

Quantum State Tomography and Post Measurement Analysis in Qiskit

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Abstract

The IBM Quantum Experience is a public platform for executing quantum circuits on superconducting back-ends. We execute the Teleportation protocol, Grover's search algorithm, Entanglement Swapping and Entanglement Purification on three superconducting devices available from IBMQ. We analyze the results from post measurement circuits and reconstruct the final quantum state using state tomography.

I. INTRODUCTION

Quantum computers exploit quantum mechanical phenomena in order to perform calculations and manipulate data in ways that would be impossible on classical computers. Quantum algorithms have been developed to teleport data from one place to another, search databases efficiently, and factor large numbers quickly. These algorithms will comprise the building blocks of the quantum computers of the future, and the current efforts towards realizing a truly universal quantum computer centre around improving the manipulation of quantum bits (or qubits), the basic units of computation in these algorithms.

There are many approaches to creating these qubits. Useful qubits instantiate a set of properties that can be at odds with each other at times. For example, a desirable trait like the ability to accurately control the state of the qubit often conflicts with the desire for the qubit to be long-lived (i.e. to have a long coherence time where its quantum state is safe from environmental degradation).

The various implementations make the trade-off between desirable traits in different ways, and a leading approach for creating qubits uses LC circuits in superconductors [1]. Already in 2014, the first demonstrated universal gate set on superconducting qubits with an aver-

age gate fidelity over 99 per cent for all gates was realized [2]. As the field has progressed since then, superconducting qubits have only become more attractive as the building blocks for quantum computers. Now, multi-qubit devices that use superconductors are available publicly, and capable of performing quantum computations that implement small (less than 10 qubits, with limited depth) circuits.

We have simulated and executed a handful of foundational circuits on superconducting devices provided publicly by the IBM Quantum Experience. We use Qiskit, an open-source quantum computing software development platform which has quickly become the most popular means with which to program circuits on publicly available quantum computers. Using 1- and 2-qubit state tomography and post-measurement selection schemes, we reconstruct the average output to characterize the fidelity with which three different superconductor devices implement our chosen circuits.

The purpose of this report is to examine various circuit in order to determine if the post measurement method is valid for different circuits and if we can improve the results form various devices by implementing 1- and 2 qubit state tomography. In the case of for example quantum teleportation or entanglement swapping circuit it is impossible to run the original

circuits on real devices since they require that initial measurements dictate which operators are used on the qubits. This is impossible on IBMQ backends because they do not support operations after measurements. The goal of these measurements is to determine the fidelity of a prepared state to a target pure state. To this end we analyze density matrices and Pauli set plots of the final states. Our state tomography results also allow us to correct for readout error, which is the error caused by the measurement of the qubits in different basis [3].

In this report we first discuss the theory needed to understand state tomography and readout error correction. Then we present our methods for developing Qiskit software and explain the relevant circuits. In results chapter the measurement data is shown and from this data we derive important performance metrics like the fidelity for each circuit on different backends. Finally in the last chapter we discuss the conclusion, recommendations and outlook.

II. THEORY

In a classical computer its internal state is measured at different points in time in order to debug the system. However, for a quantum computer, the analogy would be the measurement of its density matrix, which is called state tomography. We first define the density matrix of a single qubit,

$$\rho = \frac{1}{2} \left(I + \sum_i \alpha_i \sigma_i \right) \quad (1)$$

where σ_i are all the Pauli-matrices and α_i are the real-valued coefficients. Using the trace orthogonality of the Pauli-matrices,

$$\text{Tr}(\sigma_j \sigma_k) = 2\delta_{jk} \quad (2)$$

we can derive the real-valued coefficients by calculating the expectation values of the different Pauli-matrices.

$$\text{Tr}(\rho \sigma_i) = \langle \sigma_i \rangle = \alpha_i \quad (3)$$

By measuring the single qubit in the different basis (X,Y and Z) we can derive these expecta-

tion values. This requires a repeated preparation and measuring of the final state. In reality, the measured expectation values are estimations of $\langle X \rangle, \langle Y \rangle, \langle Z \rangle$. Often in a quantum computer the measurements are only done in the Z-basis. Other operators are realized using rotation operators before the final measurement.

In order to convert the estimated- to real expectation values we correct for readout error, which will give us a better estimation of the density matrix ρ . If $\epsilon_{10}, \epsilon_{01}$ are the probabilities that a $|0\rangle$ state gives an eigenvalue back of -1 and a $|1\rangle$ state which is measured as a eigenvalue 1, and if α, β are coefficients of the final state $|\psi\rangle$, then the measured expectation value $\langle m \rangle$ in the Z-basis is

$$\langle m \rangle = (1 - \epsilon_{10}) |\alpha|^2 + \quad (4)$$

III. METHODS

IV. RESULTS

V. CONCLUSION

To conclude, we live in a society

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