

**Advanced Calculus**  
**MA1132**

**Tutorial Exercises 10**

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**To be completed before and during tutorials of Friday, 12. April**

1. Use cylindrical coordinates to find the volume of the solid that is inside the surface  $r^2 + z^2 = 20$  but is not above the surface  $z = r^2$ .
2. Use spherical coordinates to find the volume of the solid enclosed by the sphere  $x^2 + y^2 + z^2 = 4$  and the planes  $z = 0$  and  $z = 1$ .
3. Use the transformation  $u = \frac{y}{x}$ ,  $v = xy$  to find  $\iint_R xy^3 dA$ , where  $R$  is the region in the first quadrant enclosed by  $y = x$ ,  $y = 3x$ ,  $xy = 1$  and  $xy = 4$ .
4. Use the transformation  $u = xy$ ,  $v = yz$ ,  $w = xz$  to find the volume of the region in the first octant that is enclosed by the hyperbolic cylinders  $xy = 1$ ,  $xy = 2$ ,  $yz = 1$ ,  $yz = 3$ ,  $xz = 1$  and  $xz = 4$ .