# Robotic Systems I: Homework II

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### Introduction

The homework concerns controlling a manipulator's end-effector to follow a path in 3D space. In particular, the homework is split in three parts: 1) modeling and simulation: we need to load the URDF of a Franka Panda manipulator (given as franka.urdf) and create a simulation loop using the pinocchio library, 2) task-space controller: we need to develop a task-space controller that controls the orientation and translation indepedently, and 3) evaluation: we need to evaluate the developed controller and simulator.

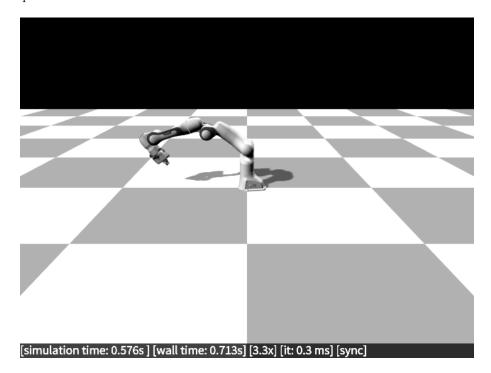


Figure 1: Visualization of the Franka manipulator

# 1 Modeling and Simulation (25%)

In this homework, we are going to use a Franka Panda manipulator (Fig. 1). The robot is a 7 degrees of freedom manipulator equipped with a gripper. In this homework, we have disabled the gripper.

In this part, you are asked to:

- 1. Write a function in Python called load\_franka() that loads the URDF file of Franka (franka.urdf) and returns the model read by pinocchio.
- 2. Write a function in Python called step\_world() that accepts the current state of the robot  $(\boldsymbol{q} \in \mathbb{R}^{7\times 1}, \boldsymbol{v} \in \mathbb{R}^{7\times 1})_k$ , the control inputs (torques)  $\boldsymbol{\tau} \in \mathbb{R}^{7\times 1}$ , a timestep  $dt \in \mathbb{R}$  and outputs

the new state of the world  $(\boldsymbol{q} \in \mathbb{R}^{7\times 1}, \boldsymbol{v} \in \mathbb{R}^{7\times 1})_{k+1}$  after applying the control inputs  $\boldsymbol{\tau}$  to the system state. You need to make sure that the robot always stays inside the joint limits (in position and velocity). You need to use the integrate() function from the pinocchio library.

3. Visualize the system using a visualization library (you can use the provided MeshCat visualization scheme; meshcat.ipynb)

For all the above, you are allowed to use only native Python functions/classes, the pinocchio library, the numpy library and some visualization library (e.g. matplotlib or MeshCat).

## 2 Task-Space Controller (50%)

In this part, we want to create a task-space controller for torque control. In essence, we assume access to a desired end-effector pose profile  $T_{wd}(t) \in \mathbb{R}^{6\times 1}$ , and we want to create an end-effector wrench signal. For example, we can create a signal using a PID controller (in the world frame):

$$\mathcal{F}_w(t) = K_p \mathcal{X}_e(t) + K_i \int_0^t \mathcal{X}_e(t) dt + K_d \dot{\mathcal{X}}_e(t), K_p, K_i, K_d > 0$$
(1)

where 
$$\mathcal{X}_e(t) = \begin{bmatrix} \log(\mathbf{R}_{wd}(t)\mathbf{R}_{wb}(t)^T) \\ \mathbf{t}_{wd}(t) - \mathbf{t}_{wb}(t) \end{bmatrix}$$
,  $\mathbf{T} = \begin{bmatrix} \mathbf{R} & \mathbf{t} \\ \mathbf{0} & 1 \end{bmatrix}$ , and  $\mathbf{T}_{wb}(t)$  is the current end-effector pose. We then need to transform this *wrench* signal  $\mathcal{F}_w(t)$  to joint torques  $\boldsymbol{\tau}$ . For this, you are free to

We then need to transform this wrench signal  $\mathcal{F}_w(t)$  to joint torques  $\boldsymbol{\tau}$ . For this, you are free to use any method: the easiest one is  $\boldsymbol{\tau} = \boldsymbol{J}_w(\boldsymbol{q})\mathcal{F}_w$ , where  $\boldsymbol{J}_w(\boldsymbol{q})$  is the Jacobian of the end-effector expressed in the world frame.

#### **Instructions:**

- 1. You need to use the panda\_ee frame as the end-effector
- 2. You are free to generate/compute the desired end-effector wrench signal,  $\mathcal{F}(t)$ , in any way that you wish
- 3. You can transform the end-effector signal to joint torques in any way that you wish
- 4. The task-space controller needs to compute the orientation and translation errors indepedently
- 5. You need to add a regularization task with a null-space controller
- 6. You need to justify and describe all of your choices

For all the above, you are allowed to use only native Python functions/classes, the pinocchio library, the numpy library and some visualization library (e.g. matplotlib or MeshCat).

# 3 Evaluation (25%)

In this part, we will test the developed simulator and controller. In essence, you need to create several end-effector pose profiles and use the task-space controller to follow them in the simulator that you developed in the first part.

### **Instructions:**

- 1. Use dt = 0.001 for the simulation
- 2. You need to use the panda\_ee frame as the end-effector
- 3. You are free to calculate the desired end-effector pose profile  $T_{wd}(t)$  in any way that you wish. You need to create at least four different profiles
- 4. Discuss and visualize the results
- 5. You need to justify and describe all of your choices

For all the above, you are allowed to use only native Python functions/classes, the pinocchio library, the numpy library and some visualization library (e.g. matplotlib or MeshCat).

## 4 Deliverables

- Python file(s) with commented code<sup>1</sup>
- A short report

### **Bonus Points**

- $\bullet$  There is a 10% bonus if you implement the task-space controller that includes the task space inertia
- $\bullet$  There is a 10% bonus if you implement your controller with a QP-based optimization scheme

 $<sup>^1\</sup>mathrm{Jupyter}$  notebooks are accepted as well.