

## 1. Vector

$$\vec{u} \cdot \vec{v} = u_1 * v_1 + u_2 * v_2 = |\vec{u}| |\vec{v}| \cos(\theta)$$

$$|\vec{u}|^2 = \vec{u} \cdot \vec{u}$$

### Linear combination

$$a_1 \vec{v}_1 + \dots + a_m \vec{v}_m$$

### Span

$$\text{span}(v_1, \dots, v_m) = \{a_1 \vec{v}_1 + \dots + a_m \vec{v}_m \mid a_1, \dots, a_m \in \mathbb{R}\}$$

### Linear independent

A list  $(v_1, \dots, v_m)$  is linear independent if the only choice of  $a_1, \dots, a_m \in \mathbb{R}$  that makes  $a_1 \vec{v}_1 + \dots + a_m \vec{v}_m = \vec{0}$  is  $a_1 = \dots = a_m = 0$

### Basic of V:

a list of vectors in V that

- linear independent
- span V

every  $\vec{v} \in V$  can be written **uniquely** in form of a linear combination of the basic

**Dim** = len(basic)