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Chapter 1

Functions

1.1 gcd – gcd algorithm

1.1.1 gcd – the greatest common divisor

```
\gcd(\mathtt{a} \colon integer, \ \mathtt{b} \colon integer) 	o integer
```

Return the greatest common divisor of two integers a and b.

a, b must be int, long or **Integer**. Even if one of the arguments is negative, the result is non-negative.

1.1.2 binarygcd – binary gcd algorithm

```
binarygcd(a: integer, b: integer) 
ightarrow integer
```

Return the greatest common divisor of two integers **a** and **b** by binary gcd algorithm.

†This function is an alias of binarygcd

a, b must be int, long, or Integer.

1.1.3 extgcd – extended gcd algorithm

```
\operatorname{extgcd}(\operatorname{a:}\ integer,\ \operatorname{b:}\ integer) 	o (integer,\ integer,\ integer)
```

Return the greatest common divisor d of two integers a and b and u, v such that d = au + bv.

a, b must be int, long, or **Integer**. The returned value is a tuple (u, v, d).

1.1.4 lcm – the least common multiple

$lcm(a: integer, b: integer) \rightarrow integer$

Return the least common multiple of two integers a and b.

†If both a and b are zero, then it raises an exception.

a, b must be int, long, or Integer.

1.1.5 gcd of list – gcd of many integers

$$\gcd$$
 of $list(integers: \mathit{list}) o \mathit{list}$

Return gcd of multiple integers.

For given integers $[x_1, \ldots, x_n]$, return a list $[d, [c_1, \ldots, c_n]]$ such that $d = c_1x_1 + \cdots + c_nx_n$, where d is the greatest common divisor of x_1, \ldots, x_n .

integers is a list which elements are int or long. This function returns $[d, [c_1, \ldots, c_n]]$, where d, c_i are an integer.

1.1.6 coprime – coprime check

```
\operatorname{coprime}(\mathtt{a} \colon integer, \, \mathtt{b} \colon integer) 	o bool
```

Return True if a and b are coprime, False otherwise.

a, b are int, long, or Integer.

1.1.7 pairwise coprime – coprime check of many integers

```
pairwise coprime(integers: list) \rightarrow bool
```

Return True if all integers in integers are pairwise coprime, False otherwise.

integers is a list which elements are int, long, or Integer.

Examples

```
>>> gcd.gcd(12, 18)
6
>>> gcd.gcd(12, -18)
6
>>> gcd.gcd(-12, -18)
6
>>> gcd.gcd(-12, -18)
6
>>> gcd.extgcd(12, -18)
(-1, -1, 6)
>>> gcd.extgcd(-12, -18)
(1, -1, 6)
>>> gcd.extgcd(0, -18)
(0, -1, 18)
>>> gcd.lcm(12, 18)
36
>>> gcd.lcm(12, -18)
-36
>>> gcd.gcd_of_list([60, 90, 210])
[30, [-1, 1, 0]]
```