This is a section-by-section list of all the major results, with their dependencies.

1. Introduction

Nothing to say here, I think.

2. ACTION OPERADS

Definition. symmetric operad **Definition.** non-symmetric operad **Definition.** braided operad **Definition.** operad map **Definition.** action operad **Definition.** map of action operads **Definition/Example.** ribbon braids, and their (action) operad Result (1). π is a map of operads. Dependency: defs Result (2). Operads internal to groups are action operads. Dependency: (1) **Result (3).** The kernel of an action operad is an action operad. Dependency: (1,2) **Result (4).** The image, in Σ of an action operad is an action operad. Dependency: (1) Result (5). A kernel/image short exact sequence. Dependency: (3,4) **Result (6).** Some calculations with $e'_i s$. Dependency: defs **Result** (7). Some calculations with $\Lambda(0)$. Dependency: (6) **Result** (8). The big β, δ theorem. Dependency: (1) Result (9). π is zero or surjective. Dependency: (8) **Examples.** Cyclic, reflexive, hyperoctahedral, alternating. Dependency: (8) **Definition.** If p stuff Result (10). The category of action operads is lfp. Dependency: defs, external Result (11). $U: AOp \rightarrow Sets/S$ preserves limits and filtered colimits. Dependency: defs Note: seriously

Result (12). $F : \mathbf{Sets/S} \to \mathbf{AOp}$ left adjoint to U. Dependency: external

Definition. presentations for action operads Dependency: (12)

3. Operads with equivariance

Definition. Λ -operad **Definition.** map of Λ -operads **Definition.** category of Λ -operads Result (13). Λ is a Λ -operad. Dependency: defs

Definition. algebra over a non-symmetric operad Note: delete?

Definition. algebra over a Λ -operad

Definition. category of algebras over a Λ -operad

Result (14). Endomorphism operad is a Λ-operad. Dependency: defs Note: should have independent endomorphism operad def beforehand, maybe rework all this stuff

Result (15). Change-of-operad functor. Dependency: defs

Result (16). Algebras are operad maps into endomorphisms operad. Dependency: (14)

Definition. monad associated to a Λ -operad

Result (17). Monad algebra category is operad algebra category. Dependency: defs

Result (18). Λ-algebras, as a Λ-operad, are monoids. Dependency: defs, maybe (16) Note: unclear hypotheses, should say in sets I think

Result (19). Three-part theorem about the adjunction between Λ - and Σ -operads and their categories of algebras. Dependency: defs Note: check proof

Definition. monad mapNote: some text after that needs to be in an environment

Definition. cocomplete SMC Note: no emph in def, is wrong

Result (19). Lax symmetric monoidal functors transport operads, with a comparison monad map. Dependency: FUTURE! Note: eep in general! where did we define the tensor product over a group notation?

Result (20). Operad maps induce monad maps. Dependency: stuff that isn't in an environment above Note: continued eep

Result (21). Combining to get an adjunction. Dependency: (19, 20) Note: continued eep

Definition. collections, maps, the category thereof

Definition. substitution product of collections

Result (22). Substitution product gives monoidal structure, and monoids are operads. Dependency: (19, 20)

Result (23). $B\Lambda$ is a strict monoidal category. Dependency: FUTURE! also (6)

Result (24). n-fold Day convolution is a functor $B\Lambda \to \mathbf{Sets}$. Dependency: (23)

Result (25). Substitution product as coend using Day convolution. Dependency: ?? Note: seriously check proof

Proof of (22). Dependency: (23,24,25) Note: seriously check proof

- 4. Operads in the category of categories
- 5. The Borel construction for action operads
- 6. Monoidal structures and multicategories