

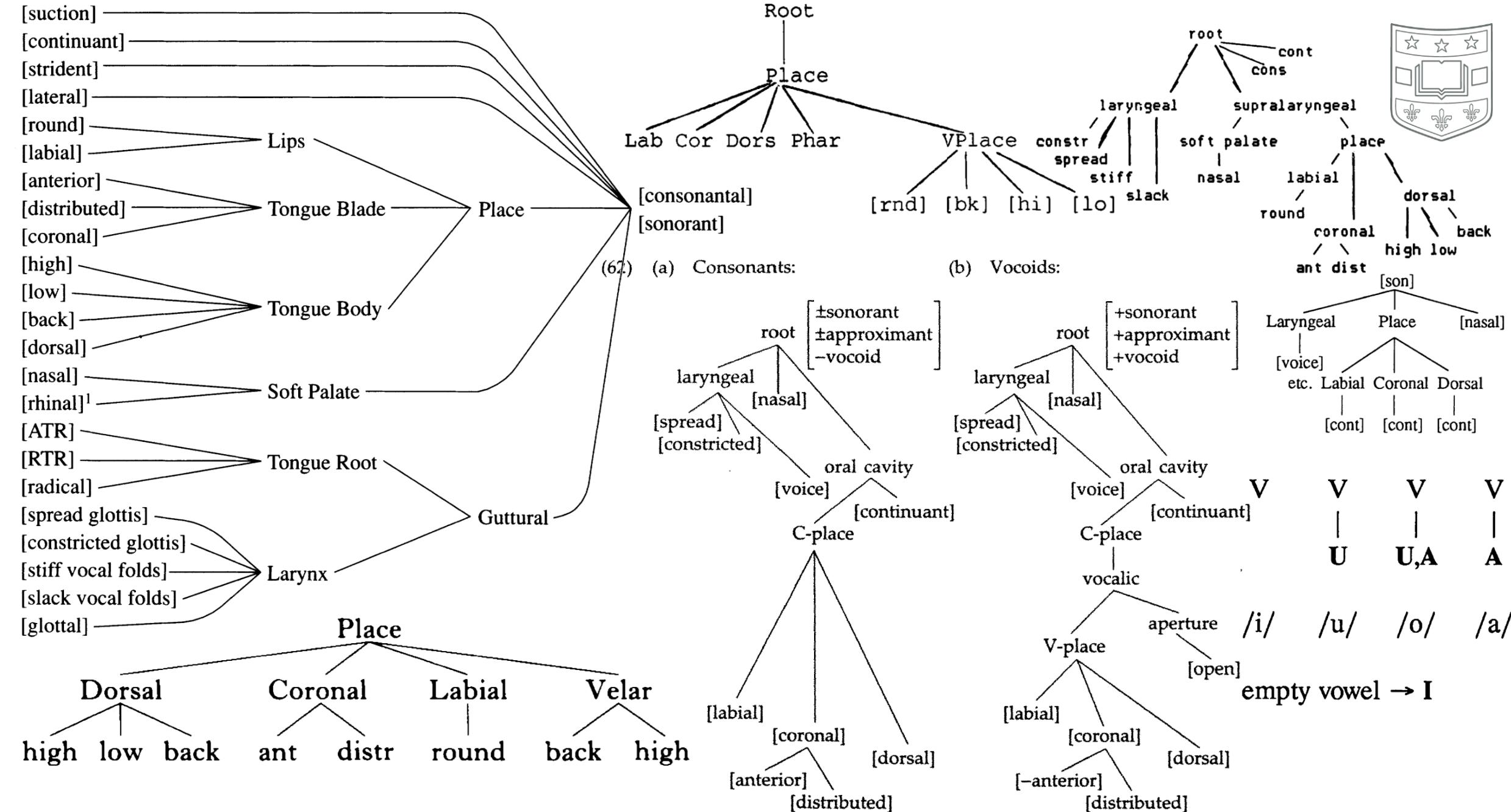
Natural class-preserving transductions among phonological representations

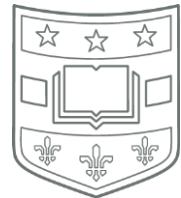
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Workshop on Model Theoretic Representations in Phonology
Stony Brook University, September 22-24, 2022

 Washington University in St. Louis

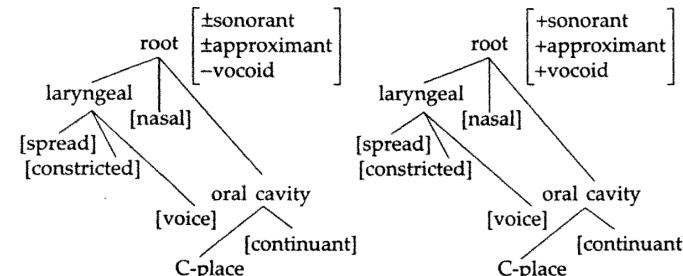




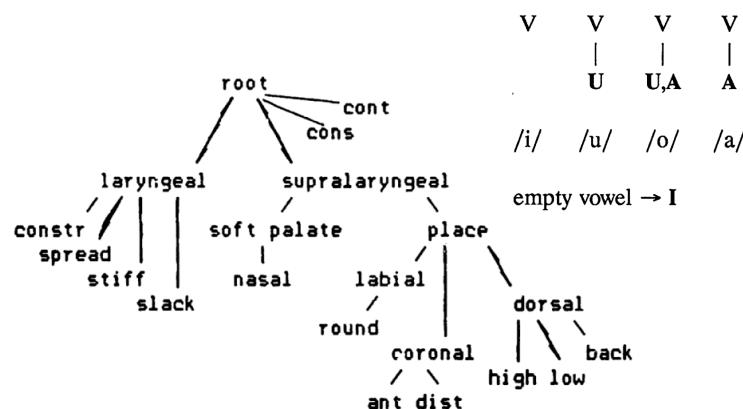
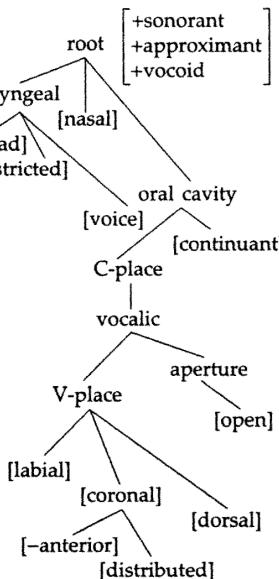


consonants and vowels probably should be natural classes

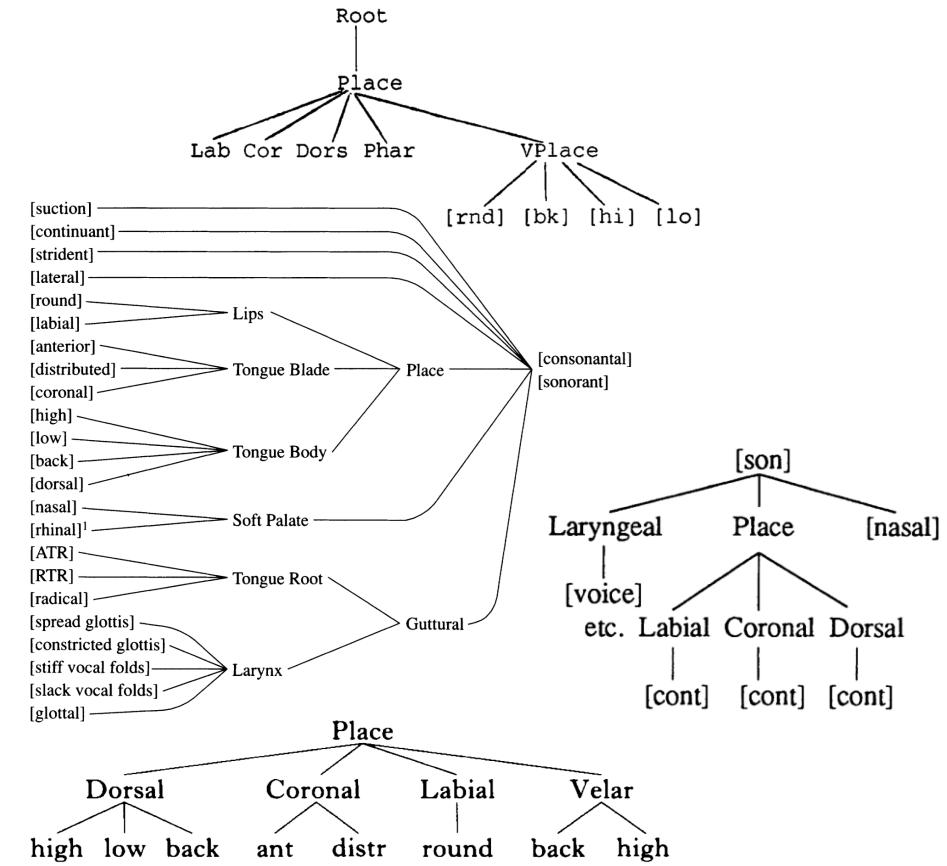
(62) (a) Consonants:



(b) Vocoids:



consonants and vowels probably *shouldn't* be natural classes





big questions

- how can we formally compare phonological representations?
- what can we learn from these comparisons?
- what does it mean for us as linguists?
- what does *anything* mean?



medium answers

- two theories can be shown to be **formally equivalent** using logic and model theory
 - given two representations A and B, a **transduction** between A and B means that any linguistic rule given with structure A can be translated into structure B, and vice versa
 - Strother-Garcia (2019), Danis & Jardine (2019), Oakden (2020), a.o.

Figure 4.5: $\mathcal{M}_{\text{plenty}}^{\text{flat}}$

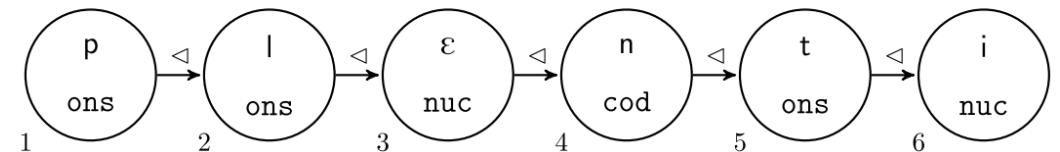
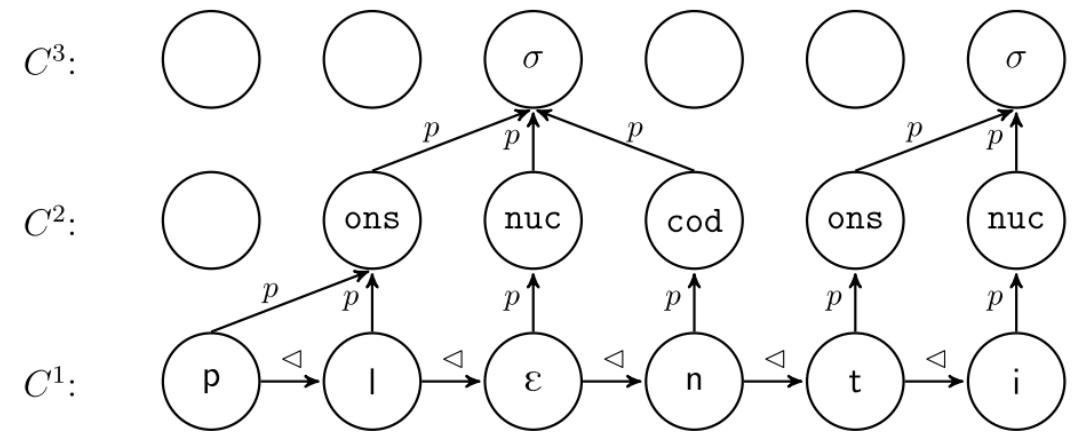


Figure 4.16: $\Gamma_{ft}(\mathcal{M}_{\text{plenty}}^{\text{flat}})$ fully specified

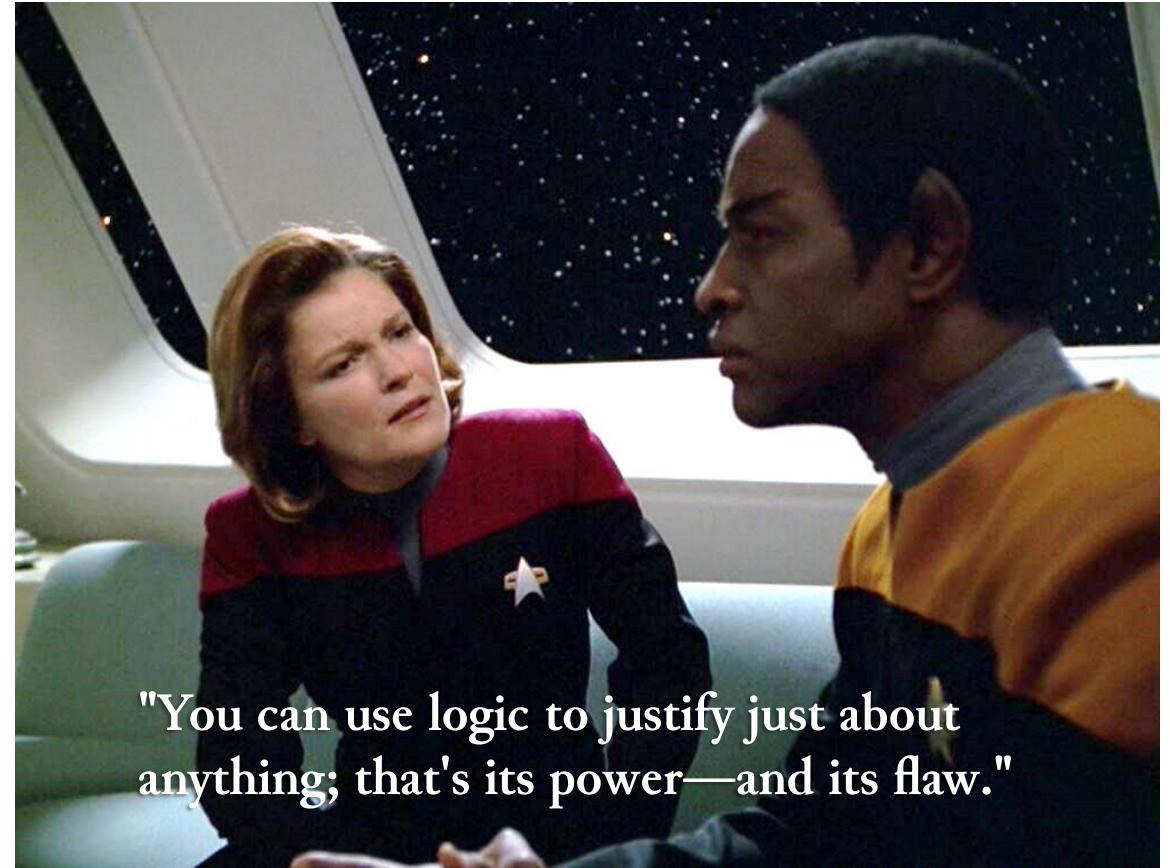


(Strother-Garcia 2019)



medium answers

- not every transduction preserves ideas of *linguistic* equivalence
 - process should respect natural classes, which may be lost in certain transductions
- the property of a **natural-class preserving transduction** is defined to find those logically equivalent representations that also share linguistic intuitions



"You can use logic to justify just about anything; that's its power—and its flaw."

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natural-class preserving transductions

- A transduction between two representations A and B is **natural-class preserving** iff the set of all natural class extensions of A exactly match those of B
 - A **natural class extension** is a maximal set of segments that share some common structural property

extension: { i u }

shared structure: [+high]

i u
e o
 a

every segment in this set is [+high]
no other segment in the theory is [+high]



assimilation: sharing is caring

- assimilation operates over like things
 - Trubetzkoy (1969), Chomsky and Halle (1968), Hyman (1974), Hayes (1986), Clements & Hume (1995) a.o.

$X \rightarrow [\alpha F] / [\alpha F]$

Y

A
|
F

or

B
|
A
|
F

Naturalness of Assimilation

the targets and triggers of an assimilation process
should constitute a natural class extension



assimilation: sharing is caring

- "Nevertheless, there is empirical evidence in favor of imposing a limitation on the use of variables with different features in different segments. **The great majority of examples involve only a single feature, and in other cases there clearly seems to be some intrinsic connection between the features involved in the process of assimilation.** At the present juncture, however, we are in no position to formulate these restrictions." (SPE 352)



assimilation: sharing is caring

- Clements & Hume (1995):
 - "Phonological rules perform single operations only." (p. 250)
 - "In the present model, in contrast, assimilation rules are characterized as the association (or "**spreading**") of a feature or node F of segment A to a neighboring segment B..." (p. 258)
- If assimilation is the result of spreading, then it directly follows from this that the resulting segments will have shared structure and therefore constitute a nontrivial natural class

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comparing theories

unified place theory

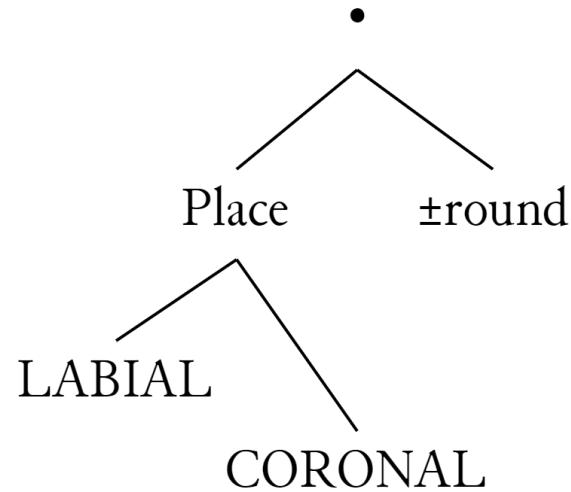
- consonants and vowels share representational primitives
 - e.g. LABIAL C-place, LABIAL V-place
- Sagey (1986), Clements & Hume (1995), a.o.

vowel feature theory

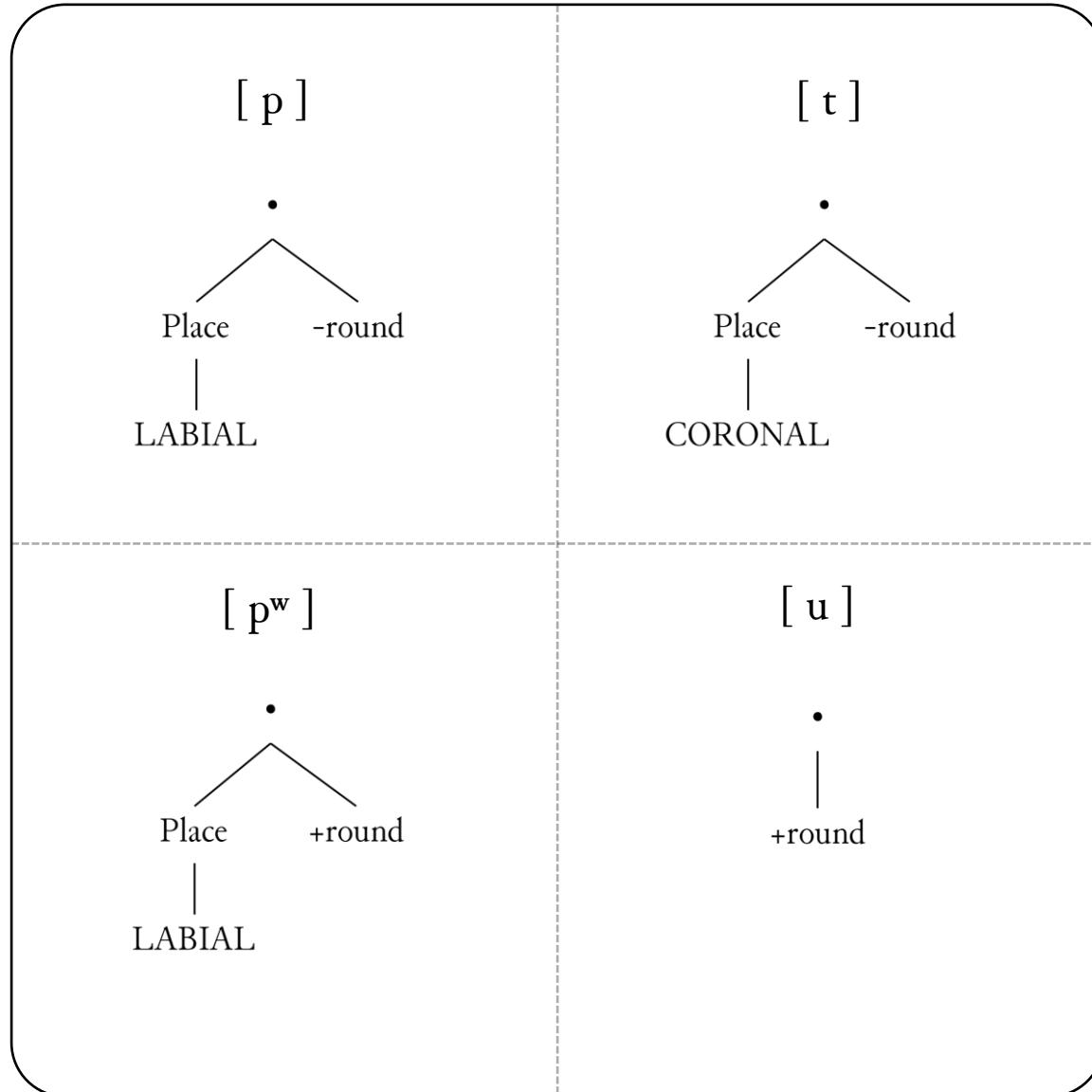
- vowel place is largely defined by primitives not used to describe consonant place
 - e.g. [+back], [-round]
- Odden (1991), Ni Chiosain & Padgett (1993), Halle et al. (2000), a.o.



v-feature theory

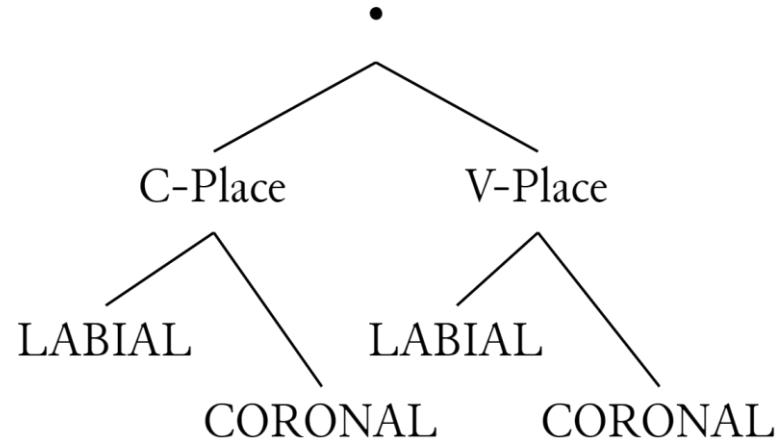


full structure

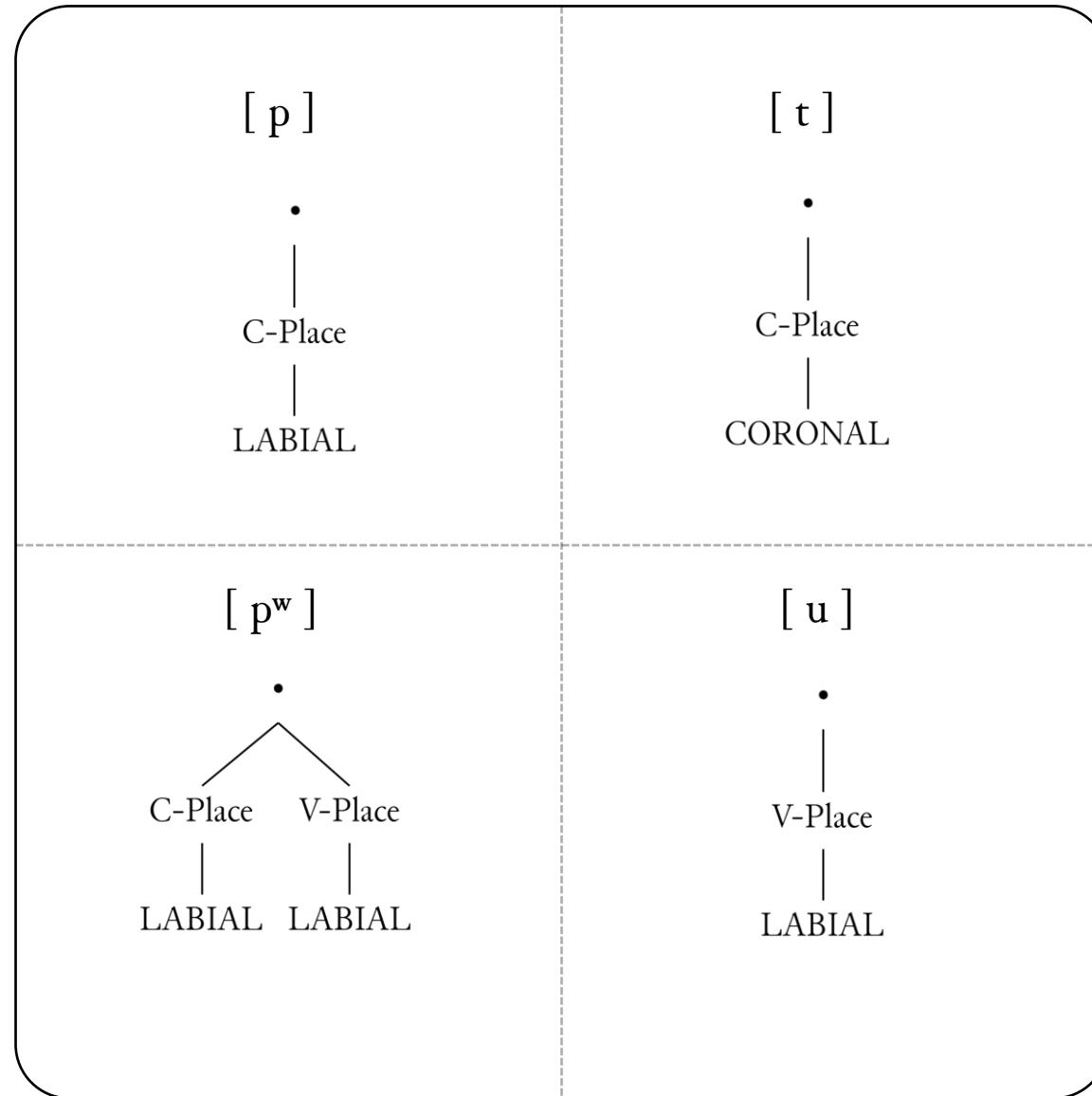


segments

unified place theory



full structure



segments

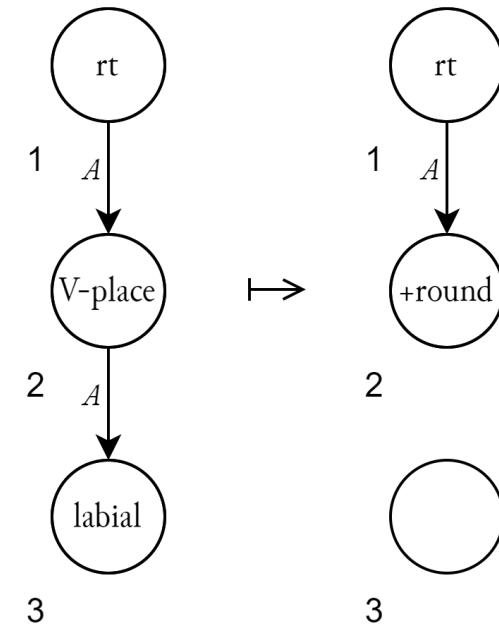




the transduction: unified \rightarrow v-feature

[u]

$$\begin{aligned} \text{rt}(x^1) &= \text{rt}(x) \\ \text{Place}(x^1) &= \text{C-place}(x) \\ \text{labial}(x^1) &= \text{labial}(x) \wedge \text{C-place}(y) \wedge A(y, x) \\ \text{coronal}(x^1) &= \text{coronal}(x) \wedge \text{C-place}(y) \wedge A(y, x) \\ +\text{round}(x^1) &= \text{labial}(x) \wedge \text{V-place}(y) \wedge A(y, x) \\ -\text{round}(x^1) &= \neg(\text{labial}(x) \wedge \text{V-place}(y) \wedge A(y, x)) \\ +\text{front}(x^1) &= \text{coronal}(x) \wedge \text{V-place}(y) \wedge A(y, x) \\ -\text{front}(x^1) &= \neg(\text{coronal}(x) \wedge \text{V-place}(y) \wedge A(y, x)) \end{aligned}$$





the transduction: v-feature → unified

$$rt(x^1) = rt(x)$$

$$\text{labial}(x^1) = +\text{round}(x) \vee \text{labial}(x)$$

$$\text{coronal}(x^1) = +\text{front}(x) \vee \text{coronal}(x)$$

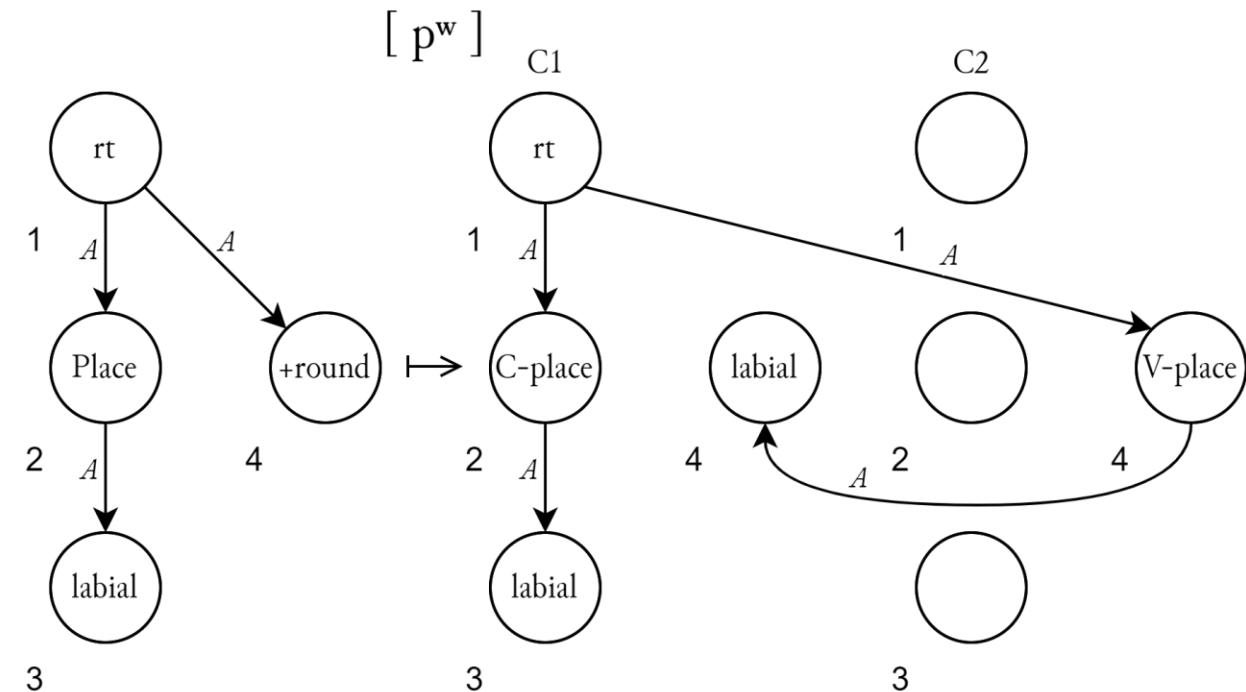
$$\text{C-place}(x^1) = \text{Place}(x)$$

$$\text{V-place}(x^2) = +\text{round}(x) \vee +\text{front}(x)$$

$$A(x^2, y^1) = (+\text{round}(x) \vee +\text{front}(x)) \wedge x = y$$

$$A(x^1, y^2) = rt(x) \wedge (+\text{round}(y) \vee +\text{front}(y))$$

$$A(x^1, y^1) = A(x, y) \wedge \neg(+\text{round}(y) \vee +\text{front}(y))$$





unified and v-features are QF-bi-interpretable

and are therefore notational variants?

"A QF transduction is extremely restricted in the degree to which the output can differ from the input because QF is a weak logical language limited to local operations. QF-bi-interpretability can therefore be considered an indication of notational equivalence."

(Strother-Garcia 2019: 39)



enumerating natural class extensions

general procedure:

- given the set of possible segments S , find all subsets of S
- for each subset N , find the shared structure G
 - for each segment not in N , check if it also contains G
 - if true, N is not a natural class extension
 - if false, continue
 - N is a natural class extension

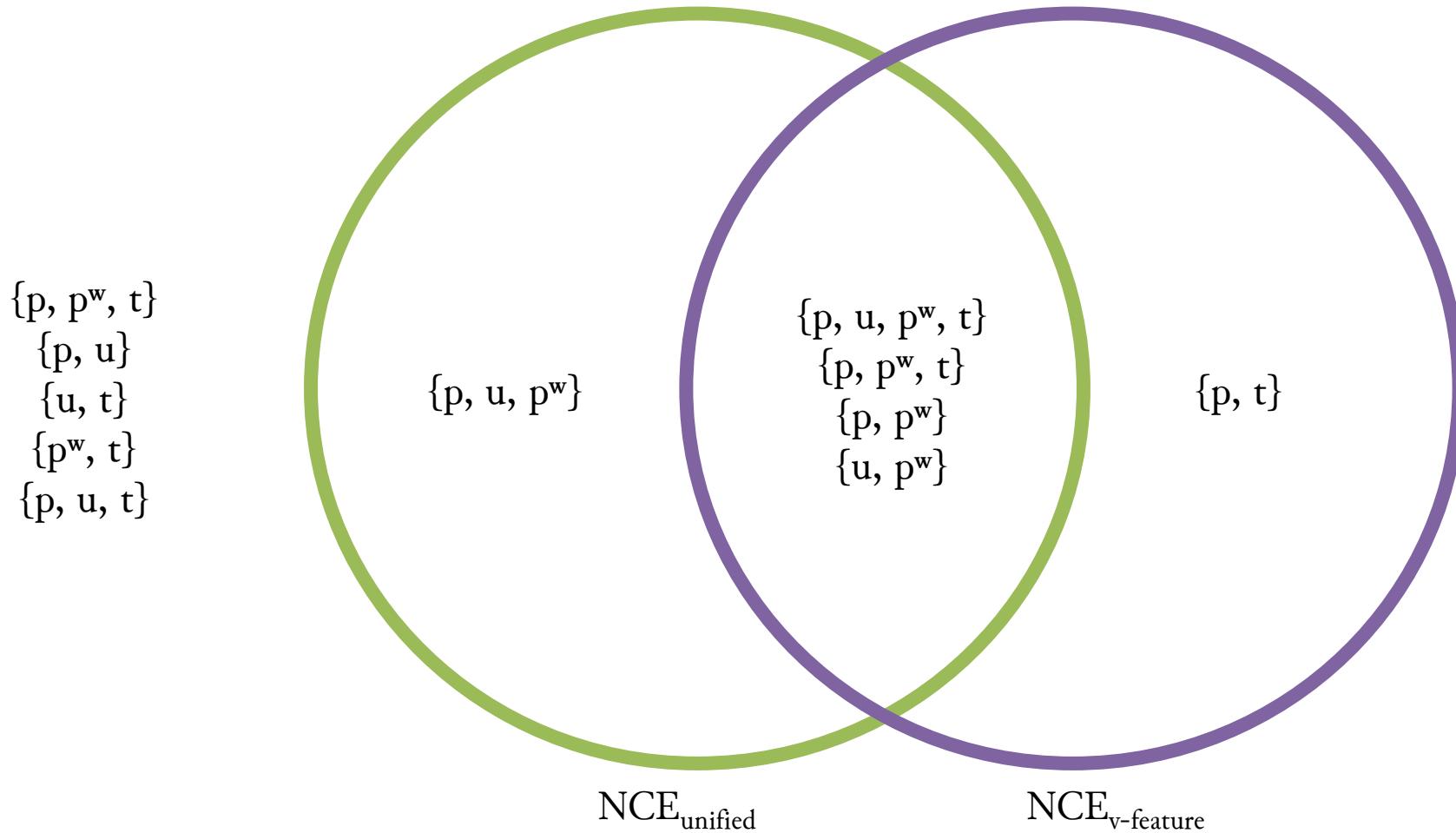


enumerating natural class extensions

	subset	$\{p, u, p^w, t\}$	$\{p, u, p^w\}$	$\{p, p^w, t\}$	$\{p, p^w\}$	$\{p, t\}$	$\{u, p^w\}$
largest unique shared structure	unified	•	•	• C-Place LABIAL	• C-Place LABIAL	\emptyset	• V-Place LABIAL
v-feature		•	\emptyset	• Place	• Place LABIAL	Place -round	• +round



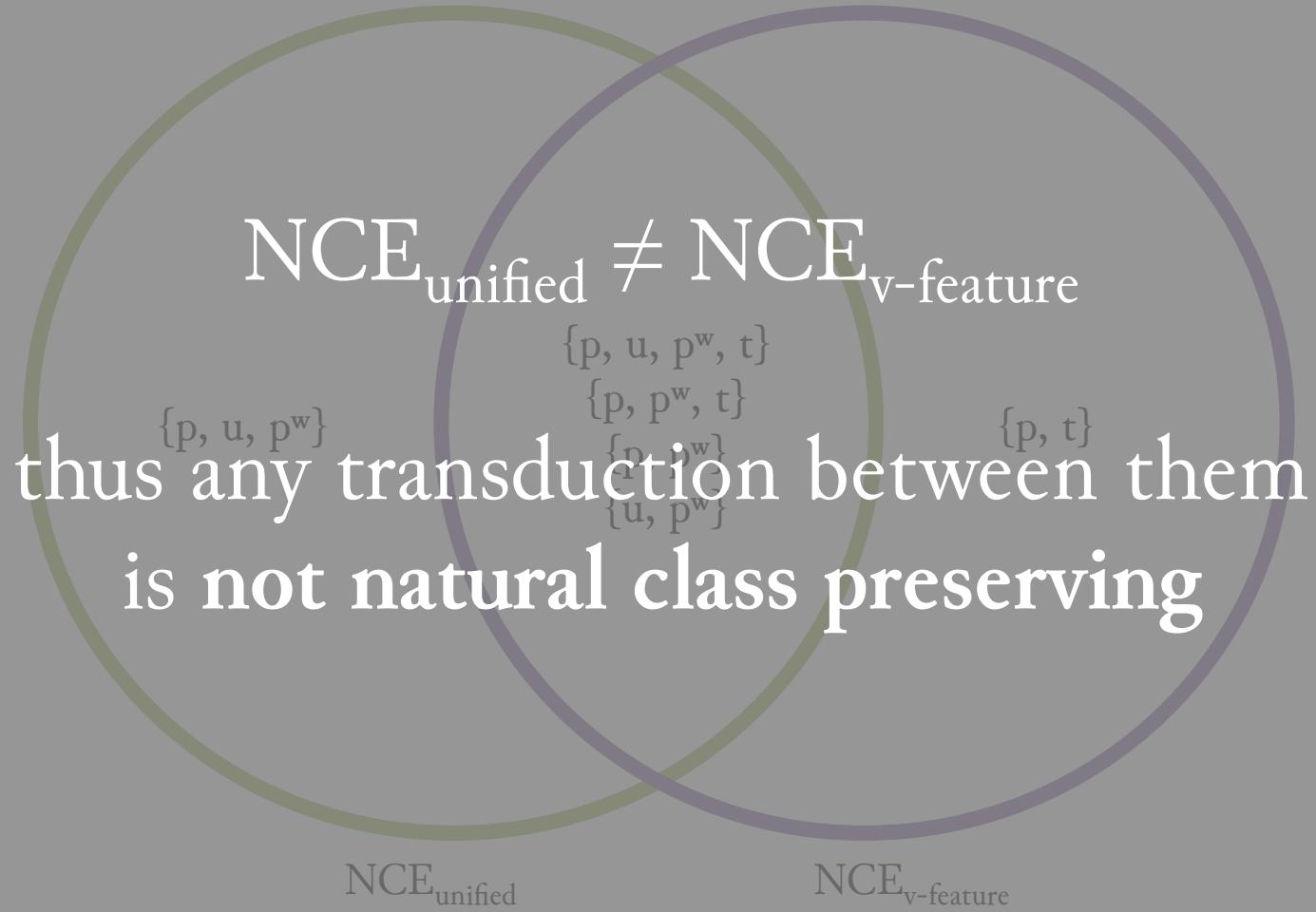
comparing natural class extensions





comparing natural class extensions

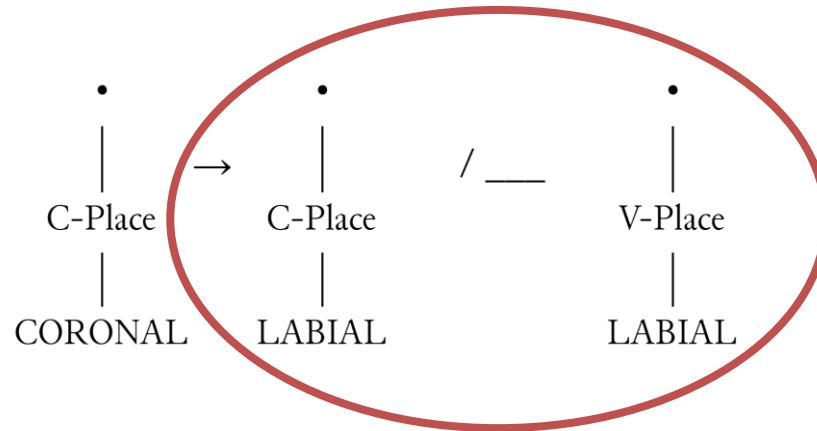
$\{p, p^w, t\}$
 $\{p, u\}$
 $\{u, t\}$
 $\{p^w, t\}$
 $\{p, u, t\}$





hypothetical assimilation

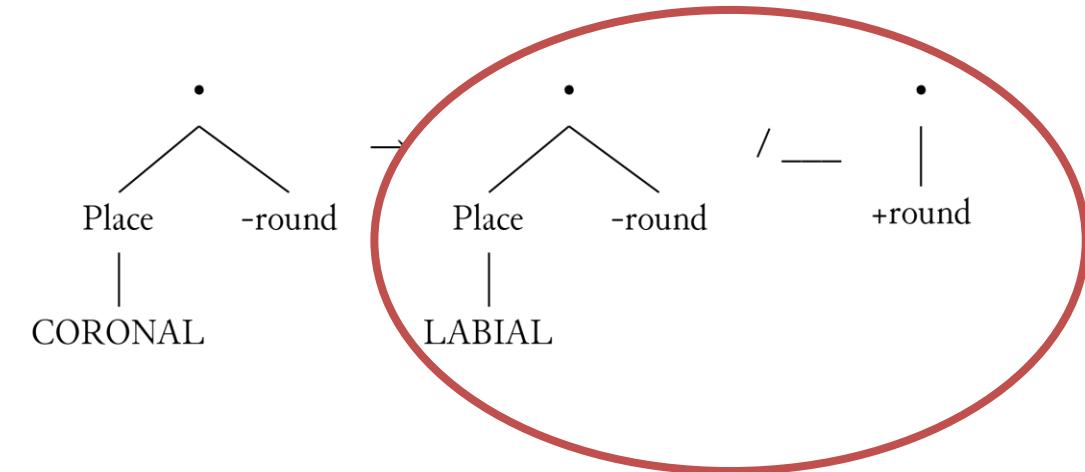
- $t \rightarrow p / _ u$



natural class extension: $\{p, u, p^w\}$
shared structure: LABIAL
• predicts [p^w] also a trigger
• seems reasonable

Naturalness of Assimilation

the targets and triggers of an assimilation process should constitute a natural class extension



natural class extension: $\{t, p, u, p^w\}$
shared structure: •
• predicts [$p^w t$] also triggers
• seems wrong
• not even an assimilation rule



comparing theories

(1) *Conditions for notational equivalence*

- a. Two models do not differ in their empirical predictions.
- b. Two models represent the same set of abstract properties, differing only superficially.

(from Oakden 2021, summarizing Fromkin 2010)

- if we take seriously assumptions like Naturalness of Assimilation  (in whatever formulation), then a **QF-bi-interpretable contrast-preserving transduction is not enough to satisfy (1a) above**

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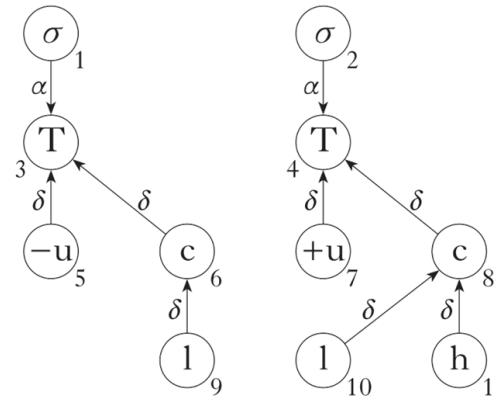


Oakden (2021)

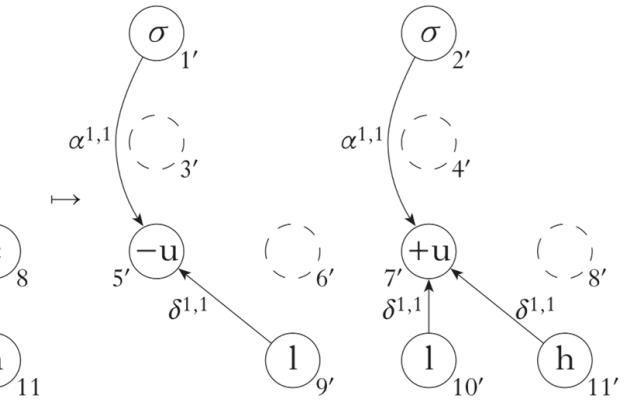
tone	Yip (1989)	Bao (1990)
low level L	σ -u 1	σ T -u c 1
high level H	σ +u h	σ T +u c h
mid level M	σ -u or +u h 1	σ T -u c or +u c h 1
high falling HM	σ +u h 1	σ T +u c h 1

tone	Yip (1989)	Bao (1990)
high rising MH	σ +u 1 h	σ T +u c 1 h
low falling ML	σ -u h 1	σ T -u c h 1
low rising LM	σ -u 1 h	σ T -u c 1 h

(38) *separated*



bundled



- Oakden (2021) provides a non-size-preserving QF transduction (above) between two theories of tone sandhi (left), arguing for notational equivalence
- **is this transduction also natural class preserving?**

Table I

Level and contour tonal contrasts in Yip (1989) and Bao (1990).

Oakden (2021)



- yes
- because Python

```
[8]:  
1 yip = {  
2     'L' : {('s', '-u'), ('-u', 'l')},  
3     'H' : {('s', '+u'), ('+u', 'h')},  
4     'M1' : {('s', '-u'), ('-u', 'h')},  
5     'M2' : {('s', '+u'), ('+u', 'l')},  
6     'HM' : {('s', '+u'), ('+u', 'h'), ('+u', 'l')},  
7     'MH' : {('s', '+u'), ('+u', 'l'), ('+u', 'h')},  
8     'ML' : {('s', '-u'), ('-u', 'l'), ('-u', 'h')},  
9     'LM' : {('s', '-u'), ('-u', 'l'), ('-u', 'h')}  
10 }  
11  
12 bao = {  
13     'L' : {('s', 'T'), ('T', '-u'), ('T', 'c'), ('c', 'l')},  
14     'H' : {('s', 'T'), ('T', '+u'), ('T', 'c'), ('c', 'h')},  
15     'M1' : {('s', 'T'), ('T', '-u'), ('T', 'c'), ('c', 'h')},  
16     'M2' : {('s', 'T'), ('T', '+u'), ('T', 'c'), ('c', 'l')},  
17     'HM' : {('s', 'T'), ('T', '+u'), ('T', 'c'), ('c', 'h'), ('c', 'l')},  
18     'MH' : {('s', 'T'), ('T', '+u'), ('T', 'c'), ('c', 'h'), ('c', 'l')},  
19     'ML' : {('s', 'T'), ('T', '-u'), ('T', 'c'), ('c', 'h'), ('c', 'l')},  
20     'LM' : {('s', 'T'), ('T', '-u'), ('T', 'c'), ('c', 'h'), ('c', 'l')},  
21 }  
22  
23 compare_theories(yip, bao)
```

Natural classes unique to theory 1:
Natural classes unique to theory 2:
Natural classes in common:
('LM', 'M1', 'ML')
('LM', 'ML')
('HM', 'M2', 'MH')
('H', 'HM', 'M2', 'MH')
('L', 'LM', 'M1', 'ML')
('H', 'HM', 'LM', 'M1', 'MH', 'ML')
('H', 'HM', 'L', 'LM', 'M1', 'M2', 'MH', 'ML')
('HM', 'L', 'LM', 'M2', 'MH', 'ML')
('H', 'HM', 'MH')
('L', 'LM', 'ML')
('HM', 'MH')
('HM', 'LM', 'MH', 'ML')

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summary

- the use of features/subsegmental structure sorts segments into natural classes based on shared structure
- while transductions can translate from model A to model B, the predicted natural classes present in the system as a whole may still differ in a linguistically significant way
- the definition of natural class preserving transductions is a start to identify comparisons of theories which still involve differing linguistic predictions

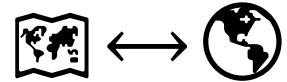


going forward

- the definition of *natural class preserving* is based on the representation themselves—can this property be identified by investigating the transduction rules alone?
- how else can transductions themselves be compared and evaluated from a linguistic standpoint?
- how strongly should our metatheoretical assumptions and expectations about linguistic processes be formalized?



thank you



& thank you Adam Jardine (for helping with the transductions like 3 years ago)
and the audience at the Wash U Linguistics Brown Bag on Sept. 16