Trig Formulas

Pythagorean Formulas: (Memorize only these)

- 1. $\sin^2(x) + \cos^2(x) = 1$
- 2. $\tan^2(x) + 1 = \sec^2(x)$
- 3. $1 + \cot^2(x) = \csc^2(x)$

Sum & Difference Formulas:

- 1. $\sin(x_1 \pm x_2) = \sin(x_1)\cos(x_2) \pm \cos(x_1)\sin(x_2)$
- 2. $\cos(x_1 \pm x_2) = \cos(x_1)\cos(x_2) \mp \sin(x_1)\sin(x_2)$
- 3. $\tan(x_1 \pm x_2) = \frac{\tan(x_1) \pm \tan(x_2)}{1 \tan(x_1)\tan(x_2)}$

Double Angle Formulas:

- $1. \sin(2x) = 2\sin(x)\cos(x)$
- 2. $\cos(2x) = \cos^2(x) \sin^2(x)$ = $2\cos^2(x) - 1$ = $1 - 2\sin^2(x)$

Half Angle Formulas:

1.
$$\sin\left(\frac{x}{2}\right) = \pm\sqrt{\frac{1-\cos(x)}{2}}$$
 OR $\sin(x) = \pm\sqrt{\frac{1-\cos(2x)}{2}}$

2.
$$\cos\left(\frac{x}{2}\right) = \pm\sqrt{\frac{1+\cos(x)}{2}}$$
 OR $\cos(x) = \pm\sqrt{\frac{1+\cos(2x)}{2}}$

Product Formulas:

1.
$$\sin(x_1)\sin(x_2) = \frac{1}{2}\left(\cos(x_1 - x_2) - \cos(x_1 + x_2)\right)$$

2.
$$\cos(x_1)\cos(x_2) = \frac{1}{2}\left(\cos(x_1 - x_2) + \cos(x_1 + x_2)\right)$$

3.
$$\sin(x_1)\cos(x_2) = \frac{1}{2}\left(\sin(x_1 - x_2) + \sin(x_1 + x_2)\right)$$