

Lab 13

Nick Gulotta

12/7/2021

```
require(markd)
require(readr)
require(gridExtra)
require(dplyr)

#data
cjs.data <- read.table("~/Users/nickg/OneDrive/Desktop/R projects/Population-dynamics-FANR/data/cawa-cjs.i
np", sep=" ",
                        colClasses=c("character","character"),
                        col.names=c("ch", "count"))

js.data <- read.table("~/Users/nickg/OneDrive/Desktop/R projects/Population-dynamics-FANR/data/CH-SO-Dean-
AllYears.inp", sep=" ",
                        colClasses=c("character","character"),
                        col.names=c("ch", "count"))
```

Exercise I

$\Phi(\cdot)p(\cdot)$ – No variation in apparent survival

```
phi0.p0 <- crm(data=cjs.data, model="CJS", hessian=TRUE,
model.parameters=list(
  Phi=list(formula=~1), ## No variation
  p=list(formula=~1)) ## No variation

phi0.p0
```

```
## crm Model Summary
##
## Npar : 2
## -2lnL: 164.6401
## AIC : 168.6401
##
## Beta
## Estimate se lcl ucl
## Phi.(Intercept) -1.0897593 0.4370454 -1.866359 -0.1531413
## p.(Intercept) -0.4517833 0.6526286 -1.730935 0.8273687
```

predict(phi0.p0)

```
## $Phi
## occ estimate se lcl ucl
## 1 4 0.2670287 0.08554845 0.1339635 0.4617893
##
## $p
## occ estimate se lcl ucl
## 1 5 0.3889369 0.155107 0.150468 0.6957983
```

$\Phi(t)p(\cdot)$ – Temporal variation in apparent survival

```
phiTime.p0 <- crm(data=cjs.data, model="cjs", hessian=TRUE,
model.parameters=list(
  Phi=list(formula=~time), ## Temporal variation
  p=list(formula=~1)) ## No variation
```

```
##
Number of evaluations: 100 -2lnL: 164.407839
Number of evaluations: 200 -2lnL: 164.4079065
Number of evaluations: 100 -2lnL: 164.4290837
```

phiTime.p0

```
## crm Model Summary
##
## Npar : 5
## -2lnL: 164.4078
## AIC : 174.4078
##
## Beta
## Estimate se lcl ucl
## Phi.(Intercept) -1.09642447 0.7582738 -2.582641 0.3897923
## Phi.time2 -0.07076579 0.8377325 -1.712722 1.5711899
## Phi.time3 -0.21627966 0.7976686 -1.347151 1.7797100
## Phi.time4 -0.17197565 0.7911950 -1.378767 1.7227179
## p.(Intercept) -0.45509195 0.6654899 -1.759452 0.8492683
```

predict(phiTime.p0)

```
## $Phi
## time occ estimate se lcl ucl
## 1 4 4 0.2840523 0.1344567 0.09794132 0.5918005
## 2 3 3 0.2931478 0.1227856 0.11490777 0.5698580
## 3 2 2 0.2373632 0.1064269 0.08951926 0.4962847
## 4 1 1 0.2564104 0.1423318 0.07026401 0.5962327
##
## $p
## occ estimate se lcl ucl
## 1 5 0.3881508 0.158047 0.146859 0.7004136
```

$\Phi(\cdot)p(t)$ – Temporal variation in capture probability

```
pTime.p0<-crm(data=cjs.data, model="cjs", hessian=TRUE,
model.parameters=list(
  Phi=list(formula=~1), ## no variation
  p=list(formula=~time))) ## variation
```

```
##
Number of evaluations: 100 -2lnL: 164.2918996
Number of evaluations: 200 -2lnL: 164.2826682
Number of evaluations: 100 -2lnL: 164.3644499
```

pTime.p0

```
## crm Model Summary
##
## Npar : 5
## -2lnL: 164.2916
## AIC : 174.2916
##
## Beta
## Estimate se lcl ucl
## Phi.(Intercept) -1.0727457 0.4417633 -1.938602 -0.2068896
## p.(Intercept) -0.7340805 0.8873394 -2.473266 1.0051947
## p.time3 -0.2493750 0.9992171 -1.709090 2.2078404
## p.time4 -0.5362343 1.0492990 -1.520392 2.5928604
## p.time5 -0.5132146 1.0604845 -1.565335 2.5917642
```

predict(pTime.p0)

```
## $Phi
## occ estimate se lcl ucl
## 1 4 0.2548813 0.08389828 0.1258015 0.4484613
##
## $p
## time occ estimate se lcl ucl
## 1 5 5 0.4450069 0.2350247 0.11046285 0.8381100
## 2 4 4 0.4506992 0.2245909 0.12175380 0.8292377
## 3 3 3 0.3811416 0.1904568 0.11231406 0.7498679
## 4 2 2 0.3242999 0.1944422 0.0775371 0.7320611
```

$\Phi(t)p(t)$ – Temporal variation in apparent survival and capture probability

```
pPhiTime.p0<-crm(data=cjs.data, model="cjs", hessian=TRUE,
model.parameters=list(
  Phi=list(formula=~time), ## variation
  p=list(formula=~time))) ## variation
```

```
##
Number of evaluations: 100 -2lnL: 164.3386705
Number of evaluations: 200 -2lnL: 164.0160127
Number of evaluations: 300 -2lnL: 164.0267951
Number of evaluations: 400 -2lnL: 164.0190582
Number of evaluations: 500 -2lnL: 164.0218229
Number of evaluations: 100 -2lnL: 164.0485203
Number of evaluations: 200 -2lnL: 164.0197031
```

pPhiTime.p0

```
## crm Model Summary
##
## Npar : 8
## -2lnL: 164.016
## AIC : 180.016
##
## Beta
## Estimate se lcl ucl
## Phi.(Intercept) -0.5878274 1.258314 -3.054123 1.878468
## Phi.time2 -0.7997844 1.616899 -3.968907 2.369338
## Phi.time3 -0.3963709 1.515245 -3.366252 2.573510
## Phi.time4 -0.1714588 93.789755 -183.656461 183.999378
## p.(Intercept) -1.1526344 1.217571 -3.539073 1.233805
## p.time3 -0.9584416 1.665046 -2.305048 4.221931
## p.time4 -0.9172804 1.658919 -2.334201 4.168762
## p.time5 -0.2284426 78.951377 -154.516256 154.973142
```

pPhiTime.pc-predict(pPhiTime.p0)

Which model is the best?

The first model that had no variation was the best model since it had the lowest AIC score.

Table 1. Results for distance sampling of gazelle for half-normal and half-hazard models.

Model	Term	occ	Estimate	SE	lcl	ucl	AIC
No variation in apprent survival or capture probability	Phi	4	0.27	0.09	0.13	0.46	168.64
	p	5	0.39	0.16	0.15	0.70	

Exercise II

Jolly-Serber w/constant capture probability (p), constant entrance probabilities (pent, b_i), and temporal variation in apparent survival

```
js.phi0.pent0.p0 <- crm(data=js.data, model="JS", hessian=TRUE,
model.parameters=list(
  Phi=list(formula=~time), ## No variation
  pent=list(formula=~1), ## No variation
  p=list(formula=~1))) ## No variation
```

```
## Starting optimization 11 parameters
##
Number of evaluations: 100 -2lnL: -113.2691248
Number of evaluations: 200 -2lnL: -134.4672245
Number of evaluations: 300 -2lnL: -139.6788414
Number of evaluations: 400 -2lnL: -141.0580399
Number of evaluations: 500 -2lnL: -141.1281802
Number of evaluations: 600 -2lnL: -141.1802195
Number of evaluations: 700 -2lnL: -141.1758874
Number of evaluations: 800 -2lnL: -141.202416
Number of evaluations: 900 -2lnL: -141.2056587
Number of evaluations: 1000 -2lnL: -141.2069943
Number of evaluations: 1100 -2lnL: -141.1842722
Number of evaluations: 1200 -2lnL: -141.2062709
Number of evaluations: 1300 -2lnL: -141.1811164
Number of evaluations: 1400 -2lnL: -141.2061162
Number of evaluations: 1500 -2lnL: -140.9573627
Number of evaluations: 1600 -2lnL: -140.7468623
Number of evaluations: 1700 -2lnL: -140.2077272Computing hessian
##
Number of evaluations: 100 -2lnL: -141.1840858
Number of evaluations: 200 -2lnL: -141.1891034
Number of evaluations: 300 -2lnL: -141.1822162
Number of evaluations: 400 -2lnL: -141.2077139
Number of evaluations: 500 -2lnL: -135.6026371
```

```
js0est <- predict(js.phi0.pent0.p0)
js0est
```

```
## $Phi
## time occ estimate se lcl ucl
## 1 1 1 0.5783605 0.089419133 4.006754e-01 0.7378348
## 2 2 2 1.0000000 0.000000000 0.000000e+00 1.00000000
## 3 3 3 0.9999863 0.002901706 1.554535e-176 1.00000000
## 4 4 4 0.1104871 0.050412366 4.347366e-02 0.2534309
## 5 5 5 0.9999894 0.002036188 4.670797e-159 1.00000000
## 6 6 6 0.1708337 0.171580991 1.881890e-02 0.6887818
## 7 7 7 0.9999006 0.009489089 2.154812e-201 1.00000000
## 8 8 8 0.9999461 0.008419764 2.464963e-129 1.00000000
##
## $p
## occ estimate se lcl ucl
## 1 1 0.2604266 0.03625413 0.1958109 0.3374184
##
## $pent
## time occ estimate se lcl ucl
## 1 2 2 6.344774e-16 6.344746e-11 0 1
## 2 3 3 6.344774e-16 6.344746e-11 0 1
## 3 4 4 6.344774e-16 6.344746e-11 0 1
## 4 5 5 6.344774e-16 6.344746e-11 0 1
## 5 6 6 6.344774e-16 6.344746e-11 0 1
## 6 7 7 6.344774e-16 6.344746e-11 0 1
## 7 8 8 6.344774e-16 6.344746e-11 0 1
## 8 9 9 6.344774e-16 6.344746e-11 0 1
##
## $N
## estimate se lcl ucl
## 1 72.82629 21.77808 40.52649 130.8692
```

```
n <- nrow(js.data) # number of individuals captured
Nsuper <- n*js0est$N$estimate # Super-population size
Nsuper
```

```
## [1] 153.8263
```

```
b <- js0est$pent$estimate # Entrance probabilities after first time period
b0 <- 1-sum(b) # Compute first entrance probability
round(b, digits=16)
```

```
## [1] 6e-16 6e-16 6e-16 6e-16 6e-16 6e-16 6e-16 6e-16
```

```
R <- Nsuper*b # Recruits
R
```

```
## [1] 9.759931e-14 9.759931e-14 9.759931e-14 9.759931e-14 9.759931e-14
## [6] 9.759931e-14 9.759931e-14 9.759931e-14
```

```
Phi <- js0est$Phi$estimate ## Apparent survival probability
Phi
```

```
## [1] 0.5783605 1.0000000 0.9999863 0.1104871 0.9999894 0.1708337 0.9999606
## [8] 0.9999461
```

Interpretation of estimates

The capture probability was p=0.26, and the estimated number of individuals not detected was n=72.82.

Compute: super population size, number of recruits in each time interval, abundance at each time point

```
n <- nrow(js.data) # number of individuals captured
Nsuper <- n*js0est$N$estimate # Super-population size
Nsuper
```

```
## [1] 153.8263
```

```
b <- js0est$pent$estimate # Entrance probabilities after first time period
b0 <- 1-sum(b) # Compute first entrance probability
round(b, digits=16)
```

```
## [1] 6e-16 6e-16 6e-16 6e-16 6e-16 6e-16 6e-16 6e-16
```

```
R <- Nsuper*b # Recruits
R
```

```
## [1] 9.759931e-14 9.759931e-14 9.759931e-14 9.759931e-14 9.759931e-14
## [6] 9.759931e-14 9.759931e-14 9.759931e-14
```

```
Phi <- js0est$Phi$estimate ## Apparent survival probability
Phi
```

```
## [1] 0.5783605 1.0000000 0.9999863 0.1104871 0.9999894 0.1708337 0.9999606
## [8] 0.9999461
```

```
nYears <- length(R)+1
N <- rep(NA, nYears)
N[1] <- Nsuper*b0 ## Initial abundance
N[2] <- N[1]*Phi + R[1] ## Abundance in year 2
```

```
## Warning in N[2] <- N[1] * Phi + R[1]: number of items to replace is not a
## multiple of replacement length
```

```
N[3] <- N[2]*Phi + R[2] ## Abundance in year 3
```

```
## Warning in N[3] <- N[2] * Phi + R[2]: number of items to replace is not a
## multiple of replacement length
```

```
N[4] <- N[3]*Phi + R[3] ## Abundance in year 4
```

```
## Warning in N[4] <- N[3] * Phi + R[3]: number of items to replace is not a
## multiple of replacement length
```

```
N[5] <- N[4]*Phi + R[4] ## Abundance in year 5
```

```
## Warning in N[5] <- N[4] * Phi + R[4]: number of items to replace is not a
## multiple of replacement length
```

```
N[6] <- N[5]*Phi + R[5] ## Abundance in year 6
```

```
## Warning in N[6] <- N[5] * Phi + R[5]: number of items to replace is not a
## multiple of replacement length
```

```
N[7] <- N[6]*Phi + R[6] ## Abundance in year 7
```

```
## Warning in N[7] <- N[6] * Phi + R[6]: number of items to replace is not a
## multiple of replacement length
```

```
N[8] <- N[7]*Phi + R[7] ## Abundance in year 8
```

```
## Warning in N[8] <- N[7] * Phi + R[7]: number of items to replace is not a
## multiple of replacement length
```

```
N[9] <- N[8]*Phi + R[8] ## Abundance in year 9
```

```
## Warning in N[9] <- N[8] * Phi + R[8]: number of items to replace is not a
## multiple of replacement length
```

```
round(N, digits=0)
```

```
## [1] 154 89 51 30 17 10 6 3 2
```

Plot

```
lambda <- N[2:9]/N[1:8]
lam<-round(lambda, digits=10)
```

```
Years<-1:8
```

```
plot(Years, lam, type="b", xlab="Year", ylab="Lambda")
```

