## Action operads comments to fix

## 1. Introduction

•

#### 2. ACTION OPERADS

- I put in G0abel (2.3.8) to prove, and we should put in a proof that all the π's are surjective or trivial (2.3.4)
- I have been changing tensor product to block sum for a lot of things, we need to go through and decide how to do that consistently

#### 3. Operads in the category of categories

- Start of 3.1: Should the 2-monad should have EP(n)? Compare with 3.3.9.
- Defn 3.3.7 of cocomplete symmetric monoidal cat
- After 3.3.9 seems repetitive (essentially description of P)
- Prop 3.3.16 The proofs need filling out
- Should we change  $E\Lambda(n) \times X^n/\Lambda(n)$  to be  $(E\Lambda(n) \times X^n)/\Lambda(n)$ ?

#### 4. Monoidal structures and multicategories

- Intro
- Use

\lmc

for lambda monoidal categories

- Theorem 4.2.11: 'Define  $\beta$  by' should have  $s_{p_1+r_1,q_1+r_1}$  on the RHS, not  $s_{p_1,q_1}$ ?
- Lemma 4.3.2: Needs rewording. Is the underlying set of the free monoid?
- Prop 4.3.3: Is  $im(\pi)$  defined? What is the underlying permutation operad? Does this mean the symmetrized operad?
- an  $E\Lambda$  or a  $\Lambda$ -monoidal
- Lemma 4.3.5: Spacing of equations needs fixing.
- $\Lambda(2)$  not G(2)
- What is an action morphism?
- Do we want another notation to emphasise the underlying monoid?
- Lemma 4.3.8: Should be a  $\Lambda(n)$ , not just  $\Lambda$ .
- 4.3.8: extra couple of steps to show  $\alpha$  is a monoid homomorphism?
- Remark 4.4.4: It's mostly described but not directly shown about the strength axioms?
- Defn 4.5.1: Odd mix of  $\alpha$  and g. Think something is mixed up here.  $(-\cdot \alpha)$ . Also should the iso have  $\pi(g)^{-1}$  in the target?

## 5. Invertible objects

- The notation in the very first sentence needs to be explained somewhere!
- Rewrite intro: Need to explain that the goal is to understand some group actions

- Decide on ELambda algebras or Lambda monoidal categories throughout (we decided the second!)
- New notation: added earlier (line 905, search beta\_to\_oplus), just need to implement, search for action maps or superscript tensors
- Fix weakly invertible section

## Leftover fixes that I'm not sure about:

- Move comment (QQQ)
- Fix paragraph; make clear we are determining composition
- Explain M strategy, include forward refs

## 6. Invertibility and group actions

- I want to write  $\Lambda^{\oplus}$  for the underlying monoid maybe??
- why? This one involves real math
- not happy with last section

## 7. Computing automorphisms of the unit

- 4.1.3 check 2.3.10: need to make sure this is in an earlier section, and ref'ed
- explain purpose
- improve proof 4.2.3
- check commutative Square
- $\bullet$  redo 4.4
- insert diagram
- consistent text after 4.5.3
- move something to earlier
- highlight that star means the inverse under tensor product for morphisms
- check the note

## 8. A FULL DESCRIPTION OF $L_n$

- Think about n vs 2n in AGndef
- check reference
- rewrite calculation
- check universal property
- ullet insert for a simple example

## 9. Examples

• Actually read this section, fix anything

## Comments addressed

### 10. Invertible objects

- Include notation for  $\eta$  as the unit here
- Change to equalizers
- Change to  $(LX)_{inv} = LX$
- Fix ()s
- Include triangle NO
- Uniform gp superscripts
- Remove actually
- Ref  $\eta$
- Replace with is, remove parts
- Remove proof
- Fix ab superscripts, same as gp
- q
- Under red line: move? make remark? delete some?
- Where do we say this?
- Need 2-adjunction: this should follow from Thm 8.6 in the enriched\_sketches paper I saved
- include forward ref to where we use crefepi: I can't find it
- Get better Eckmann-Hilton ref: don't care anymore

#### 11. Invertibility and group actions

- Forward ref
- definition env
- little wording fixes
- change G to Lambda
- S vs Sigma for symmetric groups: I picked Sigma
- Think about free monoid lem again
- Fix triangle
- lots of notation issues (e, G, length bars)
- why splitting
- missing ref?
- splits by construction: hmm
- ref?
- for v, v' not delta of something
- inverses for morphisms under comp vs tensor
- more G's (x2)
- another missing ref
- another G
- include corollary?
- forward refs
- practical?

## 12. Computing automorphisms of the unit

• in the next two results

- 4.1.2 two boxes
- the above following square
- $\bullet$  insert =
- check 4n or 2n (it is correct in 7.2.1)
- mentioned Delta, I
- fixed proof 4.3.2
- $\bullet$  remove functor
- isomorphism symbol
- clarify this
- $\bullet\,$  make sure length and size notation is introduced earlier
- bad line break at the beginning of 4.5
- change prove to shows
- bad line break
- ullet insert the proof from Ed's email
- put a short proof
- $\bullet\,$  change express to describe
- isomorphism symbol
- change make sure to ensures
- remove calculation
- change we want to do

# 13. A FULL DESCRIPTION OF $L_n$

- bad line break
- remove exposition
- fix fancy G
- change G to lambda
- isomorphism symbol
- tensor product given component wise

•

## 14. Examples

•