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Direct simulation of a zero-pressure-gradient turbulent boundary layer up to $Re_{\theta} = 6650$

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Abstract. A direct simulation of an incompressible zero-pressure-gradient turbulent boundary layer over a flat plate is performed in $Re_{\theta} = 1100 - 6650 \, (Re_{\tau} \approx 2025)$, matching the range of the available numerical channels. The logarithmic region and the separation of scales are clearly observed. Proper turbulent inflow conditions, key in boundary layers, are generated by an auxiliary simulation at lower resolution and Reynolds number. Results are in agreement with existing numerical and experimental data sets.

1. Introduction

Turbulent boundary layers are subjects of intensive research because of their technological importance. High-quality direct simulations have recently become possible for wall-bounded flows, mainly channels, featuring an appreciable logarithmic layer. Their role is essential to understand the kinematics and dynamics of the turbulent structures. Turbulent boundary layer Reynolds numbers have increased more slowly than in channels, because the streamwise inhomogeneity is harder to compute, and because of the difficulty of prescribing correct inflow conditions. Simulations have appeared in the past few years at Reynolds numbers up to $Re_{\theta} = 2100$ in [Simens, Jiménez, Hoyas & Mizuno, 2009; Jiménez, Hoyas, Simens & Mizuno, 2010], and $Re_{\theta} = 4060$ in [Schlatter & Örlü, 2010]. They show differences with respect to channels, which are also seen in experiments, but lack a good representation of the logarithmic layer. Therefore, the purpose of the present simulation is to extend the Reynolds number range to $Re_{\theta} \approx 6500$ ($Re_{\tau} = 2000$), comparable to the largest available simulations of numerical channels.

2. Methods

The boundary layer is simulated in a parallelepiped over a flat plate with periodic boundary conditions spanwise and non-periodic in streamwise direction. The turbulent inflow is generated using the method in [Lund, Wu & Squires, 1998], in which the velocities from a reference downstream plane are used to create the incoming turbulence. The effect is equivalent to the trip used in experiments [Simens, Jiménez, Hoyas & Mizuno, 2009], in that the flow must recover from an unrealistic condition to converge to an asymptotic state. The proper scale to measure the length required for that recovery is the distance, $L_{to} = U_{\infty}^{+} \delta$, by which eddies are advected during

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a turnover time δ/u_{τ} , where δ is the boundary-layer thickness, u_{τ} is the local friction velocity and U_{∞} is the free-stream velocity. The effective dimensionless length of the computational box can then be defined as $\tilde{x} = \int_0^x \mathrm{d}x/(\delta U_{\infty}^+)$. It was found in [Simens, Jiménez, Hoyas & Mizuno, 2009] that the accommodation length for most flow scales is at least $\tilde{x} = 1$. That remains true for the all but the largest fluctuations, but experiments during the present simulation convinced us that some properties of the mean profile, especially the shape factor, do not converge until $\tilde{x} \approx 4$. Unfortunately, the ratio δ_{to}/δ increases with the Reynolds number, because u_{τ} decreases, and simulations become increasingly expensive. For example, table 1 includes two of the cases run for this simulations. The first one, BL^I , spans $Re_{\theta} = 2580 - 6340$ in a box approximately twice longer (50δ) than those used in channels, but its mean profile has not reached equilibrium by the end of the box, $\tilde{L}_x \approx 2.57$.

Table 1. Parameters of the turbulent boundary layers cases considered. L_x , L_y and L_z are the box dimensions. The momentum thickness θ is taken at the middle of the box. \tilde{L}_x is the effective dimensionless computational box length. N_x, N_y and N_z are the grid sizes.

Case	Re_{θ}	$(L_x, L_y, L_z)/\theta$	\widetilde{L}_x	$\Delta x^+, \Delta y^+, \Delta z^+$	N_x,N_y,N_z
BL^{I}	2580-6340	$534\times30\times67$	2.57	$6.10\times0.30\times4.15$	$16385 \times 711 \times 4096$
				$13.00 \times 0.32 \times 7.28$ $7.00 \times 0.32 \times 4.07$	$3585 \times 315 \times 2560$ $15361 \times 535 \times 4096$

Since only the largest scales appeared to be involved, the problem was solved using an auxiliary lower-resolution simulation, BL_1^{II} , run in synchrony with the high-resolution main layer. That auxiliary boundary layer uses the rescaling technique to generate its inflow, and is used to feed the inflow of the main simulation, BL_2^{II} , from a plane near the end of BL_1^{II} at $\tilde{x} \approx 2.39$. The lower resolution of BL_1^{II} is justified because its main purpose is to allow the large scales to reach equilibrium. Only a moderate under-resolution is required. Even a linear factor of 2 reduces the computational cost of the auxiliary simulation to about 10% of the main one. In fact, the fluctuation profiles of the auxiliary simulation appear essentially correct, and the intermediate spectrum of figure 3(a) belongs to that case. Note that, since BL_2^{II} does not use a rescaling technique, its accommodation length is very short, and most of its domain can be considered valid.

3. Results

The preliminary statistics presented here are collected over a period of $Tu_{\tau}/\delta = 3$ eddy turnovers, measured at the middle of the domain of BL_2^{II} . This simulation is still in production stage, and 17 eddy turnovers are expected to be collected.

Figure 1(a)-(b) shows the friction coefficient $c_f = 2/U_{\infty}^{+2}$ and the shape factor $H = \delta^*/\theta$ as a function of Re_{θ} compared with available experimental [De Graaff & Eaton, 2000; Osterlund, Johansson, Nagib & Hites, 2000; Purtell, Klebanoff & Buckley, 1981; Erm & Joubert, 1991] and numerical data sets [Schlatter & Örlü, 2010; Simens, Jiménez, Hoyas & Mizuno, 2009]. The present simulation covers a fairly large extent of Reynolds numbers, $Re_{\theta} = 1100 - 6650$, approximately equivalent to channels in the range $Re_{\tau} = 440 - 2025$ as shown in figure 2(e). Tripping techniques are commonly used to trigger turbulence, either in experiments or numerical simulations, and as a consequence, accommodation lengths of $O(\tilde{x})$ are needed. This can be seen in the integral parameters c_f and H. Experiments in [Erm & Joubert, 1991] were tripped at

low Reynolds number by wire, grid and pins, resulting in high scatter up to about $Re_{\theta} \approx 1500$. Numerical simulations in [Simens, Jiménez, Hoyas & Mizuno, 2009], as well as the present one, show the effect of tripping by means of the rescaling technique, resulting in a high c_f and low H. These deviated values last up to distances of \tilde{x} between three and four, to finally settle in agreement with the rest of experimental and numerical data sets. This effect is especially severe at high Reynolds numbers, in which the accommodation length can be as long as the entire numerical domain or the experimental analysis region.

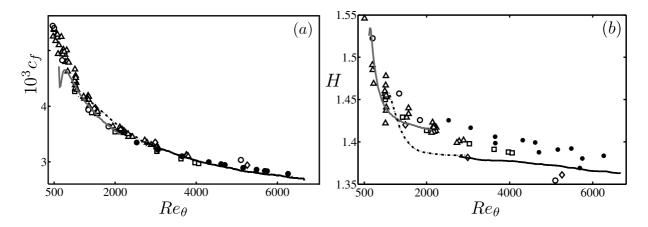


Figure 1. Friction coefficient (a) and shape factor (b) versus Re_{θ} number. Symbols are experiments by [De Graaff & Eaton, 2000], \diamondsuit ; by [Purtell, Klebanoff & Buckley, 1981], \bigcirc ; [Erm & Joubert, 1991], \triangle ; and [Osterlund, Johansson, Nagib & Hites, 2000], \bullet ; and numerical simulations by [Schlatter & Örlü, 2010], \square . Lines are for the present simulation BL_1^{II} , —— and BL_2^{II} , ——; and for [Simens, Jiménez, Hoyas & Mizuno, 2009], ——

In the present simulation, the purpose of the auxiliary BL_1^{II} is to provide realistic inlet conditions for BL_2^{II} , as already discussed. By the end of BL_1^{II} , i.e. at the beginning of BL_2^{II} , the large structures have covered about $\tilde{x} \approx 2.6$ and the values of c_f are settling into agreement with experimental data. Shape factor also falls within the scatter of the experiments.

Figure 2(a)-(d) presents mean and fluctuation velocity profiles from the present simulation compared with some of the experimental and numerical data sets used for figure 1, in the range of $Re_{\theta} = 4060 - 5160$ ($Re_{\tau} \approx 1320 - 1616$), and it shows excellent agreement. Small scales converge to nominal values within an eddy turn-over, approximately in a distance of $22\delta_{99}^{inlet}$ from the inlet. BL_1^{II} velocity fluctuations are essentially correct through the entire domain, with the exception of the inlet accommodation length seen in figure 2(e). Also presented in figure 2 are the data from the numerical channel simulation $Re_{\tau} = 2000$ [Hoyas & Jiménez, 2006] for the velocity fluctuations. While the maximum of u'^+ agrees with the boundary layer fluctuations, the transverse velocity fluctuations, v'^+ and w'^+ , do not, and are higher for the boundary layers. This was already noted by [Hoyas & Jiménez, 2008], although using boundary layer simulations at relatively low Re_{τ} . Figure 2(e) presents the maximum velocity fluctuations over the range $Re_{\tau} = 500 - 2000$ compared with channels at $Re_{\tau} = 180, 550, 950$ and 2000. Both boundary layers and channels exhibit a small Reynolds number dependence in their maximum intensities, failing the classical scaling with u_{τ} near the wall, as already discovered by [De Graaff & Eaton, 2000] in a comparative study of boundary layers. In the buffer layer the squared intensities should be proportional to $u_{\tau}^2 \log(Re_{\tau})$ when the fluctuations are scaled at fixed y^+ instead of y/δ . A slightly different scaling for the velocity fluctuations was investigated by [Jiménez, del Álamo & Flores, 2004 based on spectral arguments, noting that the intensities should be controlled by the scale ratio between the large structures in the outer region and the smallest ones at the buffer region.

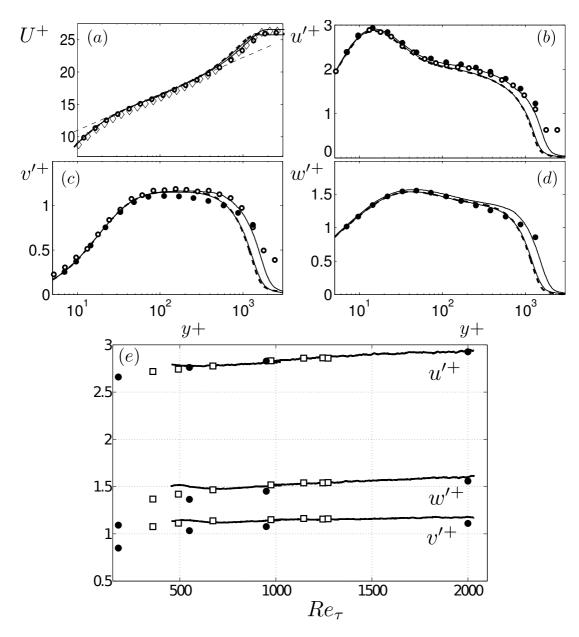


Figure 2. (a) Mean streamwise velocity; (b,c,d) root-mean-squared velocity fluctuations. Symbols are: numerical channel [Jiménez, Hoyas, Simens & Mizuno, 2010] at $Re_{\tau} = 2003$, \bullet ; boundary layer experiments by [De Graaff & Eaton, 2000] at $Re_{\theta} = 5160$, \circ ; and [Osterlund, Johansson, Nagib & Hites, 2000] at $Re_{\theta} = 5156$, \diamond . The simulations by [Schlatter & Örlü, 2010] at $Re_{\theta} = 4060$ are -- . The law $\log(y^+)/0.40 + 5$ is --; and —— are the present simulation at $Re_{\theta} = 4060, 5160$. (e) Maximum value of the velocity fluctuations versus Re_{τ} . \square stands for [Schlatter & Örlü, 2010]

Even more interesting are the spectra in figure 3, which shows premultiplied spectral energy $\Phi_{**} = k_x k_z E_{**}(k_x k_z)$, where k_x and k_z are the wavenumbers in the two wall-parallel directions, with associated wavelengths $\lambda = 2\pi/k$, and * stands for the flow field variables.

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A two-dimensional spectra for boundary layer does not exist mathematically, since the only homogeneous direction is spanwise. Spectra is therefore computed as the Fourier transform of the two-points correlation function of each Fourier mode, after symmetrizing it with respect to x. The largest streamwise wavelength is chosen to be $\lambda_x \approx 20\delta_{99}$ for all the spectra, in which the boundary layer can be approximately considered as a parallel flow (for $\Delta_x \approx 20\delta_{99}$, $\Delta\delta/\delta \approx 0.25$).

Figure 3(a) compares kinetic spectral density energy Φ_{uu}^+ for channels at $Re_{\tau} = 550 - 2000$ and boundary layers at similar values of Re_{τ} at the buffer layer, $y^+ = 15$ and for energy levels of 15% and 57% of the total energy. They clearly show the development of the scale separation with the Reynolds number, and also that the layers are slightly shorter than the channels at similar Re_{τ} [Jiménez, Hoyas, Simens & Mizuno, 2010]. On the other hand, they show that the aspect ratio of the large structures in both flows are essentially the same, $\lambda_x = 10\lambda_z$.

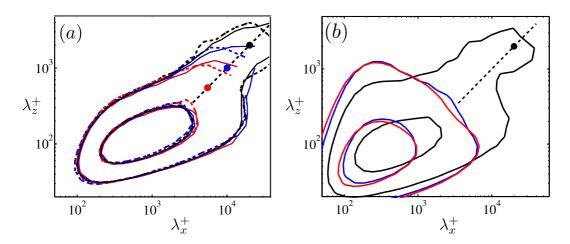


Figure 3. (a) Solid lines are two-dimensional spectral densities Φ_{uu}^+ from channels at $Re_{\tau}=550$ –2000 [Hoyas & Jiménez, 2006], and dashed ones those of boundary layers at $Re_{\tau}=550$ [Jiménez, Hoyas, Simens & Mizuno, 2010], and 1000 and 2000 from the present case at the buffer layer, $y^+=15$, in red, blue, and black respectively. (b) Large scales boundary layer footprint in the vorticity spectral densities $\Phi_{\omega\omega}^+$ at the viscous sublayer $y^+=5$ (black) and for the buffer layer at $y^+=10-15$ (red, blue) at $Re_{\tau}\approx 2000$. In both cases, the straight dashed line is $\lambda_x=10\lambda_z$ and dots are $\lambda_z=Re_{\tau}$.

It is interesting to note the effect of the Reynolds number near the wall, due to the large scale inactive motions in the sense of [Townsend, 1976]. This is clearly seen in figure 3(b), in which the spectral enstrophy density $\Phi_{\omega\omega}^+$ is presented for the boundary layer at $Re_{\tau}\approx 2000$ at different wall-normal locations and for enstrophy levels of 8% and 50% of the total. Near the wall, the flow is irrotational, because the v impermeability condition inhibits the Reynolds stresses $\langle u'v'\rangle$. This can be seen at the buffer layer locations, $y^+=10$ (red) and $y^+=15$ (blue), where the large scales are missing. The nearest wall value is $y^+=5$ (black), within the viscous layer, and in which the potential flow cannot satisfy the no-slip boundary condition, developing a thin rotational sublayer in which structures are long and wide so the no-slip condition is attained [Hoyas & Jiménez, 2008]. Very near to the wall the vorticity is the velocity gradient in the wall-normal direction, therefore, the vorticity and the velocity spectrum should be proportional at a constant y^+ , as observed in figure 3.

Further analysis of the one-dimensional spectra $k|E_{**}^{1D}|$ versus y shows that the streamwise velocities fluctuations structures are long, those for spanwise wide, and those for wall-normal tall. The pressure fluctuations structures are as tall as the wall-normal velocity, but wider and slightly shorter than the streamwise fluctuations ones. This pattern can be observed in figure

4, in which velocity fluctuations of an instantaneous realization of the flow field in the range $Re_{\theta} = 5800 - 6600 \; (Re_{\tau} \approx 1797 - 2016)$ are presented.

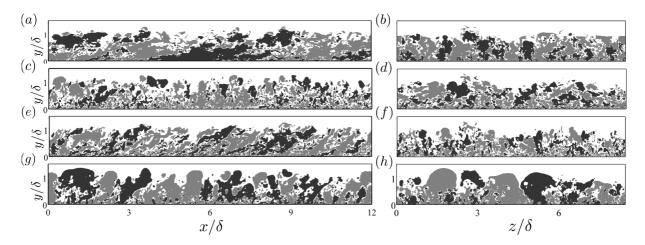


Figure 4. Instantaneous sections of the fluctuations: u^+ (a, b), v^+ (c, d), w^+ (e, f), p^+ (g, h). (a, c, e, g) are the x-y sections for $Re_{\theta}=5800-6600$. (b, d, f, h) are the z-y sections at $Re_{\theta}=5800$. Fluctuations are normalized with the friction velocity, and the coordinates are normalized with δ_{99} at $Re_{\theta}=5800$. Dark grey areas are below -0.5 wall units, and lighter areas above +0.5.

4. Conclusions

We have introduced the concept of the effective dimensionless length \tilde{x} in order to characterize the accommodation length needed for the large-scale structure of the flows to converge from artificial tripping methods to nominal values, resulting in lengths about $\tilde{x} \approx 4$. This is especially severe in the case of high Re_{θ} in which the flow may not achieve the equilibrium by the end of the physical domain. In order to perform a direct numerical simulation of a boundary layer at high Re_{θ} , an auxiliary simulation is conducted using relatively coarse resolution, and resolving correctly the large scales of the flow. The computational penalization of this auxiliary boundary layer is about 10% of the total time. It turns out that even at this low resolution the small scales are essentially well-resolved.

A preliminary analysis of the statistics of this new simulation has been conducted. Integral parameters, such as c_f and the shape factor, are within the scatter of the available experiments and numerical data sets. The same is true of the velocity fluctuations. At this relatively high Reynolds number, the mean profile exhibits a clear logarithmic region, and the fluctuations have been compared with the numerical channel at similar Reynolds numbers. Velocity fluctuations clearly show a weak dependence with the Re_{τ} at the buffer layer, failing the classical scaling with the friction velocity u_{τ} . The new simulation confirms that the transverse velocity fluctuations are stronger in boundary layers than in channels. Energy density spectra also shows the large-scale structure footprint near the wall. Boundary layer and channel kinetic energy spectra are compared in that near-wall region, revealing that the structures for channels are somewhat larger than boundary layers, but showing similar features for the small-scale structures.

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