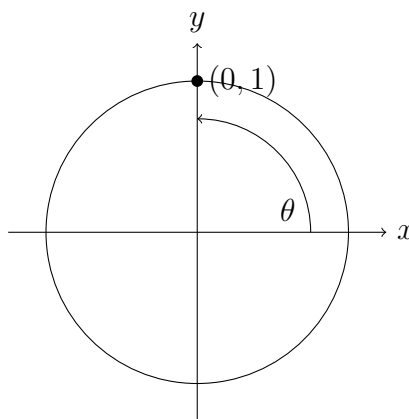


Figure 12.1: The unit circle with the point $(0,1)$ marked.

As you can see from Figure 12.1, the unit circle provides a way to visualize angles and trigonometric functions. Each point on the circle corresponds to the cosine and sine of the angle θ , where the x-coordinate represents the cosine, and the y-coordinate represents the sine.

Conclusion

This chapter surveys important topics in trigonometry relevant to the study of calculus. Please fork the LaTeX source code for PCiB (available

on GitHub) and create your own book that chooses the facts and exercises most relevant to you! Also, starring the PCiB project on GitHub would be greatly appreciated! Thanks for reading PCiB!

Chapter 13

Trigonometry for Calculus

Trigonometry is a branch of mathematics that deals with the relationships between the sides and angles of triangles. It is essential for understanding concepts in calculus, as it provides tools for modeling and solving problems involving periodic phenomena.

13.1 Angles and Their Measure

Every study of Trigonometry begins with an understanding of angles. Angles can be measured in two primary ways: degrees and radians. Degrees are traditionally used in many fields and cultures, and there are 360 degrees in a full rotation. Radians, however, provide a more natural approach in mathematics, especially calculus, because they arise from the arc length of a circle.

13.1.1 Degree Measure

One degree is defined as $\frac{1}{360}$ of a full rotation. The degree measure is subdivided into minutes and seconds, where one degree contains 60 minutes and one minute contains 60 seconds.

13.1.2 Radian Measure

A radian is a measure based on the radius of a circle. It is the angle created at the center of a circle by an arc whose length is equal to the radius of the circle. Since the circumference of a circle is 2π times the radius, a full rotation contains 2π radians.

13.1.3 Converting Between Degrees and Radians

To convert from degrees to radians, we use the relationship that 180 degrees is equal to π radians. Therefore, to convert x degrees to radians, we multiply x by $\frac{\pi}{180}$.

$$\text{radians} = \text{degrees} \times \frac{\pi}{180}$$

Conversely, to convert from radians to degrees, we multiply the radian measure by $\frac{180}{\pi}$.

$$\text{degrees} = \text{radians} \times \frac{180}{\pi}$$

13.1.4 Visualizing Angles with TikZ

To better understand how angles are measured, we can visualize them using a unit circle. Below, we depict an angle in both degrees and radians.

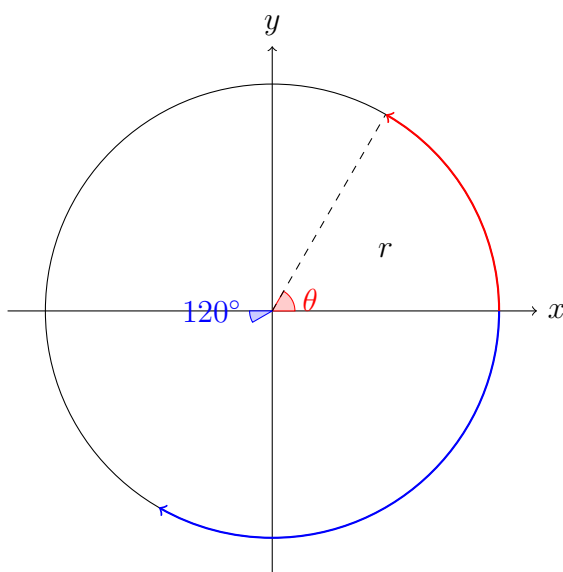


Figure 13.1: Visualization of an angle in degrees and radians on the unit circle.

Figure 13.1 shows an angle θ measured in radians (in red) and the same angle measured in degrees (in blue). This visual aid helps to understand the relationship between the two units of measurement.

13.2 Exercises on Angles and Their Measures

The following problems are designed to reinforce the concepts of angle measurement in degrees and radians as well as the conversion between them. Attempt to solve these problems before checking the provided solutions.

13.2.1 Problems

1. Convert 45° into radians.
2. Convert $\frac{\pi}{3}$ radians into degrees.
3. Find the radian measure of the angle subtended by an arc of length 10 cm in a circle of radius 20 cm.
4. If the angle θ in radians satisfies the equation $3\theta = \pi$, what is θ in degrees?
5. An angle is $\frac{3}{4}$ of a full circle. What is this angle in radians?
6. A clock's minute hand covers 30 degrees in 5 minutes. How many radians does it cover in 20 minutes?

13.2.2 Solutions

1. To convert 45° into radians, multiply by $\frac{\pi}{180}$:

$$45^\circ \times \frac{\pi}{180} = \frac{\pi}{4} \text{ radians}$$

2. To convert $\frac{\pi}{3}$ radians into degrees, multiply by $\frac{180}{\pi}$:

$$\frac{\pi}{3} \times \frac{180}{\pi} = 60^\circ$$

3. For an arc length $s = 10$ cm and radius $r = 20$ cm, the radian measure θ is given by $\theta = \frac{s}{r}$:

$$\theta = \frac{10 \text{ cm}}{20 \text{ cm}} = \frac{1}{2} \text{ radian}$$

4. If $3\theta = \pi$ radians, then $\theta = \frac{\pi}{3}$ radians. To convert this to degrees:

$$\frac{\pi}{3} \times \frac{180}{\pi} = 60^\circ$$

5. An angle that is $\frac{3}{4}$ of a full circle in radians is:

$$\frac{3}{4} \times 2\pi = \frac{3\pi}{2} \text{ radians}$$

6. In 20 minutes, the minute hand covers 4 times the distance it would in 5 minutes. Thus:

$$30^\circ \times 4 \times \frac{\pi}{180} = 2\pi \text{ radians}$$

13.2.3 Degree Measure

The measurement of an angle in degrees is a reflection of the rotation from the angle's initial side to its terminal side. One full rotation around a circle is equal to 360 degrees, meaning that a degree represents $\frac{1}{360}$ th of a full rotation. This form of measurement originates from the ancient Babylonians, who had a base-60 number system and divided the circle into 360 parts.

To visualize an angle measured in degrees, consider the following figure created using the TikZ package. It shows an angle of 45 degrees, which is an eighth of a full 360-degree rotation.

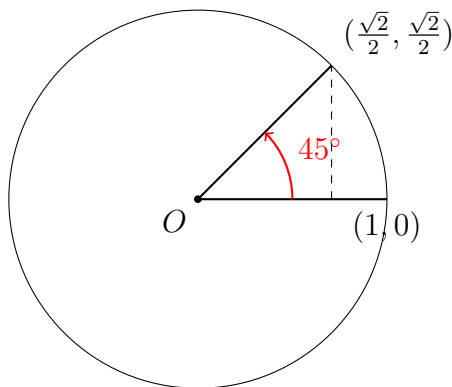


Figure 13.2: Illustration of a 45° angle in standard position.

The figure above illustrates an angle whose terminal side has rotated 45° from the positive x-axis, which is often referred to as the angle's initial side. The radius of the circle has a length of 1, hence the name "unit circle." The coordinates $(1, 0)$ and $(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2})$ correspond to the points where the radius intersects the x-axis and the circle, respectively. The dashed line represents the y-component of the terminal side's endpoint, helping to visualize the 45° angle as a right triangle within the circle.

Angles in degrees are widely used in various fields, including navigation, astronomy, and in everyday situations like measuring temperatures and geographic coordinates. Understanding how to measure angles in degrees and relate them to rotations is fundamental in trigonometry.

Practice Problems

Problem 1: Convert the following degree measurements to radians. (Note: π radians = 180°)

- a. 30°
- b. 90°
- c. 270°

Problem 2: Identify the quadrant in which the terminal side of each angle lies.

- a. 60°
- b. 150°
- c. 210°
- d. 330°

Problem 3: For each angle given, sketch the angle in standard position on the unit circle and label the point of intersection with the circle.

- a. 45°
- b. 135°
- c. 225°
- d. 315°

Problem 4: Determine the reference angle for each of the following:

- a. 120°
- b. 250°
- c. 300°

Problem 5: If the minute hand of a clock is pointing at 12 and it rotates to point at 3, what is the measure of the angle of rotation in degrees?

Solutions:

Problem 1:

a. $30^\circ \times \frac{\pi}{180^\circ} = \frac{\pi}{6}$

b. $90^\circ \times \frac{\pi}{180^\circ} = \frac{\pi}{2}$

c. $270^\circ \times \frac{\pi}{180^\circ} = \frac{3\pi}{2}$

Remarks:

- The problems above are designed to provide practice with converting between degrees and radians, identifying angle positions, and understanding the unit circle.
- The concept of a reference angle is important for understanding the standard trigonometric functions, as it is the acute angle formed by the terminal side of the given angle and the horizontal axis.
- Problem 5 illustrates a real-life application of angle measurement.

13.2.4 Radian Measure

The radian measure of an angle is the length of the arc on the unit circle subtended by the angle. One radian is the angle subtended by an arc length equal to the radius of the circle. Since the circumference of a unit circle is 2π times the radius, a full rotation around the circle is 2π radians.

Why Use Radians?

In calculus, radian measure is preferred because it provides a direct relationship between the angle measure and the arc length. This relationship simplifies the computation of derivatives and integrals involving trigonometric functions. For instance, when using radians, the derivative of $\sin x$ is simply $\cos x$, and the derivative of $\cos x$ is $-\sin x$. Such simplicity is not evident when using degrees.

Visualizing Radian Measure

To visualize an angle in radian measure, we plot it on the unit circle:

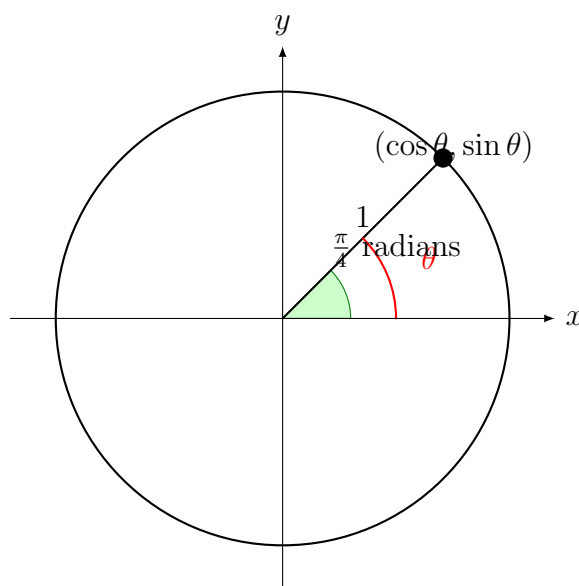


Figure 13.3: Visualization of an angle in radian measure on the unit circle.

Exercises

1. Convert the following angles from degrees to radians:
 - a. 180°
 - b. 360°
 - c. 90°
2. Show that the length of an arc subtended by a central angle of θ radians in a circle of radius r is given by $r\theta$.
3. Find the radian measure of the central angle of a circle with radius 10 units that subtends an arc of length 15 units.

Solutions

1. To convert degrees to radians, use the conversion factor $\frac{\pi \text{ radians}}{180^\circ}$:
 - a. $180^\circ \times \frac{\pi}{180^\circ} = \pi$ radians
 - b. $360^\circ \times \frac{\pi}{180^\circ} = 2\pi$ radians
 - c. $90^\circ \times \frac{\pi}{180^\circ} = \frac{\pi}{2}$ radians
2. The length of an arc l is directly proportional to the angle θ in radians, such that $l = r\theta$.

3. The radian measure of the angle is $\theta = \frac{l}{r} = \frac{15 \text{ units}}{10 \text{ units}} = 1.5$ radians.

Practice Problems

Here are some practice problems to help you solidify your understanding of the radian measure:

Problem 1: Convert the following angles from radians to degrees:

- a. $\frac{\pi}{6}$ radians
- b. $\frac{2\pi}{3}$ radians
- c. $-\frac{\pi}{4}$ radians

Problem 2: An arc on a circle of radius 8 units has a measure of 2 radians. Find the length of the arc.

Problem 3: If a sector of a circle with radius 5 units has an area of 10 square units, what is the angle in radians of the sector?

Problem 4: A central angle of $\frac{5\pi}{6}$ radians is subtended at the center of a circle with radius 12 units. Find the area of the corresponding sector.

Problem 5: The wheel of a bicycle has a diameter of 70 cm. If the wheel rolls without slipping and turns through an angle of $\frac{\pi}{2}$ radians, how far has the bicycle traveled?

Solutions to Practice Problems

Solution to Problem 1: To convert radians to degrees, multiply by $\frac{180^\circ}{\pi}$.

- a. $\frac{\pi}{6} \times \frac{180^\circ}{\pi} = 30^\circ$
- b. $\frac{2\pi}{3} \times \frac{180^\circ}{\pi} = 120^\circ$
- c. $-\frac{\pi}{4} \times \frac{180^\circ}{\pi} = -45^\circ$

Solution to Problem 2: The length L of the arc can be found using the formula $L = r\theta$.

$$L = 8 \text{ units} \times 2 \text{ radians} = 16 \text{ units}$$

Solution to Problem 3: Use the area formula for a sector $A = \frac{1}{2}r^2\theta$ and solve for θ .

$$\theta = \frac{2A}{r^2} = \frac{2 \times 10}{5^2} = \frac{20}{25} = \frac{4}{5} \text{ radians}$$

Solution to Problem 4: The area A of the sector is given by $A = \frac{1}{2}r^2\theta$.

$$A = \frac{1}{2} \times 12^2 \times \frac{5\pi}{6} = 72 \times \frac{5\pi}{6} = 60\pi \text{ square units}$$

Solution to Problem 5: The distance D traveled is equal to the length of the arc formed by the wheel, which is $D = r\theta$, where r is the radius.

$$D = \frac{70}{2} \text{ cm} \times \frac{\pi}{2} = 35\pi \text{ cm}$$

13.3 Trigonometric Functions

The six trigonometric functions are fundamental in both Trigonometry and calculus. These functions are sine (sin), cosine (cos), tangent (tan), cosecant (csc), secant (sec), and cotangent (cot). They are defined as ratios of sides in a right triangle or as certain coordinates of points on the unit circle.

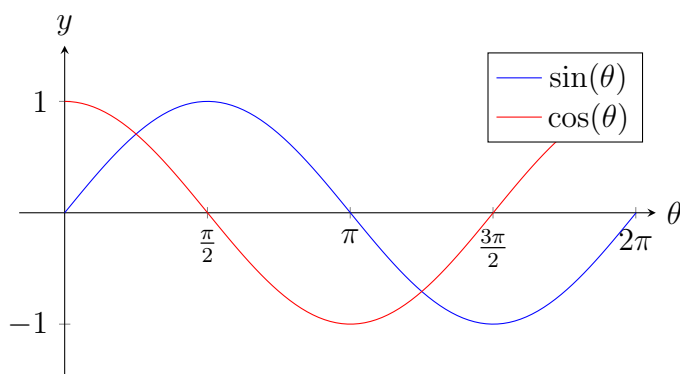
13.3.1 Sine and Cosine

The sine function (sin) represents the ratio of the length of the opposite side to the length of the hypotenuse in a right triangle. The cosine function (cos) represents the ratio of the length of the adjacent side to the length of the hypotenuse.

For a point (x, y) on the unit circle corresponding to an angle θ , the sine and cosine values are y and x , respectively.

Graph of Sine and Cosine Functions

We can graph the sine and cosine functions using their values from the unit circle.



The sine function starts at 0, reaches its maximum at $\frac{\pi}{2}$, returns to 0 at π , reaches its minimum at $\frac{3\pi}{2}$, and completes the cycle at 2π .

The cosine function starts at 1, drops to 0 at $\frac{\pi}{2}$, reaches its minimum at π , returns to 0 at $\frac{3\pi}{2}$, and completes the cycle at 2π .

13.3.2 Tangent Function

The tangent function (\tan) is defined as the ratio of the sine to the cosine of an angle in a right triangle, or $\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)}$. It represents the slope of the line that intersects the unit circle at an angle θ .

13.3.3 Reciprocal Functions

The reciprocal functions, cosecant (\csc), secant (\sec), and cotangent (\cot), are the reciprocals of the sine, cosine, and tangent functions, respectively.

- Cosecant ($\csc(\theta)$) is the reciprocal of sine: $\csc(\theta) = \frac{1}{\sin(\theta)}$
- Secant ($\sec(\theta)$) is the reciprocal of cosine: $\sec(\theta) = \frac{1}{\cos(\theta)}$
- Cotangent ($\cot(\theta)$) is the reciprocal of tangent: $\cot(\theta) = \frac{1}{\tan(\theta)}$

13.3.4 Practice Problems

To better understand trigonometric functions and their properties, try solving the following problems:

1. Evaluate $\sin\left(\frac{\pi}{6}\right)$, $\cos\left(\frac{\pi}{6}\right)$, and $\tan\left(\frac{\pi}{6}\right)$.
2. Given that a point P on the unit circle corresponding to an angle θ has coordinates $P\left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$, find $\sin(\theta)$, $\cos(\theta)$, and $\tan(\theta)$.
3. If $\cos(\theta) = -\frac{1}{2}$ and θ is in the third quadrant, what is $\sin(\theta)$?
4. Sketch the graph of the function $f(\theta) = 2\sin(\theta)$ for $0 \leq \theta \leq 2\pi$.
5. Using the graph of $f(\theta) = \cos(\theta)$, find the values of θ where the function is negative.
6. Solve the equation $\tan(\theta) = \sqrt{3}$ for $0 \leq \theta < 2\pi$.
7. Prove that $\sec^2(\theta) - \tan^2(\theta) = 1$ for all values of θ where the secant and tangent functions are defined.

8. Find the exact value of $\cot\left(\frac{3\pi}{4}\right)$.
9. Determine the amplitude and period of the function $g(\theta) = 3\cos(2\theta)$.

Answers to Practice Problems:

1. For $\frac{\pi}{6}$:

- $\sin\left(\frac{\pi}{6}\right) = \frac{1}{2}$
- $\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$
- $\tan\left(\frac{\pi}{6}\right) = \frac{\sin\left(\frac{\pi}{6}\right)}{\cos\left(\frac{\pi}{6}\right)} = \frac{1}{\sqrt{3}}$

2. With $P\left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$:

- $\sin(\theta) = \frac{1}{2}$
- $\cos(\theta) = \frac{\sqrt{3}}{2}$
- $\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)} = \frac{1}{\sqrt{3}}$

3. For $\cos(\theta) = -\frac{1}{2}$ in the third quadrant:

- $\sin(\theta)$ must also be negative in the third quadrant, and $\sin^2(\theta) + \cos^2(\theta) = 1$, so $\sin(\theta) = -\frac{\sqrt{3}}{2}$.

13.3.5 Sine and Cosine

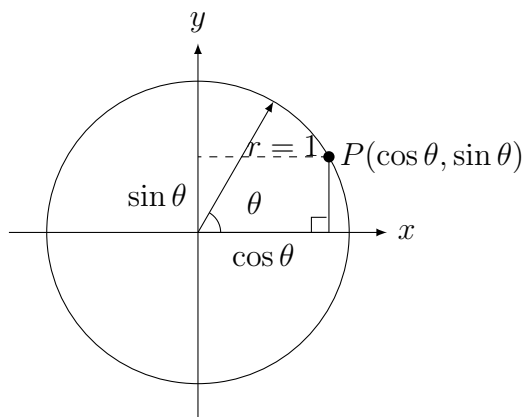
The sine and cosine functions are fundamental to trigonometry. They are defined for a given angle θ within a right-angled triangle as follows:

- The **sine** of angle θ , written as $\sin(\theta)$, is the ratio of the length of the opposite side to the length of the hypotenuse.
- The **cosine** of angle θ , written as $\cos(\theta)$, is the ratio of the length of the adjacent side to the length of the hypotenuse.

However, these definitions are not limited to angles between 0 and $\frac{\pi}{2}$ radians (or 0 and 90 degrees). By extending the concept of the unit circle, where the radius is 1 and the center is at the origin of a coordinate plane, we can define sine and cosine for any real angle.

Sine and Cosine on the Unit Circle

Consider the unit circle with a point $P(x, y)$ that corresponds to an angle θ measured from the positive x-axis. The coordinates x and y of point P on the unit circle are equal to $\cos(\theta)$ and $\sin(\theta)$, respectively.



The unit circle approach allows for a seamless transition of sine and cosine from acute angles to any angle in the coordinate plane. The definitions on the unit circle are as follows:

- For any angle θ , $\sin(\theta)$ is the y-coordinate of the corresponding point on the unit circle.
- For any angle θ , $\cos(\theta)$ is the x-coordinate of the corresponding point on the unit circle.

Properties of Sine and Cosine Functions

The sine and cosine functions have several important properties that are useful in various mathematical analyses:

- They are periodic functions with a period of 2π radians (or 360 degrees).
- The sine function is odd: $\sin(-\theta) = -\sin(\theta)$.
- The cosine function is even: $\cos(-\theta) = \cos(\theta)$.
- The maximum value of both functions is 1, and the minimum value is -1.
- They satisfy the Pythagorean identity: $\sin^2(\theta) + \cos^2(\theta) = 1$.

Understanding these functions and their properties is crucial for solving problems involving periodic behavior and waves, and they are the building blocks for defining the other trigonometric functions.

Example Problems

Below are some problems that help solidify the understanding of sine and cosine functions:

1. Given that $P(x, y)$ is a point on the unit circle corresponding to an angle θ , and $x = \frac{1}{2}$, find y and hence $\sin(\theta)$ and $\cos(\theta)$.
2. Prove the Pythagorean identity $\sin^2(\theta) + \cos^2(\theta) = 1$ using the definition of sine and cosine on the unit circle.
3. If $\sin(\theta) = \frac{3}{5}$ and θ is in the first quadrant, find $\cos(\theta)$.
4. For an angle θ with $\cos(\theta) = -\frac{\sqrt{2}}{2}$ and $\frac{\pi}{2} < \theta < \pi$, determine $\sin(\theta)$.
5. Using the unit circle, find the exact values of $\sin(\frac{\pi}{6})$, $\sin(\frac{\pi}{4})$, $\sin(\frac{\pi}{3})$, $\cos(\frac{\pi}{6})$, $\cos(\frac{\pi}{4})$, and $\cos(\frac{\pi}{3})$.
6. Sketch the unit circle and mark the points where $\sin(\theta) = \cos(\theta)$. What are the angles θ at these points?

Answers to Example Problems

Here are the answers to the example problems provided:

1. Since $x = \cos(\theta) = \frac{1}{2}$, we have $y = \sin(\theta) = \sqrt{1 - \frac{1}{4}} = \sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{2}$.
2. To prove the identity, we use the fact that for any point on the unit circle, the distance from the origin to the point is 1. Hence, $x^2 + y^2 = 1$. Since $x = \cos(\theta)$ and $y = \sin(\theta)$, it follows that $\cos^2(\theta) + \sin^2(\theta) = 1$.
3. Since θ is in the first quadrant, both sine and cosine are positive. Using the Pythagorean identity, $\cos(\theta) = \sqrt{1 - \sin^2(\theta)} = \sqrt{1 - \frac{9}{25}} = \sqrt{\frac{16}{25}} = \frac{4}{5}$.
4. In the second quadrant, sine is positive and cosine is negative. Using the Pythagorean identity, $\sin(\theta) = \sqrt{1 - \cos^2(\theta)} = \sqrt{1 - \frac{1}{2}} = \frac{\sqrt{2}}{2}$.
5. For the specified angles, the exact values can be determined from the known special angles on the unit circle: $\sin(\frac{\pi}{6}) = \frac{1}{2}$, $\sin(\frac{\pi}{4}) = \frac{\sqrt{2}}{2}$, $\sin(\frac{\pi}{3}) = \frac{\sqrt{3}}{2}$, $\cos(\frac{\pi}{6}) = \frac{\sqrt{3}}{2}$, $\cos(\frac{\pi}{4}) = \frac{\sqrt{2}}{2}$, $\cos(\frac{\pi}{3}) = \frac{1}{2}$.
6. On the unit circle, $\sin(\theta) = \cos(\theta)$ at $\theta = \frac{\pi}{4}$ and $\theta = \frac{5\pi}{4}$. These correspond to the points $(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2})$ and $(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2})$, respectively.

Note: The answers provided are meant to guide students in understanding the concepts. Instructors should verify all computations and explanations before use.

13.3.6 Tangent and Cotangent

The tangent of an angle in a right-angled triangle is the ratio of the length of the opposite side to the length of the adjacent side. In the unit circle, tangent is the y-coordinate divided by the x-coordinate when the line made by the angle intersects the circle. Symbolically, for an angle θ , this is expressed as:

$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)}$$

Conversely, the cotangent is the reciprocal of the tangent function. It represents the ratio of the length of the adjacent side to the length of the opposite side, or using the unit circle, the x-coordinate divided by the y-coordinate:

$$\cot(\theta) = \frac{1}{\tan(\theta)} = \frac{\cos(\theta)}{\sin(\theta)}$$

These functions are undefined when their denominators are zero (i.e., when $\cos(\theta) = 0$ for tangent, and when $\sin(\theta) = 0$ for cotangent). This occurs at odd multiples of $\frac{\pi}{2}$ for tangent and at integer multiples of π for cotangent.

The graphs of these functions illustrate their periodic nature and the locations of their asymptotes, which correspond to the angles where the functions are undefined.

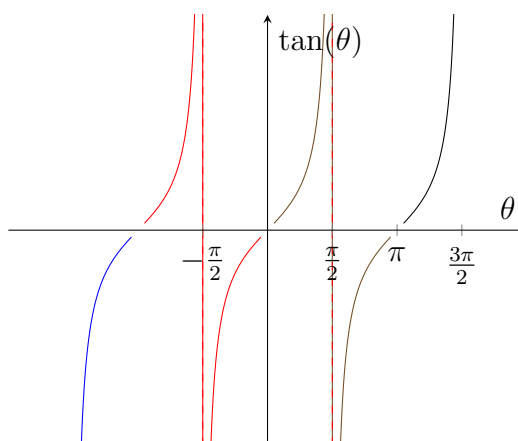


Figure 13.4: Tangent function graph showing asymptotes.

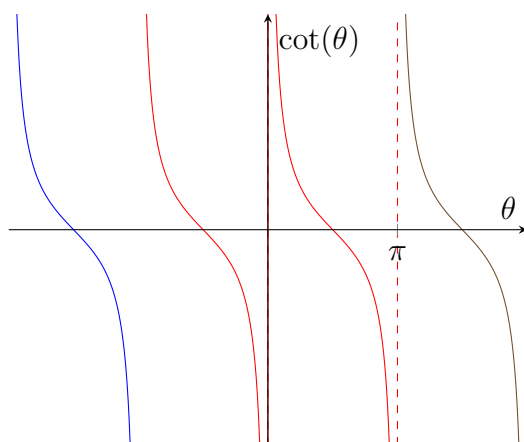


Figure 13.5: Cotangent function graph showing asymptotes.

In calculus, the tangent function is particularly important when it comes to determining the slope of a curve at a point, which is essential for understanding the concept of derivatives. Cotangent can similarly be used, especially when dealing with the slope of reciprocal functions.

13.3.7 Exercises on Tangent and Cotangent Functions

In this section, we provide some example problems involving the tangent and cotangent functions. These exercises are designed to reinforce the concepts discussed and help students gain a deeper understanding of these trigonometric functions.

Exercise Calculate the tangent of $\frac{\pi}{4}$ and verify that it equals 1.

Solution Using the unit circle or the definition of the tangent function, we have:

$$\tan\left(\frac{\pi}{4}\right) = \frac{\sin\left(\frac{\pi}{4}\right)}{\cos\left(\frac{\pi}{4}\right)} = \frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = 1$$

Exercise Find all solutions in the interval $[0, 2\pi)$ for the equation $\tan(\theta) = \sqrt{3}$.

Solution We know that $\tan(\theta) = \sqrt{3}$ when $\theta = \frac{\pi}{3}$, but since tangent has a period of π , the other solution in the given interval is $\theta = \frac{\pi}{3} + \pi = \frac{4\pi}{3}$.

Exercise Evaluate $\cot(\pi)$ and explain why it takes its particular value.

Solution Cotangent is the reciprocal of the tangent function. Since $\tan(\pi) = 0$, and since the cotangent is undefined when its sine component is 0 (which

it is at π), $\cot(\pi)$ is undefined. This reflects the asymptote of the cotangent graph at π .

Exercise Determine the exact value of $\cot\left(-\frac{\pi}{6}\right)$ using the cotangent definition.

Solution Using the cotangent definition and known values of sine and cosine for $\frac{\pi}{6}$, we get:

$$\cot\left(-\frac{\pi}{6}\right) = \frac{\cos\left(-\frac{\pi}{6}\right)}{\sin\left(-\frac{\pi}{6}\right)} = \frac{\frac{\sqrt{3}}{2}}{-\frac{1}{2}} = -\sqrt{3}$$

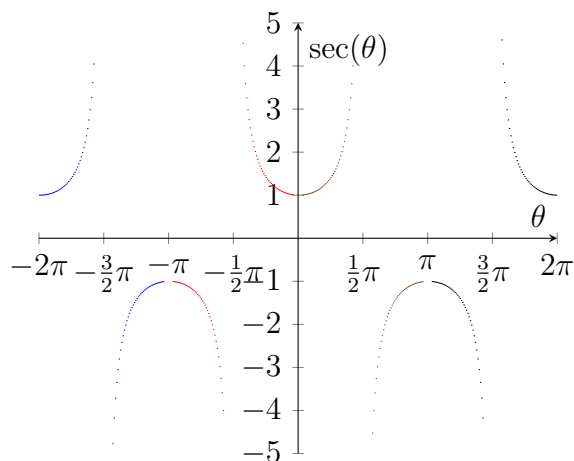
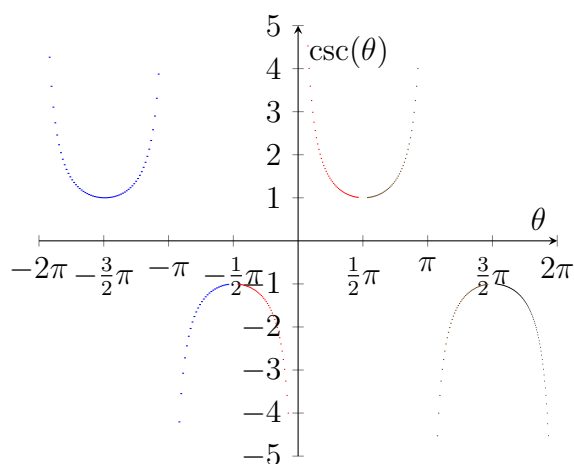
Exercise Sketch the graph of $\tan(\theta)$ and $\cot(\theta)$ from $\theta = -\frac{\pi}{2}$ to $\theta = \frac{3\pi}{2}$ and label the asymptotes.

Solution Students should refer to the graphs provided in the section above and reproduce them by hand, marking the asymptotes at $\theta = -\frac{\pi}{2}$, $\theta = \frac{\pi}{2}$ for the tangent function and at $\theta = 0$, $\theta = \pi$ for the cotangent function.

These exercises require students to apply their understanding of the unit circle, the definitions of tangent and cotangent, and the properties of these functions such as periodicity and asymptotes. Students should attempt these exercises without a calculator to improve their understanding of the trigonometric functions.

13.3.8 Secant and Cosecant

The secant (sec) and cosecant (csc) functions are the reciprocals of the cosine and sine functions, respectively. These functions are less commonly encountered in basic trigonometry but play an important role in calculus, especially in integration that involves trigonometric substitution. In sum, the reciprocal functions of cosine and sine are less commonly used but equally important, especially in certain types of integration.

Graph of the Secant Function**Graph of the Cosecant Function**

These graphs demonstrate the behavior of the secant and cosecant functions and their asymptotic nature at points where their respective sine and cosine functions are zero. Understanding these graphs is essential for solving trigonometric equations and in calculus, particularly when dealing with integrals that require trigonometric identities or substitutions involving these functions.

13.3.9 Practice Problems

Here are some problems to test your understanding of the secant and cosecant functions:

1. Find the secant and cosecant of the following angles:

- (a) 0 radians
- (b) $\frac{\pi}{4}$ radians
- (c) $\frac{\pi}{2}$ radians
- (d) $\frac{3\pi}{4}$ radians

Remember that secant and cosecant are undefined for certain angles where cosine and sine are zero, respectively.

2. Given that $\sin(\theta) = \frac{3}{5}$ in the second quadrant, find $\csc(\theta)$.
3. If $\cos(\theta) = -\frac{1}{2}$ and θ is in the third quadrant, determine $\sec(\theta)$.
4. For an angle θ where $0 < \theta < \frac{\pi}{2}$, if $\sec(\theta) = 3$, find the exact value of $\csc(\theta)$.
5. A point P on the terminal side of angle θ in standard position has coordinates $P(-2, -3)$. Calculate $\sec(\theta)$ and $\csc(\theta)$.
6. Prove the identity $\sec^2(\theta) - 1 = \tan^2(\theta)$.
7. Show that for any angle θ , $\csc(\theta) \cdot \sin(\theta) = 1$.

Solutions to these problems will reinforce your understanding of secant and cosecant and prepare you for their use in calculus.

Conclusion

This chapter serves as the foundation for understanding the vital role of Trigonometry in calculus. As you progress through your studies, these concepts will become second nature, providing the tools necessary for analyzing and solving a broad range of problems in higher mathematics.

Appendix I

Basic GitHub Guide

A Quick Start to Your GitHub Journey

Welcome to the fascinating world of GitHub, a platform that has revolutionized the way we collaborate on projects, share code, and build software together. Whether you are a programmer, a writer, or a mathematician, GitHub provides a set of powerful tools to help you collaborate with others, manage your projects, and contribute to the vast world of open-source software. In this guide, we will walk you through the foundational steps to get started with GitHub, helping you to navigate, contribute, and make the most out of this incredible platform.

Creating Your GitHub Account

The first step to joining the GitHub community is to create an account. Here's how you can do it:

1. Visit the GitHub website.
2. Click on the “Sign up” button.
3. Fill in the required information, including your username, email address, and password.
4. Verify your account and complete the sign-up process.

Once you have created your account, take a moment to explore your new GitHub dashboard. Here, you will find a variety of tools and features that will help you manage your projects, collaborate with others, and discover new and interesting repositories.

Creating Your First Repository

A repository (or “repo”) is a digital directory where you can store your project files. Here’s how you can create your first repository:

1. From your GitHub dashboard, click on the “New” button to create a new repository.
2. Give your repository a name and provide a brief description.
3. Initialize this repository with a README file. (This is an optional step, but it’s a good practice to include a README file in every repository to explain what your project is about.)
4. Click “Create repository.”

Congratulations! You have just created your first GitHub repository. You can now start adding files, collaborating with others, and managing your project right from GitHub.

Making Changes and Commits

GitHub uses Git, a version control system, to keep track of changes made to your project. Here’s a quick guide on how to make changes and commits:

1. Navigate to your repository on GitHub.
2. Find the file you want to edit, and click on it.
3. Click the pencil icon to start editing.
4. Make your changes and then scroll down to the “Commit changes” section.
5. Provide a commit message that explains the changes you made.
6. Choose whether you want to commit directly to the main branch or create a new branch for your changes.
7. Click “Commit changes.”

Your changes are now saved, and a new commit is created. Every commit has a unique ID, making it easy to track changes, revert to previous versions, and collaborate with others.

Collaborating with Others

One of the biggest strengths of GitHub is its collaborative nature. Here are some ways you can collaborate with others:

- **Forking:** You can fork a repository, create your own copy, make changes, and then propose those changes back to the original project.
- **Issues:** Use issues to report bugs, request new features, or start a discussion with the community.
- **Pull Requests:** Propose changes to a project by creating a pull request. This allows others to review your changes, discuss them, and eventually merge them into the project.

Conclusion: Embarking on Your GitHub Adventure

Now that you have a basic understanding of GitHub and how it works, you are ready to embark on your GitHub adventure. Explore repositories, contribute to open-source projects, collaborate with others, and build amazing things together. Remember, the GitHub community is vast and supportive, and there is a wealth of knowledge and resources available to help you along the way. Happy coding!

Appendix II

Basic L^AT_EX Guide

A Quick Start to Your L^AT_EX Journey

Welcome to the immersive world of L^AT_EX, a typesetting system widely used for creating scientific and professional documents due to its powerful handling of formulas and bibliographies. This guide is designed to offer you the foundational steps to grasp the basics of L^AT_EX, enabling you to craft documents of high typographic quality akin to this book.

Setting Up Your L^AT_EX Environment

Before you can start creating documents with L^AT_EX, you need to set up a working L^AT_EX environment on your computer. Here's how you can do it:

1. Download and install a T_EX distribution, which includes L^AT_EX. For Windows, MiKTeX is a popular choice, while Mac users might prefer MacTeX, and TeX Live is widely used on Linux.
2. Install a L^AT_EX editor. Some popular options include TeXShop (for Mac), TeXworks (cross-platform), and Overleaf (an online L^AT_EX editor).
3. Ensure that your T_EX distribution and L^AT_EX editor are properly configured and integrated.

Creating Your First L^AT_EX Document

Once your L^AT_EX environment is set up, you are ready to create your first L^AT_EX document. Follow these steps:

1. Open your L^AT_EX editor and create a new document.
2. Insert the following code to set up a basic L^AT_EX document:

```
\documentclass{article}
\begin{document}
Hello, \LaTeX\ world!
\end{document}
```

3. Save your document with a .tex file extension.
4. Compile your document using your L^AT_EX editor. This process converts your .tex file into a PDF document.
5. View the output PDF and admire your first L^AT_EX creation.

Understanding L^AT_EX Commands and Environments

L^AT_EX documents are created using a series of commands and environments. Commands typically start with a backslash `\` and are used to format text, insert special characters, or execute functions. Environments are used to define specific sections of your document that require special formatting.

- **Commands:** For example, `\{italics}` will render the word "italics" in italic font.
- **Environments:** To create a bulleted list, you would use the *itemize* environment:

```
\begin{itemize}
  \item First item
  \item Second item
\end{itemize}
```

Adding Structure to Your Document

L^AT_EX makes it easy to structure your documents with sections, subsections, and chapters. Here's how you can add structure:

```
\section{Introduction}
This is the introduction of your document.
\subsection{Background}
This subsection provides background information.
\subsubsection{Details}
This is a subsubsection for more detailed information.
```


Including Mathematical Formulas

L^AT_EX excels at typesetting mathematical formulas. Use the *equation* environment or the \$ sign for inline formulas. For example:

The quadratic formula is $\left(x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \right)$.

Adding Images and Tables

You can also include images and tables in your L^AT_EX documents:

- **Images:** Use the *graphicx* package and the *includegraphics* command.
- **Tables:** Use the *tabular* environment to create tables.

Compiling Your Document

L^AT_EX documents need to be compiled to produce a PDF. This can be done through your L^AT_EX editor. If your document includes bibliographies or cross-references, you may need to compile multiple times.

Conclusion: Embracing the Power of L^AT_EX

Congratulations! You have taken your first steps into the world of L^AT_EX. With practice, you will discover that L^AT_EX is a powerful tool for creating professional-quality documents, from simple articles to complex books. Embrace the learning curve, explore the vast array of packages available, and join the community of L^AT_EX users who are ready to help you on your journey. Happy typesetting!

Bibliography

- [MT77] F. Mosteller and J. W. Tukey. *Data Analysis and Regression: A Second Course in Statistics*. Addison-Wesley Pub Co, Reading, MA, 1977.