

$$\begin{aligned}\mathbf{F} &= \frac{1}{4\pi\epsilon_0} \frac{Qq}{z^2} \hat{\mathbf{z}} = q\mathbf{E} \\ \mathbf{E}(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \int d\tau' \rho(\mathbf{r}') \frac{\hat{\mathbf{z}}}{z^2} \\ \oint_{\sigma} d\mathbf{a} \cdot \mathbf{E} &= Q_{enc}/\epsilon_0 \\ \nabla \cdot \mathbf{E} &= \rho(\mathbf{r})/\epsilon_0 \quad \nabla \times \mathbf{E} = 0 \\ V(\mathbf{r}) &= - \int_{\infty/ref}^{\mathbf{r}} d\hat{\ell} \cdot \mathbf{E} \\ \Delta V &= \int_a^b d\hat{\ell} \cdot \mathbf{E} \quad \mathbf{E} = -\nabla V \\ V(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \int d\tau' \frac{\rho(\mathbf{r}')}{z} \\ \mathbf{E}_{\perp}^{above} - \mathbf{E}_{\perp}^{below} &= \sigma \hat{\mathbf{n}}/\epsilon_0 \\ \frac{\partial V^{above}}{\partial \hat{\mathbf{n}}} - \frac{\partial V^{below}}{\partial \hat{\mathbf{n}}} &= -\sigma/\epsilon_0 \\ \nabla \cdot \frac{\hat{\mathbf{z}}}{z^2} &= 4\pi\delta(\hat{\mathbf{z}}) \quad \epsilon_{123} = 0 \\ c &= \sqrt{a^2 + b^2 - 2ab \cos \theta} \\ &= \\ \nabla \times (r^n \hat{\mathbf{r}}) &= 0\end{aligned}$$

$$\begin{aligned}\nabla^2 V &= -\frac{1}{\epsilon_0} \rho \\ V_{grounded} &= 0 \\ A_n &= \frac{2}{a} \int_0^a f(x) \cos(n\pi x/a) dx \\ B_n &= \frac{2}{a} \int_0^a f(x) \sin(n\pi x/a) dx \\ \cosh(x) &= (e^x + e^{-x})/2 \\ \sinh(x) &= (e^x - e^{-x})/2 \\ P_0(x) &= 1 \quad P_1(x) = x \\ P_2(x) &= \frac{1}{2}(3x^2 - 1) \\ P_3(x) &= \frac{1}{2}(5x^3 - 3x) \\ V_{spher}(r, \vartheta) &= \\ &= \sum_{l=0}^{\infty} (A_l r^l + \frac{B_l}{r^{l+1}}) P_l(\cos \vartheta) \\ V_{cyl}(f, \varphi) &= G \ln r + H + \\ \sum_{k=1}^{\infty} [(C_k r^k + D_k r^{-k}) \times \\ & (A_k \cos k\varphi + B_k \sin k\varphi)]\end{aligned}$$

$$\begin{aligned}W &= \frac{1}{2} \sum_i q_i V_i \equiv \frac{1}{2} \int \rho V d\tau \\ W &= \frac{1}{2} \int_V d\tau \rho(\mathbf{r}) V(\mathbf{r}) \\ W &= \frac{\epsilon_0}{2} \int_V E^2 d\tau + \\ & \oint_{\sigma} V \mathbf{E} \cdot d\mathbf{a} \\ W &= \frac{\epsilon_0}{2} \int_{\text{all space}} E^2 d\tau \\ V_{cap} &\equiv V_+ - V_- \\ C &\equiv Q/V_{cap} \\ E_{plane} &= \sigma/2\epsilon_0 \\ V_{plates} &= Qd/A\epsilon_0 \\ W_{cap} &= QV_{cap} = Q^2/2C \\ \mathbf{A} \times \mathbf{B} &= \sum_{i,j,k} \epsilon_{ijk} \hat{e}_i A_j B_k \\ \nabla \cdot (\nabla f \times \nabla g) &= 0 \\ \delta(kx - x') &\propto \delta(x - x'/k)\end{aligned}$$

$$\begin{aligned}V_{mp}(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \int d\tau' \frac{\rho(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} \quad \nabla'(1/z) = \hat{\mathbf{z}}/z^2 \\ \frac{1}{|\mathbf{r}-\mathbf{r}'|} &\simeq \frac{1}{r} + (-\mathbf{r}') \cdot \nabla \frac{1}{r} + \frac{1}{2} (-\mathbf{r}' \cdot \nabla)^2 \frac{1}{r} + \dots \\ V_{mp}(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \left[\frac{q}{r} + \frac{\hat{\mathbf{r}} \cdot \mathbf{p}}{r^2} + \frac{1}{2r^3} \hat{\mathbf{r}} \cdot \underline{\underline{\mathbf{Q}}} \cdot \hat{\mathbf{r}} + \dots \right] \\ \underline{\underline{\mathbf{Q}}} &= \int d\tau' \rho(\mathbf{r}') [-(\mathbf{r}')^2 \mathbb{1} + 3\mathbf{r}'\mathbf{r}'] \\ \frac{1}{|\mathbf{r}-\mathbf{r}'|} &= \sum_{\ell=0}^{\infty} \frac{(r')^{\ell}}{r^{\ell+1}} P_{\ell}(\cos \alpha) \quad \cos \alpha = \hat{\mathbf{r}} \cdot \hat{\mathbf{r}}' \\ V_{mp}(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \sum_{\ell=0}^{\infty} \frac{1}{r^{\ell+1}} \int d\tau' \rho(\mathbf{r}') (\mathbf{r}')^{\ell} P_{\ell}(\cos \alpha) \\ V_{dp} &= \frac{1}{4\pi\epsilon_0} \frac{1}{r^2} \hat{\mathbf{r}} \cdot \mathbf{p} \quad \mathbf{E}_{dp} = -\frac{1}{4\pi\epsilon_0} \frac{1}{r^3} [\mathbf{p} - 3\hat{\mathbf{r}}\hat{\mathbf{r}} \cdot \mathbf{p}] \\ \mathbf{p} &= \int d\tau' \rho(\mathbf{r}') \mathbf{r}' = \sum_i q_i \mathbf{r}_i \quad \mathbf{p}_{phys} = q\mathbf{d} \\ (\mathbf{a} \cdot \nabla) \mathbf{f} &= \mathbf{a} \cdot \nabla \mathbf{f} \quad \nabla \mathbf{r} = \mathbb{1} = \nabla \hat{\mathbf{r}} \\ \nabla \nabla \frac{1}{r} &= \frac{1}{r^3} (-\mathbb{1} + 3\hat{\mathbf{r}}\hat{\mathbf{r}}) \quad \nabla(r^n) = nr^{n-1} \hat{\mathbf{r}} \\ \nabla(\mathbf{a} \cdot \mathbf{b}) &= (\nabla \mathbf{a}) \cdot \mathbf{b} + (\nabla \mathbf{b}) \cdot \mathbf{a} \\ \mathbf{p} &= \alpha \mathbf{E} \quad \mathbf{N}_{dp} = \mathbf{p} \times \mathbf{E} \\ \mathbf{F}_{dp} &= q(\Delta \mathbf{E}) \simeq (\mathbf{p} \cdot \nabla) \mathbf{E}\end{aligned}$$

$$\begin{aligned}W_{dp} &= -\mathbf{p} \cdot \mathbf{E} \quad D_{ab}^{\perp} - D_{bel}^{\perp} = \sigma_f \\ V_{de}(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \int_V \frac{\mathbf{P}(\mathbf{r}') \cdot \hat{\mathbf{z}}}{z^2} d\tau' \\ V_{de}(\mathbf{r}) &= \frac{1}{4\pi\epsilon_0} \left[\oint_S \frac{\sigma_b}{z} da' + \int_V \frac{\rho_b}{z} d\tau' \right] \\ \sigma_b &= \mathbf{P} \cdot \hat{\mathbf{n}} \quad \rho_b = -\nabla \cdot \mathbf{P} \\ \nabla \cdot \mathbf{D} &= \rho_f \quad \mathbf{D} \equiv \epsilon_0 \mathbf{E}_{tot} + \mathbf{P} \\ \oint d\mathbf{a} \cdot \mathbf{D} &= Q_{f,enc} \quad \mathbf{P} = \epsilon_0 \chi_e \mathbf{E}_{tot} \\ \mathbf{D} &= \epsilon_0 (1 + \chi_e) \mathbf{E}_{tot} \\ \rho_b &= -\frac{\chi_e}{1+\chi_e} \rho_f \quad \mathbf{E}_{sph,unif} = -\frac{1}{3\epsilon_0} \mathbf{P} \\ \mathbf{D} &= \epsilon_0 \mathbf{E}_{vac} \quad \mathbf{E} = \mathbf{E}_{vac}/\kappa \\ \epsilon_{ab} \frac{\partial V_{ab}}{\partial n} - \epsilon_{bel} \frac{\partial V_{bel}}{\partial n} &= -\sigma_f \\ \frac{\partial \mathbf{E}}{\partial t} + \frac{\mathbf{J}}{\epsilon_0} - \frac{\nabla \times \mathbf{B}}{\epsilon_0 \mu_0} &= 0 \\ \mathbf{B}(\mathbf{r}) &= \frac{\mu_0}{4\pi} \int d\tau' \frac{\mathbf{J}(\mathbf{r}') \times \hat{\mathbf{z}}}{z^2} \\ \mathbf{B}(\mathbf{r}) &= \frac{\mu_0}{4\pi} \nabla \times \int d\tau' \frac{\mathbf{J}(\mathbf{r}')}{z}\end{aligned}$$

$$\begin{aligned}\kappa &\equiv 1 + \chi_e \equiv \epsilon_r \\ C &= \kappa Q/V_{vac} \\ W_C &= \kappa C V^2/2 \\ W &= \frac{1}{2} \int d\tau \mathbf{D} \cdot \mathbf{E} \\ \mathbf{v} \times \mathbf{E} &= \mathbf{B}/\epsilon_0 \mu_0 \\ \nabla \cdot \mathbf{J}_{ms} &= 0 \\ \nabla \cdot \mathbf{B}_{ms} &= 0 \\ \nabla \times \mathbf{B} &= \mu_0 \mathbf{J} \\ \mathbf{I} &= \lambda \mathbf{v} = q/\Delta t \\ \mathbf{F} &= q(\mathbf{E} + \mathbf{v} \times \mathbf{B}) \\ \mathbf{F} &= \int d\tau' \mathbf{J} \times \mathbf{B} \\ \oint d\ell \cdot \mathbf{B} &= \mu_0 I_{enc} \\ &= \mu_0 \int d\mathbf{a} \cdot \mathbf{J}(\mathbf{r}) \\ \mathbf{B} &= \nabla \times \mathbf{A} \\ \nabla^2 \mathbf{A} &= -\mu_0 \mathbf{J}\end{aligned}$$

$$\begin{aligned}\mathbf{A}(\mathbf{r}) &= \frac{\mu_0}{4\pi} \int d\tau' \frac{\mathbf{J}(\mathbf{r}')}{z} \quad \mathbf{I} \equiv I d\ell \\ \mathbf{v}_{rot} &= \boldsymbol{\omega} \times \mathbf{r}' \\ \nabla \cdot \mathbf{B} &= 0 \\ \oint d\mathbf{a} \cdot \mathbf{B} &= 0 \\ B_{\mathbf{n},\perp}^{ab} - B_{\mathbf{n},\perp}^{bel} &= 0 \\ B_{cp,\perp}^{ab} - B_{cp,\perp}^{bel} &= \mu_0 K \\ B_{cp,\parallel}^{ab} - B_{cp,\parallel}^{bel} &= 0 \\ \mathbf{B}^{ab} - \mathbf{B}^{bel} &= \mu_0 \mathbf{K} \times \mathbf{n} \\ \mathbf{A}^{ab} - \mathbf{A}^{bel} &= 0 \\ \frac{\partial \mathbf{A}^{ab}}{\partial n} - \frac{\partial \mathbf{A}^{bel}}{\partial n} &= -\mu_0 \mathbf{K} \\ \mathbf{A}_{mp,m}(\mathbf{r}) &= \\ &= \frac{\mu_0}{4\pi} \left[\frac{1}{r} \int d\tau' \mathbf{J}(\mathbf{r}') + \frac{\mathbf{r}}{r^3} \int d\tau' \mathbf{r}' \mathbf{J}(\mathbf{r}') + \dots \right] \\ \frac{\partial \rho}{\partial t}_{ms} &= 0 \quad \int_V \mathbf{J}(\mathbf{r}') = \frac{d\mathbf{p}}{dt} \\ \mathbf{J}(\mathbf{r}') &= \mathbf{r}' \nabla' \cdot \mathbf{J}(\mathbf{r}') \\ \mathbf{m} &= \frac{1}{2} \int d\tau' \mathbf{r}' \times \mathbf{J}(\mathbf{r}')\end{aligned}$$

$$\begin{aligned}\mathbf{A}_{dp,m}(\mathbf{r}) &= \frac{\mu_0}{4\pi} \frac{\mathbf{m} \times \mathbf{r}}{r^3} \\ \mathbf{B}_{dp,m}(\mathbf{r}) &= \frac{\mu_0}{4\pi} \frac{3\mathbf{m} \cdot \hat{\mathbf{r}} \hat{\mathbf{r}} - \mathbf{m}}{r^3} \\ \nabla \frac{\mathbf{r}}{r^3} &= \frac{\mathbb{1} - 3\hat{\mathbf{r}}\hat{\mathbf{r}}}{r^3} \\ \mathbf{m}_{loop} &= I \mathbf{a} = I \frac{1}{2} \int \mathbf{r}' \times d\ell' \\ \mathbf{f} &\equiv \mathbf{F}/q \quad \mathbf{f} \equiv \mathbf{v} \times \mathbf{B}, \mathbf{E} \dots \\ \mathbf{J} &= \frac{nq^2}{m\gamma} \mathbf{f} = \sigma_{cond} \mathbf{f} \\ \mathbf{J} &= \sigma \mathbf{E} \quad I = \int \mathbf{J} \cdot d\mathbf{a} \\ \varepsilon &\equiv \oint \mathbf{f} \cdot d\mathbf{l} \quad \mathbf{E} = -\mathbf{f}_{src,ideal} \\ \varepsilon &\equiv \oint \mathbf{E} \cdot d\mathbf{l} \quad \varepsilon \equiv IR \quad \varepsilon = -\frac{d\Phi_B}{dt} \\ \Phi_B &= \int \mathbf{B} \cdot d\mathbf{a} \quad \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \\ \oint d\ell \cdot \mathbf{E} &= -\frac{d}{dt} \int d\mathbf{a} \cdot \mathbf{B} = -d\Phi_B/dt \\ \nabla \times \mathbf{B} &= \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \\ \oint \mathbf{B} \cdot d\ell &= \mu_0 I_{enc} + \mu_0 \epsilon_0 \int \frac{\partial \mathbf{E}}{\partial t} \cdot d\mathbf{a}\end{aligned}$$

$$\begin{aligned}\lim_{\mathbf{r} \rightarrow \infty} A &\neq 0: \\ \oint \mathbf{A} \cdot d\ell &= \int \mathbf{B} \cdot d\mathbf{a} \\ \rho, \mathbf{J} &= 0: \\ \mathbf{E} &\rightarrow \frac{1}{\sqrt{\epsilon_0 \mu_0}} \mathbf{B} \\ \mathbf{B} &\rightarrow -\sqrt{\epsilon_0 \mu_0} \mathbf{E}\end{aligned}$$