Understanding model terms and coefficients

Author: Nicholas G Reich

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Today's topics

- Model terms: recap and a visual tour
- Smooth terms
- Fitting and interpreting models

Model terms: recap

- **The intercept** is a "baseline" that is included in nearly every model. What would your guess of disease severity be in the absence of any other information?
- Main terms model the effect of explanatory variables directly.
- Interaction terms allow for different explanatory variables to modulate the relationship of each other to the response variable.
- **Smooth terms** allow for the modeled relationships to be flexibly curved, not just linear.

Formulas for Statistical Models (Linear Regression)

In general, linear models can be thought of as having these components

$$y = intercept + terms + error$$

With a single predictor variable, this is simply a line (plus error):

$$y_i = \beta_0 + \beta_1 \cdot x_i + \epsilon_i$$

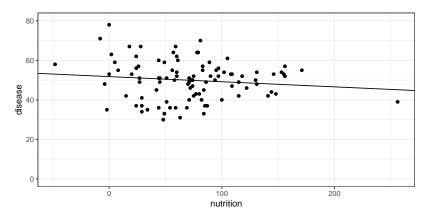
However, there can be multiple variables and different types of "terms" in this equation

- intercept
- main effects
- interaction terms
- smooth terms

Main effects model terms

equation: $\widehat{disease}_i = \beta_0 + \beta_1 \cdot nutrition_i$

```
m1 <- lm(disease ~ nutrition, data=dat)
ggplot(dat, aes(x=nutrition, y=disease)) +
  geom_point() + ylim(c(0,80)) +
  geom_abline(intercept = coef(m1)[1], slope = coef(m1)[2])</pre>
```



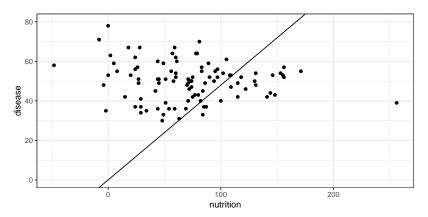
Back to HS algebra: what is an intercept?

$$y = \beta_1 \cdot x$$
 vs. $y = \beta_0 + \beta_1 \cdot x$

Main effects w/no intercept

equation: $\widehat{disease}_i = \beta_1 \cdot nutrition_i$

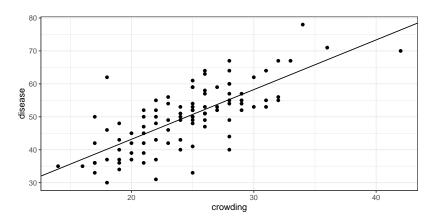
```
m1_no_intcpt <- lm(disease ~ nutrition - 1, data=dat)
ggplot(dat, aes(x=nutrition, y=disease)) +
  geom_point() + ylim(c(0,80)) +
  geom_abline(intercept = 0, slope = coef(m1_no_intcpt)[1])</pre>
```



Main effects model terms (crowding)

equation: $\widehat{disease}_i = \beta_0 + \beta_1 \cdot crowding_i$

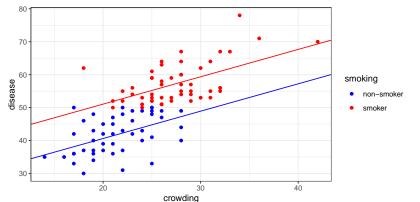
```
m1 <- lm(disease ~ crowding, data=dat)
ggplot(dat, aes(x=crowding, y=disease)) + geom_point() +
  geom_abline(intercept = coef(m1)[1], slope = coef(m1)[2])</pre>
```



2 main effects: 1 continous, 1 categorical

equation: $\widehat{disease}_i = \beta_0 + \beta_1 \cdot crowding_i + \beta_2 \cdot smoker$

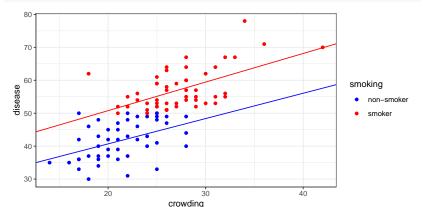
```
m2 <- lm(disease ~ crowding + smoking, data=dat)
ggplot(dat, aes(x=crowding, y=disease, color=smoking)) + geom_point() +
scale_color_manual(values = c("blue", "red")) +
geom_abline(intercept = coef(m2)[1], slope = coef(m2)[2], color="blue") +
geom_abline(intercept = coef(m2)[1]+coef(m2)[3], slope = coef(m2)[2], color="blue")</pre>
```



Interaction model terms

equation: $\widehat{disease}_i = \beta_0 + \beta_1 \cdot crowd_i + \beta_2 \cdot smoke_i + \beta_3 \cdot crowd_i \cdot smoke_i$

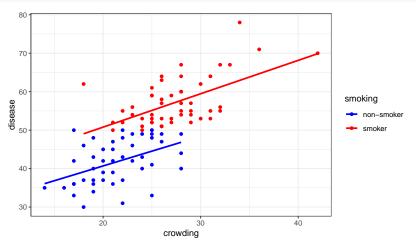
```
m3 <- coef(lm(disease ~ crowding*smoking, data=dat))
ggplot(dat, aes(x=crowding, y=disease, color=smoking)) + geom_point() +
scale_color_manual(values = c("blue", "red")) +
geom_abline(intercept = m3[1], slope = m3[2], color="blue") +
geom_abline(intercept = m3[1]+m3[3], slope = m3[2]+m3[4], color="red")
```



Interaction via geom_smooth()

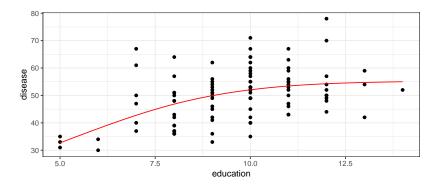
equation: $\widehat{disease}_i = \beta_0 + \beta_1 \cdot crowd_i + \beta_2 \cdot smoke_i + \beta_3 \cdot crowd_i \cdot smoke_i$

ggplot(dat, aes(x=crowding, y=disease, color=smoking)) + geom_point() +
geom_smooth(method="lm", se=FALSE) + scale_color_manual(values = c("blue", "r



Smooth model terms

equation: $\widehat{disease} = \beta_0 + s(education)$



Fitting models in R

Quick recap of key syntax for linear models

- For linear models, use lm().
- Equations look like y x1 + x2.
- Plus signs (+) indicate main effect terms.
- Multiplication signs (*) indicate main effect AND interaction terms.

Reading model output

$$\text{equation:} \ \ \widehat{\textit{disease}}_i = \beta_0 + \beta_1 \cdot \textit{crowd}_i + \beta_2 \cdot \textit{smoke}_i + \beta_3 \cdot \textit{crowd}_i \cdot \textit{smoke}_i$$

```
m3 <- lm(disease ~ crowding*smoking, data=dat)
round(summary(m3)$coef, 2)
##
                      Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                         25.31 4.90
                                          5.17
                                                  0.00
## crowding
                         0.77
                                  0.23 3.39 0.00
  smokingsmoker
                         8.11 6.93 1.17 0.24
## crowding:smokingsmoker
                         0.10
                                   0.29 0.34
                                                 0.73
```

