

PHYS 407

5.1 no, plot is not linear

5.2 -10 m/s
 $\frac{20-0}{0-2} = -10$

5.3 no

5.4

~~$v(t) = 30.49t^2 + 12.49t$~~

$v(t) = \frac{x(t+\Delta t) - x(t)}{\Delta t}$

$v(t) = \lim_{\Delta t \rightarrow 0} \left(\frac{20 - 4.9(t+\Delta t)^2 - 20 - 4.9t^2}{\Delta t} \right)$

lim $\Delta t \rightarrow 0$

$\lim_{\Delta t \rightarrow 0} \left(\frac{20 - 4.9t^2 - 9.8t\Delta t - 4.9\Delta t^2 - 20 - 4.9t^2}{\Delta t} \right)$

lim $\Delta t \rightarrow 0$

$\lim_{\Delta t \rightarrow 0} \left(\frac{-9.8t\Delta t - 4.9\Delta t^2}{\Delta t} \right)$

lim $\Delta t \rightarrow 0$

$\lim_{\Delta t \rightarrow 0} (-9.8t - 4.9\Delta t) = -9.8t = v(t)$

PHYS 407

5.5

$x(t) = A + Bt^n$
 $v(t) = \lim_{\Delta t \rightarrow 0} \left(\frac{A + B(t+\Delta t)^n - A - Bt^n}{\Delta t} \right)$

~~$(A + B(t+\Delta t)^n)$~~

$v(t) = \lim_{\Delta t \rightarrow 0} \left(\frac{B(t+\Delta t)^n + Bt^n}{\Delta t} \right)$

$t^n + t^{n-1}\Delta t + \dots + t\Delta t^{n-1} + \Delta t^n$
 $\lim_{\Delta t \rightarrow 0} \left(\frac{2Bt^{n-1} + \Delta t}{\Delta t} \right)$

~~$Bt^{n-1} + \Delta t$~~

5.6

$A = 20 \quad B = -4.9 \quad n = 2 \rightarrow -4.9 \cdot 2 \cdot t = -9.8t = v(t)$

yes

5.7

-9.8 m/s^2 , no other forces acting upon the ball after it leaves the ground

5.8

constant

PHYS 407

