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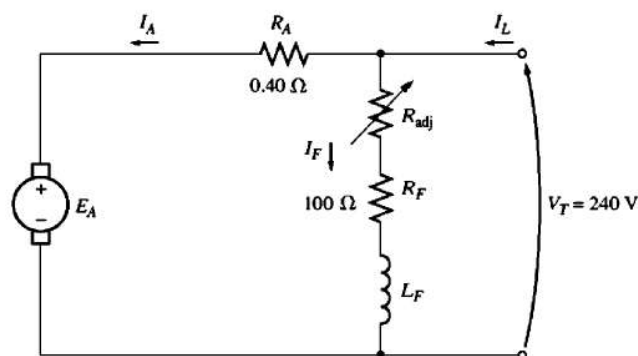
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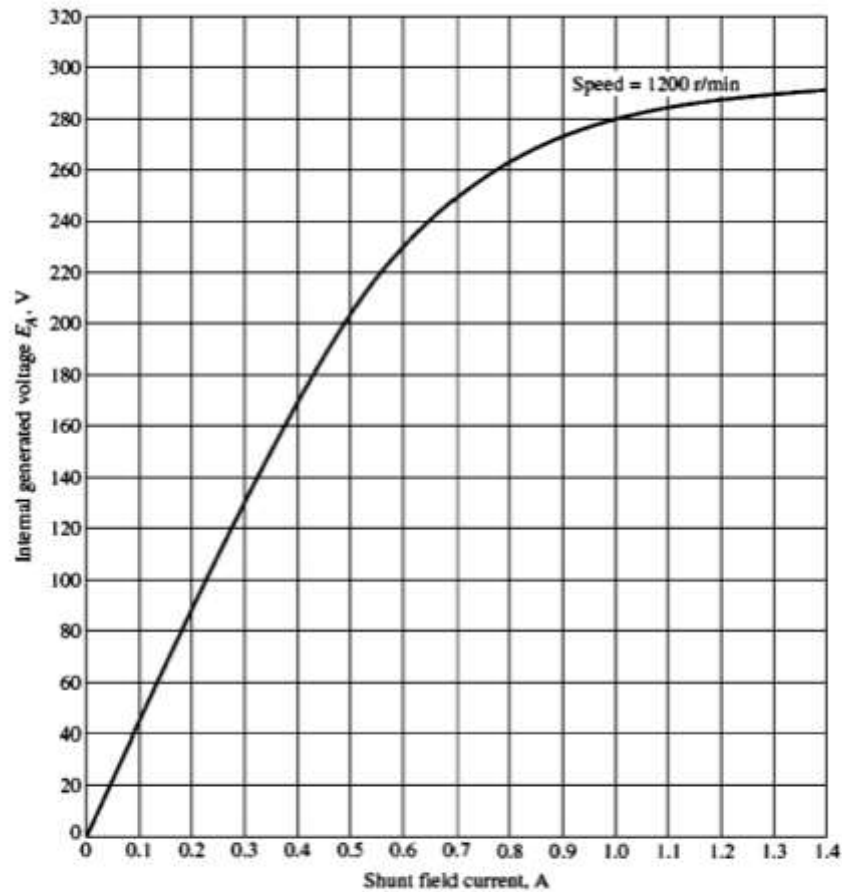
## First Cut Exercises

1. Problems next refer to the following dc motor:

$P_{\text{rated}} = 15 \text{ hp}$	$I_{L,\text{rated}} = 55 \text{ A}$
$V_T = 240 \text{ V}$	$N_F = 2700 \text{ turns per pole}$
$n_{\text{rated}} = 1200 \text{ r/min}$	$N_{SE} = 27 \text{ turns per pole}$
$R_A = 0.40 \Omega$	$R_F = 100 \Omega$
$R_S = 0.04 \Omega$	$R_{\text{adj}} = 100 \text{ to } 400 \Omega$

Rotational losses are 1800 W at full load. Magnetization curve is as shown in Figure P9-1. Assume that the motor described above is connected in shunt. The equivalent circuit of the shunt motor is shown in Figure.





**FIGURE P9-1**

The magnetization curve for the dc motor in Problems 9-1 to 9-12. This curve was made at a constant speed of 1200 r/min.

If the resistor  $R_{adj}$  is adjusted to  $175\Omega$ . What is the efficiency of the motor?

$I_L := 55 \text{ A}$	$V_i := 240 \text{ V}$	$R_f := 100 \Omega$	$R_{adj} := 175 \Omega$
$P_{nominal} := 15 \cdot 746 \text{ W} = 11.19 \text{ kW}$		$P_{rotor} := 1800 \text{ W}$	$R_a := 0.4 \Omega$
$I_a := I_L - \frac{V_i}{R_{adj} + R_f} = 54.127 \text{ A}$			
$P_{in} := V_i \cdot I_L = 13.2 \text{ kW}$			
$P_{out} := P_{in} - \frac{V_i^2}{R_{adj} + R_f} - I_a^2 \cdot R_a - 0.01 \cdot P_{nominal} - P_{rotor} = 9.907 \text{ kW}$			
$\eta_{efficiency} := \frac{P_{out}}{P_{in}} \cdot 100 = 75.051$			

- If  $R_{adj}$  can be adjusted from  $100$  to  $400 \Omega$ . What are the maximum and minimum no load speeds possible with this motor?

$V_i := 240 \text{ V}$	$I_{linea} := 55 \text{ A}$	
$R_{adj} := 100 \text{ } \Omega$	$R_f := 100 \text{ } \Omega$	$R_a := 0.4 \text{ } \Omega$
$I_f := \frac{V_i}{R_f + R_{adj}} = 1.2 \text{ A}$	$n_0 := 1200$	$E_{a0} := 290 \text{ V}$
$I_a := I_{linea} - I_f$	$E_a := V_i - I_a \cdot R_a = 218.48 \text{ V}$	
$n := \frac{E_a}{E_{a0}} \cdot n_0 = 904.055$		
$R_{adj} := 400 \text{ } \Omega$		
$I_f := \frac{V_i}{R_f + R_{adj}} = 0.48 \text{ A}$	$E_{a0} := 200 \text{ V}$	
$n := \frac{E_a}{E_{a0}} \cdot n_0 = 1310.88$		

3. A 15-hp, 230 V, 1800 r/min shunt dc motor has a full-load armature current of 60A when operations at rated condition. The armature resistance of the motor is  $R_a=0.15\Omega$ , and the field resistance  $R_f=80\Omega$ . The adjustable resistance in the field circuit  $R_{adj}$  may be varied over the range from 0 to  $200\Omega$  is currently set to  $90\Omega$ . Armature reaction may be ignored in this machine.

What is the efficiency of the motor at full load?

$I_a := 60 \text{ A}$	$V_i := 230 \text{ V}$	$R_f := 80 \text{ } \Omega$	$R_{adj} := 90 \text{ } \Omega$
$P_{nominal} := 15 \cdot 746 \text{ W} = 11.19 \text{ kW}$	$R_a := 0.15 \text{ } \Omega$		
$I_f := I_a + \frac{V_i}{R_{adj} + R_f} = 61.353 \text{ A}$			
$P_{in} := V_i \cdot I_f = 14.111 \text{ kW}$			
$P_{out} := P_{in} - \frac{V_i^2}{R_{adj} + R_f} - I_a^2 \cdot R_a - 0.01 \cdot P_{nominal} = 13.148 \text{ kW}$			
$\eta_{efficiency} := \frac{P_{out}}{P_{in}} \cdot 100 = 93.175$			

4. A 250 Vdc shunt motor has an armature resistance of  $0.4 \text{ } \Omega$  a field resistance of  $300 \text{ } \Omega$ . Find the start resistance value for 2 nominals current  $I_{line}=30 \text{ A}$ ,  $n=1200 \text{ rpm}$ . Find the

$I_{nominal} := 30 \text{ A}$	$V_i := 250 \text{ V}$	$R_f := 300 \text{ } \Omega$	$R_a := 0.4 \text{ } \Omega$
$I_f := \frac{V_i}{R_f} = 0.833 \text{ A}$	$I_a := I_{nominal} - I_f = 29.167 \text{ A}$	$I_{max} := 2 \cdot I_a = 58.333 \text{ A}$	
$R_t := \frac{V_i}{I_{max}} = 4.286 \text{ } \Omega$	$R_s := R_t - R_a = 3.886 \text{ } \Omega$		

5. From the last exercise. Find the speed resistance value for  $n=800$  rpm and  $30$  N m.

$$\begin{aligned}
 E_a &:= V_i - I_a \cdot R_a = 238.333 \text{ V} & n_{\text{nominal}} &:= 1200 & T &:= 30 \text{ N} \cdot \text{m} & n &:= 800 \\
 w_{\text{nominal}} &:= n_{\text{nominal}} \cdot \frac{2 \pi}{60 \cdot \text{s}} \cdot \text{rad} = 125.664 \frac{\text{rad}}{\text{s}} \\
 K\phi &:= \frac{E_a}{w_{\text{nominal}}} = 1.897 \text{ Wb} \\
 w &:= n \cdot \frac{2 \pi}{60 \cdot \text{s}} \cdot \text{rad} = 83.776 \frac{\text{rad}}{\text{s}} \\
 R_s &:= -R_a - \frac{(K\phi)^2}{T} \cdot \left( w - \frac{V_i}{K\phi} \right) = 5.36 \Omega
 \end{aligned}$$

6. An automatic starter circuit is to be designed for a shunt motor rated at 15hp, 240V, and 80A. The armature resistance of the motor is  $0.15\Omega$ , and the shunt field resistance is  $40\Omega$ . The motor is to start with no more than 250% of its rated armature current, and as soon as the current falls to rated value, a starting resistor stage is to be cut out. How many stages of starting resistance are needed, and how big should each one be?

$$R_a := 0.15 \Omega \quad R_f := 40 \Omega \quad V_i := 240 \text{ V} \quad I_{\text{min}} := 80 \text{ A}$$

We get the resistance number

$$\begin{aligned}
 I_{\text{max}} &:= 2.5 \cdot I_{\text{min}} = 200 \text{ A} \\
 R_t &:= \frac{V_i}{I_{\text{max}}} = 1.2 \Omega & I_f &:= \frac{V_i}{R_f} = 6 \text{ A} \\
 n &:= \frac{\log\left(\frac{R_a}{R_t}\right)}{\log\left(\frac{I_{\text{min}}}{I_{\text{max}}}\right)} = 2.269 & n &:= 3
 \end{aligned}$$

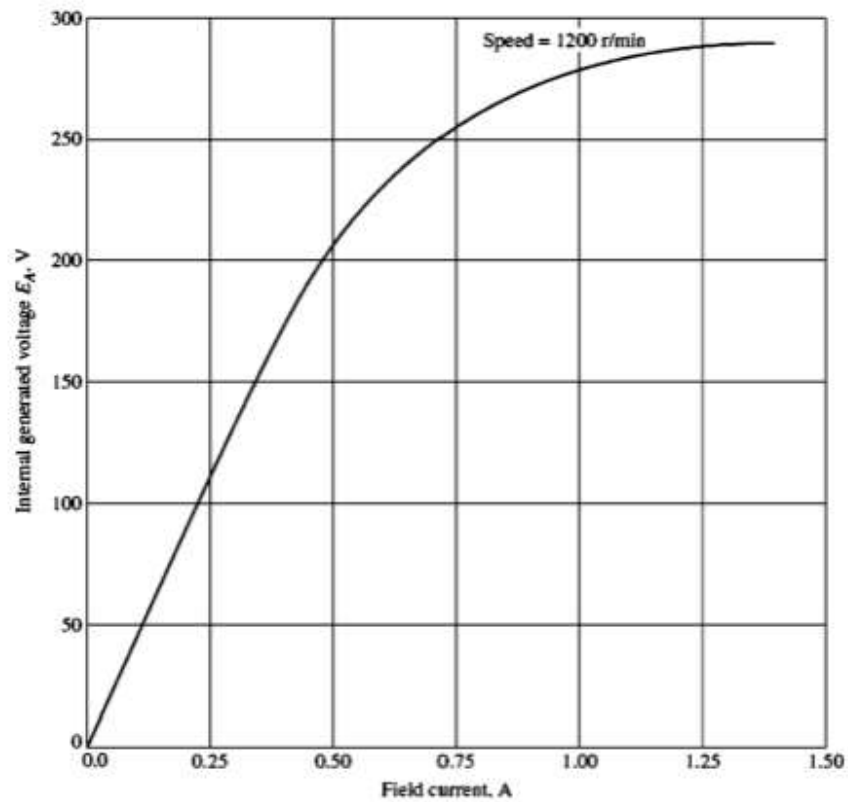
We calculate the resistor values

$$\begin{aligned}
 E_a &:= V_i - I_{\text{min}} \cdot R_t = 144 \text{ V} \\
 R_{t1} &:= \frac{V_i - E_a}{I_{\text{max}}} = 0.48 \Omega \\
 E_a &:= V_i - I_{\text{min}} \cdot R_{t1} = 201.6 \text{ V} \\
 R_{t2} &:= \frac{V_i - E_a}{I_{\text{max}}} = 0.192 \Omega \\
 R_3 &:= R_{t2} - R_a = 0.042 \Omega \\
 R_2 &:= R_{t1} - R_3 - R_a = 0.288 \Omega \\
 R_1 &:= R_t - R_2 - R_3 - R_a = 0.72 \Omega
 \end{aligned}$$

7. This problem refers to a 240V, 100A dc motor which has both shunt and series windings. Its characteristics are

$$\begin{aligned}
 R_A &= 0.14 \, \Omega & N_F &= 1500 \text{ turns} \\
 R_S &= 0.04 \, \Omega & N_{SE} &= 12 \text{ turns} \\
 R_F &= 200 \, \Omega & n_m &= 1200 \text{ r/min} \\
 R_{adj} &= 0 \text{ to } 300 \, \Omega, \text{ currently set to } 120 \, \Omega
 \end{aligned}$$

This motor has compensating windings and interpoles. The magnetization curve for this motor at 1200 rpm is shown in Figure P9-6.



**FIGURE P9-6**  
The magnetization curve for the dc motor in Problems 9-16 to 9-19.

The motor described above is connected in shunt. Under no-load conditions, what range of possible speeds can be achieved by adjusting  $R_{adj}$ ?

When  $R_{adj}=0\Omega$

$V_i := 240 \text{ V}$	$I_a := 100 \text{ A}$	
$R_{adj} := 0 \, \Omega$	$R_f := 200 \, \Omega$	$R_a := 0.14 \, \Omega$

Speed

$$\begin{aligned}
 E_a &:= V_i - I_a \cdot R_a = 226 \text{ V} \\
 n &:= \frac{E_a}{E_{a0}} \cdot n_0 = 986.182
 \end{aligned}$$

When  $R_{adj}=300\Omega$

$$R_{adj} := 300 \, \Omega$$

$$I_f := \frac{V_i}{R_f + R_{adj}} = 0.48 \, A \quad E_{a0} := 200 \, V$$

$$n := \frac{E_a}{E_{a0}} \cdot n_0 = 1356$$

8. A 15 hp, 240V shunt motor takes a full-load line current of 50A. The armature and field resistance are  $0.2\Omega$  and  $100\Omega$  respectively. The total brush-contact drop is 2V and core and friction losses are 280W. Calculate the efficiency of the motor.

$$I_{linea} := 50 \, A \quad V_i := 240 \, V \quad V_{esc} := 2 \, V \quad P_{rotor} := 280 \, W$$

$$I_a := I_{linea} - \frac{V_i}{R_f} = 47.6 \, A$$

$$P_{nominal} := 15 \cdot 746 \, W = 11.19 \, kW$$

$$P_{in} := V_i \cdot I_{linea} = 12 \, kW$$

$$P_{out} := P_{in} - \frac{V_i^2}{R_f} - I_a^2 \cdot R_a - 0.01 \cdot P_{nominal} - P_{rotor} - V_{esc} \cdot I_a = 10.031 \, kW$$

$$\eta_{efficiency} := \frac{P_{out}}{P_{in}} \cdot 100 = 83.588$$

9. A 100hp, 250V, 350 A shunt dc motor with an armature resistance of  $0.05\Omega$ . It is desired to design a starter circuit for this motor which will limit the maximum starting current to twice its rated value and which will switch out sections of resistance as the armature current falls to its rated value.

$$R_a := 0.05 \, \Omega \quad V_i := 250 \, V \quad I_{min} := 350 \, A$$

$$I_{max} := 2 \cdot I_{min} = 700 \, A$$

$$R_t := \frac{V_i}{I_{max}} = 0.357 \, \Omega$$

$$n := \frac{\log\left(\frac{R_a}{R_t}\right)}{\log\left(\frac{I_{min}}{I_{max}}\right)} = 2.837 \quad n := 3$$

$$E_a := V_i - I_{min} \cdot R_t = 125 \, V$$

$$R_{t1} := \frac{V_i - E_a}{I_{max}} = 0.179 \, \Omega$$

$$E_a := V_i - I_{min} \cdot R_{t1} = 187.5 \, V$$

$$R_{t2} := \frac{V_i - E_a}{I_{max}} = 0.089 \, \Omega$$

$$R_3 := R_{t2} - R_a = 0.039 \, \Omega$$

$$R_2 := R_{t1} - R_3 - R_a = 0.089 \, \Omega$$

$$R_1 := R_t - R_2 - R_3 - R_a = 0.179 \, \Omega$$