# Algorithm Library $^*$

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<sup>\*</sup>Based on the ply-template by palayutm

## 1 vimrc

#### $\mathbf{2}$ $\mathbf{Z}$

```
using u32 = unsigned;
using u64 = unsigned long long;
const u32 MOD = 1E9 + 7;
struct Z {
    u32 v;
    Z(u32 v = 0) : v(v) {}
    Z& operator += (const Z &z) {
        v += z.v;
        if (v \ge MOD) v = MOD;
        return *this;
    }
    Z& operator -= (const Z &z) {
        if (v < z.v) v += MOD;
        v -= z.v;
        return *this;
    Z& operator *= (const Z &z) {
        v = \text{static cast} < u64 > (v) * z.v % MOD;
        return *this;
};
Z operator + (const Z &x, const Z &y) {
    return Z(x.v + y.v >= MOD ? x.v + y.v - MOD :
   x.v + y.v);
}
Z operator - (const Z &x, const Z &y) {
    return Z(x.v < y.v ? x.v + MOD - y.v : x.v -
   y.v);
}
Z operator * (const Z &x, const Z &y) {
    return Z(static_cast<u64>(x.v) * y.v % MOD);
Z qpow(Z base, u32 e) {
    Z ret(1);
    for (; e; e >>= 1) {
        if (e & 1) ret *= base;
        base *= base;
    }
    return ret;
istream& operator >> (istream &in, Z &x) {
    in >> x.v;
    return in;
ostream& operator << (ostream &os, const Z &z) {
    return os << z.v;
}
i64 n, lim, val[N];
int id1[N], id2[N];
bool npr[N]; int pri[N], pcnt; Z pg0[N], pg1[N];
Z g0[N], g1[N];
void prep() {
    for (int i = 2; i < (int) N; ++i) {
```

```
if (!npr[i]) {
            pri[++pcnt] = i;
            pg0[pcnt] = pg0[pcnt - 1] + i;
            pg1[pcnt] = pg1[pcnt - 1] - 1;
        for (int j = 1, k; j \le pcnt && (k = i *
   pri[j]) < (int) N; ++j) {</pre>
            npr[k] = true;
            if (i % pri[j] == 0) break;
    }
int get_id(i64 x) {
    return x <= lim ? id1[x] : id2[n / x];</pre>
Z calc_f(int p, int c) {
    return p ^ c;
Z S(i64 n, int x) {
    if (n <= 1 || pri[x] > n) return 0;
    Z ret = g0[get_id(n)] + g1[get_id(n)];
    if (x == 1) ret += 2; // #6035 特殊 f(2) = 2 +
  1 = 3 != 1
    ret -= pg0[x - 1] + pg1[x - 1];
    for (int k = x; k \le pcnt; ++k) {
        i64 p1 = pri[k], p2 = p1 * pri[k];
        if (p2 > n) break;
        for (int e = 1; p2 <= n; p2 = (p1 = p2) *
\hookrightarrow pri[k], ++e) {
            ret += S(n / p1, k + 1) *
    calc_f(pri[k], e);
            ret += calc_f(pri[k], e + 1);
    }
    return ret;
}
int main() {
    n = read();
    lim = sqrt(n + .5);
    prep();
    int cnt = 0;
    for (i64 i = 1, j; i \le n; i = j + 1) {
        j = n / (t = val[++cnt] = n / i);
        (t <= lim ? id1[t] : id2[i]) = cnt;
        t %= MOD;
        g0[cnt] = (n - 1) \% MOD;
        g1[cnt] = t * (t - 1) / 2 % MOD;
    }
    for (int i = 1; i <= pcnt; ++i) {
        i64 bnd = (i64) pri[i] * pri[i];
        for (int j = 1, id; val[j] >= bnd; ++j) {
            id = get_id(val[j] / pri[i]);
            g0[j] = (g0[id] - pg0[i - 1]);
            g1[j] -= (g1[id] - pg1[i - 1]) *
→ pri[i];
        }
```

```
}
                                                                   mul[i] = ww[j].v;
    cout << 1 + S(n, 1) << ' \setminus n';
                                                              for (int i = 0; i < n; i += 1) {
    return 0;
                                                                   w = mul;
}
                                                                   for (int j = 0; j < m; ++j, ++x, ++y,
                                                         ++w) {
                                                                       xx = *x;
    随机数生成器
3
                                                                       yy = *y \% MOD * *w;
                                                                       *x = xx + yy;
                                                                       *y = xx - yy;

¬ rnd(chrono::steady_clock().now().time_since_epoch().count());

                                                                   x += m;
    数列
                                                                   y += m;
                                                              if (1 >> 15 & 1)
4.1 多项式板子
                                                                   for (int i = 0; i < n; ++i)
// SZ: size * 4
                                                                       a[i] %= MOD;
const size_t SZ = 1 << 19;</pre>
using Poly = vector<Z>;
                                                          for (int i = 0; i < n; ++i) {
using i64 = long long;
                                                              a[i] %= MOD;
                                                              if (flag) (a[i] *= inv[n].v) %= MOD;
template <typename InputZ, typename Output>
                                                              if (a[i] < 0) a[i] += MOD;
void sp_copy(InputZ begin, InputZ end, Output
                                                          }
→ output) {
    while (begin != end) *output++ = begin++->v;
                                                      void fft(Z a[], int lg, bool flag) {
                                                          static i64 ta[SZ];
int get_lg(int x) {
                                                          sp_copy(a, a + (1 << lg), ta);</pre>
    return 32 - __builtin_clz(x) - ((x & (-x)) ==
                                                          fft(ta, lg, flag);
                                                          copy(ta, ta + (1 << lg), a);
}
Z inv[SZ + 5], ww[SZ];
                                                      Poly operator += (Poly &f, const Poly &g) {
void prep() {
                                                          if (g.size() > f.size()) f.resize(g.size());
    static bool has_prep = false;
                                                          auto it = f.begin();
    if (has_prep) return;
                                                          auto jt = g.begin();
    inv[0] = inv[1] = 1;
                                                          while (jt != g.end()) *it++ += *jt++;
    for (unsigned i = 2; i \le SZ; ++i)
                                                          return f;
        inv[i] = MOD - MOD / i * inv[MOD % i];
    ww[0] = 1;
                                                      Poly operator + (const Poly &f, const Poly &g) {
    Z \text{ mul} = \text{qpow}(3, (MOD - 1) / SZ);
                                                          Poly ret = f; return ret += g;
    for (unsigned i = 1; i < SZ; ++i)
        ww[i] = ww[i - 1] * mul;
                                                      Poly operator -= (Poly &f, const Poly &g) {
   has_prep = true;
                                                          if (g.size() > f.size()) f.resize(g.size());
                                                          auto it = f.begin();
void fft(i64 a[], int lg, bool flag) {
                                                          auto jt = g.begin();
                                                          while (jt != g.end()) *it++ -= *jt++;
    int n = 1 \ll lg;
                                                          return f;
    if (flag) reverse(a + 1, a + n);
    static int rev[SZ], rev_lg = -1;
                                                      Poly operator - (const Poly &f, const Poly &g) {
    if (rev_lg != lg) {
                                                          Poly ret = f; return ret -= g;
        for (int i = 0; i < n; ++i)
            rev[i] = (rev[i >> 1] >> 1) | ((i & 1)
                                                      Poly operator * (const Poly &f, const Poly &g) {
   << lg >> 1);
                                                          u32 n = f.size() + g.size() - 1;
        rev_lg = lg;
                                                          if ((i64) f.size() * g.size() <= 2048) {</pre>
    }
                                                              static u64 ans[SZ];
    for (int i = 0; i < n; ++i)
                                                              memset(ans, 0, sizeof(u64) * n);
        if (rev[i] > i) swap(a[i], a[rev[i]]);
                                                              for (u32 i = 0; i < f.size(); ++i)
    for (int m = 1, 1 = 2; m < n; m <<= 1, 1 <<=
                                                                   for (u32 j = 0; j < g.size(); ++j)</pre>
   1) {
                                                                       if ((ans[i + j] += (u64) f[i].v *
        i64 *x = a, *y = a + m, xx, yy; int *w,
                                                       \rightarrow g[j].v) >> 62)
                                                                           ans[i + j] %= MOD;
        for (int i = 0, j = 0, step = SZ / 1; i <
                                                              Poly ret(n);
   m; ++i, j += step)
```

```
for (u32 i = 0; i < n; ++i) ret[i] =
                                                          Poly ret = tf * calc_inv(tg);
                                                          ret.resize(f.size() - g.size() + 1);
    ans[i] % MOD;
                                                           reverse(ret.begin(), ret.end());
        return ret;
    }
                                                           return ret;
    Poly ret(f.size() + g.size() - 1);
    static i64 a[SZ], b[SZ];
                                                      Poly& operator /= (Poly &f, const Poly &g) {
                                                           return f = f / g;
    int lg = get_lg(n);
    memset(a, 0, sizeof(i64) << lg);
                                                      Poly operator % (const Poly &f, const Poly &g) {
    memset(b, 0, sizeof(i64) << lg);</pre>
                                                           Poly ret = f - (f / g) * g;
    sp_copy(f.begin(), f.end(), a);
    sp_copy(g.begin(), g.end(), b);
                                                           ret.resize(g.size() - 1);
    fft(a, lg, 0);
                                                           return ret;
    fft(b, lg, 0);
                                                      Poly& operator %= (Poly &f, const Poly &g) {
    for (u32 i = 0, _ = 1 << lg; i < _; ++i)
        (a[i] *= b[i]) %= MOD;
                                                          return f = f % g;
    fft(a, lg, 1);
    copy(a, a + n, ret.begin());
                                                      Poly calc_der(const Poly &f) {
    return ret;
                                                           Poly ret(f.size() - 1);
                                                           for (u32 i = 1; i < f.size(); ++i) ret[i - 1]</pre>
Poly& operator *= (Poly &f, const Poly &g) {
                                                          = f[i] * i;
    return f = f * g;
                                                          return ret;
Poly& operator *= (Poly &f, const Z &x) {
                                                      Poly calc_pri(const Poly &f) {
    for (Z &c : f) c *= x;
                                                           prep();
                                                           Poly ret(f.size() + 1);
    return f;
                                                           for (u32 i = 1; i <= f.size(); ++i) ret[i] =
                                                          f[i - 1] * inv[i];
Poly operator * (const Poly &f, const Z &x) {
    Poly ret = f; return ret *= x;
                                                           return ret;
                                                      Poly calc_ln(const Poly &f) {
void calc_inv(Z arr[], Z brr[], int n) {
    if (n == 1) {
                                                           assert(f[0].v == 1);
        brr[0] = qpow(arr[0], MOD - 2);
                                                           Poly g = calc_der(f) * calc_inv(f);
                                                           g.resize(f.size() - 1);
        return;
    }
                                                           return calc_pri(g);
    calc_inv(arr, brr, n >> 1);
    int lg = get_lg(n \ll 1);
                                                      Poly calc_exp(int arr[], int n) {
    static Z ta[SZ], tb[SZ];
                                                           if (n == 1) {
                                                              assert(arr[0] == 0);
    memset(ta, 0, sizeof(Z) << lg);</pre>
    memset(tb, 0, sizeof(Z) << lg);</pre>
                                                               return Poly{1};
    copy(arr, arr + n
                          , ta);
    copy(brr, brr + (n >> 1), tb);
                                                          Poly f = calc_exp(arr, n >> 1);
                                                          Poly tf = f;
    fft(ta, lg, 0);
    fft(tb, lg, 0);
                                                           tf.resize(n);
    for (int i = 0, _ = 1 << lg; i < _; ++i)
                                                          Poly a = Poly(arr, arr + n);
        ta[i] = (2 - ta[i] * tb[i]) * tb[i];
                                                          Poly g = f * (Poly{1} - calc_ln(tf) + a);
    fft(ta, lg, 1);
                                                           g.resize(n);
    copy(ta, ta + n, brr);
                                                           return g;
Poly calc_inv(const Poly &f) {
                                                      Poly calc_exp(const Poly &f) {
    static Z a[SZ], b[SZ];
                                                           static int a[SZ];
    int lg = get_lg(f.size());
                                                           int lg = get_lg(f.size());
    memset(a, 0, sizeof(Z) << lg);</pre>
                                                          memset(a, 0, sizeof(int) << lg);</pre>
    copy(f.begin(), f.end(), a);
                                                          sp_copy(f.begin(), f.end(), a);
                                                          Poly ret = calc_exp(a, 1 << lg);</pre>
    calc_inv(a, b, 1 << lg);
    return Poly(b, b + f.size());
                                                          ret.resize(f.size());
                                                          return ret;
Poly operator / (const Poly &f, const Poly &g) {
    if (f.size() < g.size()) return Poly();</pre>
                                                      Poly operator ^ (const Poly &f, const int &e) {
    Poly tf = f; reverse(tf.begin(), tf.end());
                                                           u32 trail = 0;
    Poly tg = g; reverse(tg.begin(), tg.end());
                                                           for (u32 i = 0; i < f.size(); ++i)</pre>
    tg.resize(f.size() - g.size() + 1);
                                                               if (f[i].v) break; else ++trail;
```

```
if ((i64) trail * e >= f.size())
                                                              if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
        return Poly(f.size(), 0);
                                                          for (int m = 1, l = 2; m < n; m <<= 1, l <<=
    Z lst = f[trail], inv = qpow(lst, MOD - 2);
                                                         1) {
    Poly g;
                                                              static Complex ww[N];
    for (u32 i = trail; i < f.size(); ++i)</pre>
                                                              for (int i = 0, j = 0, step = N / 1; i < 0
        g.emplace_back(f[i] * inv);
                                                         m; ++i, j += step)
    Poly ret = calc_exp(calc_ln(g) * e) *
                                                                  ww[i] = w[j];
   qpow(lst, e);
                                                              Complex *xx = a, *yy = a + m, x, y;
    Poly t0 = Poly(trail * e, 0);
                                                              for (int i = 0, j; i < n; i += 1) {
    ret.insert(ret.begin(), t0.begin(), t0.end());
                                                                  for (j = 0; j < m; ++j, ++xx, ++yy) {
    ret.resize(f.size());
                                                                      x = *xx; y = *yy * ww[j];
    return ret;
                                                                      *xx = x + y;
                                                                      *yy = x - y;
Poly& operator ^= (Poly &f, const int &e) {
                                                                  }
    return f = f ^ e;
                                                                  xx += m;
                                                                  yy += m;
                                                              }
4.2 MTT
                                                     }
// N: size * 4
                                                     void mul(int a[], int b[], int c[], int n, int m)
// MOD
const size_t N = 1 \ll 18;
                                                          static Complex d[N], e[N], f[N], g[N];
const int MOD = 1E9 + 7;
                                                          int lg = 0;
struct Complex {
                                                          while ((1 << lg) < n + m) ++ lg;
    double a, b;
                                                          int tot = 1 \ll \lg;
    Complex() {}
                                                          for (int i = 0; i < n; ++i)
    Complex(double a, double b) : a(a), b(b) {}
                                                              d[i] = Complex(a[i] & 32767, a[i] >> 15);
    Complex operator + (const Complex &c) const {
                                                          for (int i = 0; i < m; ++i)
        return Complex(a + c.a, b + c.b);
                                                              e[i] = Complex(b[i] & 32767, b[i] >> 15);
                                                          fft(d, lg); fft(e, lg);
    Complex operator - (const Complex &c) const {
                                                          for (int i = 0; i < tot; ++i) {</pre>
        return Complex(a - c.a, b - c.b);
                                                              int j = i? tot -i : 0;
                                                              Complex da = (d[i] + d[j].conj()) *
    Complex operator * (const Complex &c) const {
                                                         Complex(.5, 0);
       return Complex(a * c.a - b * c.b, a * c.b
                                                              Complex db = (d[i] - d[j].conj()) *
   + b * c.a);
                                                         Complex(0, -.5);
                                                              Complex dc = (e[i] + e[j].conj()) *
    Complex conj() const {
                                                         Complex(.5, 0);
        return Complex(a, -b);
                                                              Complex dd = (e[i] - e[j].conj()) *
    }
                                                         Complex(0, -.5);
} w[N];
                                                              f[j] = da * dc + da * dd * Complex(0, 1);
void prep() {
                                                              g[j] = db * dc + db * dd * Complex(0, 1);
    const double PI = acos(-1);
    for (int i = 0; i <= N >> 1; ++i) {
                                                          fft(f, lg); fft(g, lg);
        double ang = 2 * i * PI / N;
                                                          for (int i = 0; i < n + m - 1; ++i) {
        w[i] = Complex(cos(ang), sin(ang));
                                                              i64 da = round(f[i].a / tot); da %= MOD;
    }
                                                              i64 db = round(f[i].b / tot); db \%= MOD;
}
                                                              i64 dc = round(g[i].a / tot); dc \%= MOD;
struct _ {
                                                              i64 dd = round(g[i].b / tot); dd %= MOD;
    _() { prep(); }
                                                              c[i] = (da + ((db + dc) << 15) + (dd <<
                                                         30)) % MOD;
void fft(Complex a[], int lg) {
                                                         }
    int n = 1 \ll lg;
                                                     }
    static int rev[N], rev_lg = -1;
    if (rev_lg != lg) {
                                                     4.3 FWT
        for (int i = 0; i < n; ++i)
            rev[i] = rev[i >> 1] >> 1 | ((i & 1)
                                                      // N: size * 2
   << lg >> 1);
                                                     const size_t N = 1 \ll 17;
                                                     void div2(Z &x) {
        rev_lg = lg;
                                                          if (x.v \& 1) x.v += MOD;
    for (int i = 0; i < n; ++i)
                                                          x.v >>= 1;
```

```
void _solve(Z a[], Z b[], i64 n, int m) {
}
void fwt and(Z a[], int n, bool rev) {
                                                           if (n < m - 1) {
    for (int m = 1, 1 = 2; m < n; m <<= 1, 1 <<=
                                                               b[n] = 1; return;
   1)
        for (int i = 0; i < n; i += 1)
                                                           static Z ta[N], tb[N];
            for (int j = 0; j < m; ++j)
                                                           if (n & 1) {
                                                               _{\text{solve}}(a, b, n - 1, m);
                if (rev) a[i + j] -= a[i + j + m];
                else a[i + j] += a[i + j + m];
                                                               ta[1] = 1;
                                                               mul(b, ta, tb, m, 2);
void fwt_or(Z a[], int n, bool rev) {
                                                               get_mod(tb, a, b, m + 1, m);
    for (int m = 1, 1 = 2; m < n; m <<= 1, 1 <<=
                                                           } else {
                                                               _{\text{solve}}(a, b, n >> 1, m);
        for (int i = 0; i < n; i += 1)
                                                               mul(b, b, tb, m, m);
            for (int j = 0; j < m; ++j)
                                                               get_mod(tb, a, b, (m << 1) - 1, m);
                if (rev) a[i + j + m] -= a[i + j];
                else a[i + j + m] += a[i + j];
}
                                                       Z solve(const Poly &init, const Poly &a, i64 n) {
void fwt_xor(Z a[], int n, bool rev) {
                                                           int m = a.size();
    for (int m = 1, 1 = 2; m < n; m <<= 1, 1 <<=
                                                           static Z ta[N], b[N];
                                                           for (int i = 0; i < m; ++i)
   1)
        for (int i = 0; i < n; i += 1)
                                                               ta[i] = 0 - a[m - 1 - i];
            for (int j = 0; j < m; ++j) {
                                                           ta[m] = 1;
                Z xx = a[i + j], yy = a[i + j +
                                                           _{\text{solve}}(\text{ta, b, n, m + 1});
   m];
                                                           Z ans = 0;
                a[i + j] = xx + yy;
                                                           for (int i = 0; i < m; ++i)
                a[i + j + m] = xx - yy;
                                                               ans += init[i] * b[i];
                if (rev) {
                                                           return ans;
                     div2(a[i + j]);
                     div2(a[i + j + m]);
                }
            }
                                                      namespace BM {
}
                                                      Poly& operator += (Poly &p, const Poly &q) {
                                                           if (q.size() > p.size()) p.resize(q.size());
                                                           for (size_t i = 0; i < q.size(); ++i)</pre>
4.4 BM
                                                               p[i] += q[i];
// N: size * 2
                                                           return p;
const size_t N = 1E4 + 5;
using Poly = vector<Z>;
                                                      Poly operator * (const Poly &p, Z x) {
namespace Rec {
                                                           Poly ret(p.size());
u64 tmp[N];
                                                           for (size_t i = 0; i < p.size(); ++i)</pre>
void mul(Z a[], Z b[], Z c[], int n, int m) {
                                                               ret[i] = p[i] * x;
    for (int i = 0; i < n; ++i)
                                                           return ret;
        for (int j = 0; j < m; ++j)
            if ((tmp[i + j] += (u64) a[i].v *
                                                      Poly solve(const Poly &a) {
  b[j].v) >> 62)
                                                           Poly P, R; int cnt = 1;
                tmp[i + j] \%= MOD;
                                                           for (size_t i = 0; i < a.size(); ++i) {</pre>
    for (int i = 0; i < n + m - 1; ++i) {
                                                               Poly tmp = P; tmp.insert(begin(tmp), MOD -
        c[i] = tmp[i] % MOD; tmp[i] = 0;
                                                          1);
                                                               Z delta = 0;
                                                               for (size_t j = 0; j < tmp.size(); ++j)
void get_mod(Z a[], Z b[], Z c[], int n, int m) {
                                                                   delta += tmp[j] * a[i - j];
    static Z tc[N];
                                                               if (delta.v) {
    copy(a, a + n, tc);
                                                                   vector<Z> t(cnt);
    Z iv = qpow(b[m - 1], MOD - 2);
                                                                   R.insert(begin(R), begin(t), end(t));
    for (int i = n; i-- >= m; ) {
                                                                   P += R * (MOD - delta);
        Z \text{ mul} = tc[i] * iv;
                                                                   R = tmp * qpow(delta, MOD - 2);
        for (int j = m, k = i; j--; --k)
                                                                   cnt = 0;
            tc[k] -= mul * b[j];
                                                               } else {
                                                                   ++cnt;
    copy(tc, tc + m - 1, c);
}
                                                           }
```

```
for (size_t i = P.size(); i < a.size(); ++i) {</pre>
                                                                     if (y == 1 && x != 1 && x != num - 1)
        Z cur = 0;
                                                                         return false;
        for (size_t j = 0; j < P.size(); ++j)</pre>
                                                                     x = y;
            cur += a[i - 1 - j] * P[j];
                                                                }
        assert(cur.v == a[i].v);
                                                                if (y != 1) return false;
    }
    return P;
                                                            return true;
}
                                                        }
}
int main() {
                                                        vector<i64> fac;
    vector<Z> p(read());
                                                        i64 gcd(i64 a, i64 b) {
    i64 m = read();
    generate(begin(p), end(p), read);
                                                            return b ? gcd(b, a % b) : a;
    Poly P = BM::solve(p);
    for (Z x : P) cout << x << ' ';</pre>
    cout << '\n';
                                                        void rho(i64 n) {
    cout << Rec::solve(p, P, m) << ' \setminus n';
                                                            if (isp(n)) {
    return 0;
                                                                fac.emplace_back(n);
}
                                                                return;
                                                            while (true) {
    数论
5
                                                                i64 \times 0 = Rand() \% n, \times 1 = \times 0, d = 1, c =
                                                           Rand() % n, cnt = 0;
5.1 判素数 (miller-rabin)
                                                                while (d == 1) {
                                                                     x0 = (mul_mod(x0, x0, n) + c) % n;
i64 Rand() {
                                                                     d = gcd(abs(x1 - x0), n);
    return (i64) rand() * rand() + rand();
                                                                     ++cnt;
};
                                                                     if (!(cnt & (cnt - 1))) x1 = x0; //
                                                            Floyd 倍增判环
i64 mul_mod(i64 a, i64 b, i64 mod) {
                                                                }
    i64 tmp = (long double) a * b / mod;
                                                                if (d < n) {
    i64 \text{ ret} = a * b - tmp * mod;
                                                                     rho(d); rho(n / d); return;
    while (ret >= mod) ret -= mod;
    while (ret < 0) ret += mod;</pre>
                                                            }
    return ret;
                                                        }
};
i64 pow_mod(i64 base, i64 e, i64 mod) {
                                                        5.2 二次剩余(Cipolla)
    i64 ret = 1;
                                                        欧拉判定:
    for (; e; e >>= 1) {
                                                                        x^{\frac{p-1}{2}} \equiv \left(\frac{x}{p}\right) \pmod{p}
        if (e & 1) ret = mul_mod(ret, base, mod);
        base = mul_mod(base, base, mod);
    }
                                                        // input mod
    return ret;
                                                        // method: cipolla(int n)
};
                                                        int mod;
                                                        namespace Cipolla {
const int pri[] {
                                                        int omega;
    2, 3, 5, 7, 11, 13, 17, 19, 23, 29
                                                        int sqr(int x) {
};
                                                            return (i64) x * x % mod;
bool isp(i64 num) {
                                                        struct Number {
    for (int x : pri) if (num == x) return true;
                                                            int x, y;
    i64 a = num - 1;
                                                            Number() {}
    int b = 0;
                                                            Number(int x, int y = 0) : x(x), y(y) {}
    while (!(a & 1)) {
                                                            Number operator * (const Number &n) const {
        a >>= 1; ++b;
                                                                Number ret;
                                                                ret.x = ((i64) x * n.x + (i64) y * n.y %
    for (int p : pri) {
                                                            mod * omega) % mod;
        i64 x = pow_mod(p, a, num), y = x;
                                                                ret.y = ((i64) x * n.y + (i64) y * n.x) %
        for (int i = 0; i < b; ++i) {
                                                            mod:
            y = mul_mod(x, x, num);
                                                                return ret;
```

```
}
                                                     Z g0[N], g1[N];
   Number& operator *= (const Number &n) {
        return *this = *this * n;
                                                     void prep() {
    }
                                                         for (int i = 2; i < (int) N; ++i) {
};
                                                             if (!npr[i]) {
Number npow(Number base, int e) {
                                                                  pri[++pcnt] = i;
   Number ret(1);
                                                                  pg0[pcnt] = pg0[pcnt - 1] - 1;
    for (; e; e >>= 1) {
                                                                  pg1[pcnt] = pg1[pcnt - 1] + i;
        if (e & 1) ret *= base;
        base *= base;
                                                             for (int j = 1, k; j <= pcnt && (k = i *
    }

→ pri[j]) < (int) N; ++j) {</pre>
                                                                  npr[k] = true;
   return ret;
                                                                  if (i % pri[j] == 0) break;
int get_num(int n) {
    while (true) {
                                                         }
        int x = rand();
                                                     }
        int tmp = (sqr(x) - n) \% mod;
        if (tmp < 0) tmp += mod;
                                                     int get_id(i64 x) {
        if (qpow(tmp, (mod - 1) / 2) == mod - 1) {
                                                         return x \le \lim ? id1[x] : id2[n / x];
            omega = tmp;
            return x;
        }
                                                     Z calc_f(int p, int c) {
   }
                                                         return p ^ c;
}
int cipolla(int n) {
    if (!n) return 0;
                                                     Z S(i64 n, int x) {
    if (qpow(n, (mod - 1) / 2) != 1) {
                                                         // 求 \sum f(1 ~ n 中最小质因子 >= pri[x])
        return -1;
                                                         if (n <= 1 || pri[x] > n) return 0;
                                                         Z ret = g0[get_id(n)] + g1[get_id(n)];
                                                         if (x == 1) ret += 2; // #6035 特殊 f(2) = 2 +
    int a = get_num(n);
   Number res = npow(Number(a, 1), (mod + 1) /
                                                      → 1 = 3 != 1
                                                         ret -= pg0[x - 1] + pg1[x - 1];
   assert(!res.y);
                                                         // 当前 ret 为 \sum f(1 ~ n 中 >= pri[x] 的质
   return res.x;
}
                                                         for (int k = x; k <= pcnt; ++k) {</pre>
}
                                                             i64 p1 = pri[k], p2 = p1 * pri[k];
                                                             if (p2 > n) break;
5.3 杜教筛
                                                             for (int e = 1; p2 \le n; p2 = (p1 = p2) *
                                                         pri[k], ++e) {
// prep_calc[N]: pre-calculated
                                                                  ret += S(n / p1, k + 1) *
map<i64, i64> mp;
                                                         calc_f(pri[k], e);
i64 calc(i64 n) {
                                                                  ret += calc_f(pri[k], e + 1);
    if (n < N) return pre_calc[n];</pre>
                                                             }
    if (mp.count(n)) return mp[n];
                                                         }
    i64 ret = 1LL * n * (n + 1) / 2; // 这里改成
                                                         return ret;
  (f * g) 的前缀和
                                                     }
    for (i64 l = 2, r; l \le n; l = r) {
        r = n / (n / 1) + 1;
                                                     int main() {
        ret -= (r - 1) * calc(n / 1); // 这里 r -
                                                         n = read();
   1 改成 g 在 [l, r] 的和
                                                         lim = sqrt(n + .5);
                                                         prep();
    return mp[n] = ret;
                                                         int cnt = 0;
}
                                                         for (i64 i = 1, j; i \leq n; i = j + 1) {
                                                              j = n / (t = val[++cnt] = n / i);
5.4 \quad \min_{25}
                                                              (t \le \lim ? id1[t] : id2[i]) = cnt;
const size_t N = 2E5 + 5; // 2 * sqrt(N)
                                                             t %= MOD;
                                                             g0[cnt] = 1 - Z(t);
i64 n, lim, val[N];
                                                             g1[cnt] = (t - 1) * (t + 2) / 2 % MOD;
int id1[N], id2[N];
bool npr[N]; int pri[N], pcnt; Z pg0[N], pg1[N];
```

```
for (int i = 1; i <= pcnt; ++i) {</pre>
                                                              assert(m == mat.n);
        // 筛掉最小质因子为 pri[i] 的数
                                                              Matrix ret(n, mat.m);
        i64 bnd = (i64) pri[i] * pri[i];
                                                              for (size_t i = 0; i < n; ++i)</pre>
        if (bnd > n) break;
                                                                  for (size_t j = 0; j < mat.m; ++j)</pre>
        for (int j = 1, id; val[j] >= bnd; ++j) {
                                                                      for (size_t k = 0; k < m; ++k)
                                                                          ret.a[i][j] += a[i][k] *
            id = get_id(val[j] / pri[i]);
            g0[j] = (g0[id] - pg0[i - 1]);
                                                         mat.a[k][j];
            g1[j] -= (g1[id] - pg1[i - 1]) *
                                                              return ret;
   pri[i];
                                                          }
                                                          Matrix& operator *= (const Z &x) {
    }
                                                              for (size_t i = 0; i < n; ++i) for (size_t</pre>
    // g[i] = \sum 1~val[i] 中质数
                                                          j = 0; j < m; ++j) a[i][j] *= x;
    cout << 1 + S(n, 1) << ' \setminus n';
                                                              return *this;
    return 0;
                                                          Matrix operator * (const Z &x) const {
}
                                                              Matrix ret = *this; return ret *= x;
    线性代数
6
                                                         Matrix& operator *= (const Matrix &mat) {
                                                         return *this = *this * mat; }
6.1 线性基
                                                          Matrix get_inv() const {
                                                              assert(n == m);
// N: size
                                                              Matrix m = *this, r(n, n); r.do_diag(1);
const size_t N = 50;
                                                              for (size_t i = 0; i < n; ++i) {
u64 base[N];
                                                                  int pivot = -1;
void add(u64 val) {
                                                                  for (size_t j = i; j < n; ++j) if
    for (int i = 49; ~i; --i) if (val >> i & 1)
                                                          (m.a[j][i].v && !~pivot) pivot = j;
        if (!base[i]) {
                                                                  assert(~pivot);
            for (int j = 0; j < i; ++j) if (val >>
                                                                  for (size_t j = i; j < n; ++j) {
   j & 1) val ^= base[j];
                                                                      swap(m.a[i][j], m.a[pivot][j]);
            base[i] = val;
                                                                      swap(r.a[i][j], r.a[pivot][j]);
            for (int j = i + 1; j < 50; ++j) if
                                                                  }
    (base[j] >> i & 1) base[j] ^= val;
                                                                  Z \text{ mul} = qpow(m.a[i][i], MOD - 2);
            break;
                                                                  for (size_t j = 0; j < n; ++j) { // 矩
        } else {
                                                          阵求逆时切勿从 i 开始枚举
            val ^= base[i];
                                                                      m.a[i][j] *= mul; r.a[i][j] *=
        }
                                                         mul:
}
                                                                  for (size_t j = 0; j < n; ++j) {
6.2 矩阵求逆
                                                                      if (j == i) continue;
                                                                      Z mul = m.a[j][i]; if (!mul.v)
struct Matrix {
                                                          continue;
    size_t n, m;
                                                                      for (size_t k = 0; k < n; ++k) {</pre>
    vector<vector<Z>> a;
                                                                          m.a[j][k] -= mul * m.a[i][k];
   Matrix() {}
                                                                          r.a[j][k] -= mul * r.a[i][k];
    Matrix(size_t n, size_t m) : n(n), m(m) {
        a = vector<vector<Z>>(n, vector<Z>(m));
                                                                      assert(!m.a[j][i].v);
    void do_diag(Z x) {
        for (size_t i = 0; i < n && i < m; ++i)
                                                              for (size_t i = 0; i < n; ++i) {
   a[i][i] = x;
                                                                  for (size_t j = 0; j < n; ++j)
                                                         assert(m.a[i][j].v == (i == j));
   Matrix& operator += (const Matrix &mat) {
        assert(n == mat.n && m == mat.m);
                                                              }
                                                              return r;
        for (size_t i = 0; i < n; ++i) for (size_t
                                                          }
    j = 0; j < m; ++j) a[i][j] += mat.a[i][j];</pre>
                                                     };
        return *this;
                                                      Matrix qpow(Matrix base, int e) {
   Matrix operator + (const Matrix &mat) const {
                                                          Matrix ret(2, 2); ret.do_diag(1);
        Matrix ret = *this; return ret += mat;
                                                          for (; e; e >>= 1) {
                                                              if (e & 1) ret *= base;
   Matrix operator * (const Matrix &mat) const {
```

```
void rotate(int x) {
        base *= base;
   }
                                                          int y = pa[x], z = pa[y], k = getd(x);
                                                          if (\neg getd(y)) ch[z][getd(y)] = x;
   return ret;
}
                                                          pa[x] = z; pa[y] = x;
                                                          ch[y][k] = ch[x][k^1];
ostream& operator << (ostream &os, const Matrix
                                                          ch[x][k ^1] = y;
if (ch[y][k]) pa[ch[y][k]] = y;
    for (size_t i = 0; i < mat.n; ++i) {</pre>
                                                          pushup(y);
        for (size_t j = 0; j < mat.m; ++j) os <<
   mat.a[i][j] << ' ';
                                                      void splay(int x) {
                                                          static int stk[N];
        os << ' \ n';
    }
                                                          int y = x, tp = 0;
                                                          stk[++tp] = y;
   return os;
                                                          while (\neg getd(y)) stk[++tp] = y = pa[y];
                                                          while (tp) pushdown(stk[tp--]);
                                                          while (~getd(x)) {
    数据结构
                                                              y = pa[x];
                                                              if (~getd(y))
     左偏树
                                                                  rotate(getd(x) ^ getd(y) ? x : y);
                                                              rotate(x);
// N
                                                          }
struct Node {
                                                          pushup(x);
    int lc, rc, val, dis;
   Node() {}
                                                      void access(int x) {
} t[N];
                                                          for (int y = 0; x; x = pa[y = x]) {
int arr[N], rt[N];
                                                              splay(x);
bool del[N];
                                                              val[x] += siz[ch[x][1]];
int merge(int x, int y) {
                                                              ch[x][1] = y;
    if (!x \mid | !y) return x \mid y;
                                                              val[x] -= siz[ch[x][1]];
    if (arr[y] < arr[x]) swap(x, y);
                                                              pushup(x);
    t[x].rc = merge(t[x].rc, y);
                                                          }
    if (t[t[x].lc].dis < t[t[x].rc].dis)
                                                      }
        swap(t[x].lc, t[x].rc);
                                                      void makeroot(int x) {
   t[x].dis = t[t[x].rc].dis + 1;
                                                          access(x);
   return x;
                                                          splay(x);
}
                                                          update(x);
7.2 LCT
                                                      void link(int x, int y) {
// N
                                                          makeroot(x);
                                                          access(y); splay(y);
const size_t N = 1E5 + 5;
                                                          pa[x] = y;
int pa[N], ch[N][2], siz[N], val[N];
                                                          val[y] += siz[x];
bool tag[N];
                                                          pushup(y);
void update(int x) {
    swap(ch[x][0], ch[x][1]);
                                                      i64 split(int x, int y) {
    tag[x] = 1;
                                                          makeroot(y);
}
                                                          access(x); splay(x);
void pushdown(int x) {
                                                          // x \rightarrow y is now a link from the root
    if (tag[x]) {
                                                          return (i64) (siz[x] - siz[y]) * siz[y];
        if (ch[x][0]) update(ch[x][0]);
                                                      }
        if (ch[x][1]) update(ch[x][1]);
        tag[x] = 0;
    }
                                                      7.3 KD-Tree
}
void pushup(int x) {
                                                      using P = pair<int, int>;
    siz[x] = siz[ch[x][0]] + val[x] +
                                                      #define fi first
   siz[ch[x][1]];
                                                      #define se second
}
                                                      const size_t N = 2E5 + 5;
int getd(int x) {
                                                      struct Node {
    return ch[pa[x]][0] == x ? 0 : ch[pa[x]][1] ==
                                                          int xl, yl, xm, ym, xr, yr;
   x ? 1 : -1;
                                                          int lc, rc, pa;
}
```

```
if (!x || t[x].xr < a || t[x].yr < b) return;</pre>
    i64 sum, val, tag;
    int cnt; bool exist;
                                                          if (t[x].xl \ge a \&\& t[x].yl \ge b) return
    Node() {}
                                                         update(x, val);
} t[N];
                                                          pushdown(x);
int tot;
                                                          if (t[x].xm >= a \&\& t[x].ym >= b) t[x].val +=
P point[N];
                                                          modify(t[x].lc, a, b, val);
map<P, int> mp;
int build(int 1, int r, bool d = 0, int pa = 0) {
                                                          modify(t[x].rc, a, b, val);
    if (1 > r) return 0;
                                                          pushup(x);
    int x = ++tot;
    t[x].pa = pa;
                                                      void doit(int x, int y, int d) {
    int mid = (1 + r) >> 1;
                                                          int u = mp[\{x, y\}];
    nth_element(point + 1, point + mid, point + r
                                                          link_pd(u);
                                                          i64 e = t[u].val * d;
   + 1,
                                                          t[u].exist ^= 1;
            [&](const P &p, const P &q) {
                                                          for (; u; u = t[u].pa) {
        P a = p, b = q;
        if (d) swap(a.fi, a.se), swap(b.fi, b.se);
                                                              t[u].cnt += d;
        return a < b;
                                                              t[u].sum += e;
                                                          }
    });
    mp[point[mid]] = x;
                                                          modify(1, x + 1, y + 1, d);
    t[x].xl = t[x].xm = t[x].xr = point[mid].fi;
    t[x].yl = t[x].ym = t[x].yr = point[mid].se;
                                                      void query(int x, int a, int b, i64 &sum, int
    if ((t[x].lc = build(l, mid - 1, d ^ 1, x))) {
                                                      int y = t[x].lc;
                                                          if (!x || t[x].xl > a || t[x].yl > b) return;
        chkmin(t[x].xl, t[y].xl); chkmax(t[x].xr,
                                                          if (t[x].xr <= a && t[x].yr <= b) {</pre>
   t[y].xr);
                                                              sum += t[x].sum;
        chkmin(t[x].yl, t[y].yl); chkmax(t[x].yr,
                                                              cnt += t[x].cnt;
   t[y].yr);
                                                              return;
    if ((t[x].rc = build(mid + 1, r, d^1, x))) {
                                                          pushdown(x);
        int y = t[x].rc;
                                                          if (t[x].xm \le a \&\& t[x].ym \le b \&\&
        chkmin(t[x].xl, t[y].xl); chkmax(t[x].xr,
                                                      \rightarrow t[x].exist) {
                                                              sum += t[x].val;
   t[y].xr);
        chkmin(t[x].yl, t[y].yl); chkmax(t[x].yr,
                                                              cnt += 1;
   t[y].yr);
                                                          query(t[x].lc, a, b, sum, cnt);
    return x;
                                                          query(t[x].rc, a, b, sum, cnt);
                                                      }
void pushup(int x) {
    t[x].sum = t[t[x].lc].sum + t[t[x].rc].sum;
                                                          图论
                                                      8
    if (t[x].exist) t[x].sum += t[x].val;
                                                      8.1
                                                          点双
void update(int x, i64 v) {
    t[x].sum += v * t[x].cnt;
                                                      void dfs1(int u, int p = 0) {
    t[x].val += v;
                                                          static int tme = 0, stk[N], tp;
    t[x].tag += v;
                                                          dfn[u] = low[u] = ++tme;
}
                                                          stk[++tp] = u;
void pushdown(int x) {
                                                          int child = 0;
    if (t[x].tag) {
                                                          for (int v: g[u]) {
        if (t[x].lc) update(t[x].lc, t[x].tag);
                                                              if (!dfn[v]) {
        if (t[x].rc) update(t[x].rc, t[x].tag);
                                                                  dfs1(v, u); ++child;
        t[x].tag = 0;
                                                                  low[u] = min(low[u], low[v]);
    }
                                                                  if (low[v] >= dfn[u]) {
}
                                                                      cut[u] = true;
void link_pd(int x) {
    static int stk[N];
                                                                      do bcc[cc].emplace_back(stk[tp]);
    int tp = 0;
                                                                      while (stk[tp--] != v);
    for (; x; x = t[x].pa) stk[++tp] = x;
                                                                      bcc[cc].emplace_back(u);
    while (tp) pushdown(stk[tp--]);
                                                                  }
                                                              } else
void modify(int x, int a, int b, int val) {
```

```
low[u] = min(low[u], dfn[v]);
                                                     }
    }
                                                     int rt;
    if (!child) {
                                                     int build() { rt = build(1); }
        cut[u] = true;
                                                     void pushup(x) {
        bcc[++cc].emplace_back(u);
                                                          sum[x] = val[x];
                                                          if (ch[x][0]) sum[x] = sum[ch[x][0]] + sum[x];
}
                                                          if (ch[x][1]) sum[x] = sum[x] + sum[ch[x][1]];
                                                     void modify(int x) {
8.2 全局平衡二叉树
                                                          int y;
vector<int> g[];
                                                          while ((x = pa[y = x])) {
int siz[], son[], lsiz[];
                                                              if (ch[x][0] != y && ch[x][1] != y)
int pa[], ch[][2];
                                                                  // del sum[y] \rightarrow val[x]
T val[], sum[];
                                                              pushup(y);
void dfs1(int u, int p = 0) {
                                                              if (ch[x][0] != y && ch[x][1] != y)
    siz[u] = 1;
                                                                  // add sum[y] \rightarrow val[x]
    for (int v : g[u]) {
                                                          }
        if (v == p) continue;
                                                         pushup(y);
        dfs1(v, u);
                                                     }
        siz[u] += siz[v];
        if (siz[v] > siz[son[u]]) son[u] = v;
                                                     8.3 MCS 求 PEO
                                                     // 一个图是弦图当且仅当它有 PEO
}
void dfs2(int u, int p = 0) {
                                                     // input: N
                                                     // n: number of vertices
    for (int v : g[u]) {
        if (v == p) continue;
                                                     // g: edges
        dfs2(v, u);
        if (v == son[u]) continue;
                                                     const size_t N = 1E4 + 5;
        lsiz[u] += siz[v];
        // val[v] -> val[u]
                                                     int n; vector<int> g[N];
    sum[u] = val[u];
                                                     int label[N], pos[N], peo[N];
}
                                                     vector<int> que[N];
int build(vector<int> &vc, int 1, int r) {
    if (1 > r) return 0;
                                                     int main() {
    int tot = 0;
                                                          for (int i = 1; i <= n; ++i) {
    for (int i = 1; i <= r; ++i) tot +=
                                                              que[0].emplace_back(i);

    lsiz[vc[i]];

    for (int i = 1, sum = 0; i <= r; ++i)
                                                          int j = 0;
        if ((sum += lsiz[vc[i]]) * 2 >= tot) {
                                                          for (int i = n; i >= 1; --i) {
            int x = vc[i];
                                                              int u;
            if ((ch[x][0] = build(vc, 1, i - 1)))
                                                              while (j \ge 0) {
                                                                  while (!que[j].empty()) {
   pa[ch[x][0]] = x;
            if ((ch[x][1] = build(vc, i + 1, r)))
                                                                      u = que[j].back();
    pa[ch[x][1]] = x;
                                                                      if (pos[u]) {
                                                                          que[j].pop_back();
            return x;
        }
                                                                      } else {
}
                                                                          break;
int build(int u) {
    static bool vis[N];
                                                                  if (!que[j].empty()) break;
    vector<int> stk;
                                                                  --j;
    for (int v = u; v; v = son[v]) {
        vis[v] = true;
                                                              assert(j >= 0);
        stk.emplace_back(v);
                                                              pos[u] = i; peo[i] = u;
    }
                                                              for (int v : g[u]) {
    int x = build(stk, 0, (int) stk.size() - 1);
                                                                  if (!pos[v]) {
    for (int v = u; v; v = son[v])
                                                                      ++label[v];
        for (int w : g[v])
                                                                      que[label[v]].emplace_back(v);
            if (!vis[w]) pa[build(w)] = v;
                                                                      if (label[v] > j) j = label[v];
    return x;
                                                                  }
```

```
字符串
        }
    }
                                                      9.1 后缀树组
                                                      // input: n, s
8.4 求欧拉回路
                                                      // output: sa, rnk, hei
                                                      // method: init(const string@); calc_sa();
// input: N, k, graph

    calc_hei();

// output: print_ans (an euler tour whose length
\rightarrow is \geq k)
                                                      struct GetSa {
                                                          int n;
                                                          string s;
int k;
                                                          vector<int> sa, rnk, hei;
bool vis[N];
                                                          GetSa() {}
vector<int> g[N];
                                                          void init(const string &_s) {
vector<int> ans1, ans2;
                                                              s = _s; n = _s.size();
void print_ans(const vector<int> &vc) {
                                                          }
    for (int x : vc) cout << x << ' ';</pre>
                                                          void calc_sa() {
    exit(0);
                                                              sa.resize(n);
}
                                                              rnk.resize(n);
void dfs(int u) {
                                                              vector<int> x(n), y(n);
    vis[u] = true;
                                                              for (int i = 0; i < n; ++i) x[i] = s[i];
    if (ans1.size() >= k) print_ans(ans1);
                                                              int tot = *max_element(ALL(x)) + 1;
    for (int v : g[u]) {
                                                              vector<int> cnt(tot);
        if (vis[v]) continue;
                                                              for (int i = 0; i < n; ++i) ++cnt[x[i]];</pre>
        ans1.emplace_back(u);
                                                              partial_sum(ALL(cnt), begin(cnt));
        dfs(v);
                                                              for (int i = 0; i < n; ++i)
        ans1.pop_back(); ans2.emplace_back(u);
                                                                  sa[--cnt[x[i]]] = i;
        if (ans2.size() >= k) {
                                                              for (int 1 = 1; ; 1 <<= 1) {
            reverse(begin(ans2), end(ans2));
                                                                  vector<int> cnt(tot);
            print_ans(ans2);
        }
                                                                   int p = n;
                                                                   for (int i = n - 1; i < n; ++i) y[--p]
    }
}
                                                          = i;
                                                                   for (int i = 0; i < n; ++i)
                                                                       if (sa[i] >= 1) y[--p] = sa[i] -
8.5 SPFA
                                                         1;
                                                                   for (int i = 0; i < n; ++i)
// input: N, n - number of vertices
// output: dis - distance, return - no negative
                                                       \rightarrow ++cnt[x[y[i]]];
→ loops
                                                                  partial_sum(ALL(cnt), begin(cnt));
                                                                   for (int i = 0; i < n; ++i)
int dis[N], cnt[N];
                                                                      sa[--cnt[x[y[i]]]] = y[i];
bool inque[N];
bool spfa(int n) {
                                                                   y[sa[0]] = 0;
    memset(dis, 0x3f, sizeof dis);
                                                                   for (int i = 1; i < n; ++i)
    queue<int> que;
                                                                      y[sa[i]] = y[sa[i-1]] +
                                                                           (x[sa[i-1]] < x[sa[i]] | |
    que.emplace(0);
    dis[0] = 0; inque[0] = true; cnt[0] = 1;
                                                      \rightarrow (sa[i]+l < n && (sa[i-1]+l >= n ||
                                                      \rightarrow x[sa[i-1]+1] < x[sa[i]+1]));
    while (!que.empty()) {
        int u = que.front(); que.pop();
                                                                  tot = y[sa.back()] + 1;
        inque[u] = false;
                                                                   x.swap(y);
        for (auto [v, w] : g[u]) {
                                                                   if (tot == n) break;
            if (chkmin(dis[v], dis[u] + w) &&
                                                              copy(ALL(x), begin(rnk));
   !inque[v]) {
                que.emplace(v);
                inque[v] = true;
                                                          void calc_hei() {
                if (++cnt[v] > n) return false;
                                                              hei.resize(n);
                                                              for (int i = 0, j = 0; i < n; ++i) {
        }
                                                                  if (!rnk[i]) continue;
                                                                   int ii = sa[rnk[i]-1];
                                                                   if (j) --j;
    return true;
                                                                  while (ii+j < n && i+j < n && s[ii+j]
}
                                                         == s[i+j]) ++j;
```

hei[rnk[i]] = j;

}

9.3 Manacher

```
}
                                                      void manacher(int n, char s[], int f[]) {
};
                                                          int id = 0, r = 0;
                                                          for (int i = 1; i < n; ++i) {
9.2 后缀自动机
                                                              f[i] = r > i ? min(f[2 * id - i], r - i) :
// N: length of string
                                                              while (f[i] \le i \&\& i + f[i] \le n \&\& s[i +
// AL: alphabet size
                                                          f[i]] == s[i - f[i]])
// method: add(), build()
                                                                  ++f[i];
namespace Sam {
                                                              if (i + f[i] > r) \{ id = i; r = i + f[i];
const size_t V = N << 1;</pre>
                                                          }
const size t AL = 26;
                                                          }
int ch[V][AL], par[V], len[V], pos[V], tot = 1,
\rightarrow lst = 1, s[N];
bool ed[V];
                                                      9.4 回文自动机
void add(int po, int c) {
    int p = lst, np = ++tot;
                                                      // N: length of string
    s[po] = c;
                                                      // method: prep, add
    len[np] = len[lst] + 1;
                                                      namespace PAM {
    pos[np] = po;
                                                      const size_t AL = 26;
    ed[np] = true;
                                                      int n, s[N];
    for (; p && !ch[p][c]; p = par[p])
                                                      int tot, lst, ch[N][AL], par[N], len[N], dep[N];
        ch[p][c] = np;
                                                      void prep() {
    if (p) {
                                                          par[0] = par[1] = 1;
        int q = ch[p][c];
                                                          s[0] = len[1] = -1;
        if (len[p] + 1 == len[q]) {
                                                          lst = tot = 1;
            par[np] = q;
                                                      }
        } else {
                                                      int get_link(int x) {
            int nq = ++tot;
                                                          for (; s[n] != s[n - len[x] - 1]; x = par[x])
            len[nq] = len[p] + 1;
            par[nq] = par[q];
                                                          return x;
            pos[nq] = pos[q];
            memcpy(ch[nq], ch[q], sizeof ch[q]);
                                                      int add(int c) {
            for (; p && ch[p][c] == q; p = par[p])
                                                          s[++n] = c;
                ch[p][c] = nq;
                                                          int p = get_link(lst);
            par[q] = par[np] = nq;
                                                          if (!ch[p][c]) {
        }
                                                              int np = ++tot;
    } else {
                                                              len[np] = len[p] + 2;
        par[np] = 1;
                                                              par[np] = ch[get_link(par[p])][c];
    }
                                                              dep[np] = dep[par[np]] + 1;
    lst = np;
                                                              ch[p][c] = np;
}
int fch[V][AL], cnt;
                                                          return dep[lst = ch[p][c]];
void dfs(int u = 1) {
                                                      }
    if (!u) return;
                                                      }
    if (ed[u]) {
        ++cnt;
                                                          Lyndon 分解
                                                      9.5
        sa[cnt] = pos[u];
        rnk[pos[u]] = cnt;
                                                      // input: n, s[]
                                                      void lyndon() {
    for (int v : fch[u]) dfs(v);
                                                          for (int i = 0; i < n; ) {
}
                                                              int j = i, k = i + 1;
void build() {
                                                              for (; k < n \&\& s[j] \le s[k]; ++k)
    for (int i = 2; i <= tot; ++i)</pre>
                                                                   j = s[j] < s[k] ? i : j + 1;
        fch[par[i]][s[pos[i] + len[par[i]]]] = i;
                                                              while (i \leq j) i += k - j; // right pos
    dfs();
                                                          }
}
                                                          return 0;
                                                      }
```

```
9.6 Z Function
                                                              return ret;
                                                          }
void z_func(string s, int f[]) {
                                                     } flow;
    int 1 = 0, r = 0;
    for (int i = 1; i < (int) s.size(); ++i) {</pre>
                                                      10.2 网络流 (HLPP)
        f[i] = i < r ? min(r - i, f[i - 1]) : 0;
        while (i + f[i] < (int) s.size() &&
                                                      // N: vertices, M: edges
            s[f[i]] == s[i + f[i]]) ++f[i];
                                                      // method: add_edge(int u, int v, i64 cap),
        if (i + f[i] > r) r = (l = i) + f[i];
                                                      \rightarrow maxflow(int s, int t)
   }
                                                      struct Maxflow {
}
                                                          int n;
                                                          struct Edge {
                                                              int to; i64 cap; int nxt;
      其他
10
                                                              Edge() {}
                                                              Edge(int to, i64 cap, int nxt) : to(to),
10.1 网络流 (ISAP)
                                                         cap(cap), nxt(nxt) {}
// N: vertices, M: edges
                                                          } e[M << 1];
// method: add_edge(int u, int v, int cap),
                                                          int tot_e, head[N], cur[N], deg[N];
\rightarrow maxflow(int s, int t)
                                                          Maxflow() {
struct Maxflow {
                                                              memset(this, 0, sizeof *this);
   struct Edge {
                                                              tot_e = 1;
        int to, cap, nxt;
        Edge(int to = 0, int cap = 0, int nxt =
                                                          void add_edge(int u, int v, i64 cap) {
  0):
                                                              e[++tot_e] = {v, cap, head[u]}; head[u] =
            to(to), cap(cap), nxt(nxt) {}
                                                         tot_e;
    } e[M];
                                                              e[++tot_e] = \{u, 0, head[v]\}; head[v] =
    int head[N], cur[N], d[N], f[N], tot = 1;
                                                          tot_e;
    int n, s, t;
                                                              ++deg[u]; ++deg[v];
    void add_edge(int u, int v, int cap) {
                                                          }
        e[++tot] = Edge(v, cap, head[u]); head[u]
                                                          int cnt_upd_h, max_h, h[N], cnt[N]; i64
                                                         rest[N];
        e[++tot] = Edge(u, 0, head[v]); head[v]
                                                          vector<int> vc1[N], vc2[N];
                                                          void update_h(int v, int nh) {
   = tot;
   }
                                                              ++cnt upd h;
    int dfs(int v, int fl = INF) {
                                                              if (h[v] < INF) --cnt[h[v]];</pre>
        if (v == t) return fl;
                                                              h[v] = nh;
        int ret = 0;
                                                              if (h[v] == INF) return;
        for (int &i = cur[v]; i; i = e[i].nxt) {
                                                              ++cnt[h[v]];
            if (e[i].cap && d[e[i].to] + 1 ==
                                                              \max_h = h[v];
   d[v]) {
                                                              vc1[h[v]].emplace_back(v);
                int tmp = dfs(e[i].to, min(fl,
                                                              if (rest[v]) vc2[h[v]].emplace_back(v);
→ e[i].cap));
                                                          }
                ret += tmp; fl -= tmp;
                                                          void relabel(int t) {
                e[i].cap -= tmp;
                                                              cnt_upd_h = max_h = 0;
                e[i ^ 1].cap += tmp;
                                                              fill(h, h + n + 1, INF);
                if (!fl) return ret;
                                                              fill(cnt, cnt + n + 1, 0);
            }
                                                              for (int i = 0; i <= max_h; ++i) {</pre>
                                                                  vc1[i].clear();
        cur[v] = head[v];
                                                                  vc2[i].clear();
        if (!(--f[d[v]])) d[s] = n;
                                                              }
        ++f[++d[v]];
                                                              queue<int> que;
        return ret;
                                                              que.emplace(t);
    }
                                                              update_h(t, 0);
    int maxflow(int _s, int _t) {
                                                              while (!que.empty()) {
        n = _n; s = _s; t = _t;
                                                                  int u = que.front(); que.pop();
        memset(cur, 0, sizeof cur);
                                                                  for (int i = head[u]; i; i = e[i].nxt)
        memset(d, 0, sizeof d);
                                                      ← {
        memset(f, 0, sizeof f);
                                                                      int v = e[i].to;
        f[0] = n;
                                                                      if (h[u] + 1 < h[v] && e[i ^
        int ret = 0;
                                                          1].cap) {
```

 $update_h(v, h[u] + 1);$ 

while (d[s] < n) ret += dfs(s);

```
que.emplace(v);
                                                           const double EPS = 1e-14;
                                                           double curx = ansx, cury = ansy;
                }
            }
                                                           for (double temp = INIT_TEMP; temp > EPS; temp
        }
                                                           *= DELTA) {
    }
                                                               double xx = curx + ((rand() << 1) -</pre>
    void push(int i) {
                                                           RAND_MAX) * temp;
        int u = e[i ^1].to, v = e[i].to;
                                                               double yy = cury + ((rand() << 1) -</pre>
        i64 w = min((i64) rest[u], e[i].cap);
                                                           RAND_MAX) * temp;
        if (!w) return;
                                                               double cure = calcEnergy(xx, yy);
        if (!rest[v]) vc2[h[v]].emplace_back(v);
                                                               double diff = cure - anse;
        e[i].cap -= w; e[i ^ 1].cap += w;
                                                               if (diff < 0) {</pre>
        rest[u] -= w; rest[v] += w;
                                                                   ansx = curx = xx;
                                                                   ansy = cury = yy;
    void push_flow(int u) {
                                                                   anse = cure;
        int nh = INF;
                                                               } else if (exp(-diff / temp) * RAND_MAX >
        for (int &i = cur[u], j = 0; j < deg[u]; i</pre>
                                                       \rightarrow rand()) {
    = e[i].nxt, ++j) {
                                                                   curx = xx;
            if (!i) i = head[u];
                                                                   cury = yy;
            int v = e[i].to;
                                                               }
            if (e[i].cap) {
                                                           }
                if (h[u] == h[v] + 1) {
                                                       }
                    push(i);
                     if (!rest[u]) return;
                } else if (nh > h[v] + 1) {
                    nh = h[v] + 1;
                }
            }
        }
        if (cnt[h[u]] > 1) {
            update_h(u, nh);
        } else {
            for (int i = h[u]; i <= max_h; ++i) {</pre>
                for (int v : vc1[i]) update_h(v,
   INF);
                vc1[i].clear();
            }
        }
    }
    int maxflow(int s, int t, int lim = 10000) {
        rest[s] = 1E18;
        relabel(t);
        for (int i = head[s]; i; i = e[i].nxt)
   push(i);
        for (int &i = max_h; ~i; --i) {
            while (!vc2[i].empty()) {
                int u = vc2[i].back();
                vc2[i].pop_back();
                if (h[u] != i) continue;
                push_flow(u);
                if (cnt_upd_h > lim) relabel(t);
            }
        return rest[t];
    }
} flow;
10.3 模拟退火
void simulateAnneal() {
    const double INIT_TEMP = 2e5;
    const double DELTA = 0.997;
```