

# Capture-mark-recapture methods for abundance estimation

---



Same old equation:

$$\hat{N} = \frac{n}{\hat{p}}$$

- $N$  is abundance (population size)
- $n$  is the number of individuals detected
- $\hat{p}$  is an estimate of detection probability: The probability of detecting an individual

Same old equation:

$$\hat{N} = \frac{n}{\hat{p}}$$

- $N$  is abundance (population size)
- $n$  is the number of individuals detected
- $\hat{p}$  is an estimate of detection probability: The probability of detecting an individual

Most methods differ in how they estimate  $p$

## Estimating $p$

- Set traps in a study area and mark each captured individual

## Estimating $p$

- Set traps in a study area and mark each captured individual
- Repeat the trapping on  $K$  occasions

## Estimating $p$

- Set traps in a study area and mark each captured individual
- Repeat the trapping on  $K$  occasions
- On each occasion, mark new individuals and record recaptures

## Estimating $p$

- Set traps in a study area and mark each captured individual
- Repeat the trapping on  $K$  occasions
- On each occasion, mark new individuals and record recaptures
- If capture probability is high. . .

## Estimating $p$

- Set traps in a study area and mark each captured individual
- Repeat the trapping on  $K$  occasions
- On each occasion, mark new individuals and record recaptures
- If capture probability is high. . .
  - ▶ You will detect most of the population on the first occasion



## Estimating $p$

- Set traps in a study area and mark each captured individual
- Repeat the trapping on  $K$  occasions
- On each occasion, mark new individuals and record recaptures
- If capture probability is high. . .
  - ▶ You will detect most of the population on the first occasion
  - ▶ Most of the captures on subsequent occasions will be recaptures

## Estimating $p$

- Set traps in a study area and mark each captured individual
- Repeat the trapping on  $K$  occasions
- On each occasion, mark new individuals and record recaptures
- If capture probability is high. . .
  - ▶ You will detect most of the population on the first occasion
  - ▶ Most of the captures on subsequent occasions will be recaptures
- And vice versa

$n = 5$  individuals captured over 3 sampling occasions

	Occasion 1	Occasion 2	Occasion 3
Animal 1	0	0	1
Animal 2	1	1	0
Animal 3	1	1	1
Animal 4	1	0	0
Animal 5	0	1	0

$n = 5$  individuals captured over 3 sampling occasions

	Occasion 1	Occasion 2	Occasion 3
Animal 1	0	0	1
Animal 2	1	1	0
Animal 3	1	1	1
Animal 4	1	0	0
Animal 5	0	1	0

These data tell us about  $p$  and hence  $N$ . Estimation is usually achieved using maximum likelihood methods.

# LINCOLN-PETERSON METHOD

The original method was first used by Pierre-Simon LaPlace to estimate the human population in France.



# LINCOLN-PETERSON METHOD

The original method was first used by Pierre-Simon LaPlace to estimate the human population in France.



Later it was used by Lincoln (shown above) and Peterson to estimate fish and wildlife populations

- There are only 2 capture occasions



# LINCOLN-PETERSON STUDY DESIGN

- There are only 2 capture occasions
- On the first,  $n_1$  animals are captured and marked





- There are only 2 capture occasions
- On the first,  $n_1$  animals are captured and marked
- On the second,  $n_2$  animals are captured and  $m_2$  of them are recaptures



How can we use  $n_1$ ,  $n_2$ , and  $m_2$  to estimate  $N$ ?

How can we use  $n_1$ ,  $n_2$ , and  $m_2$  to estimate  $N$ ?

$$\frac{n_1}{N} = \frac{m_2}{n_2}$$

How can we use  $n_1$ ,  $n_2$ , and  $m_2$  to estimate  $N$ ?

$$\frac{n_1}{N} = \frac{m_2}{n_2}$$

And so . . .

$$\hat{N} = \frac{n_1 n_2}{m_2}$$

## (1) Population closure

- ▶ No births
- ▶ No deaths
- ▶ No immigration or emigration

- (1) Population closure
  - ▶ No births
  - ▶ No deaths
  - ▶ No immigration or emigration
  
- (2) All individuals are assumed to have the same capture probability

- (1) Population closure
  - ▶ No births
  - ▶ No deaths
  - ▶ No immigration or emigration
- (2) All individuals are assumed to have the same capture probability
- (3) No tag loss or mis-identification

Using more than 2 sampling occasions has many advantages, including the ability to account for:

- Temporal variation



Using more than 2 sampling occasions has many advantages, including the ability to account for:

- Temporal variation
- Behavioral effects

Using more than 2 sampling occasions has many advantages, including the ability to account for:

- Temporal variation
- Behavioral effects
  - ▶ Trap happiness

Using more than 2 sampling occasions has many advantages, including the ability to account for:

- Temporal variation
- Behavioral effects
  - ▶ Trap happiness
  - ▶ Trap shyness

Using more than 2 sampling occasions has many advantages, including the ability to account for:

- Temporal variation
- Behavioral effects
  - ▶ Trap happiness
  - ▶ Trap shyness
- Individual heterogeneity

Using more than 2 sampling occasions has many advantages, including the ability to account for:

- Temporal variation
- Behavioral effects
  - ▶ Trap happiness
  - ▶ Trap shyness
- Individual heterogeneity
- Combinations of the above

Model	Description
$M_0$	The most basic model in which $p$ and $c$ are constant
$M_t$	$p$ differs among sampling occasions and $p_t = c_t$ .
$M_b$	Behavioral response model in which $p$ and $c$ differ. Can describe trap happiness or trap shiness.
$M_{tb}$	A combination of models $M_t$ and $M_b$ .

where

$p$  = capture probability

$p_t$  = capture probability on occasion  $t$

$c$  = recapture probability

Suppose you remove individuals on each survey

Suppose you remove individuals on each survey

Eventually you should deplete the population



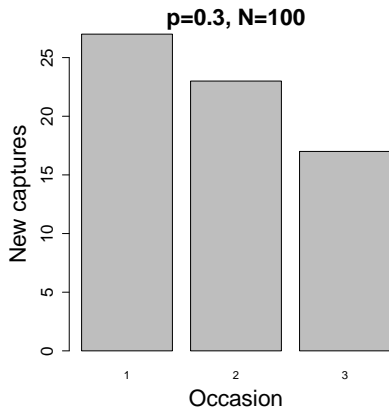
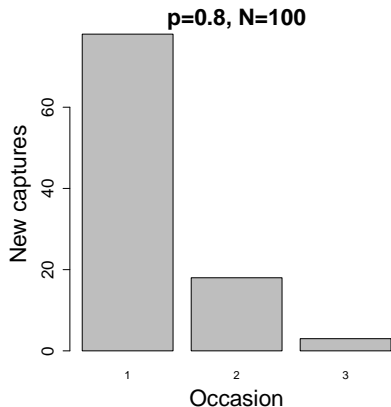
Suppose you remove individuals on each survey

Eventually you should deplete the population

The number of captures you would expect on each occasion:

Occasion	Expected count
1	$pN$
2	$p(1 - p)N$
3	$p(1 - p)^2N$
4	$p(1 - p)^3N$
$\vdots$	$\vdots$
K	$p(1 - p)^{K-1}N$

The rate at which the population is depleted tells us about  $p$ .



## Key points

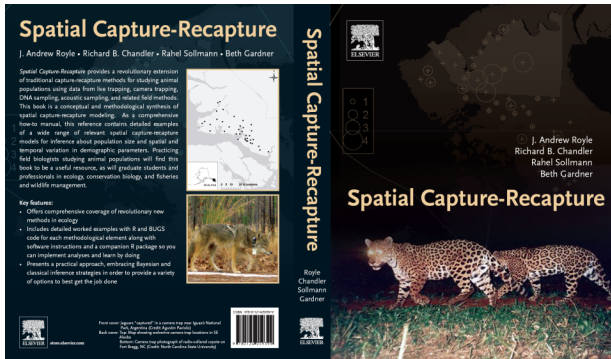
- Capture-recapture methods use information about recapture rates to estimate capture probability and abundance
- More advanced methods can be used to estimate density and vital rates
- Modern field methods use camera traps or DNA sampling techniques to collect non-invasive capture-recapture data

## Lingering questions

- How do we convert abundance to density?
- What is the area surveyed?

## Lingering questions

- How do we convert abundance to density?
- What is the area surveyed?



Read Chapter 11