

Lecture #23

Cache Part II: Set/Fully Associative Cache



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Cache II: Set/Fully Associative Cache

- 1. Types of Cache Misses
- 2. Block Size Trade-off
- 3. Set Associative Cache
- 4. Fully Associative Cache
- 5. Block Replacement Policy
- 6. Additional Examples
- 7. Summary
- 8. Exploration

1. (Recall) Types of Cache Misses

Compulsory misses

- On the first access to a block; the block must be brought into the cache
- Also called cold start misses or first reference misses

Conflict misses

- Occur in the case of direct mapped cache or set associative cache, when several blocks are mapped to the same block/set
- Also called collision misses or interference misses

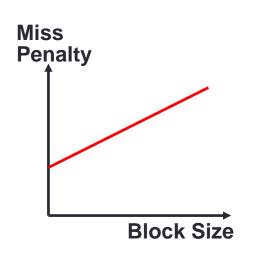
Capacity misses

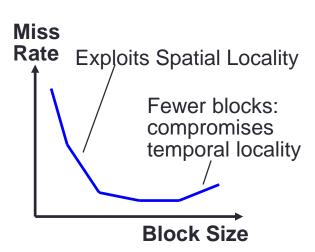
 Occur when blocks are discarded from cache as cache cannot contain all blocks needed

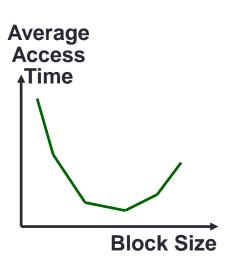
2. Block Size Trade-off (1/2)

Average Access Time

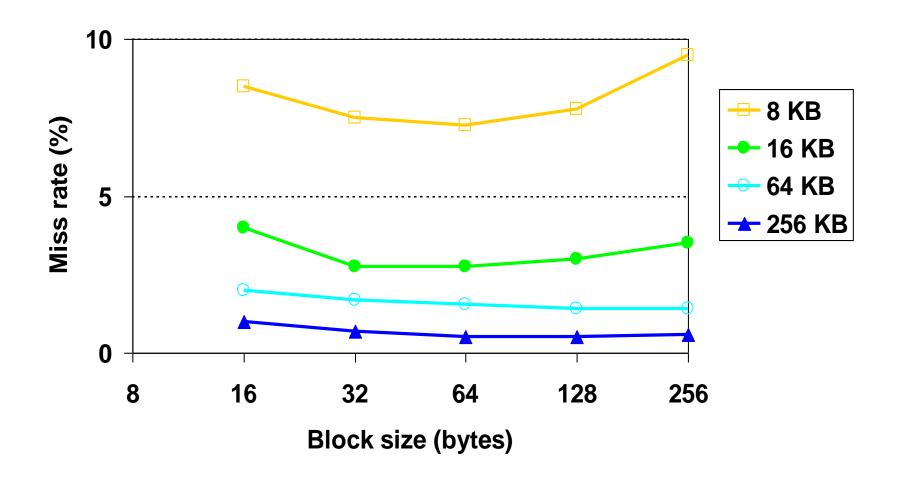
- = Hit rate x Hit Time + (1-Hit rate) x Miss penalty
- Larger block size:
 - + Takes advantage of spatial locality
 - Larger miss penalty: Takes longer time to fill up the block
 - If block size is too big relative to cache size
 - → Too few cache blocks → miss rate will go up







2. Block Size Trade-off (2/2)



3. Set Associative (SA) Cache

Compulsory misses

- On the first access to brought into the cach
- Also called cold start

Solution: Set Associative Cache

nisses

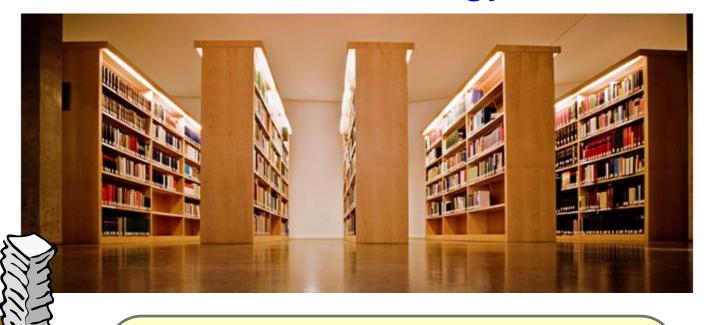
Conflict misses

- Occur in the case of direct mapped cache or set associative cache, when several blocks are mapped to the same block/set
- Also called collision misses or interference misses

Capacity misses

 Occur when blocks are discarded from cache as cache cannot contain all blocks needed

3. Set Associative Cache: Analogy



Many book titles start with "T"

→ Too many conflicts!

Hmm... how about we give more slots per letter, 2 books start with "A", 2 books start with "B", etc?

3. Set Associative (SA) Cache

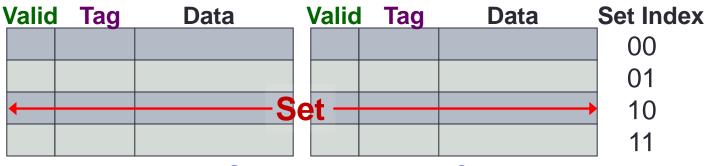
N-way Set Associative Cache

 A memory block can be placed in a fixed number (N) of locations in the cache, where N > 1

Key Idea:

- Cache consists of a number of sets:
 - Each set contains N cache blocks
- Each memory block maps to a unique cache set
- Within the set, a memory block can be placed in any of the N cache blocks in the set

3. Set Associative Cache: Structure



2-way Set Associative Cache

- An example of 2-way set associative cache
 - Each set has two cache blocks
- A memory block maps to a unique set
 - In the set, the memory block can be placed in either of the cache blocks
 - → Need to search both to look for the memory block

3. Set Associative Cache: Mapping

Memory Address



Cache Block size = 2^N bytes

Cache Set Index

= (BlockNumber) modulo (NumberOfCacheSets)



Cache Block size = 2^N bytes

Number of cache sets = 2^{M}

Offset = N bits

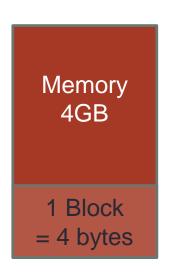
Set Index = M bits

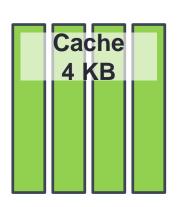
Tag = 32 - (N + M) bits

Observation:

It is essentially unchanged from the direct-mapping formula

3. Set Associative Cache: Example









Offset, N = 2 bits

Block Number = 32 - 2 = 30 **bits**

Check: Number of Blocks = 2^{30}



Number of Cache Blocks

$$= 4KB / 4bytes = 1024 = 2^{10}$$

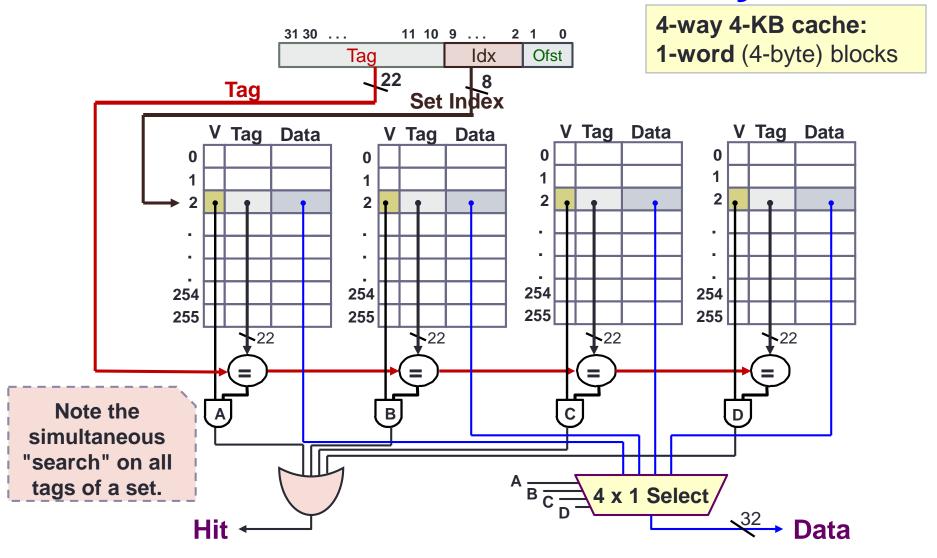
4-way associative, number of sets

$$= 1024 / 4 = 256 = 28$$

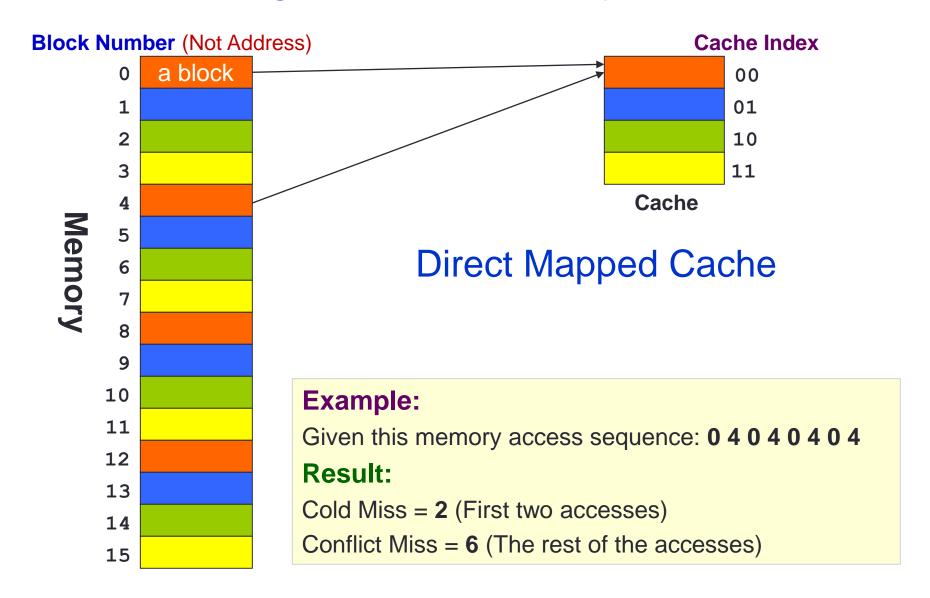
Set Index, M = 8 bits

Cache Tag =
$$32 - 8 - 2 = 22$$
 bits

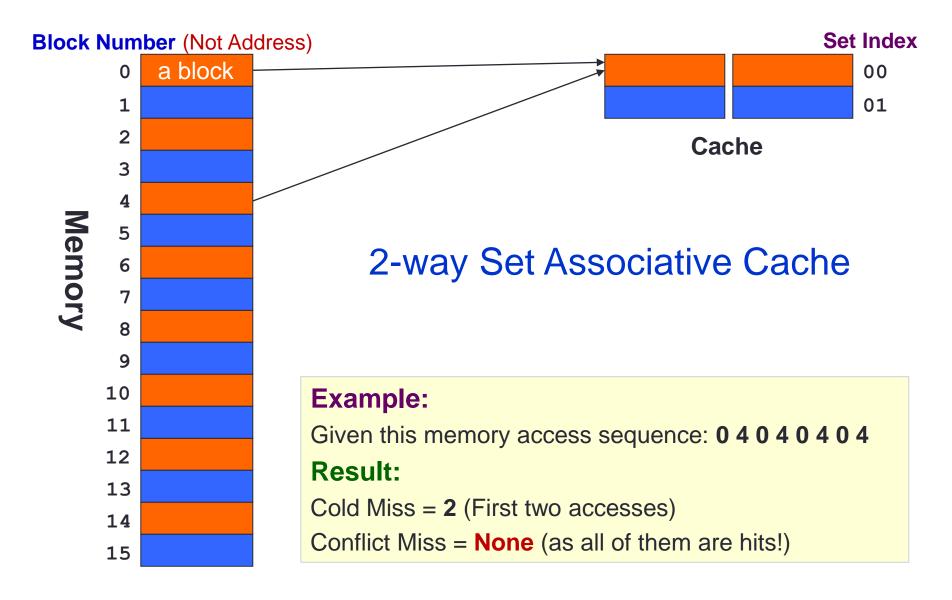
3. Set Associative Cache: Circuitry



3. Advantage of Associativity (1/3)



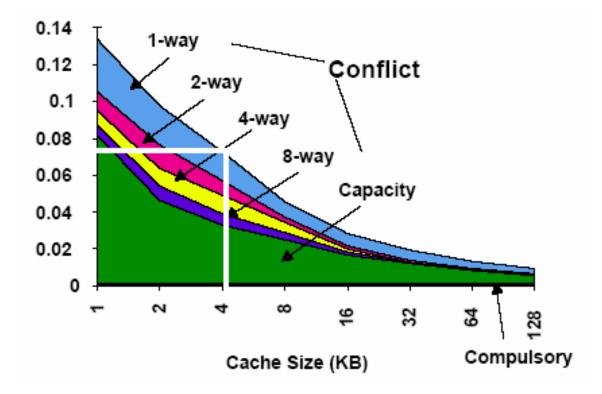
3. Advantage of Associativity (2/3)



3. Advantage of Associativity (3/3)

Rule of Thumb:

A direct-mapped cache of size **N** has about the same miss rate as a 2-way set associative cache of size **N/2**



3. SA Cache Example: Setup

- Given:
 - Memory access sequence: 4, 0, 8, 36, 0
 - 2-way set-associative cache with a total of four
 8-byte blocks → total of 2 sets
 - Indicate hit/miss for each access



Offset, N = 3 bits Block Number = 32 - 3 = 29 bits

2-way associative, number of sets= $2 = 2^1$ Set Index, M = 1 bits

Cache Tag = 32 - 3 - 1 = 28 bits

Miss 0, 8, 36, 0

Tag

Index Offset

Check: Both blocks in **Set 0** are invalid [Cold Miss]

Result: Load from memory and place in Set 0 - Block 0

		Blo	ock 0		Block 1			
Set Index	Valid	Tag	wo	W1	Valid	Tag	wo	W1
0	Ø1	0	M[0]	M[4]	0			
1	0				0			

Miss Hit 4,0, 8, 36, 0

Tag

Index Offset

■ Load from **0** →

0 (0)

Result:

[Valid and Tags match] in Set 0-Block 0 [Spatial Locality]

		Blo	ock 0		Block 1			
Set Index	Valid	Tag	wo	W1	Valid	Tag	wo	W1
0	1	0	M[0]	M[4]	0			
1	0				0			

Miss Hit Miss 4, 0, (8) 36, 0

Tag

Index Offset

Load from 8 ->

1 0000

Check: Both blocks in Set 1 are invalid [Cold Miss]

Result: Load from memory and place in Set 1 - Block 0

		Blo	ock 0		Block 1			
Set Index	Valid	Tag	wo	W1	Valid	Tag	WO	W1
0	1	0	M[0]	M[4]	0			
1	<i>Ø</i> 1	0	M[8]	M[12]	0			

Miss Hit Miss Miss 4, 0, 8, 36, 0

Tag

Index Offset

Check: [Valid but tag mismatch] Set 0 - Block 0

[Invalid] Set 0 - Block1 [Cold Miss]

Result: Load from memory and place in Set 0 - Block 1

		BI	ock 0		Block 1			
Set Index	Valid	Tag	W0	W1	Valid	Tag	W0	W1
0	1	0	M[0]	M[4]	Ø1	2	M[32]	M[36]
1	1	0	M[8]	M[12]	0			

Miss Hit Miss Miss Hit 4, 0, 8, 36, 0

Tag

Index Offset

■ Load from **0** →

0 000

Check: [Valid and tags match] Set 0-Block 0
[Valid but tags mismatch] Set 0-Block1

[Temporal Locality]

		BI	ock 0		Block 1				
Set Idx	Valid	Tag	wo	W1	Valid	Tag	WO	W1	
0	1	0	M[0]	M[4]	1	2	M[32]	M[36]	
1	1	0	M[8]	M[12]	0				

4. Fully Associative (FA) Cache

- Compulsory misses
 - On the first access to a block; the block must be brought into the cache
 - Also called cold start misses or first reference misses
- Conflict misses
 - Occur in the case of direct mapped cache or set associative cache, when several blocks are mapped to the same block/set

 Occurs in
 - Also called collision m Fully Associative Cache ses
- Capacity misses
 - Occur when blocks are discarded from cache as cache cannot contain all blocks needed

4. Fully Associative (FA) Cache: Analogy



Let's not restrict the book by title any more. A book can go into any location on the desk!

4. Fully Associative (FA) Cache

Fully Associative Cache

A memory block can be placed in any location in the cache

Key Idea:

- Memory block placement is no longer restricted by cache index or cache set index
- ++ Can be placed in any location, BUT
- --- Need to search all cache blocks for memory access

4. Fully Associative Cache: Mapping

Memory Address



Cache Block size = 2^N bytes



Cache Block size = 2^N bytes

Number of cache blocks = 2^{M}

Offset = N bits

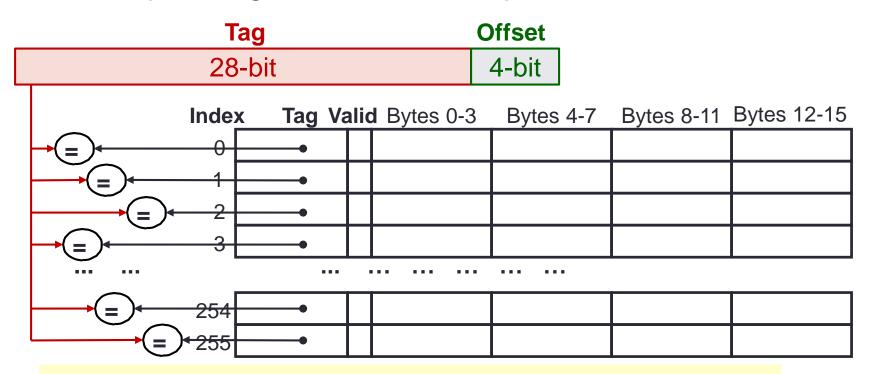
Tag = 32 - N bits

Observation:

The block number serves as the tag in FA cache.

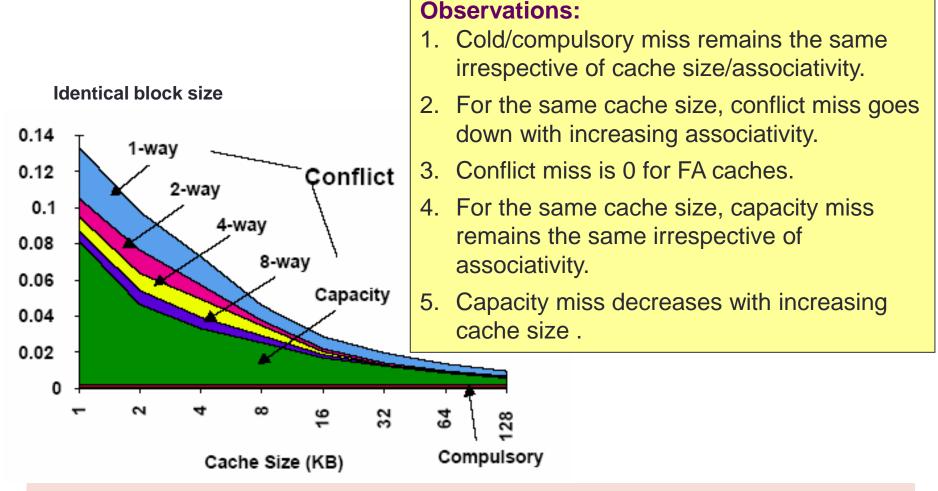
4. Fully Associative Cache: Circuitry

- Example:
 - 4KB cache size and 16-Byte block size
 - Compare tags and valid bit in parallel



No Conflict Miss (since data can go anywhere)

4. Cache Performance



Total Miss = Cold miss + Conflict miss + Capacity miss

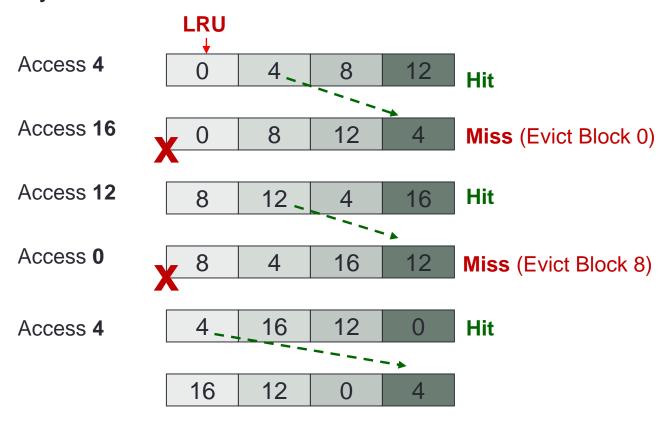
Capacity miss (FA) = Total miss (FA) − Cold miss (FA), when Conflict Miss→0

5. Block Replacement Policy (1/3)

- Set Associative or Fully Associative Cache:
 - Can choose where to place a memory block
 - Potentially replacing another cache block if full
 - Need block replacement policy
- Least Recently Used (LRU)
 - How: For cache hit, record the cache block that was accessed
 - When replacing a block, choose one which has not been accessed for the longest time
 - Why: Temporal locality

5. Block Replacement Policy (2/3)

- Least Recently Used policy in action:
 - 4-way SA cache
 - Memory accesses: 0 4 8 12 4 16 12 0 4



5. Block Replacement Policy (3/3)

- Drawback for LRU
 - Hard to keep track if there are many choices
- Other replacement policies:
 - First in first out (FIFO)
 - Random replacement (RR)
 - Least frequently used (LFU)

6. Additional Examples #1

- Direct-Mapped Cache:
 - Four 8-byte blocks
- Memory accesses:(4.8.36)(48)(68)(0.32)

Addr:	Tag	Index	Offset
4:	00000	00	100
8:	00000	01	000
36:	00001	00	100
48:	00001	10	000
68:	00010	00	100
0:	00000	00	000
32:	00001	00	000

Index	Valid	Tag	Word0	Word1
0	Ø 1	-0 1 -0 2	M[0] M[32] M[32] M[0]	M[4].
1	Ø 1	0	M[8]	M[12]
2	Ø 1	1	M[48]	M[52]
3	0			

6. Additional Examples #2

- Fully-Associative Cache:
 - Four 8-byte blocks
 - LRU Replacement Policy
- Memory accesses: Hit
 4,8,36,48,68,0,32

Addr:	Tag	Offset
4:	0000	100
8:	0000001	000
36:	0000100	100
48:	0000110	000
68:	0001000	100
0:	0000000	000
32:	0000100	000

Index	Valid	Tag	Word0	Word1
0	Ø 1	0 8	M[0] M[64]	M[4] M[68]
1	& 1	-1 0	M[8] _{M[0]}	M[12] _{M[4]}
2	Ø 1	4	M[32]	M[36]
3	01	6	M[48]	M[52]

6. Additional Examples #3

- 2-way Set-Associative Cache:
 - Four 8-byte blocks
 - LRU Replacement Policy
- Memory accesses:

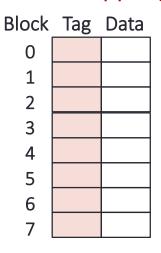
			\bigcirc	
(A YO YOE)		(CO)	(١
(4,)(8,)(36)	//40 1	(00)	(U.)(3Z)
				,

Addr:	Tag	Index	Offset
4:	000000	0	100
8:	000000	1	000
36:	000010	0	100
48:	000011	0	000
68:	000100	0	100
0:	000000	0	000
32:	000010	0	000

	Block 0				Block 1			
Set Index	Valid	Tag	Word0	Word1	Valid	Tag	Word0	Word1
0	ø 1	φ φ Ο	M[0] M[48] M[0]	M[4] M[52] M[4]	ø 1	2 4 2	M[32] M[64] M[32]	M[36] M[68] M[36]
1	9 1	0	M[8]	M[12]	0			

7. Summary: Cache Organizations

One-way set associative (direct mapped)



Two-way set associative

Set	Tag	Data	Tag	Data
0				
1				
2				
3				

Four-way set associative

Set	Tag	Data	Tag	Data	Tag	Data	Tag	Data
0								
1								

Eight-way set associative (fully associative)

Tag	Data														

7. Summary: Cache Framework (1/2)

Block Placement: Where can a block be placed in cache?

Direct Mapped:

 Only one block defined by index

N-way Set-Associative:

 Any one of the N blocks within the set defined by index

Fully Associative:

Any cache block

Block Identification: How is a block found if it is in the cache?

Direct Mapped:

 Tag match with only one block

N-way Set Associative:

 Tag match for all the blocks within the set

Fully Associative:

 Tag match for all the blocks within the cache

7. Summary: Cache Framework (2/2)

Block Replacement: Which block should be replaced on a cache miss?

Direct Mapped:

No Choice

N-way Set-Associative:

Based on replacement policy

Fully Associative:

Based on replacement policy

Write Strategy: What happens on a write?

Write Policy: Write-through vs write-back

Write Miss Policy: Write allocate vs write no allocate

8. Exploration: Improving Cache Penalty

Average Access Time

- = Hit rate x Hit Time + (1-Hit rate) x Miss penalty
- So far, we tried to improve Miss Rate:
 - Larger block size
 - Larger Cache
 - Higher Associativity
- What about Miss Penalty?

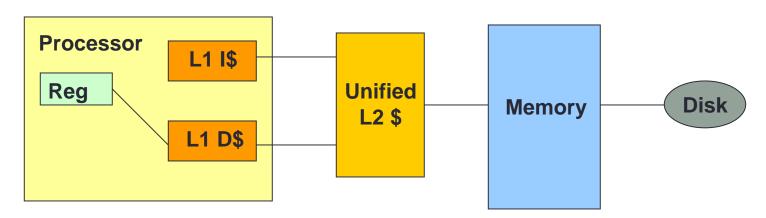
8. Exploration: Multilevel Cache

Options:

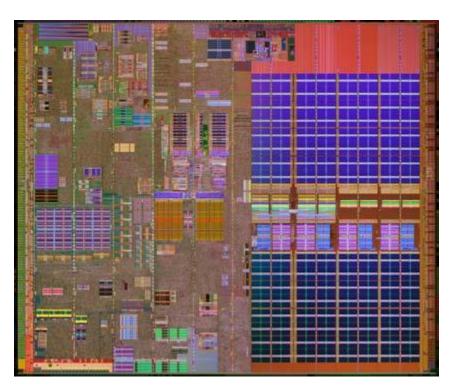
Separate data and instruction caches, or a unified cache

Sample sizes:

- L1: 32KB, 32-byte block, 4-way set associative
- L2: 256KB, 128-byte block, 8-way associative
- L3: 4MB, 256-byte block, Direct mapped



8. Exploration: Intel Processors

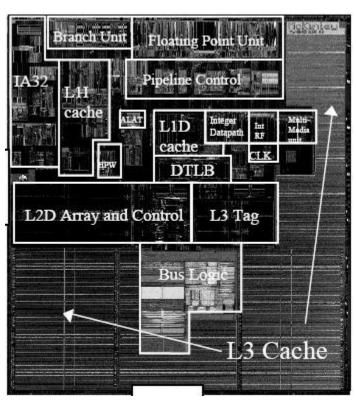


Pentium 4 Extreme Edition

L1: 12KB I\$ + 8KB D\$

L2: 256KB

L3: 2MB



Itanium 2 McKinley

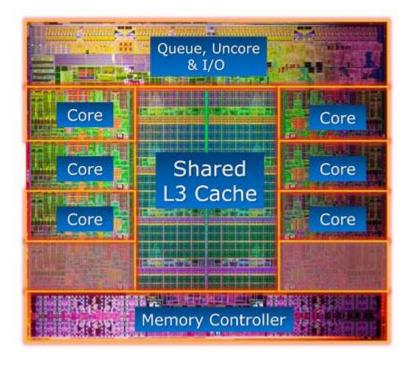
L1: 16KB I\$ + 16KB D\$

L2: 256KB

L3: 1.5MB - 9MB

8. Exploration: Trend: Intel Core i7-3960K

Intel® Core™ i7-3960X Processor Die Detail



Intel Core i7-3960K

per die:

- -2.27 billion transistors
- -15MB shared Inst/Data Cache (LLC)

per Core:

- -32KB L1 Inst Cache
- -32KB L1 Data Cache
- -256KB L2 Inst/Data Cache
- -up to 2.5MB LLC

Reading

- Large and Fast: Exploiting Memory Hierarchy
 - Chapter 7 sections 7.1 7.2 (3rd edition)
 - Chapter 5 sections 5.1 5.2 (4th edition)



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