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## READ THESE INSTRUCTIONS CAREFULLY BEFORE YOU BEGIN.

- 1. This exam consists of this cover page and 8 pages of questions (total of 9 pages) worth a total of 150 points. You will have 75 minutes to complete this exam.
- 2. You are authorized to use your course notes and R/Rstudio (blank scripts only). You may NOT use any resources that are not on the authorized reference list, including computers, phones, the Internet, your textbook, and your classmates.
- 3. All work written on this exam will be graded unless it is clearly marked through. To receive full credit for your answer, you must show ALL mathematical work and provide explanations within the context of the associated research question.
- Clearly indicate your final answer for questions that require calculations and round all numbers to at least three significant digits.
- 5. Use a blank continuation sheet and clearly identify that the problem is continued both on the exam and on the continuation sheet. Use one continuation sheet per problem continued. Be sure to put your name on each continuation sheet.
- Cadets are not authorized to discuss the content, structure, or any other information about this exam
  until this exam has been released from academic security. Discussion includes all forms of written,
  electronic, and verbal communication.
- Honor Acknowledgement Statement: Sign and date the statement below when you have finished the exam and are ready to submit it for grading.

"I did not use any sources nor did I receive any assistance while completing this exam. I will not discuss this exam with anyone until it is released from academic security on hours."

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Joshun Blachman

Printed Name of Cadet

Signature of Cadet

Time and Data Signed

Time and Date Signed

Question	1	2	3	Total
Points	55	70	25	150
Total	37	37	15	89

## Part 1 (55 pts)

The Donner Party were a group of emigrants moving to start a new life in California. But between 1846 and 1847, 45 out of the 87 people on the wagon train would die from sickness, starvation, murder, and cannibalism. You conduct an analysis on the data and get the following output:

```
library(tidyverse)
library(faraway)
donner_dat <- read.table("https://dnett.github.io/S510/Donner.txt",header=T)</pre>
donner_dat <- donner_dat %>% mutate(survive=ifelse(status=="DIED",0,1))
our_glm <- glm(survive~sex+age,data=donner_dat,</pre>
               family="binomial")
summary(our_glm)
##
## Call:
## glm(formula = survive ~ sex + age, family = "binomial", data = donner_dat)
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.23041
                           1.38686
                                     2.329 0.0198 *
## sexMALE
               -1.59729
                           0.75547 -2.114
                                              0.0345 *
## age
               -0.07820
                           0.03728 - 2.097
                                             0.0359 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 61.827 on 44 degrees of freedom
## Residual deviance: 51.256 on 42 degrees of freedom
## AIC: 57.256
##
## Number of Fisher Scoring iterations: 4
```

P1.1 (20) Write the complete estimated regression equation of the model using the summary output ensuring you have properly identified the function, linear predictor and distribution of the data.

$$N_{i} = \frac{1}{3.23041} = 1.59724 \text{ (Male)} - 0.07820 \text{ (age)}$$

$$N_{i} = \frac{2}{3.23041} = 1.59724 \text{ (Male)} - 0.07820 \text{ (age)}$$

$$This = \frac{2}{1+2\pi i} = -7 \quad N_{i} = \log\left(\frac{7\pi i}{1-7\pi i}\right) = \frac{2}{1+2\pi i}$$

```
You next run the model:
our_glm2 <- glm(survive-sex+age+sex:age,data=donner_dat,family="binomial")</pre>
summary(our glm2)
##
## Call:
##
    glm(formula = survive ~ sex + age + sex:age, family = "binomial",
 ##
        data = donner_dat)
 ##
 ## Coefficients:
 ##
                Estimate Std. Error z value Pr(>|z|)
 ## (Intercept) 7.24638
                            3.20517
                                     2.261
                                              0.0238 *
 ## sexMALE
                -6.92805
                                              0.0415 *
                            3.39887 -2.038
                -0.19407
                            0.08742 -2.220
                                              0.0264 *
                                              0.0865 .
 ## sexMALE:age 0.16160
                            0.09426
                                      1.714
 ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
    (Dispersion parameter for binomial family taken to be 1)
 ##
##
##
        Null deviance: 61.827 on 44 degrees of freedom
## Residual deviance: 47.346 on 41 degrees of freedom
## AIC: 55.346
##
## Number of Fisher Scoring iterations: 5
P1.2 (10) Based on all the information given, which model would you prefer and why? To
answer this question, perform a statistical test, ensure you give the test statistic and the
distribution of that test statistic.
The AIC of our-glow & is lower homes better as it accomts for the complexity of the convention and the Libellihood of id.
                       AI( i) not a statistical

test

AI( i) not a statistical
    +6
P1.3 (5) According to our_glm how does the person's age impact the odds that they survived?
      According to on-glm, for every year own someone's age, they are
e (-0.07520) = 0.92477
```

0.07522 less likely to die.

P1.4 (10) Assuming you wanted to compare our_glm with a model that was not nested explain how you could do this WITHOUT relying on AIC or BIC.
I would use log trephood and compare each midels as a medic. It
and of All and BIL but Joesn's account for devices or
middle necessarily the 18 18 18 18 18 18
Wo-11 always Pactor make complex modes
- train / teat split
- trein / team split. Calcular Auc in 7, min chassifie
+5
P1.5 (10) Your officemate states that you should conduct a goodness of fit test by testing the deviance of the model and runs the test:
1-pchisq(51.256,41)
## [1] 0.1308893
Is this a correct approach? If no, provide an alternative approach. If it is a correct approach provide a conclusion. Note here if you provide an alternative approach you do not have to actually carry out the test.
This carnette as it uses flax residul dorme of the model with the
corresponding degrees at freedom. What would be better to it we used
the Superence bedroom the null and reniting domined and It. This would
be No. data all
1 - pibrisar (10.571,2)
Need
Hosmer - Lene them
+15

## Part 2 (70 pts)

You are interested in exploring factors that impact the number of burglaries in Chicago so you collect data on 552 different city blocks and count the number of burglaries that occur over a month. You also collect data on the percent of the population that is unemployed and the average salaries on the block. In this class we have discussed at least four different models that could be used to analyze this data. In particular, you could use a negative binomial distribution, a Poisson distribution, a Quasi-Poisson, or a zero inflated Poisson.

P2.1 (30) Discuss how you would go about picking between these four models. Give examples It of the models can be used for count data but to choose which one I use, I would first fit the model to pier variance by man plot in a fitted possession model and charle a goodness of fix there we would use possion specifically for data distribution that have a lot of four numbers but infinish by. If the plot shows (a non-harmal pattory then it is overtispersed. If the Lata is overlyppised then the options for an ordervade model frop to quisi poisson hogolar smountat. As we are not doing a strong on where an ortrane occurs, We cannot attribute the use of negative barmin ! I stry cointing the days und) biglion orins in a city block would be better for negative & mininto House wouldn't be able to tell of the overlisposeran files to a gamma Easth Hon, we garner person. In the every that we can the the data will but the obspired frequency of zorocs is expossive than ZIP model would be iden! Hich , Owall, I would use Cooling hood to thoose which made I and the higher and more interpretable. It is [poisson and negative barrains are better), the befor the model,

+20

See South

P2.2 (15) Your friend decides to fit the following model, write out the model that they are fitting and explain what issues they may have fitting this model:

chi\_df <- read.csv("chi\_burg.csv")</pre>

The identity link is used for linear regression. To use poisson, we must use the log link. ( glp) = log(w). I

Bor why?

i = buglan zi ~ Porss (Xi)

 $\begin{array}{ccc}
\lambda \in (0,\infty) \\
\beta \in (-\infty,\infty)
\end{array}$   $\gamma_{i} = \beta_{0} + \beta_{i} \text{ then playmod} + \beta_{2} \text{ wealth}$ 

America Line Co.

+7

e== bo + pi; manplaymet + pz; wenth

P2.3(15) You fit the model below and run the below lines of code to assess your model. Explain what you are checking in the model, what your findings suggest, and what you would do next.

sum(residuals(chi\_mod,type="pearson")^2)/chi\_mod\$df.residual

## [1] 1.332808

1-pchisq(deviance(chi\_mod),df.residual(chi\_mod))

## [1] 1.746496e-10

We are thorning goodness of the hore with the Pearson x2 toit.

P2.3(10) Your roommate has heard about quasi-Poisson models and decides to a quasi-Poisson model to the data, they argue that they can use AIC to compare their model to your Poisson regression model. Are they correct? Why/why not?

We can use All butnot a dovimic to conduct goodness of fit.
Log libelihood files beder however.

All relies on livelihous "
Q-P connet collecte likelihood

So connet 440

+5



## P3 (25 Pts) For the distribution listed below:

- Show that it is part of the exponential dispersion family
- Identify the canonical parameter  $\theta$
- Show that the expected value is  $\mu$  and find the variance function (in terms of  $\mu$ )

$$f(y|\mu,\lambda) = \left(\frac{\lambda}{2\pi y^3}\right)^{1/2} \exp\left(\frac{\lambda}{2\mu^2} \frac{(y-\mu)^2}{y}\right)$$

*HINT:* Let  $\phi = \frac{1}{\lambda}$  and  $b(\theta) = -\sqrt{-2\theta}$ 

$$b(\theta) = -(-20)^{1/2}$$

$$\theta = ? - \sqrt{\theta = \mu^2/y}$$

$$\frac{2\mu^{2}}{\lambda} - \frac{4\mu^{3}}{\lambda} + \frac{2\mu^{4}}{\lambda y}$$