

# STATS 250 Lab 07

## Simulation-Based Hypothesis Testing

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Week of 10/12/2020

# Reminders



Your tasks for the week running Friday 10/9 - Friday 10/16:

Task	Due Date	Submission
<b>MIDTERM EXAM</b>	Thursday 10/15, any 2-hr window	<b>GRADESCOPE</b>
Lab 7	Sunday 10/18 11:59PM ET	Canvas

Modified office hours schedule this week due to midterm

# Homework 5 Comments

We'll address many of these in the next few slides, but:

1. Hypotheses are about *parameters* and involve specific *numeric values*.
2. The *p-value* is different from  $p$  (population proportion) is different from  $\hat{p}$  (sample proportion).
3. Be specific when you talk about "extreme" values (also note these are not outliers)

# Learning Objectives

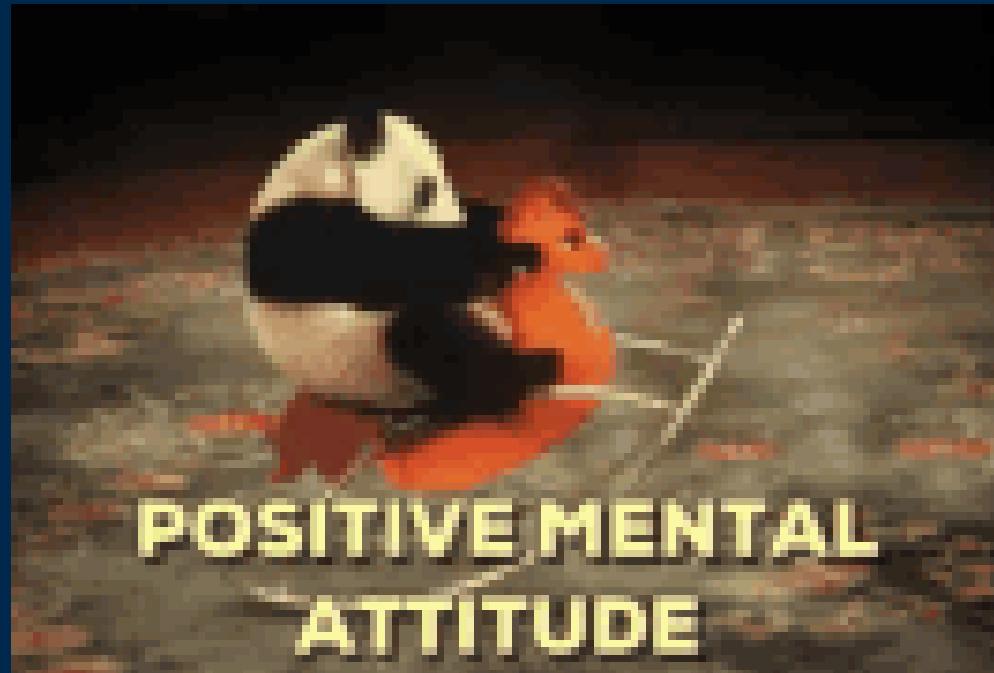
## Statistical Learning Objectives

1. Get experience with randomization under an independence model
2. Explore hypothesis testing and p-values

## R Learning Objectives

1. Learn how to perform simulations under an independence model

# Weekly Advice



"Negative self-talk will only limit you."

# Setup

Follow along! Page 66 of *ISRS*; slides on Canvas or <https://nickseewald.com/250fa20-slides/>

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How rational and consistent is the behavior of the typical American college student? Let's explore whether college student consumers always consider an obvious fact: money not spent now can be spent later.

# Setup

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How rational and consistent is the behavior of the typical American college student? Let's explore whether college student consumers always consider an obvious fact: money not spent now can be spent later.

**QUESTION:** Does reminding students about this fact cause them to be thriftier?



# Study

150 students recruited, each given the following statement:

Imagine that you have been saving some extra money on the side to make some purchases, and on your most recent visit to the video store you come across a special sale on a new video. This video is one with your favorite actor or actress, and is of your favorite genre. This particular video that you are considering is one you have been thinking about buying for a long time. It is available for a special sale price of \$14.99. What would you do in this situation?

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(lol remember buying movies?)

# Study

150 students split into two groups and given two options:

## Control

- (A) Buy this entertaining video
- (B) Not buy this entertaining video

## Treatment

- (A) Buy this entertaining video
- (B) Not buy this entertaining video.  
Keep the \$14.99 for other purchases.

*Notice the reminder in the treatment group!*

# Hypothesis Statements



Two perspectives:

1. **Skeptic:** The reminder isn't going to work
2. **Believer:** The reminder will work: students in the treatment group will not buy the DVD more often than students in the control.

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**Poll: What are the null and alternative hypotheses?**

# Hypothesis Statements



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1. **Skeptic:** The reminder isn't going to work
2. **Believer:** The reminder will work: students in the treatment group will not buy the DVD more often than students in the control.

## Poll: What are the null and alternative hypotheses?

- $H_0 : p_{\text{treatment}} = p_{\text{control}}$
- $H_A : p_{\text{treatment}} > p_{\text{control}}$

where  $p_{\text{group}}$  is the proportion of students who *do NOT buy* the DVD in that group.

# Study Data (line ~68)

Read in the data from the study stored in `dvd.csv`. How do we do this?

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```

Let's see what the data look like

```
head(dvd)
```

```
group decision
1 control buy DVD
2 control buy DVD
3 control buy DVD
4 control buy DVD
5 control buy DVD
6 control buy DVD
```

# Tabulating the Data

Let's make a two-way frequency table to better see the study results. How do we do this?

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```
addmargins(  
  table(dvd$group, dvd$decision)  
)
```

	buy DVD	not buy DVD	Sum
control	56	19	75
treatment	41	34	75
Sum	97	53	150

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We want to know how many students in each group didn't buy the DVD. Let's make a table of *row proportions*. Fill in the table in the lab file. (Zoom poll)

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	buy DVD	not buy DVD	Total
control	0.747	0.253	1.000
treatment	0.547	0.453	1.000
Total	0.647	0.353	1.000

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What's the **observed** difference in proportions of students who didn't buy the DVD,  
 $\hat{p}_{\text{trmt}} - \hat{p}_{\text{ctrl}}$ ?

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What's the **observed** difference in proportions of students who didn't buy the DVD,  
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$$0.453 - 0.253 = 0.200$$

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What's the **observed** difference in proportions of students who didn't buy the DVD,  
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$$0.453 - 0.253 = 0.200$$

Is this difference "statistically significant?"

# Simulation

## Big Idea

- Assume treatment status is independent of buying decision (i.e., that  $H_0$  is true).
- Simulate this study many times
- See if our observed difference in proportions is "weird".
- If "weird", this is evidence against the null hypothesis.

## In Practice

- Randomly shuffle buying decisions among treatment & control groups
- `sample_two_groups()`

# Simulation: A Single Replicate

```
set.seed(106) # we just picked this number, it's not special.
```

```
shuffle1 <- sample_two_groups(dvd)
table(shuffle1)
```

	decision	
group	buy DVD	not buy DVD
control	55	20
treatment	42	33

```
rt <- rowTable(shuffle1) # we wrote this function for you
```

```
rt[2, 2] - rt[1, 2]
```

```
[1] 0.1733333
```

# The replicate() function

- Sounds similar to `rep()` but **quite different**
  - `rep()` is copy/paste
  - `replicate()` re-runs code

Watch this:

```
rep(sample(1:20, size = 5), 3)
[1] 11 18 20  8  4 11 18 20  8  4 11 18 20  8  4
replicate(3, sample(1:20, size = 5))
 [,1] [,2] [,3]
[1,] 17   18   7
[2,] 19   5    3
[3,] 2    6   20
[4,] 12   9   17
[5,] 13   20  16
```

# The replicate() function

`rep()`



# The replicate() function

`rep()`



`replicate()`



# Simulation

This code runs 2 simulations. Modify it to run 1000.

```
pHatDiff <- replicate(2, {  
  shuffle <- sample_two_groups(dvd)  
  shuffle_table <- rowTable(shuffle)  
  shuffle_table[2, 2] - shuffle_table[1, 2] # p-hat_treatment minus p-hat_control  
})
```

# Simulation

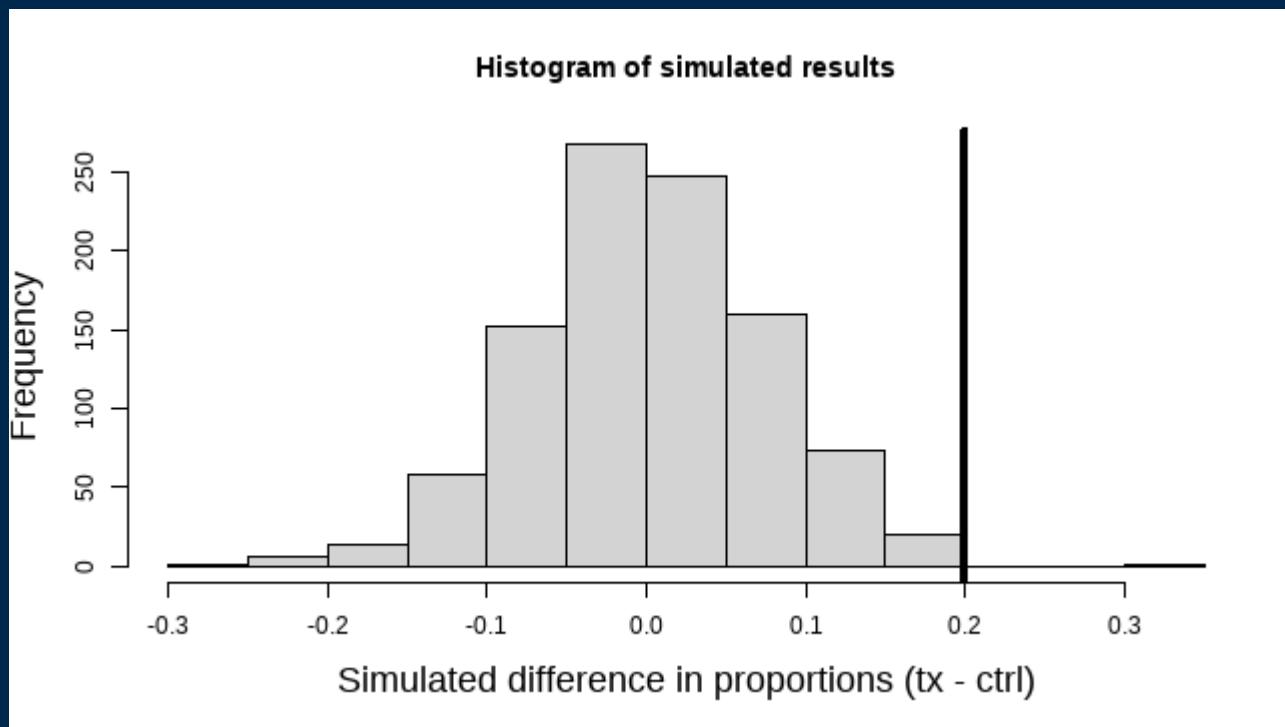
This code runs 2 simulations. Modify it to run 1000.

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  shuffle_table[2, 2] - shuffle_table[1, 2] # p-hat_treatment minus p-hat_control  
})
```

```
pHatDiffss <- replicate(1000, {  
  shuffle <- sample_two_groups(dvd)  
  shuffle_table <- rowTable(shuffle)  
  shuffle_table[2, 2] - shuffle_table[1, 2] # p-hat_treatment minus p-hat_control  
})
```

# Simulation Results

```
hist(pHatDiff, main = "Histogram of simulated results",
     xlab = "Simulated difference in proportions (tx - ctrl)",
     cex.lab = 1.5) #just for slides
abline(v = 0.2, lwd = 4)
```



# Simulation Results: Approximate p-value

The p-value is the proportion of simulated results *as extreme or more extreme* than our observed result. What does "extreme" mean?

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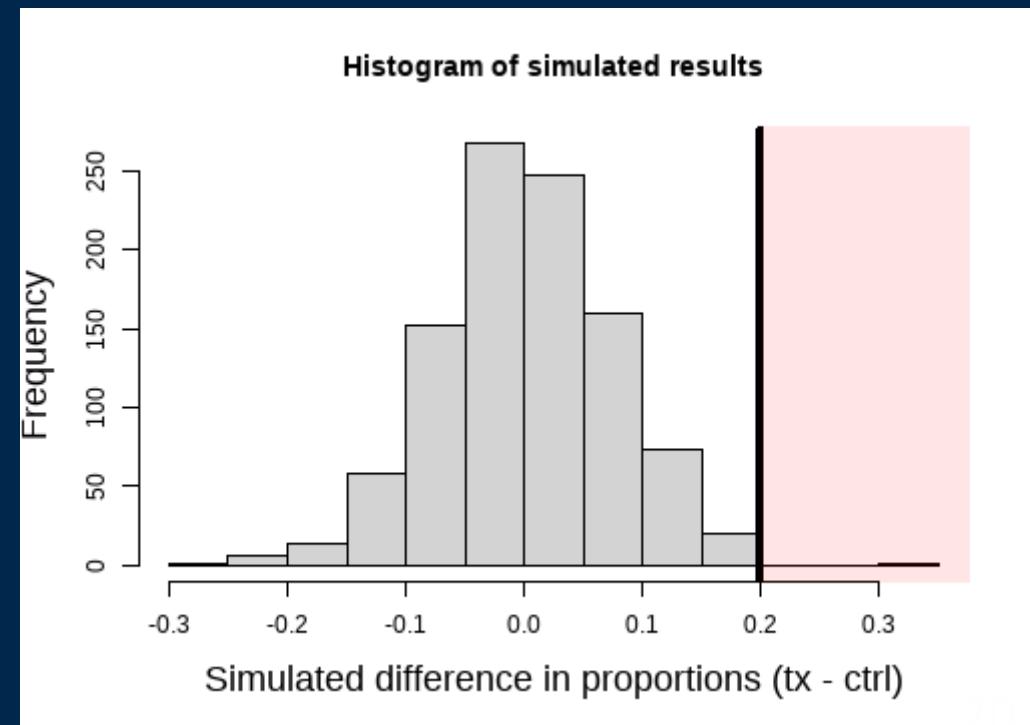
The p-value is the proportion of simulated results *as extreme or more extreme* than our observed result. What does "extreme" mean?

**Extreme** means *provides more evidence for the alternative hypothesis*. What will that mean here? (Zoom poll)

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**Extreme** means *provides more evidence for the alternative hypothesis*. What will that mean here? (Zoom poll)



# Simulation Results: Approximate p-value

Let's count the number of simulations that led to a difference in proportions of 20% or greater:

```
sum(pHatDiff >= 0.2)
```

```
[1] 1
```

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Let's count the number of simulations that led to a difference in proportions of 20% or greater:

```
sum(pHatDiff >= 0.2)
```

```
[1] 1
```

So the estimated p-value is  $1/1000 = 0.001 = 0.1\%$ .

## Poll

- Is our observed data rare?
- Is our null hypothesis reasonable?
- Does the reminder about using money later reduce spending now?

# Lab Project



## Your tasks

- Complete the "Try It!" and "Dive Deeper" portions of the lab assignment by copy/pasting and modifying appropriate code from earlier in the document.
- Introduce yourself to your collaborators
- Do not leave people behind.

## How to get help

- Ask your collaborators -- share your screen!
- Use the "Ask for Help" button to flag me down.

