Data Generation

The dataset contains 2000 simulated images, with 1000 images each in groups A and B. Each image has 256 pixels arranged in a 16×16 grid. The β matrix, set to 1 in an 8×8 central region and 0 elsewhere, modifies the pixel values in group A. The group_ind vector differentiates the groups, assigning 1 to group A and 0 to group B. Noise ϵ_i , generated from a multivariate normal distribution with zero mean and a covariance matrix from an exponential correlation function with rate 1, is added to the pixel values.

To adapt the data for the input specifications of the myresf_vc function, the dataset was transformed into a long format. In this format, the columns x and y denote the coordinates, while pixel_value corresponds to the simulated y values.

VBM

In the VBM analysis, a Generalized Linear Model (GLM) was applied pixel-wise to assess group effects on pixel intensities across 100 iterations. For each iteration, the model generated effect size estimates and p-values for each pixel. These p-values were then corrected for multiple comparisons using the Bonferroni method. Figure 1 depicts the frequency of significant p-values in across pixels, with pixels showing significant β in all 100 iterations appearing in black, and those never showing significance in white.

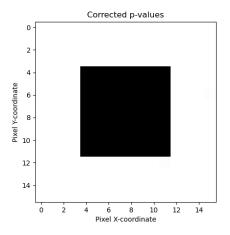
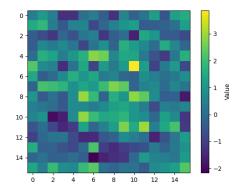
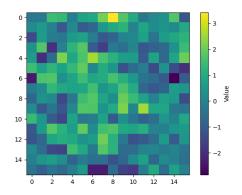


Figure 1:





spVBM

The spVBM model is:

$$y_{s}^{i} = \sum_{k=1}^{K} x_{s,k}^{i} \beta_{s,k}^{SVC} + \mathbf{Z}^{i} \mathbf{b}^{i} + \varepsilon_{s}^{i}$$

$$\beta_{s,k}^{SVC} = \beta_{k} + [\mathbf{E}\Gamma]_{s,k}$$

$$\mathbf{b}^{i} \sim \mathcal{N}(\mathbf{0}, G), \quad \varepsilon_{i} \sim \mathcal{N}\left(0, \sigma^{2}\right), \quad \Gamma_{,k} \sim \mathcal{N}\left(\mathbf{0}, \sigma_{k}^{2} \mathbf{\Lambda}\left(\alpha_{k}\right)\right)$$

 y_s^i denote the spatial outcome for subject i voxel s. $\mathbf Z$ denote non-spatial subject-level covariates for non-spatial random effects.

In our simulated data, this could be simplified to $y_s^i = x_s^i \beta_s^{SVC} + (?)$. My question is, which term captures the exponential correlation structure in the model? G or Γ ?

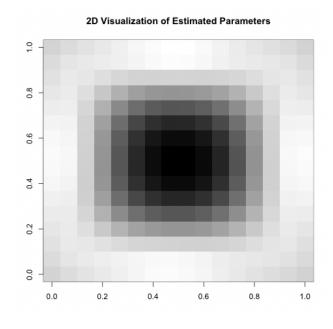


Figure 2: Estimated coefficients