



$$Z_{R_1} = R_1 \quad Z_{R_2} = R_2 \quad Z_C = 1/s$$

$$H(s) = \frac{R_2}{R_2 + R_1 \parallel 1/s} = \frac{R_2}{R_2 + \frac{R_1/s}{R_1 + 1/s} \left(\frac{Cs}{Cs} \right)}$$

$$\stackrel{\left(\frac{R_1 Cs}{R_1 Cs + 1} \right)}{=} \frac{R_2}{R_2 + \frac{R_1}{R_1 Cs + 1}} = \frac{R_2}{\frac{R_2 R_1 Cs + R_2 + R_1}{R_1 Cs + 1}} \cdot \left(\frac{R_1 Cs + 1}{R_1 Cs + 1} \right)$$

$$= \frac{R_2 R_1 Cs + R_2}{R_2 R_1 Cs + R_2 + R_1}$$

$$V_{in}(t) = 10 \sin(200t) + 20 \cos(1000t)$$

$$R_1 = R_2 = 1000 \Omega \quad C = 2 \mu F$$

$$V_{out}(t) = V_{out_1}(t) + V_{out_2}(t)$$

$$V_{out_1}(t) = A_1 |H(j\omega_1)| \cos(\omega_1 t + \theta_1 + \angle H(j\omega_1))$$

$$V_{out_2}(t) = A_2 |H(j\omega_2)| \cos(\omega_2 t + \theta_2 + \angle H(j\omega_2))$$

$$H(s) = \frac{R_2 R_1 C s + R_2}{R_2 R_1 C s + R_2 + R_1} \quad H(j\omega) = \frac{(1000)(1000)(0.000002)j\omega + 1000}{(1000)(1000)(0.000002)j\omega + 1000 + 1000}$$

$$H_1(j\omega) = \frac{400j + 1000}{400j + 2000} = \frac{4j + 10}{4j + 20} = \frac{2j + 5}{2j + 10}$$

$$= \frac{5 + j2}{10 + j2} \cdot \frac{10 - j2}{10 - j2} = \frac{50 - 40j + j20 - 4}{100 + 40j - j20 - 4} = \frac{46 + j10}{96}$$

$$= 0.48 + j0.1$$

$$|H(j\omega_1)| = 0.49$$

$$\angle H(j\omega_1) = 11.77^\circ$$

$$H_2(j\omega_2) = \frac{1000 + j2000}{2000 + j2000} = \frac{1 + j2}{1 + j} \cdot \frac{1 - j}{1 - j} = \frac{1 - j + j2 + 2}{2}$$

$$= \frac{3 + j}{2} = \frac{3}{2} + j\frac{1}{2} \quad |H(j\omega_2)| = 1.58 \quad \angle H(j\omega_2) = 18.43^\circ$$

$$V_{out}(t) = 4.9 \cos(200t - 78.23^\circ) + 31.6 \cos(1000t + 18.43^\circ)$$