

**MA1125 – Calculus**

**Homework #6**

due Thursday, Nov. 1

1. Find the global minimum and the global maximum values that are attained by

$$f(x) = x^3 - 6x^2 + 9x - 5, \quad 0 \leq x \leq 2.$$

2. If a right triangle has a hypotenuse of length  $a > 0$ , how large can its area be?
3. A balloon is rising vertically at the rate of 1 m/sec. When it reaches 48m above the ground, a bicycle passes under it moving at 3 m/sec along a flat, straight road. How fast is the distance between the bicycle and the balloon increasing 16 seconds later?
4. Find the linear approximation to the function  $f$  at the point  $x_0$  in the case that

$$f(x) = \frac{x^3 - 2x + 4}{x^2 + 2}, \quad x_0 = 0.$$

5. Show that  $f(x) = x^3 - 4x + 1$  has two roots in  $(0, 2)$  and use Newton's method with initial guesses  $x_1 = 0, 2$  to approximate these roots within two decimal places.

- This assignment is due by Thursday noon, either in class or else in my office.
- Write your name and course (Maths, TP, TSM) on the first page of your homework.
- NO LATE HOMEWORK WILL BE ACCEPTED.