

This is a section-by-section list of all the major results, with their dependencies. Throughout: track down specific refs, ie Theorem 2.7 in [3], not just [3]

1. INTRODUCTION

Nothing to say here, I think.

2. ACTION OPERADS

Definition. symmetric operad

Definition. non-symmetric operad

Definition. braided operad

Definition. operad map

Definition. action operad

Definition. map of action operads

Definition/Example. ribbon braids, and their (action) operad

Result (1). π is a map of operads. **Dependency:** defs

Result (2). Operads internal to groups are action operads. **Dependency:** (1)

Result (3). The kernel of an action operad is an action operad. **Dependency:** (1,2)

Result (4). The image, in Σ of an action operad is an action operad. **Dependency:** (1)

Result (5). A kernel/image short exact sequence. **Dependency:** (3,4)

Result (6). Some calculations with e'_i s. **Dependency:** defs

Result (7). Some calculations with $\Lambda(0)$. **Dependency:** (6)

Result (8). The big β, δ theorem. **Dependency:** (1)

Result (9). π is zero or surjective. **Dependency:** (8)

Examples. Cyclic, reflexive, hyperoctahedral, alternating. **Dependency:** (8)

Definition. lfp stuff

Result (10). The category of action operads is lfp. **Dependency:** defs, external

Result (11). $U : \mathbf{AOp} \rightarrow \mathbf{Sets}/\mathcal{S}$ preserves limits and filtered colimits. **Dependency:** defs **Note:** seriously check proof

Result (12). $F : \mathbf{Sets}/\mathcal{S} \rightarrow \mathbf{AOp}$ left adjoint to U . **Dependency:** external

Definition. presentations for action operads **Dependency:** (12)

3. OPERADS WITH EQUIVARIANCE

Definition. Λ -operad

Definition. map of Λ -operads

Definition. category of Λ -operads

Result (13). Λ is a Λ -operad. **Dependency:** defs

Definition. algebra over a non-symmetric operad **Note:** delete?

Definition. algebra over a Λ -operad

Definition. category of algebras over a Λ -operad

Result (14). Endomorphism operad is a Λ -operad. **Dependency:** defs **Note:** should have independent endomorphism operad def beforehand, maybe rework all this stuff

Result (15). Change-of-operad functor. **Dependency:** defs

Result (16). Algebras are operad maps into endomorphisms operad. **Dependency:** (14)

Definition. monad associated to a Λ -operad

Result (17). Monad algebra category is operad algebra category. **Dependency:** defs

Result (18). Λ -algebras, as a Λ -operad, are monoids. **Dependency:** defs, maybe (16) **Note:** unclear hypotheses, should say in sets I think

Result (19). Three-part theorem about the adjunction between Λ - and Σ -operads and their categories of

algebras. **Dependency:** defs **Note:** check proof

Definition. monad map **Note:** some text after that needs to be in an environment

Definition. cocomplete SMC **Note:** no emph in def, is wrong

Result (19). Lax symmetric monoidal functors transport operads, with a comparison monad map. **Dependency:** FUTURE! **Note:** eep in general! where did we define the tensor product over a group notation?

Result (20). Operad maps induce monad maps. **Dependency:** stuff that isn't in an environment above **Note:** continued eep

Result (21). Combining to get an adjunction. **Dependency:** (19, 20) **Note:** continued eep

Definition. collections, maps, the category thereof

Definition. substitution product of collections

Result (22). Substitution product gives monoidal structure, and monoids are operads. **Dependency:** (19, 20)

Result (23). $B\Lambda$ is a strict monoidal category. **Dependency:** FUTURE! also (6)

Result (24). n -fold Day convolution is a functor $B\Lambda \rightarrow \mathbf{Sets}$. **Dependency:** (23)

Result (25). Substitution product as coend using Day convolution. **Dependency:** ?? **Note:** seriously check proof

Proof of (22). **Dependency:** (23,24,25) **Note:** seriously check proof

4. OPERADS IN THE CATEGORY OF CATEGORIES

Note: worth revisiting introductory material, maybe some of it needs environments

Definition. pseudoalgebras

Definition. strict algebras **Dependency:** previous defn

Definition. pseudomorphisms

Definition. strict morphisms **Dependency:** previous defn

Definition. algebra transformations

Definition. P -alg, strict and strong

Definition. 2-monads versions of the above

Result (26). 2-monad and operad algebra 2-categories agree, strict and strong. **Dependency:** definitions here

Result (27). 2-monad from an operad is finitary. **Dependency:** definitions here **Note:** check proof

Result (28). 2-monad from an operad preserves bijective-on-objects functors. **Dependency:** definitions here

Result (29). Pseudoalgebras equivalent to strict ones. **Dependency:** definitions here **Note:** worth explaining how this strictifies unbiased monoidal categories to strict ones, but not biased ones

Definition. 2-cartesian 2-monad **Note:** we seem to need some definitions here

Result (30). Coequalizer of actions is sometimes the quotient. **Dependency:** none **Note:** this looks like it could be improved, many aspects unclear

Result (31). Unit for \underline{P} is cartesian for any symmetric operad P . **Dependency:** definitions here

Result (32). The 2-monad \underline{P} preserves pullbacks iff group action is free. **Dependency:** (30)

Result (33). Multiplication for \underline{P} is cartesian if all group actions are free. **Dependency:** (30) **Note:** has some suspect proof-by-example looking text

Result (34). \underline{P} is 2-cartesian if and only if all group actions are free (symmetric case). **Dependency:** (31, 32, 33; 30)

Result (35). \underline{P} is 2-cartesian if and only if all group actions are free (symmetric case). **Dependency:** (31, 32, 33; 30)

Result (36). Lemma about free Σ -actions on categories with Λ -action. **Dependency:** defs **Note:** needs to be fixed up a bit in the whole groups actions on categories rework

Result (37). \underline{P} is 2-cartesian if and only if all group actions are free (Λ case). **Dependency:** (35, 36; 30, 31, 32, 33, 34)

5. THE BOREL CONSTRUCTION FOR ACTION OPERADS

6. MONOIDAL STRUCTURES AND MULTICATEGORIES