

# STATS 250 Lab 08

## Sampling Distributions of Proportions

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Week of 10/19/2020

# Reminders



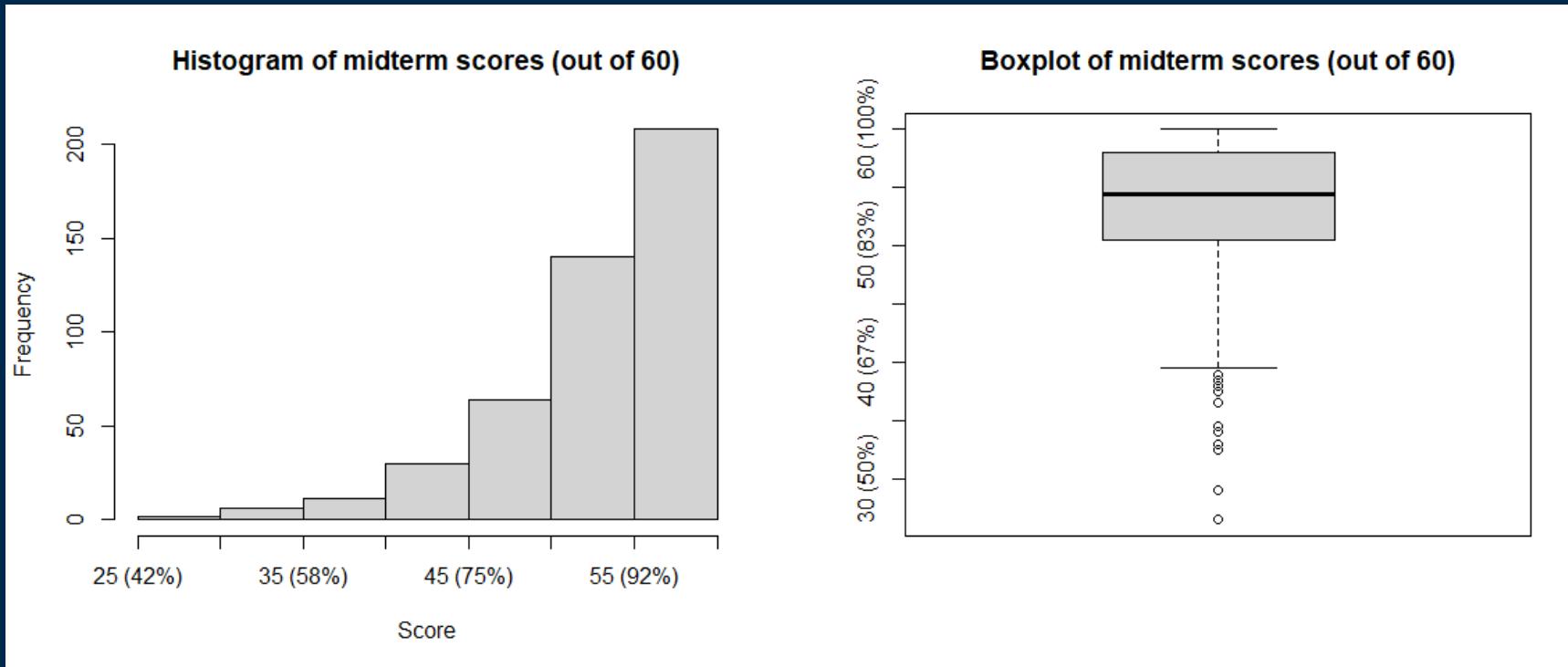
Your tasks for the week running Friday 10/19 - Friday 10/23:

Task	Due Date	Submission
Lab 8	Friday 10/23 8:00AM ET	Canvas
<i>No homework this week</i>	--	course.work

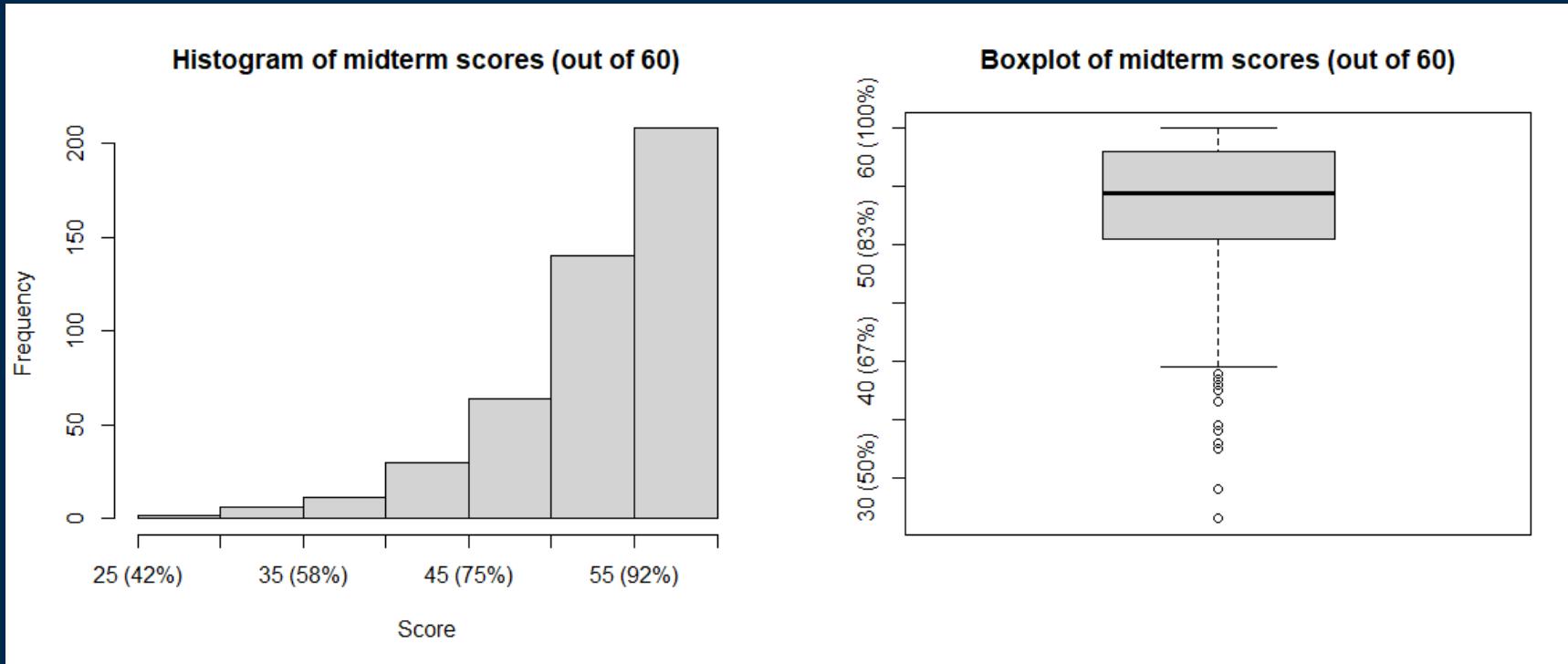
Office hours are back to normal this week (with a few small tweaks)

Midterm regrade requests through Gradescope due \*\*Tuesday 10/27 8a

# Midterm Recap



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If the midterm didn't go as expected *that's OKAY*. There's plenty of semester left.

# What's the plan?

Today we're going to learn about "sampling distributions" and something called the **Central Limit Theorem** (CLT).

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The central limit theorem is sort of magical. We'll talk about it in more detail in lecture!



# Sampling Distributions

A **sampling distribution** refers to the possible values for a *statistic* (e.g.,  $\hat{p}$ ) and how often those values occur.

We've sort of seen sampling distributions already. Can you think of how?

# Sampling Distributions

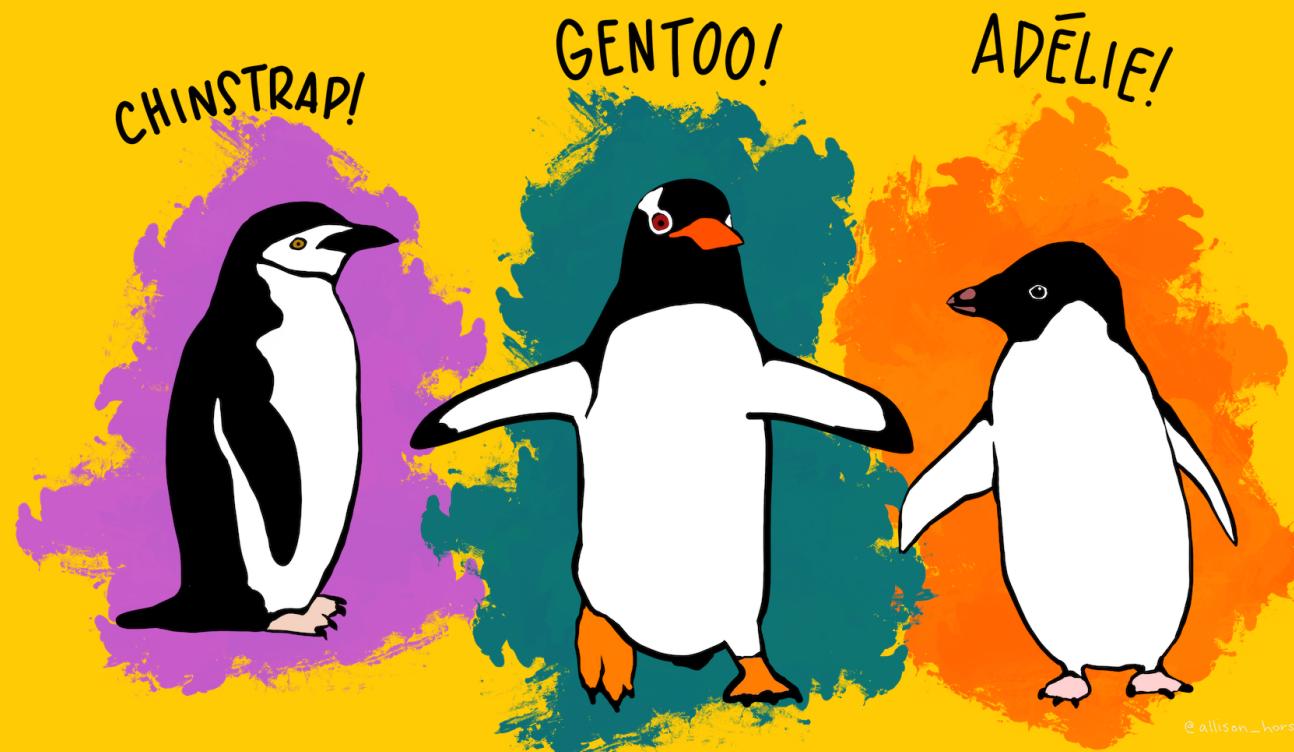
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We've sort of seen sampling distributions already. Can you think of how?

The histograms we've made of  $\hat{p}_{\text{sim}}$  are sampling distributions of  $\hat{p}$  (under the null hypothesis model)!

# Penguins!

```
penguins <- read.csv("https://raw.githubusercontent.com/STATS250SBI/palmerpenguins/master/inst/extdata/penguins.csv")
stringsAsFactors = TRUE)
```



@allison\_horst

# Penguins!

Let's remind ourselves of what variables are in this data:

```
# Use your favorite function or two to explore the data
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names(penguins)
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```
[1] "species"           "island"            "bill_length_mm"
[4] "bill_depth_mm"    "flipper_length_mm" "body_mass_g"
[7] "sex"               "year"
```

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```

IMPORTANT NOTE: For the purposes of this example, we're going to assume that the penguins in the data represent the *population* of all penguins in the Palmer Archipelago. This is obviously not true: there are more than 333 penguins living on these islands. *This is just to illustrate ideas.*

# "Population" proportions

Assuming our data is on the full population of penguins in the archipelago, how could we find the population proportion of Gentoo penguins?

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proportions(table(penguins$species))
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Adelie Chinstrap Gentoo  
0.4384384 0.2042042 0.3573574
```

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```

$$p = 0.357$$

where  $p$  is the population proportion of Gentoo penguins in the Palmer Archipelago

# set.seed()

Start by setting the seed:

```
set.seed(7923)
```

Things to remember when setting the seed:

- Guaranteed to get the same results from the same code in the *knitted* document
- Determines the *sequence* of random numbers: things can get knocked off sequence
- Use "Run All Chunks Above" to get back on sequence and to get the same numbers as in the knitted document

# Taking a sample

Take a sample of size 20 from the "population" of all penguins:

```
sample1 <- penguins[sample(1:333, size = 20), ]
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species island bill_length_mm bill_depth_mm flipper_length_mm body_mass_g  
271 Chinstrap Dream      45.2        17.8          198       3950  
252   Gentoo Biscoe     43.3        14.0          208       4575  
      sex year  
271 female 2007  
252 female 2009
```

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      sex year  
271 female 2007  
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```

```
proportions(table(sample1$species))
```

```
Adelie Chinstrap   Gentoo  
0.50      0.15      0.35
```

# Taking another sample

```
sample2 <- penguins[sample(1:333, size = 20), ] # reusing the same code as above  
proportions(table(sample2$species))
```

Adelie	Chinstrap	Gentoo
0.65	0.20	0.15

We get different results! This is expected, it's *sample-to-sample variability*.

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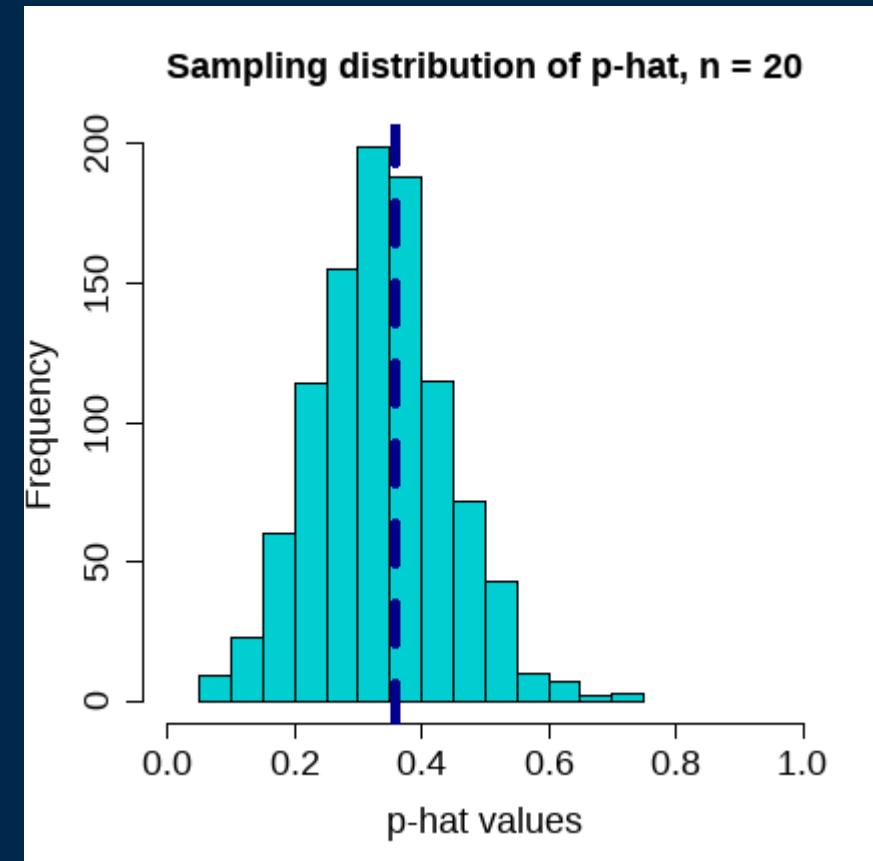
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# 1000 more samples

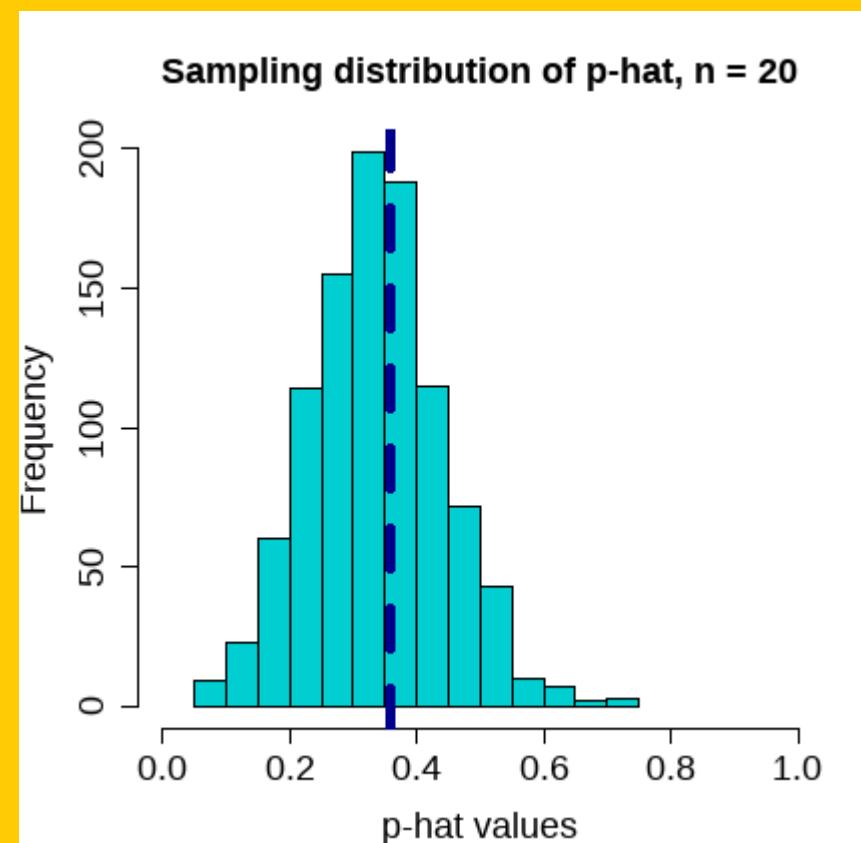
```
samplesOfSize20 <- replicate(1000, {
  s <- penguins[sample(1:333, size = 20), ]
  proportions(table(s$species))["Gentoo"]
})
```

```
hist(samplesOfSize20,
  main = "Sampling distribution of p-hat, n = 20",
  xlab = "p-hat values",
  col = "darkturquoise",
  xlim = c(0, 1),
  cex.lab = 1.5,
  cex.main = 1.5,
  cex.axis = 1.5)
abline(v = proportions(table(penguins$species)),
  lwd = 5, lty = "dashed", col = "darkblue")
```



# Describe this distribution

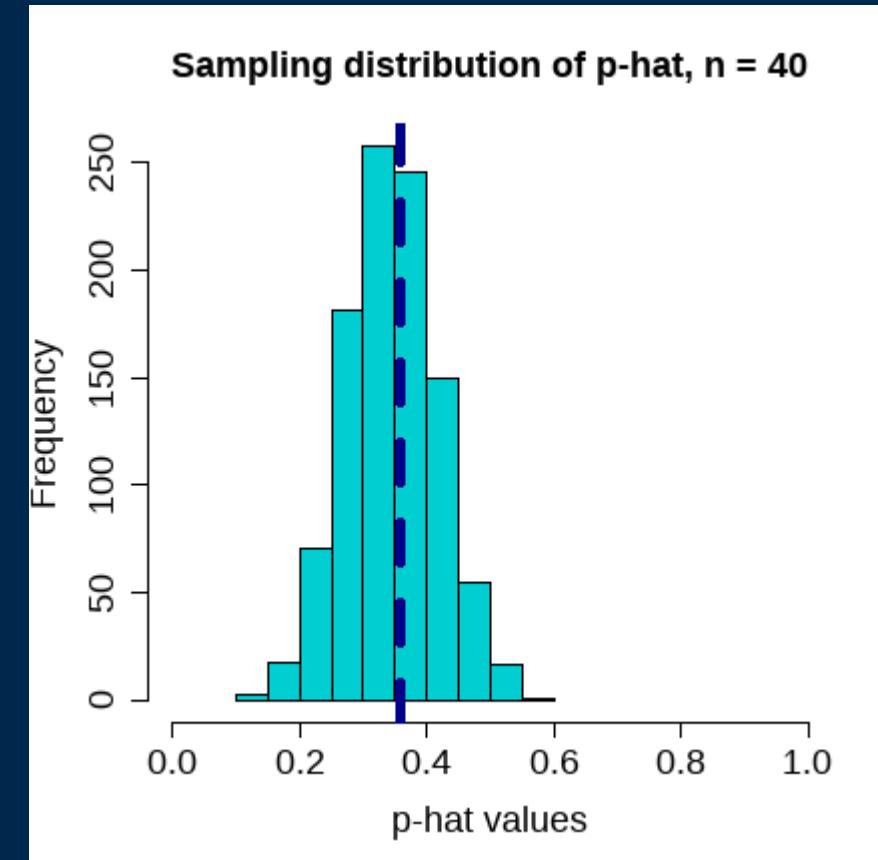
<https://pollev.com/nickseewald611>



# Larger samples: $n = 40$

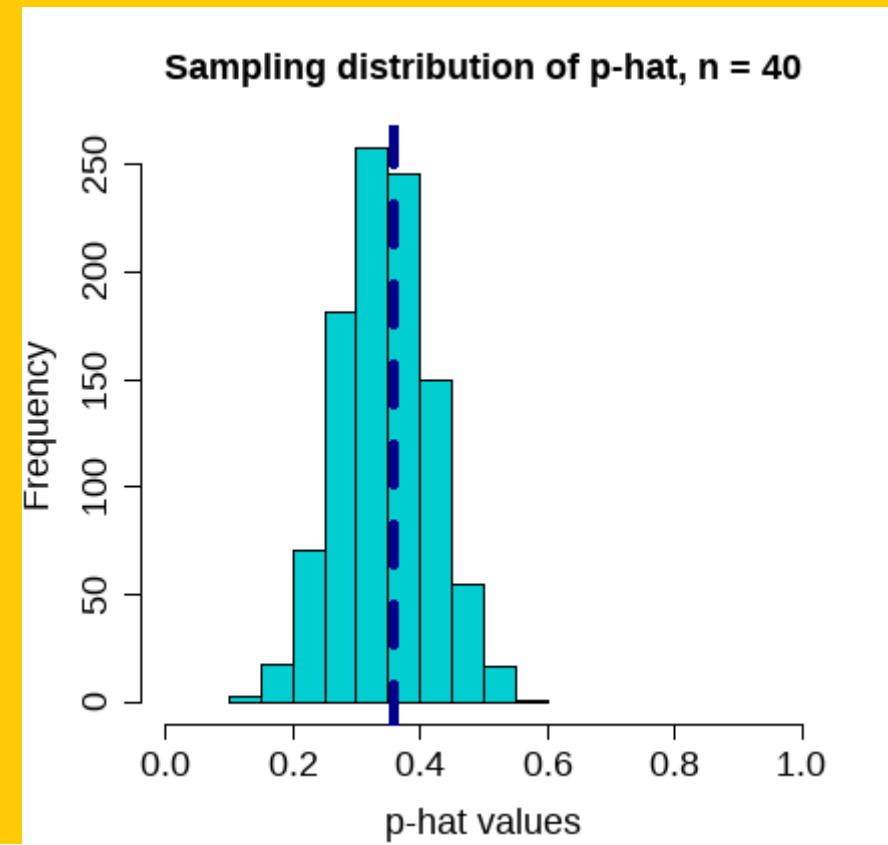
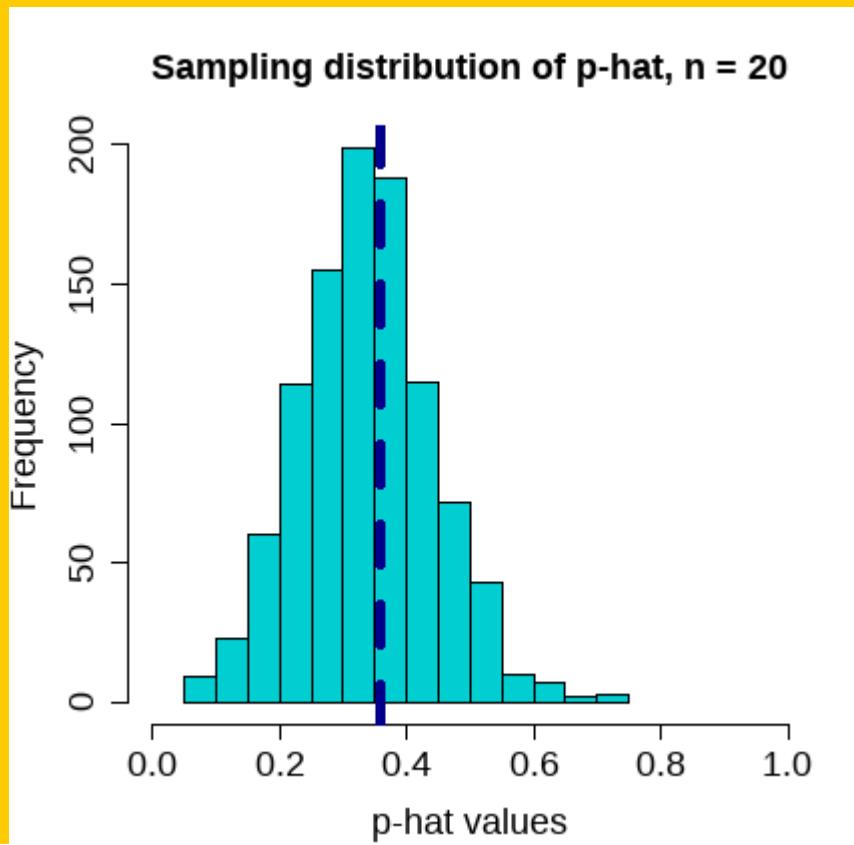
```
samplesOfSize40 <- replicate(1000, {
  s <- penguins[sample(1:333, size = 40), ]
  proportions(table(s$species))["Gentoo"]
})
```

```
hist(samplesOfSize40,
  main = "Sampling distribution of p-hat, n = 40",
  xlab = "p-hat values",
  col = "darkturquoise",
  xlim = c(0, 1),
  cex.lab = 1.5,
  cex.main = 1.5,
  cex.axis = 1.5)
abline(v = proportions(table(penguins$species)),
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```



# How do these distributions compare?

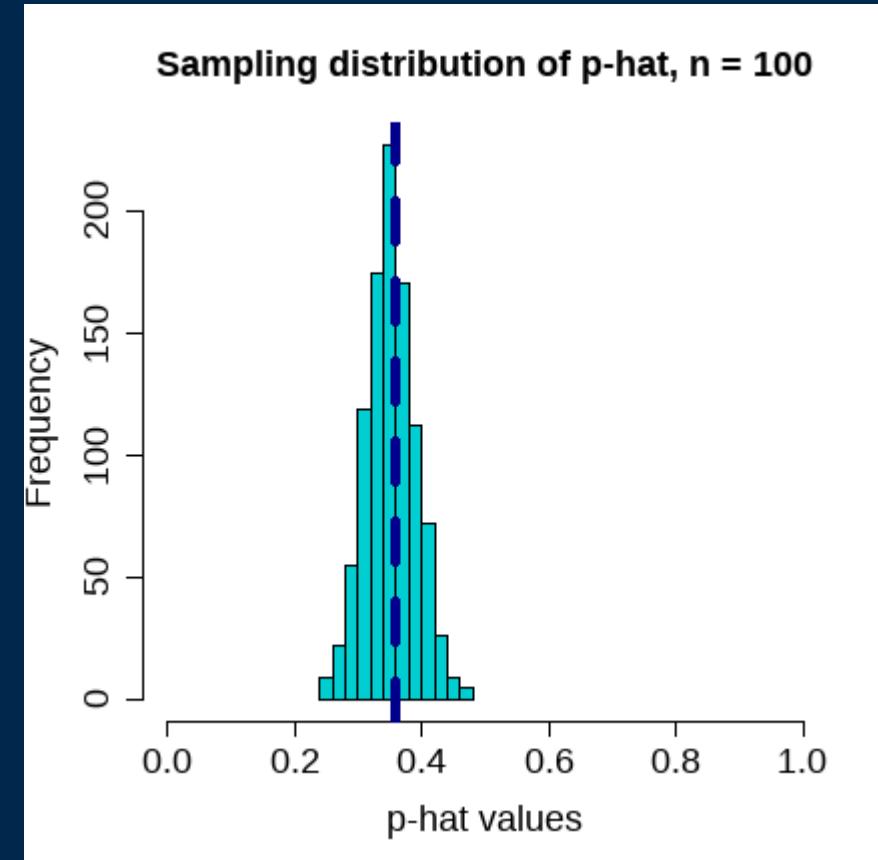
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# Even larger samples: $n = 100$

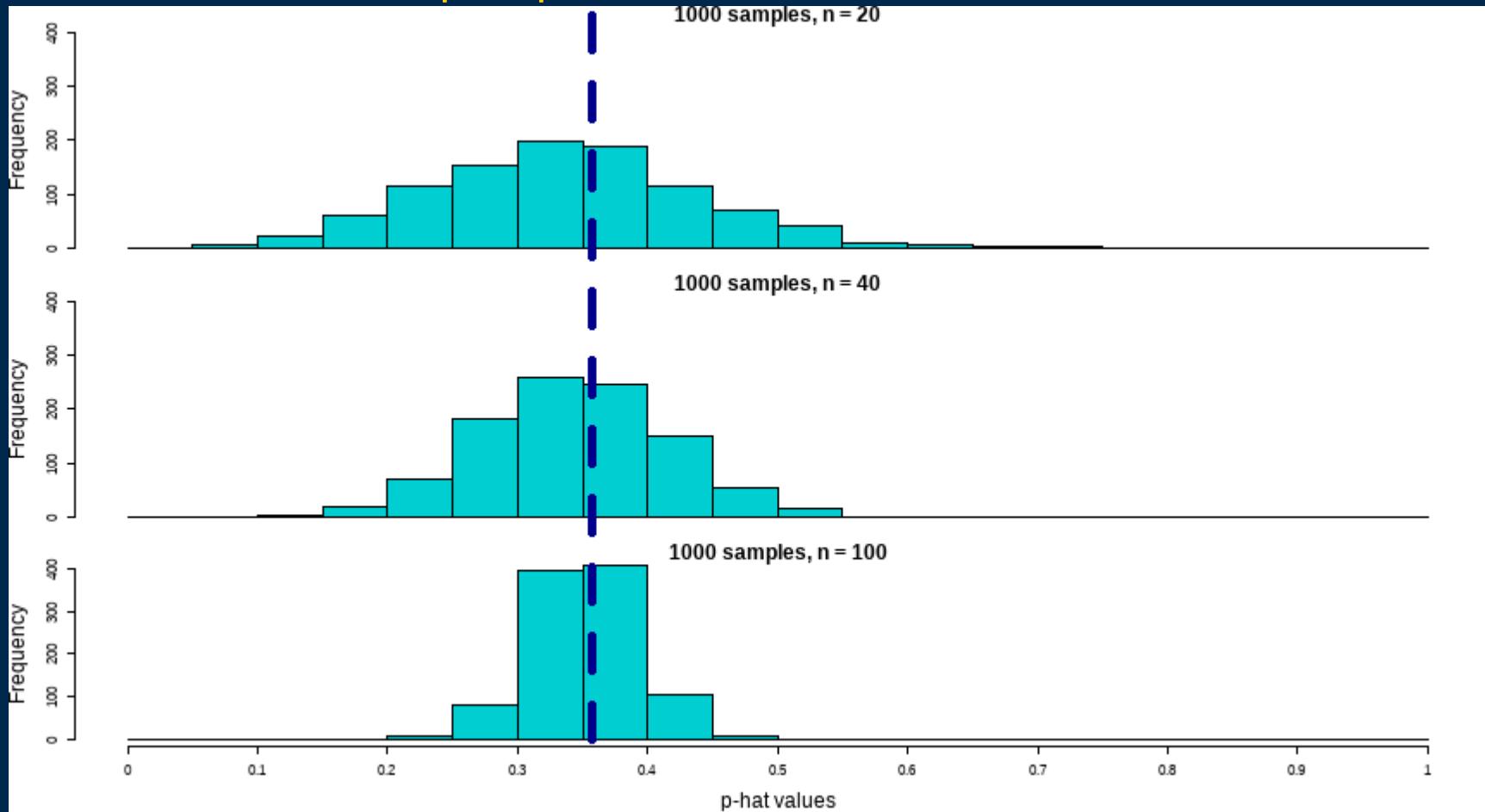
```
samplesOfSize100 <- replicate(1000, {
  s <- penguins[sample(1:333, size = 100), ]
  proportions(table(s$species))["Gentoo"]
})
```

```
hist(samplesOfSize100,
  main = "Sampling distribution of p-hat, n = 100",
  xlab = "p-hat values",
  col = "darkturquoise",
  xlim = c(0, 1),
  cex.lab = 1.5,
  cex.main = 1.5,
  cex.axis = 1.5)
abline(v = proportions(table(penguins$species)),
  lwd = 5, lty = "dashed", col = "darkblue")
```

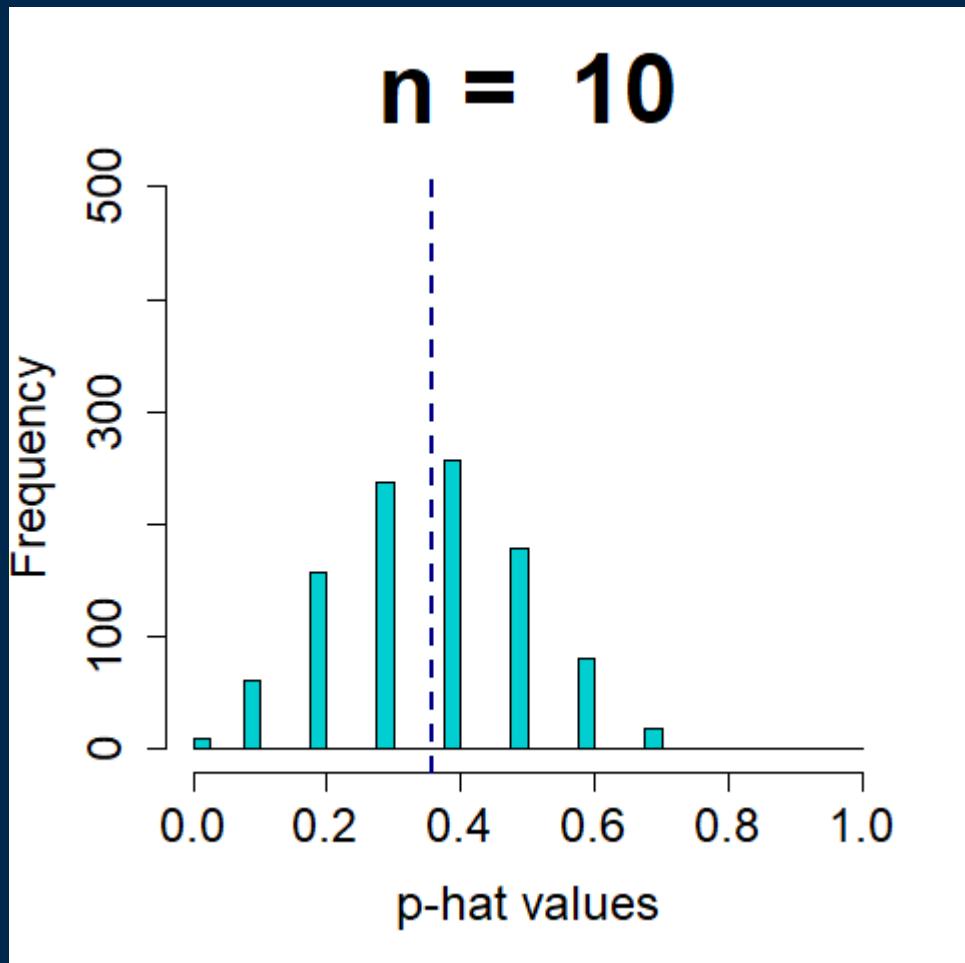


# Comparing Results

<https://pollev.com/nickseewald611>



# More Detail



As the size of our samples increases, the sampling distribution of  $\hat{p}$  becomes...

1. more obviously centered around  $p$
2. narrower
3. more bell-shaped

# Central Limit Theorem

If we look at a proportion (or difference in proportions) and the scenario satisfies certain conditions, then the sample proportion (or difference in proportions) will appear to follow a bell-shaped curve called the *normal distribution*.

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## Conditions:

1. **Observations in the sample are independent.** Guaranteed by random sampling or random allocation to treatment/control.
2. **The sample is large enough.** "Large enough" means  $n \times p \geq 10$  and  $n \times (1 - p) \geq 10$  ( $p$  the population proportion).

# Lab Project



## Your tasks

- Complete the "Try It!" and "Dive Deeper" portions of the lab assignment by copy/pasting and modifying appropriate code from earlier in the document.
- Introduce yourself to your collaborators
- Do not leave people behind.

## How to get help

- Ask your collaborators -- share your screen!
- Use the "Ask for Help" button to flag me down.

# Reminders



**<http://bit.ly/250ticket8>**

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