

Having established that the determinants of school choice vary dramatically between caste-homogeneous and caste-heterogeneous villages in Section ??, this section now turns to an analysis of how differences in sorting impact the performance differential between government and private schools. If private schools outperform government schools primarily due to differences in the quality of instruction, then the government-private performance differential should be relatively stable across villages with different caste compositions. If, however, private schools outperform government schools primarily due to differences in the composition of their students, then villages that are subject to different sorting processes should also see differences in the government-private differential. Specifically, the degree to which private schools out performance government schools should decline as one moves from caste-homogeneous villages (where students sort on academic potential) to caste-heterogeneous villages (where sorting is driven by considerations of caste politics).

## 0.1 Measuring Learning

To measure learning, this analysis employs a lagged-value-added model. Lagged-value-added models have increasingly become the norm in the education research (???) due to their potential to take into account not only observational differences between students, but also the potential to control for some unobserved differences, a subject discussed in more detail below.<sup>1</sup>

The lagged-value-added model incorporates the assumption that current knowledge is an additive function of all current and past inputs and an i.i.d. stochastic error term, and can be expressed as:

$$Y_{i,t} = X_{i,t}\alpha + Y_{i,t-1}\beta + \epsilon_{i,t} \quad (1)$$

where  $Y_{i,t}$  is child  $i$ 's test scores at time  $t$  and  $X_{i,t}$  is a vector of child, school, and village controls at time  $t$  (a full discussion of the lagged-value-added model and its assumptions can be found in Appendix ??).

Note that while the inclusion of a lagged dependent variable effectively controls for unobserved differences that affect differences in test *levels*, it cannot control for unobserved heterogeneity that affects learning *rates*. It is for this reason that while superior to other available methods, value-added analyses can not fully overcome selection issues.<sup>2</sup>

In the lagged-value-added model, coefficients on independent variables are interpreted as the contribution of each variable to learning. In this analysis, village-school-type dummies are added to measure the performance of each type of school in each village. (In other words, regressions include one dummy for private schools in village 1, one dummy government schools in village 1, one dummy for private schools in village 2, etc.). The difference between the private school and government school dummy coefficients within a village is the village-level measure of government-private performance differential.

<sup>1</sup>Lagged value-added models also account for the fact that learning is not entirely persistent (things learned in the past are often forgotten). This flexibility is discussed in more detail in Appendix ??.

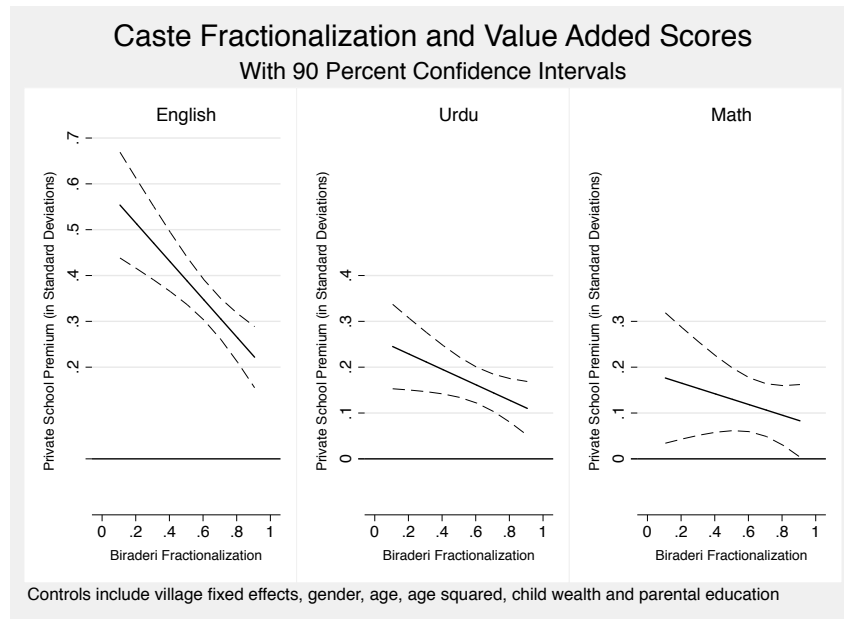
<sup>2</sup>Some analysis have turned to second-differencing the data and focusing on students who change schools (?), but these analyses have their own limitations, among them limited sample sizes (given that changes between types of school are relatively infrequent in most surveys) and the assumption that school changes are not the result of some unobserved shock (i.e. that school switches are not accompanied by contemporaneous with other changes – a potentially problematic assumption given the relative infrequency with which students change schools).

## 0.2 Convergence in Government-Private Test Scores

Table 1 presents lagged-valued-added estimates of learning as a function of various demographic controls and village fractionalization. It shows that the effect of caste fractionalization on the government-private performance differential is negative and significant for English and Urdu, and negative (albeit insignificant) for math. Further, as shown in columns (2), (5), and (8) of Table 1, the inclusion of various demographic controls such as a child wealth index and dummies for parental education along with the village fixed effects has no significant effect on the results.

To aid in interpretation, Figure 1 plots the government-private performance differential as a function of caste fractionalization (these plots correspond to columns (2), (5), and (8) respectively). In all three cases, the rise in fractionalization is associated with a near 50% decline in the private school premium, although this is by far most striking in the case of English – which is generally considered the path to upward mobility in Pakistan, and is often the focus of private schools in Punjab.

Figure 1: Private School Test Score Premium with Lagged Scores



## 0.3 Decomposition of Convergence

Further evidence that the convergence in government-private school test scores is driven differences in student sorting – not differences in actual learning outcomes – comes from the fact that while the government-private school test gap decreases, overall learning remain relatively unchanged. As shown in Table 2, overall test scores are essentially flat across all villages – English scores are slightly higher in more fractionalized villages in Column 1, but the magnitude of this difference is relatively small, and once more demographic controls are added in Column 2 this effect disappears. No relationship exists for other subjects. Government scores increase and private scores decline with fractionalization, in other words, but those changes are almost perfectly offsetting. Indeed, this is also illustrated in Column 3 of Table 1, where village fixed effects are replaced with district fixed effects, allowing for a comparison of test scores levels (rather than just

Table 1: Child Test Scores

	English			Urdu			Math		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Private School	0.63*** (8.35)	0.60*** (7.28)	0.59*** (7.31)	0.27*** (4.16)	0.26*** (4.01)	0.20*** (2.93)	0.19* (1.67)	0.19* (1.88)	0.12 (1.25)
Fractionalization * Private	-0.43*** (-3.77)	-0.41*** (-3.46)	-0.42*** (-3.68)	-0.17* (-1.71)	-0.17* (-1.74)	-0.094 (-0.98)	-0.082 (-0.53)	-0.12 (-0.83)	-0.052 (-0.39)
Lagged English Scores	0.37*** (21.16)	0.36*** (20.03)	0.39*** (20.61)	0.15*** (13.05)	0.14*** (11.37)	0.14*** (11.69)	0.16*** (10.78)	0.15*** (10.06)	0.16*** (9.86)
Lagged Math Scores	0.069*** (8.55)	0.072*** (8.91)	0.071*** (8.49)	0.12*** (14.10)	0.12*** (13.51)	0.12*** (13.96)	0.37*** (29.56)	0.38*** (27.37)	0.40*** (28.76)
Lagged Urdu Scores	0.15*** (14.04)	0.15*** (13.28)	0.15*** (12.71)	0.38*** (34.36)	0.38*** (32.65)	0.40*** (31.74)	0.23*** (17.67)	0.22*** (17.01)	0.22*** (16.84)
Child's Wealth Index		0.017*** (5.19)	0.015*** (4.29)		0.0073** (2.46)	0.0068** (2.28)		0.014*** (3.52)	0.016*** (3.73)
Educated Parent		0.058*** (4.75)	0.053*** (4.07)		0.052*** (4.77)	0.049*** (4.40)		0.046*** (3.35)	0.043*** (3.08)
Biraderi Fractionalization			0.21** (2.56)			0.095 (1.40)		0.14 (1.38)	
Village: Pct Adults Literate			0.00017 (0.18)			-0.00054 (-0.62)		0.00036 (0.27)	
Log Village Size			0.019 (1.47)			0.014 (1.01)		0.0088 (0.50)	
Village Land Gini			0.053 (0.47)			0.061 (0.63)		-0.25* (-1.88)	
Constant	0.25 (0.99)	0.40* (1.78)	0.57** (2.28)	0.56** (2.58)	0.69*** (2.78)	0.78*** (2.80)	0.12 (0.37)	0.31 (0.99)	0.60* (1.74)
Village Fixed Effects	Yes	Yes	No	Yes	Yes	No	Yes	Yes	No
District Fixed Effects	No	No	Yes	No	No	Yes	No	No	Yes
Observations	37147	26141	26141	37147	26141	26141	37147	26141	26141

Controls for age, age squared, gender, and class omitted from table. Standard errors clustered at village level.

\* p&lt;0.10, \*\* p&lt;0.05, \*\*\* p&lt;0.01

the government-private gap) across villages. In the case of English the convergence appears to be driven in equal parts by improvements in government schools and a decline in private schools.

The fact overall educational attainment remains constant is further evidence that as the determinants of school choice changes, it is the *distribution* of academically inclined students that changes, not the performance of the schools themselves.

#### **0.4 Caste and Residual Academic Potential**

For it to be the case that sorting by caste reduces the degree to which private schools enroll disproportionately academically inclined students, it must be the case that residual academic potential – potential that cannot be explained by things like parental education and wealth – must be equally distributed across different castes (or be distributed slightly in favor of lower status *biraderis*). If not, and even the least talented “high status” students were more talented than the most talented “low status” students, then the concentration of “high status” students in private schools would result in *divergence*, rather than *convergence*, of test scores. As shown in Table 3, however, there is no evidence that those from higher social status *biraderis* have higher residual talent than those from low status *biraderis*. As evident from the top row of coefficients, after controlling for other observational factors, student caste does not appear to have any consistent effect on test scores.

Table 2: Child Test Scores and Fractionalization

	English		Urdu		Math			
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Private School	0.31*** (10.98)	0.29*** (10.42)	0.31*** (10.98)	0.29*** (10.42)	0.14*** (5.74)	0.14*** (5.65)	0.11*** (3.17)	0.087** (2.58)
Biraderi Fractionalization	0.13* (1.70)	0.096 (1.33)	0.13* (1.70)	0.096 (1.33)	0.085 (1.26)	0.069 (1.08)	0.13 (1.34)	0.13 (1.46)
Lagged English Scores	0.40*** (22.32)	0.39*** (21.10)	0.40*** (22.32)	0.39*** (21.10)	0.16*** (13.39)	0.14*** (11.90)	0.17*** (10.27)	0.16*** (9.92)
Lagged Math Scores	0.067*** (8.18)	0.070*** (8.37)	0.067*** (8.18)	0.070*** (8.37)	0.12*** (14.51)	0.12*** (14.00)	0.39*** (30.92)	0.40*** (28.87)
Lagged Urdu Scores	0.15*** (13.26)	0.15*** (12.80)	0.15*** (13.26)	0.15*** (12.80)	0.39*** (34.01)	0.40*** (31.76)	0.23*** (17.96)	0.22*** (16.87)
Village: Pct Adults Literate	0.00067 (0.68)	0.00022 (0.23)	0.00067 (0.68)	0.00022 (0.23)	-0.00018 (-0.21)	-0.00053 (-0.61)	0.00043 (0.31)	0.00036 (0.27)
Log Village Size	0.017 (1.33)	0.019 (1.39)	0.017 (1.33)	0.019 (1.39)	0.011 (0.73)	0.014 (1.01)	0.0070 (0.35)	0.0087 (0.50)
Village Land Gini	0.0097 (0.08)	0.045 (0.39)	0.0097 (0.08)	0.045 (0.39)	0.013 (0.13)	0.059 (0.61)	-0.28** (-2.22)	-0.25* (-1.90)
Child's Wealth Index		0.015*** (4.22)		0.015*** (4.22)		0.0068** (2.27)		0.016*** (3.73)
Educated Parent		0.053*** (4.13)		0.053*** (4.13)		0.049*** (4.42)		0.043*** (3.08)
Constant	0.44 (1.57)	0.63** (2.52)	0.44 (1.57)	0.63** (2.52)	0.67*** (2.65)	0.80*** (2.83)	0.32 (0.87)	0.61* (1.76)
District Fixed Effects	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations	37147	26141	37147	26141	37147	26141	37147	26141

Controls for age, age squared, gender, and class omitted from table. Standard errors clustered at village level.

\* p&lt;0.10, \*\* p&lt;0.05, \*\*\* p&lt;0.01

Table 3: Child Social Status and Residual Talent

	English			Urdu			Math		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
High Status Biraderi	-0.035 (-0.79)	-0.062 (-0.93)	-0.11** (-2.41)	-0.044 (-0.75)	-0.11 (-1.55)	-0.081 (-1.61)	0.0056 (0.09)	-0.019 (-0.22)	0.034 (0.50)
Private School	0.30** (2.53)	0.20 (1.50)	0.18 (1.46)	0.22* (1.92)	0.18 (1.37)	0.026 (0.21)	-0.10 (-0.96)	-0.13 (-0.96)	-0.24 (-1.55)
Fractionalization * Private	0.0010 (0.01)	0.12 (0.60)	0.100 (0.54)	-0.097 (-0.60)	-0.057 (-0.29)	0.11 (0.63)	0.35** (2.02)	0.42* (1.97)	0.47** (2.13)
Lagged English Scores	0.32*** (7.79)	0.31*** (6.95)	0.40*** (10.37)	0.15*** (4.80)	0.15*** (4.19)	0.15*** (5.12)	0.17*** (3.81)	0.17*** (3.74)	0.16*** (3.93)
Lagged Math Scores	0.066** (2.21)	0.061* (1.68)	0.050 (1.51)	0.12*** (3.04)	0.094** (2.23)	0.10** (2.57)	0.31*** (6.38)	0.29*** (5.93)	0.38*** (8.33)
Lagged Urdu Scores	0.17*** (4.72)	0.18*** (4.11)	0.16*** (4.04)	0.34*** (8.85)	0.35*** (7.57)	0.40*** (8.74)	0.25*** (5.51)	0.25*** (4.96)	0.25*** (4.94)
Child's Wealth Index		-0.0055 (-0.43)	-0.0080 (-0.69)		0.0060 (0.57)	0.0046 (0.52)		-0.0094 (-0.57)	-0.0062 (-0.44)
Educated Parent		0.12*** (2.95)	0.13*** (3.52)		0.14*** (3.25)	0.14*** (4.01)		0.15*** (2.85)	0.17*** (3.68)
Biraderi Fractionalization			-0.0096 (-0.09)			-0.076 (-0.70)		-0.024 (-0.16)	
Village: Pct Adults Literate			0.00000016 (0.00)			-0.0030** (-2.03)		-0.0022 (-0.84)	
Log Village Size			0.011 (0.33)			0.016 (0.52)		0.026 (0.44)	
Village Land Gini			-0.031 (-0.17)			0.054 (0.28)		-0.11 (-0.37)	
Constant	-0.62 (-1.25)	0.20 (0.29)	1.00* (1.71)	-0.15 (-0.26)	2.16*** (3.07)	2.28*** (3.46)	-0.71 (-1.07)	2.98*** (3.44)	2.59*** (2.90)
Village Fixed Effects	Yes	Yes	No	Yes	Yes	No	Yes	Yes	No
District Fixed Effects	No	No	Yes	No	No	Yes	No	No	Yes
Observations	1859	1381	1381	1859	1381	1381	1859	1381	1381

Controls for age, age squared, gender, and class omitted from table. Standard errors clustered at village level.

\* p&lt;0.10, \*\* p&lt;0.05, \*\*\* p&lt;0.01