ວງກບ້ານ

💠 ຈົ່ງໃຊ້ວິທີ Gradient ແລະ ວິທີ Laplacian ເພື່ອຊອກຫາພາບຂອບ ຂອງຂໍ້ມູນພາບລຸ່ມນີ້.

56	90	21	234
18	9	12	2
0	5	0	0
0	2	1	9

0	1	0
1	-4	1
0	1	0

	$H_{\scriptscriptstyle R}$				
	-1	-2	-1		
$\frac{1}{4}$	0	0	0		
•	1	2	1		

	H_{c}				
	1	0	-1		
$\frac{1}{4}$	2	0	-2		
4	1	0	-1		

I(x, y)

ໜ້າກາກ H(x, y) ສຳລັບວິທີ Laplacian.

ໜ້າກາກ Sobel ສໍາລັບວິທີ Gradient

ແກ້

- ວິທີ Gradient ໂດຍໃຊ້ໜ້າກາກ Sobel:
- ຂັ້ນຕອນທີ 1: ຂະຫຍາຍຂອບພາບໂດຍການຕື່ມຄ່າສູນ

0	0	0	0	0	0
0	56	90	21	234	0
0	18	9	12	2	0
0	0	5	0	0	0
0	0	2	1	9	0
0	0	0	0	0	0

I(x,y) ທີ່ຕື່ມຄ່າສູນແລ້ວ

- ຂັ້ນຕອນທີ 2: ຫາຄ່ຳ
$$G_R(x,y)=|I(x,y)*H_R(x,y)|$$

0	0	0	0	0	0
0	56	90	21	234	0
0	18	9	12	2	0
0	0	5	0	0	0
0	0	2	1	9	0
0	0	0	0	0	0

$$G_R(1,1) = \frac{1}{4}|(18x2) + (9x1)| = \frac{1}{4}|36 + 9| = 11.25 \approx 11$$

$$G_R(1,2) = \frac{1}{4} |(18x1) + (9x2) + (12 x 1)| = \frac{1}{4} |18 + 18 + 12| = 12$$

$$G_R(1,3) = \frac{1}{4}|(9x1) + (12x2) + (2 x 1)| = \frac{1}{4}|9 + 24 + 2| = 8.75 \approx 9$$

$$G_R(1,4) = \frac{1}{4}|(12x1) + (2x2)| = \frac{1}{4}|12 + 4| = 4$$

$$G_R(2,1) = \frac{1}{4} |(56x(-2)) + (90x(-1)) + (5 \times 1)| = \frac{1}{4} |-112-90+5| = 49.25 \approx 49$$

$$G_R(2,2) = \frac{1}{4} |(56x(-1)) + (90x(-2)) + (21 x(-1)) + (5x2)| = \frac{1}{4} |-56 - 180 - 21 + 10| = 61.75 \approx 62$$

$$G_R\left(2,3\right) = \frac{1}{4}|(90x(-1)) + (21x(-2)) + (234\ x(-1)) + (5x1)| = \frac{1}{4}|-90-42-234+5| = 90.25 \approx 90$$

$$G_R(2,4) = \frac{1}{4} |(21x(-1)) + (234x(-2))| = \frac{1}{4} |-21-468| = 122.25 \approx 122$$

$$G_R\left(3,1\right) = \frac{1}{4}|(56x(-2)) + (90x(-1)) + (5 \ x \ 1)| = \frac{1}{4}|-112-90+5| = 49.25 \approx 49$$

$$G_R\left(3,2\right) = \frac{1}{4}|(56x(-1)) + (90x(-2)) + (21\ x(-1)) + \ (5\ x\ 2)| = \frac{1}{4}|-56-180-21+10| = 61.75 \approx 62$$

$$G_R\left(3,3\right) = \frac{1}{4}|(90x(-1)) + (21x(-2)) + (234\ x(-1)) + \ (5\ x\ 1)| = \frac{1}{4}|-90-42-234+5| = 90.25 \approx 90$$

$$G_R(3,4) = \frac{1}{4}|(21x(-1)) + (234x(-2))| = \frac{1}{4}|-21-468| = 122.25 \approx 122$$

$$G_R(4,1) = \frac{1}{4} |(5 \times (-1))| = 1.25 \approx 1$$

$$G_R(4,2) = \frac{1}{4} |(5 \text{ x}(-2))| = 2.5 \approx 3$$

$$G_R(4,3) = \frac{1}{4} |(5 \text{ x (-1)}| = 1.25 \approx 1)$$

 $G_R(4,4) = 0$

ສຸດທ້າຍຈະໄດ້:

11	12	9	4
49	62	90	122
49	62	90	122
1	3	1	0

- ຂັ້ນຕອນທີ 3: ຫາຄ່ຳ
$$G_C(x,y) = |I(x,y) * H_C(x,y)|$$

0	0	0	0	0	0
0	56	90	21	234	0
0	18	9	12	2	0
0	0	5	0	0	0
0	0	2	1	9	0
0	0	0	0	0	0

$$\begin{split} G_c\left(1,1\right) &= \frac{1}{4}|(90x(-2) + (9x(-1))| = \frac{1}{4}|-180 - 9| = 47.25 \approx 48 \\ G_c\left(1,2\right) &= \frac{1}{4}|(56x2) + (21x(-2)) + (18 \ x \ 1) \ x \ (12 \ x(-1))| = \frac{1}{4}|112 - 42 + 18 - 12| = 19 \\ G_c\left(1,3\right) &= \frac{1}{4}|(90x2) + (234x(-2) + (9 \ x \ 1) + (2 \ x \ (-1))| = \frac{1}{4}|180 - 468 + 9 - 2| = 70.25 \approx 70 \\ G_c\left(1,4\right) &= \frac{1}{4}|(21x2) + (12x1)| = \frac{1}{4}|42 + 12| = 13.5 \approx 14 \\ G_c\left(2,1\right) &= \frac{1}{4}|(90x(-1)) + (9x(-2)) + (5 \ x(-1)| = \frac{1}{4}|-90 - 18 - 5| = 28.25 \approx 28 \\ G_c\left(2,2\right) &= \frac{1}{4}|(56x1) + (21 \ x(-1)) + (18x2) + (12x(-2))| = \frac{1}{4}|56 - 21 + 36 - 24| = 11.75 \approx 12 \\ G_c\left(2,3\right) &= \frac{1}{4}|(90x1)) + (234 \ x(-1)) + (9x2) + (2x(-2)) + (5x1)| = \frac{1}{4}|90 - 234 + 18 - 4 + 5| = 31.25 \approx 31 \\ G_c\left(2,4\right) &= \frac{1}{4}|(21x1) + (12x2)| = \frac{1}{4}|21 + 24| = 11.25 \approx 11 \end{split}$$

$$G_c(3,1) = \frac{1}{4}|(9x(-1)) + (5x(-2)) + (2x(-1))| = \frac{1}{4}|-9-10-2| = 5.25 \approx 5$$

$$G_c\left(3,2\right) = \frac{1}{4}|(18x-1) + (12x(-1)) + (1\ x(-\ 1))| = \frac{1}{4}|-18-12-1| = 7.75 \approx 8$$

$$G_c\left(3,3\right) = \frac{1}{4}|(9x1) + (2x(-1)) + (5\ x\ 2) + \ (2\ x\ 1) + (9x(-1))\ | = \frac{1}{4}|9 - 2 + 10 + 2 - 9| = 2.5 \approx 3$$

$$G_c\left(3,4\right) = \tfrac{1}{4} \! |(12x1) + (1x1)| = \tfrac{1}{4} \! |12\!+\!1| = 3.25 \approx 3$$

$$G_c\left(4,1\right) = \frac{1}{4} |(5 \ x \ (\text{-}1) + (2x(\text{-}2))| = \frac{1}{4} |\text{-}5\text{-}4| = 2.25 \approx 2$$

$$G_c(4,2) = \frac{1}{4}|(1 \text{ x}(-2))| = 0.5 \approx 1$$

$$G_c\left(4,3\right) = \frac{1}{4} |(5 \ x \ 1) + (2x2) + (9x(-2))| = 2.25 \approx 2$$

$$G_c(4,4) = \frac{1}{4} |(1x \ 2)| = 0.5 \approx 1$$

ສຸດທ້າຍຈະໄດ້:

48	19	70	14
28	12	31	11
5	8	3	3
2	1	2	1

- ຜົນໄດ້ຮັບການຫາຂອບພາບ ໂດຍໃຊ້ວິທີ Gradient ໂດຍໃຊ້ໜ້າກາກ Sobel

11	12	9	4
49	62	90	122
49	62	90	122
1	3	1	0

$$G_R(x,y) = |I(x,y) * H_R(x,y)|$$

$$G_C(x,y) = |I(x,y) * H_C(x,y)|$$

59	31	79	28
77	74	121	133
54	70	93	125
3	4	3	1

$$G(x,y) = |I(x,y)*H(x,y)|$$

- \succ ວິທີ Laplacian ໂດຍໃຊ້ໜ້າກາກ $\mathbf{H}(x,y)$
- ຂັ້ນຕອນທີ 1: ຂະຫຍາຍຂອບພາບໂດຍການຕື່ມຄ່າສູນ

0	0	0	0	0	0
0	56	90	21	234	0
0	18	9	12	2	0
0	0	5	0	0	0
0	0	2	1	9	0
0	0	0	0	0	0

I(x,y) ທີ່ຕື່ມຄ່າສູນແລ້ວ

- ຂັ້ນຕອນທີ 2: ຫາຄ່ຳ $G(x,y) = \|I(x,y)*H(x,y)\|$

0	0	0	0	0	0
0	56	90	21	234	0
0	18	9	12	2	0
0	0	5	0	0	0
0	0	2	1	9	0
0	0	0	0	0	0

0	1	0			
1	-4	1			
0	1	0			
H(x,y)					

$$G(1,1) = |(56x(-4) + (90x1) + (18x1))| = |-244 + 90 + 18| = 116$$

$$G(1,2) = G(1,2) = |(56 \times 1) + (90 \times (-4)) + (21 \times 1) + (9 \times 1)| = 274$$

$$G(1,3) = |(90x1) + (21x(-4)) + (234x1) + (12x1)| = |90-84+234+12| = 252$$

$$G(1,4) = |(21x1) + (234x(-4)) + (2x1)| = |21-936 + 2| = 913$$

$$G(2,1) = |(56x1) + (18x(-4)) + (9x1)| = |56-72 + 9| = 7$$

$$G(2,2) = |(90x1) + (18x1) + (9x(-4)) + (12x1) + (5x1)| = |90 + 18 - 36 + 12 + 5| = 89$$

$$G(2,3) = |(21x1) + (9x1) + (12x(-4)) + (2x1)| = |21 + 9 - 48 + 2| = 16$$

$$G(2,4) = |(234x1) + (12x1) + (2x(-4))| = |234 + 12 - 8| = 238$$

$$G(3,1) = |(18x1) + (5x1)| = |18 + 5| = 23$$

$$G(3,2) = |(9x1) + (5x(-4)) + (2x1)| = |9-20 + 2| = 9$$

$$G(3,3) = |(12x1) + (5x1) + (1x1)| = |12 + 5 + 1| = 18$$

$$G(3,4) = |(2x1) + (9x1)| = |2 + 9| = 11$$

$$G(4,1) = |(2x1)| = 2$$

$$G(4,2) = |(5x1) + (2x(-4)) + (1x1)| = |5 - 8 + 1| = 2$$

$$G(4,3) = |(2x1) + (1x(-4)) + (9x1)| = |2-4+9| = 7$$

$$G(4,4) = |(1x1) + (9x(-4))| = |1-36| = 35$$

- ຜົນໄດ້ຮັບການຫາຂອບພາບ ໂດຍໃຊ້ວິທີ Laplacian ໂດຍໃຊ້ໜ້າກາກ H(x,y)

56	90	21	234
18	9	12	2
0	5	0	0
0	2	1	9

$$G(x,y) = |I(x,y) * H(x,y)|$$