

# Action operads comments to fix

## 1. INTRODUCTION

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## 2. ACTION OPERADS

- I put in G0abel (2.3.8) to prove: typed in proof of abelianness but need to show that  $\mu(e_2; g, h) = gh$  (suffices to show that  $\mu(e_2; g, e_0) = g$ ). Thought it would be a straightforward Eckmann-Hilton argument but it gets stuck.
- Proof of 2.3.4: just needs checking
- I have been changing tensor product to block sum for a lot of things, we need to go through and decide how to do that consistently
- Prop 2.5.19 follows from Theorem 3.3.8, except for the part about the monad map (it can't be  $(F, id)$  as it needs to use the coherence cells of  $F$ , so I've called it  $(F, \psi^F)$  and added details to the propositions).

## 3. OPERADS IN THE CATEGORY OF CATEGORIES

- Prop 3.3.11-4 The proofs need filling out
- Should we change  $E\Lambda(n) \times X^n / \Lambda(n)$  to be  $(E\Lambda(n) \times X^n) / \Lambda(n)$ ?

## 4. MONOIDAL STRUCTURES AND MULTICATEGORIES

- Intro
- Use  
     $\backslash \text{lmc}$   
for lambda monoidal categories
- Lemma 4.3.2: Needs rewording. Is the *underlying set of the free monoid*?
- Re: What is an action morphism? Added a remark (4.3.5 or near) to give some reference.
- Do we want another notation to emphasise the underlying monoid?
- Lemma 4.3.8: Should be a  $\Lambda^\oplus$ , not just  $\Lambda$ .
- Defn 4.5.1: Odd mix of  $\alpha$  and  $g$ . Think something is mixed up here.  $(-\cdot\alpha)$ . Also should the iso have  $\pi(g)^{-1}$  in the target?
- Monad maps are defined in the specific case of the 2-category of categories in Section 2.5 - refer back to these definitions.

## 5. INVERTIBLE OBJECTS

- The notation in the very first sentence needs to be explained somewhere!
- Rewrite intro: Need to explain that the goal is to understand some group actions
- Decide on ELambda algebras or Lambda monoidal categories throughout (we decided the second!)
- New notation: added earlier (line 905, search beta\_to\_oplus), just need to implement, search for action maps or superscript tensors
- Fix weakly invertible section

Leftover fixes that I'm not sure about:

- Move comment (QQQ)
- Fix paragraph; make clear we are determining composition
- Explain M strategy, include forward refs

## 6. INVERTIBILITY AND GROUP ACTIONS

- I want to write  $\Lambda^\oplus$  for the underlying monoid maybe??
- **why? This one involves real math**
- not happy with last section

## 7. COMPUTING AUTOMORPHISMS OF THE UNIT

- 4.1.3 check 2.3.10: need to make sure this is in an earlier section, and ref'ed
- explain purpose
- improve proof 4.2.3
- check commutative Square
- redo 4.4
- insert diagram
- consistent text after 4.5.3
- move something to earlier
- highlight that star means the inverse under tensor product for morphisms
- check the note

## 8. A FULL DESCRIPTION OF $L_n$

- Think about  $n$  vs  $2n$  in AGndef
- check reference
- rewrite calculation
- check universal property
- insert for a simple example

## 9. EXAMPLES

- Actually read this section, fix anything

## Comments addressed

### 10. INVERTIBLE OBJECTS

- Include notation for  $\eta$  as the unit here
- Change to equalizers
- Change to  $(LX)_{inv} = LX$
- Fix  $()_s$
- Include triangle NO
- Uniform gp superscripts
- Remove actually
- Ref  $\eta$
- Replace with is, remove parts
- Remove proof
- Fix ab superscripts, same as gp
- qi
- Under red line: move? make remark? delete some?
- Where do we say this?
- Need 2-adjunction: this should follow from Thm 8.6 in the enriched\_\_sketches paper I saved
- include forward ref to where we use crefpi: I can't find it
- Get better Eckmann-Hilton ref: don't care anymore

### 11. INVERTIBILITY AND GROUP ACTIONS

- Forward ref
- definition env
- little wording fixes
- change G to Lambda
- S vs Sigma for symmetric groups: I picked Sigma
- Think about free monoid lem again
- Fix triangle
- lots of notation issues (e, G, length bars)
- why splitting
- missing ref?
- splits by construction: hmm
- ref?
- for v, v' not delta of something
- inverses for morphisms under comp vs tensor
- more G's (x2)
- another missing ref
- another G
- include corollary?
- forward refs
- practical?

### 12. COMPUTING AUTOMORPHISMS OF THE UNIT

- in the next two results

- 4.1.2 two boxes
- the above following square
- insert =
- check  $4n$  or  $2n$  (it is correct in 7.2.1)
- mentioned Delta, I
- fixed proof 4.3.2
- remove functor
- isomorphism symbol
- clarify this
- make sure length and size notation is introduced earlier
- bad line break at the beginning of 4.5
- change prove to shows
- bad line break
- insert the proof from Ed's email
- put a short proof
- change express to describe
- isomorphism symbol
- change make sure to ensures
- remove calculation
- change we want to do

### 13. A FULL DESCRIPTION OF $L_n$

- bad line break
- remove exposition
- fix fancy G
- change G to lambda
- isomorphism symbol
- tensor product given component wise
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### 14. EXAMPLES

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