

Bi-Directional Tilting Quadrotor

An investigation into the overactuatedness thereof



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Declaration

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Abstract

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The aim of this project is to design, simulate and control a novel quadrotor platform which can articulate all 6 Degrees of Freedom by vectoring its' propellers thrust. To achieve this the air-frames' structure needs to be able redirect those thrust vectors to any given orientation. This means it has to be able to dynamically change its structure during flight, rotating the thrust vectors whilst still maintaining stable attitude & position control in spite of the bodies relative motion. In sight of the required articulation of the thrust vectors, the proposal is 2 additional axes of actuation, introduced such that each lift propeller can be pitched or rolled. The implementation of such actuation, to what is otherwise a well understood and researched platform, results in an over-actuated control problem. The allocation of which is the primary contribution of this paper with novel elements of non-linear control treatment for UAV quadrotor airspace platforms.

The structure of the research first presents the design which the subsequent dynamics and control are derived with respect to. Thereafter the kinematics associated with rigid bodies are developed and the unique effects which apply to the design; gyroscopic, aerodynamic and the like, are investigated and incorporated into the dynamics. Hence control algorithms and a simulation environment are developed around that holistic model, which includes the implication of discretization on the system. The relative performance of the controllers are evaluated and standard performance metrics of attitude and position controllers are discussed. Finally the design is built and tested using readily available Radio-Control components and a conclusion is made thereon.

The purpose of the investigation is the practicality and feasibility of such a design, most importantly weather the added complexity of the mechanical system is a worthwhile compromise for the added degrees of control actuation. As a result the outcome of the build is weather its' both economically (cost and control effort) feasible and practical to build such a prototype. The design and control treatment presented here are by no means the most optimal or exhaustive solutions, focus is placed on the system as a whole and not just one aspect of it.

Acknowledgements

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Chapter 1

Introduction

1.1 Foreward

1.1.1 A Brief Background to the Study

Currently the most popular topic for control and automation research is the around quadrotor UAV, specifically its' attitude control. A wide range of work has been done on quadrotors and their attitude control, mostly designing control systems around a stable trim point adjacent to the inertial frames origin, to which the control algorithm always tends to. The highly coupled non-linear dynamics for a rigid bodies linear and angular motions arise as a result of gyroscopic torques [3.2.1] and Coriolis accelerations [3.2.2]. Such affects are can be linearised around the origin when they can be approximated to $\approx \vec{0}$, thus decoupling the system and allowing for traditional SISO control techniques to be applied.

As every quadrotor based research paper will tell you, the current interest in them is as a result of the recent emergence in availability of MEMS systems and low-cost ARM microprocessor sectors, allowing the on-board flight computer to perform complicated control calculations and state estimation in real time. As a result this led to development and expansion in the field and introduction of a large range of hobbyist solutions, from professionally made units to DIY kits, with large room for modification, depending on how much your wallet can spare. A rapidly growing enthusiast community was borne from this progression, meaning the environment was no longer open only to those willing spend lots of money.

The avenues of potential applications for both fixed wing and VTOL UAVs is expansive and the quadrotor configuration provides a mechanically simple and low cost platform on which to test advanced aerospace control algorithms. Considering that commercial drone usage is such an emerging sector; especially in Southern Africa following the revision of aviation laws [26] which have legalized the use of UAVs for commercial application, any research into a non-trivial aspect of the field is extremely valuable.

Large scale quadrotor, hexrotor and even octorotor UAVs are a popular intermediate choice for aerial cinematography. Whilst still expensive, the cost of a commercial drone like the SteadiDrone Maverik [20] is far less exorbitant than the cost of chartering a helicopter to achieve the same panoramic aerial scenes or on-site inspections. Another interesting application for UAVs is in the agricultural sector, introducing crop dusting drones instead of the traditional bi-planes which perform the same job. One problem which hinders the progress of the commercial drone sector is that of inertia, specifically when scaling up any vehicle, its performance is adversely affected, due to the increased mass inertial effect.

1.1.2 Research Questions & Hypotheses

The difficulty with a quadrotors' control is that fundamentally it's unstable and under-actuated, having only 4 controllable inputs (each propellers rotational speed and hence net lift force) available to manipulate all 6 degrees of freedom (linear X-Y-Z position and angular Pitch, ϕ , Roll, θ and Yaw, ψ rotations). The resulting solution, whose derivation is explored in Appendix A, is to control the perpendicular heave thrust, \vec{T} , and angular torques about each axis, $[\tau_\phi \ \tau_\theta \ \tau_\psi]^T$. So the attitude control problem of a quadrotor is a zero set point problem as any other attempt to track attitude can't be achieved.

The aim of this project is to then implement dynamic set point tracking of a quadrotors' attitude and position by solving the problem of its' inherent under-actuation. Inspired by Boeing/Bell Helicopters' V22 Osprey and the tilting articulation of its' propellers, the prototype on which this paper is focused introduces two additional actuators for each of the four quadrotors' lift propellers. Specifically, adding rotations about the X and Y axes for each of the propellers. The resultant is a vectored thrust force which exists in 3-Dimensions with respect to the body frame, unlike a traditional quadrotor helicopter which has a bound perpendicular lift force. The control problem is then posed as the design of net forces, $\vec{F}_{net} = [F_x \ F_y \ F_z]^T$, and torques, $\vec{\tau}_{net} = [\tau_\phi \ \tau_\theta \ \tau_\psi]^T$, such that for any given trajectory, X_d , the error state, $X_e = X_d - X$, asymptotically tends to $\vec{0}$.

$$\lim_{t \rightarrow \infty} X_e = \vec{0} \ \forall X \in \mathbb{R}^n \quad (1.1)$$

Where n is the degrees of freedom. The over-actuation brings about the need for a control allocation scheme which distributes the 6 commanded system inputs (net torques and forces) among the actuator set (12 actuators) in order to optimize some objective function secondary to that of Eq:1.1.

Part of the control research question is the multivariate treatment of the system without making any simplifications to the non-linear dynamics involved in the quadrotors motion or making any assumptions about its' operational conditions. The standard linearisations usually applied to the quadrotors control plant won't hold true for the more aggressive angular maneuvers envisioned for this prototype. Inherent to this is the expansion and simulation of existing kinematic models describing an aerial body and applying them to a quadrotor vehicles' motion. Thereafter, design, development and control of this new actuator suite to be implemented on such a quadrotor platform. The final key outcomes for the project are the simulation analysis and prototype construction of the proposed design.

Introducing relative motion within an unconstrained body is going to produce a lot of unwanted dynamics. The obvious consequences of which are the inertial and gyroscopic responses. Pitching a rotating propeller is going to react much like a Control Moment Gyroscope, [27]. A less trivial result is the aerodynamic torque produced from the propellers aerofoil profile. Such induced responses occur in obscure planes, normal to whatever the propellers thrust direction is. These aspects are normally canceled out because a regular quadrotors' propellers all have the same plane of rotation. Because of these factors, a plant dependent control solution needs to be used to compensate for these dynamics, which if left unaccounted for would cause instability.

1.1.3 Significance of Study

Given the of popularity of quadrotor platforms as research tools, any research which furthers the general body of knowledge on such vehicles is going to be valuable to the community as a whole. With that being said, for the proposed systems identification and control treatment (design and allocation), a generic and modular approach is adopted. The intention is that applicability here falls not only within the UAV and quadrotor sections but to any other aerospace and freely rotating bodies needing attitude control, such as orbital satellites or underwater vehicles. Or perhaps further and more in-depth

research can be done on a system subset without compromising the functionality of the remainder of the system.

One possible improvement that the investigation could yield is a higher actuator bandwidth and thus a faster control response for larger aerospace bodies. A standard quadrotor uses differential thrust to develop a torque about its' body which suffers a slow inertial deceleration when changes speeds. Prioritizing pitching the propellers principle plane of rotation away rather than changes the propellers speed could improve response. This depends on what or how the allocator block is prioritized, presented in 4.3.

At the time of writing, there appears to be only two other projects which have been published that bear some similarity. Discussion is given later in Section ?? where comparison is made to justify how they are different and why this project is still unique and perhaps even novel. The concepts developed here are unique to the application of quadrotor control, mostly having been developed in the late 90s for satellite control. Similarly, the non-linearity with which the control solution is developed is uncommon with respect to UAV control.

Whilst the control treatment does close the position and attitude control loops, there is no discussion of trajectory or flight path planning. Such topics are well discussed and it is the Authors opinion that once closed loop position and attitude control has been achieved, the control algorithms can be adjusted to account for velocity and acceleration set point tracking to be used with nodal way point planning. The heuristics involved with flight path planning are well documented elsewhere and implementation of them is an academic task.

1.1.4 Scope and Limitations

Scope

The requirements of this project start with a theoretical investigation and result in a final complete prototype. So there are investigations in kinematic derivations and control theory associated with non-linear systems as well as electronic system design, which physically implements the control algorithms. The scope of control is limited not only to attitude but position control too. The kinematic derivations which precede the control design are all done in order to identify the plant needed to be controlled and its' associated dynamics that need to be compensated for.

As mentioned before in the antecedent ,Section 1.1.3, trajectory & flight path planning are not deeply considered here. The kinematic derivation for a 6-DOF body is wholly applicable to any dynamic (rigid or otherwise) aerospace body, although some particular standards are used [sic ZYX Euler Aerospace Sequence, ??]. Similarly the control of the plant is that of a non-linear multivariate control aided and justified by Lyapunov theorem, alternative solutions through Model Predictive Control or Quantitative Feedback Theory aren't presented here but remain open to further investigation. Standard fare for quadrotor control is feedback linearisation of the plant around a trim point to decouple it and apply SISO techniques, whilst a derivation of the linearisation is presented in A, there are no further discussions beyond that. Comparison between attitude set point tracking proposed here and normal zero-set point attitude control of fixed rotor quads' is difficult as the fundamental objects are in stark contrast with one another.

Arguably the most important, and perhaps novel, aspect of this project is the controller allocation. Seeing as the system has 12 controllable inputs and 6 possible responses to that input, hence system is classified as over-actuated. Ergo, there needs to be some logical process to how those 12 inputs are articulated and combined to achieve the desired 6 movements. Applicable techniques are first investigated in section ?? and compared before a final solution is presented. As with most of this report, it is by no means a comprehensive investigation of all possible solutions but rather an analysis

of the sub-set of problems and design of what is regarded as a logical and appropriate solution.

With regards to the actual prototype design [??], its' assumed that certain aspects are a given certainty. Namely the state estimation, updated through a 4-camera positioning system fused with a 6-axis IMU through Kalman Filtering, is assumed to be precise and readily disposable at a consistent 50 Hz. Hence state estimation is presented but bereft of intricate detail, this is another topic which has been well documented elsewhere.

Limitations

The most obvious constraining factor for this project is the cost of the prototype. Unfortunately, funding that awards freedom of choice with regards to components used is unaviable. So to keep the cost low, off-the-shelf components are used where possible, otherwise 3D printed and laser cut parts are fabricated. Most parts are sourced through HobbyKing [13] and kept to a strict budget, more details on the design are discussed in Chapter ??.

A self imposed limitation of the design is to only make use of Turnigy DST-700 motors, the department has a surplus of these from previous projects. One consequence of this is that the net thrust disposable for actuation is limited to around 800g per motor (see ??). Everything else must be designed around this limitation to ensure the control algorithm doesn't command over-saturation of the motor actuations. Saturation conditions are derived in ?? in more detail.

Another physical design decision taken, to reduce costs, is to use 180 °rotatable servos, ideally 360 °or continuous rotation servos could provide a further range of motion but they would increase the cost of the prototype exponentially. The best solution for the added articulation would be to use closed loop DC motor control, as with commercial camera stabilizing gimbals, but the I/O requirements from the flight control μC were already a major limitation.

Some of the discretionary elements of the whole system will limit performance and are mitigated where possible. For example an analogue servo with an update rate of 20 Hz will have a 1 ms zero-order hold response over and above the existing servo motor dynamics. This can be improved by using digital servos with an update rate of 333 Hz update. The requirements by the flight controller used are quite cumbersome, apply PWM outputs to 12 different actuators as well as receiving command updates from a ground control station.

1.2 Literature Review

1.2.1 Existing & Related Work

The field of transformable aerospace frames is not necessarily a new one, with many commercial examples having seen a lot of success over their life time. The most notable tilting-rotor application is that of the Boeing/Bell V22 Osprey aircraft. Having the ability to pitch its' two lift propellers forward to aid in translational flight after the VTOL manoeuvre has been completed. In addition to this there have been a handful of papers published on similar tilting bi-rotor UAVs' 1.1¹ for research purposes.

The particular research field is termed Opposed Active Tilting actuation, wherein the design either adopts an *oblique* 45°tilting axis relative to the body; [4, 6, 12], or a tilting axis adjacent to the body, *opposed lateral tilting*; [14, 22]. More advanced papers have proposed introducing dual-axis tilting in which each propeller can pitch and roll, [2, 11]. The control of which ranges from basic PD [4] and PID [22] to Ideal and Adaptive backstepping controllers, presented in [14] and [15] respectively.

¹Image used from G. Gress: [11]

In an interesting progression from the norm, Lee et al, [16], proposed a PID co-efficient selection algorithm Swarm-Optimization technique which iteratively searched for the globally optimized design. However their performance criterion was a basic ITAE term and not anything more unique involving effects specific to flight.

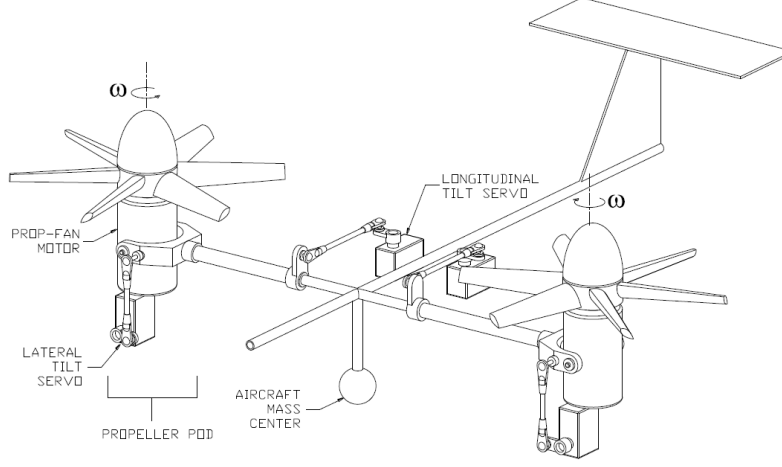


Figure 1.1: General Structure for Opposed Tilting Platform

Quadrotor UAVs' mostly have a fixed and rigid body with no capacity for relative movement. Some hobbyists and enthusiasts introduce an angled bracket to pitch the motors in order to improve forward translational speeds. This however adds no extra actuation and reliance is put on the autopilot flight controller to account for the actuator changes. An expensive commercial quadrotor which has some transformation capability is the Inspire 1 [8], made by Shenzhen DJI Technologies who are more commonly known for their Phantom drone.

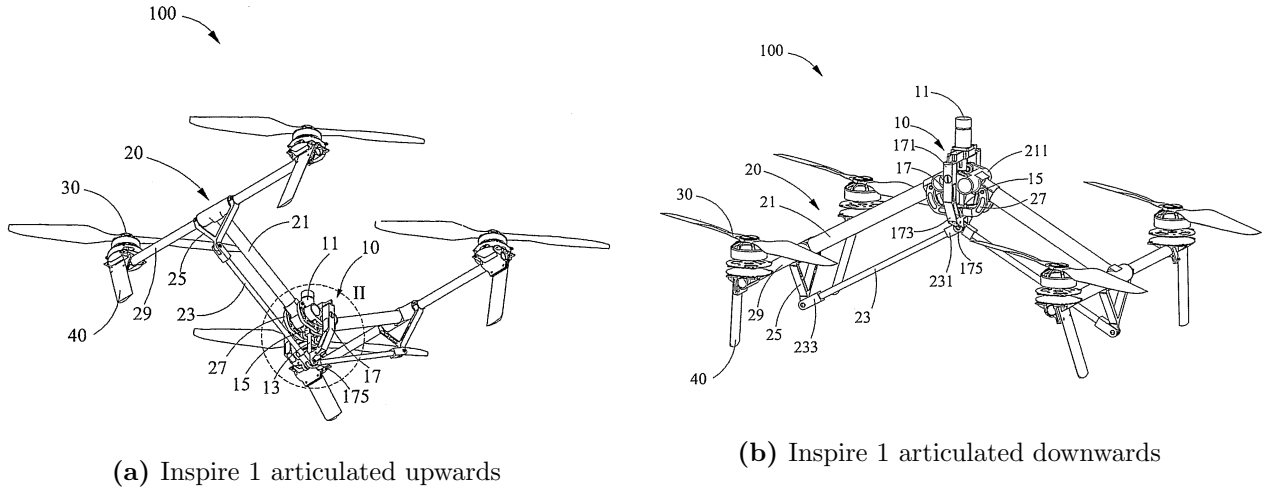


Figure 1.2: DJI Inspire 1

The Inspire can articulate its' supporting arms up and down [Fig: 1.2 ²]. The purpose of such movements is to both alter the center of gravity and further expose the belly mounted camera gimbal to achieve panoramic sequences. The change in the center of gravity affects the bodies inertial response to angular acceleration (reducing the magnitude of the mass moment of inertia about each axis). However the range of "transformation" the frame can undergo is just limited to articulating the arms up and down.

²Both images were sourced from the drones patent, held by SZ DJI Tech Co [28]

It is worth mentioning that hardly any research has been done into aerospace frames that can dynamically transform their structure during flight. Rigid body dynamics are mostly used to solve the control problem so introducing relative motion within the body frame during flight complicates matters. In two reports, [25], [24], M. Ryll et al adapted and tested a QuadroXL from MikroKopter [10] which has a single axis of tilt aligned with the X-axis to change the direction of the propellers. Their dynamic equations neglect any second order aerodynamic responses and the gyroscopic and inertial effects. The simplified solution also fails to address the inherent singularity associated with their Rotation Matrix solution. A similar implementation of single axis tilting was done by Nemati et al [21] but had a far more brief kinematic derivation and only featured a simulation as proof of concept.

Lastly, the most advanced implementation of over actuation for quadrotor control is that of Pau Segui Gasco [9], which was a dual presented MSc project with Yazan Al-Rihani [1]. At the time of writing, this would appear to be the only published project which bears semblance to the proposed concept of this paper. The work was split between the two authors who completed the control/electronic design and the mechanical platform design for their respect MSc projects. Shown in Fig:1.3 ³, their dual-axis articulation is achieved with an adapted helicopter tail bracket, reducing the mass of the articulated component but limiting the range of rotation. Their justification for adding extra actuators is to ensure control reliability even in the event of losing up to 2 rotors.



Figure 1.3: Dual-axis tilt-rotor mechanism

In the control and dynamics derivation, Gesco et al provides an excellent model for 6-DOF motion. As is standard fare with quadrotor papers, the dynamic equations are linearised around a trim point parallel to the inertial frame to allow for SISO control analysis of the system. It is important to note the difference between this papers' prototype and the Bi-Directional Tilting Quadrotor Prototype developed in Chapter [?] ,the added actuation in [9] is not used to vector thrust produced but rather to leverage induced gyroscopic torques as an actuation input. The control allocation technique developed is wholly unique, fusing differential torque and torques induced from the relative motion with a (simplified) weighted pseudo inverse method. This all resulted in a control plant with a far higher control bandwidth.

In practice the gyroscopic response (see Section ??), or rather regarding the spinning propellers as control moment gyroscopes [27], has a response two orders of magnitude smaller than that of the inertial response from pitching the mass of the motor & propeller combination. And so such an inertial response is far more important to account for, weather it be compensation or exploitation, that the gyroscopic torques induced.

Another interesting project is that by G.Gres [11] which attempts to use oblique active tilting of a bi-rotor helicopter to induce gyroscopic torques. Whilst the eVader prototype referred to in the

³Development of a Dual Axis Tilt Rotorcraft UAV: Modelling, Simulation and Control [9]

paper has dual axis tilting, the actuators are coupled together making the tilt axis 45° to the bodies' frame. The paper discusses in depth the mechanical system identification aspects of the prototype but, however, gives no insight into attitude control. The author instead discusses the dynamic equations of motion applicable in different flight modes. Whilst the later is irrelevant to quadrotor attitude control, the derivation of induced gyroscopic torque responses as a result of pitching the propellers from their principle plane of rotation is highly pertinent and appears to be the most accurate and well thought out of its' kind.

1.2.2 Notable Quadrotor Control Implementations

The majority of papers based on Quadrotor research, [23], [5], [18] all make the assumption that the coupled non-linear dynamics can be linearised. This assumption holds true as long as the angular rate, $\vec{\Omega}$ is small and the inertial matrix, \mathbb{I} is a diagonal matrix. As a consequence the gyroscopic term, (see ??) which manifests itself as: $\tau_{gyro} = \vec{\Omega} \times \mathbb{I} \vec{\Omega} \approx \vec{0}$. This decouples the angular equations of motion and similarly the coriolis acceleration term becomes negligible; $-\vec{a} \times \vec{\Omega} \approx \vec{0}$.

A PID structure for attitude controllers are the norm, with [5], [23], [24] all implementing standard PID controllers and even [21] using only a PD controller despite having an over-actuated platform. Even commercial hardware flight controllers like Arducopter [3] and OpenPilot [17] (whose firmware source code is available at [7]) all use PID structures with some manner of feedforward or feedback elements, [19].

However, in [5] the controller coefficients were selected through a learning social algorithm, a particle swarm optimization, instead of the regular "tuning" by hand.

As a result of the inherent singularity with using Rotation Matrices to represent attitude,

Chapter 2

Prototype Design

2.1 Conventions Used

2.1.1 Reference Frames Convention

2.1.2 Motor Axis Layout

2.2 Design

2.2.1 Gimbal Articulation

2.2.2 Inertial Matrix Function

2.2.3 Overall Aspects

Vibration Damping

Duct

Landing Skids

Motors & ESCs

2.3 System Layout

Chapter 3

Kinematics & Dynamics

3.1 Rigid Body Dynamics

3.1.1 Lagrange Derivation

3.1.2 Rotation Matrix Peculiarities

3.1.3 Quaternion Dynamics

3.1.4 The Unwinding Problem

3.2 Non-linearities

3.2.1 Gyroscopic Torques

3.2.2 Coriolis Acceleration

3.2.3 Inertial Matrix

3.3 Aerodynamics

3.3.1 Thrust Forces & Propeller Torques

3.3.2 Drag

3.3.3 Coning & Flapping

3.3.4 Vortex Ring State

3.4 Consolidated Model

Chapter 4

Control Treatment

Control Plant & Discussion

Control Plant Inputs

Model Dependent & Independent Controllers

4.1 Attitude Control

4.1.1 The Attitude Control Problem

4.1.2 Quaternion Based Controllers

PD Controller

Auxilliary Plant Controller

PID Controller

4.1.3 Non-linear Controllers

Ideal Back-stepping Controller

Adaptive Back-stepping Controller

Lyupanov Derived Ideal Controller

4.2 Position Control

4.2.1 Backstepping Position Controller

4.3 Controller Allocation

4.3.1 Non-linear Plant Control Allocation

4.3.2 Pseudo Inverse Allocator

Chapter 5

Simulations & Results

5.1 Controller Tuning

5.1.1 Partical Swarm Based Optimization

5.1.2 Performance Metric

5.1.3 Global & Local Minima

5.1.4 Fmincon Differences

5.2 Simulation Block

5.3 Optimized Controller Comparisons

5.3.1 Allocator Performance

5.3.2 Attitude Control Results

5.3.3 Autopilot Outcome

Appendix A

Standard Quadrotor Dynamics

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