



Istituto Nazionale di Fisica Nucleare



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DEGLI STUDI
DI MILANO



Including QED corrections in PDFs fits

The NNPDF4.0QED PDFs set

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Summary

Introduction

Adding QED to a PDF fit

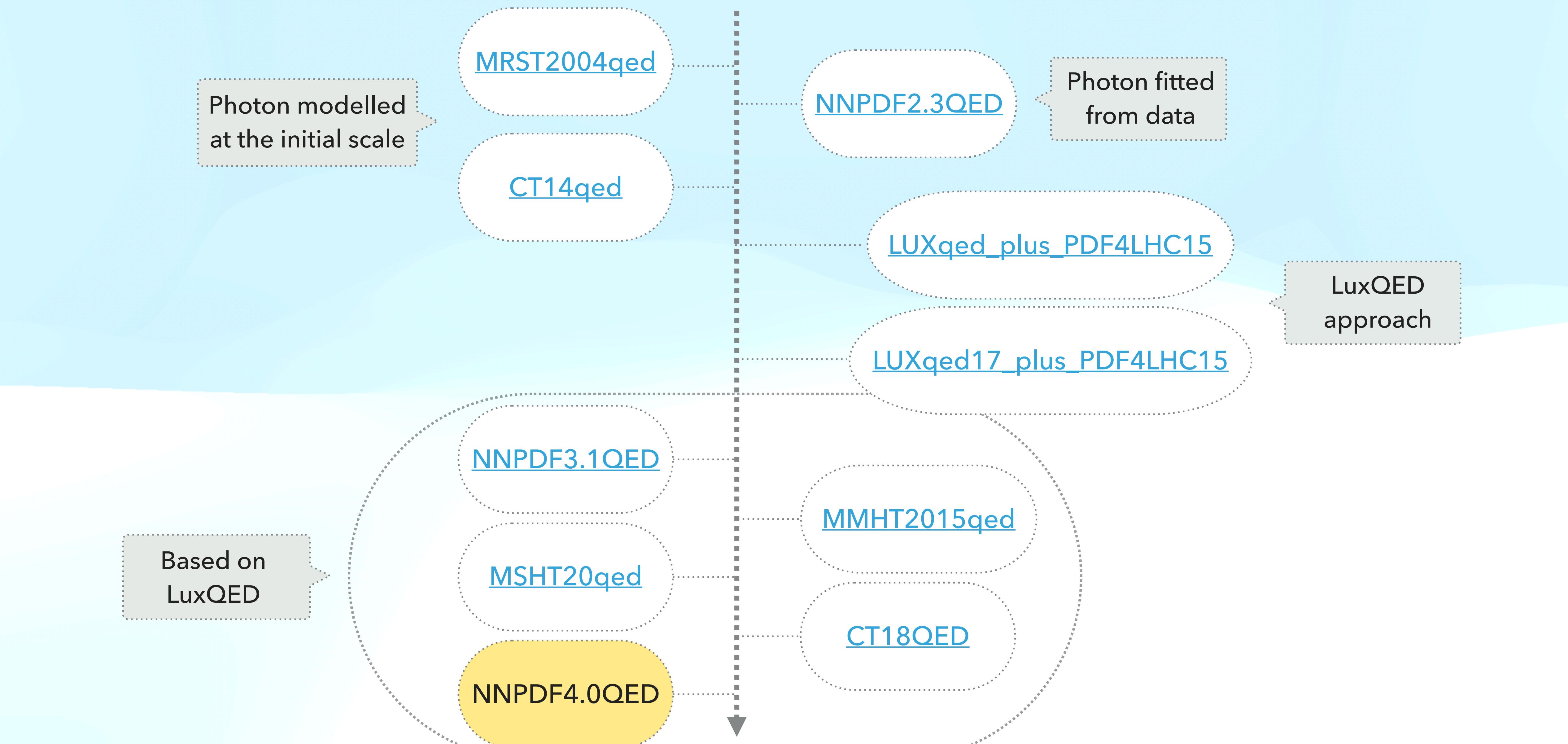
Results

Impact on phenomenology

Conclusions

INTRODUCTION

Introduction: QED fits done in the past



ADDING QED TO A PDF FIT

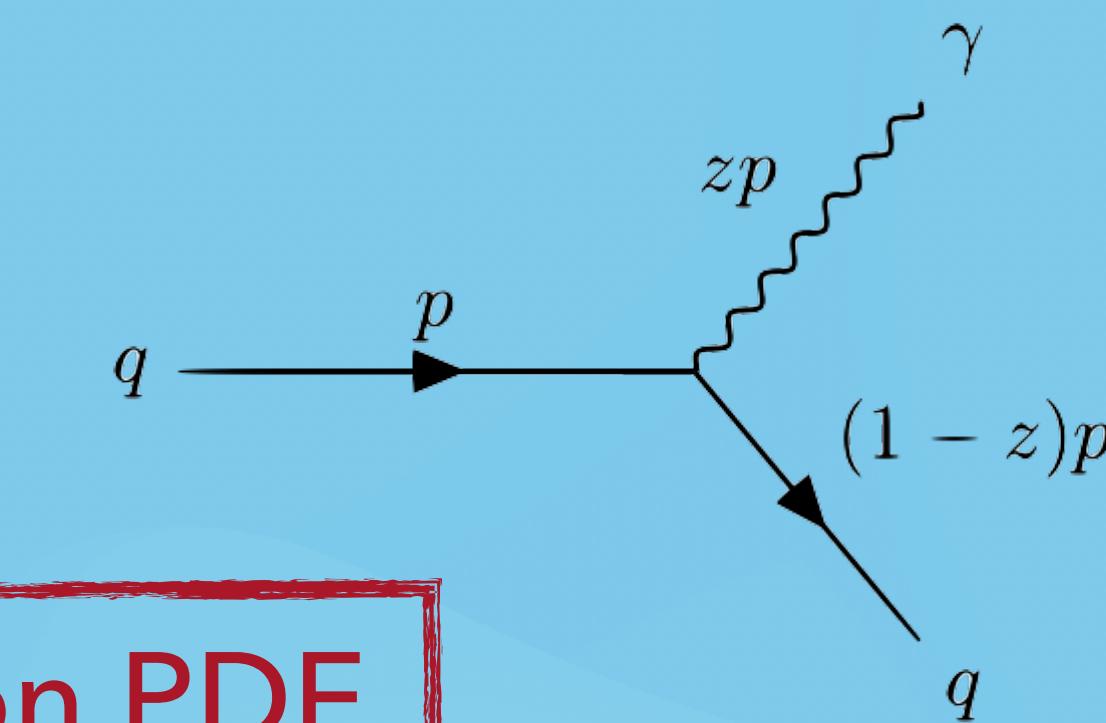
Adding QED: motivation

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$$\alpha \sim \mathcal{O}(\alpha_s^2) \sim \mathcal{O}(1\%)$$

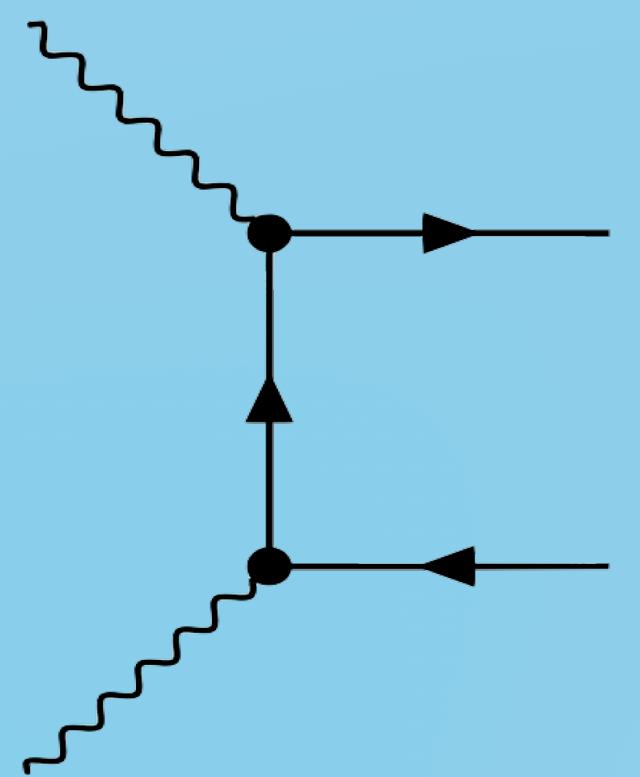
percent correction

quarks can emit photons



we get a photon PDF

For some processes we can't neglect photon induced contributions



starts at $\mathcal{O}(\alpha_s^0)$

In some kinematical regions QED corrections are important

see phenomenology section

Adding QED: corrections to DGLAP

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$$\mu^2 \frac{d}{d\mu^2} f_i(x, \mu^2) = \sum_{j=q, \bar{q}, g, \gamma} \int_x^1 \frac{dz}{z} P_{ij} \left(\frac{x}{z}, \alpha_s(\mu^2), \alpha(\mu^2) \right) f_j(z, \mu^2) \quad i = q, \bar{q}, g, \gamma$$

$$P_{ij}(\alpha_s, \alpha) = P_{ij}(\alpha_s) + \tilde{P}_{ij}(\alpha_s, \alpha)$$

$\alpha_s P_{ij}^{(0)} + \alpha_s^2 P_{ij}^{(1)} + \alpha_s^3 P_{ij}^{(2)} + \dots$

pure QCD terms

Gluon couples in the same way to all quarks

pure QED and QCD \otimes QED terms

$$\alpha P_{ij}^{(0,1)} + \alpha_s \alpha P_{ij}^{(1,1)} + \alpha^2 P_{ij}^{(0,2)} + \dots$$

Photon couples in different ways to up-like and down-like quarks

More difficult to diagonalize
(see next slide)

Solving the system

Pure QCD case

$$\mu^2 \frac{d}{d\mu^2} \begin{pmatrix} g \\ \Sigma \end{pmatrix} = \begin{pmatrix} P_{gg} & P_{gq} \\ P_{qg} & P_{qq} \end{pmatrix} \otimes \begin{pmatrix} g \\ \Sigma \end{pmatrix}$$

$$\mu^2 \frac{d}{d\mu^2} V = P_{ns,v} \otimes V$$

$$\mu^2 \frac{d}{d\mu^2} f_{ns,\pm} = P_{ns,\pm} \otimes f_{ns,\pm}$$

$$\Sigma = \sum_{i=1}^{n_f} q_i^+ \quad V = \sum_{i=1}^{n_f} q_i^- \quad f_{ns,\pm} = \begin{cases} u^\pm - d^\pm \\ u^\pm + d^\pm - 2s^\pm \\ u^\pm + d^\pm + s^\pm - 3c^\pm \\ u^\pm + d^\pm + s^\pm + c^\pm - 4b^\pm \\ u^\pm + d^\pm + s^\pm + c^\pm + b^\pm - 5t^\pm \end{cases}$$

$$q^\pm = q \pm \bar{q}$$

QCD \otimes QED case

$$\mu^2 \frac{d}{d\mu^2} \begin{pmatrix} g \\ \gamma \\ \Sigma \\ \Sigma_\Delta \end{pmatrix} = \mathbf{P}_s \otimes \begin{pmatrix} g \\ \gamma \\ \Sigma \\ \Sigma_\Delta \end{pmatrix}$$

$$\mu^2 \frac{d}{d\mu^2} \begin{pmatrix} V \\ V_\Delta \end{pmatrix} = \mathbf{P}_v \otimes \begin{pmatrix} V \\ V_\Delta \end{pmatrix}$$

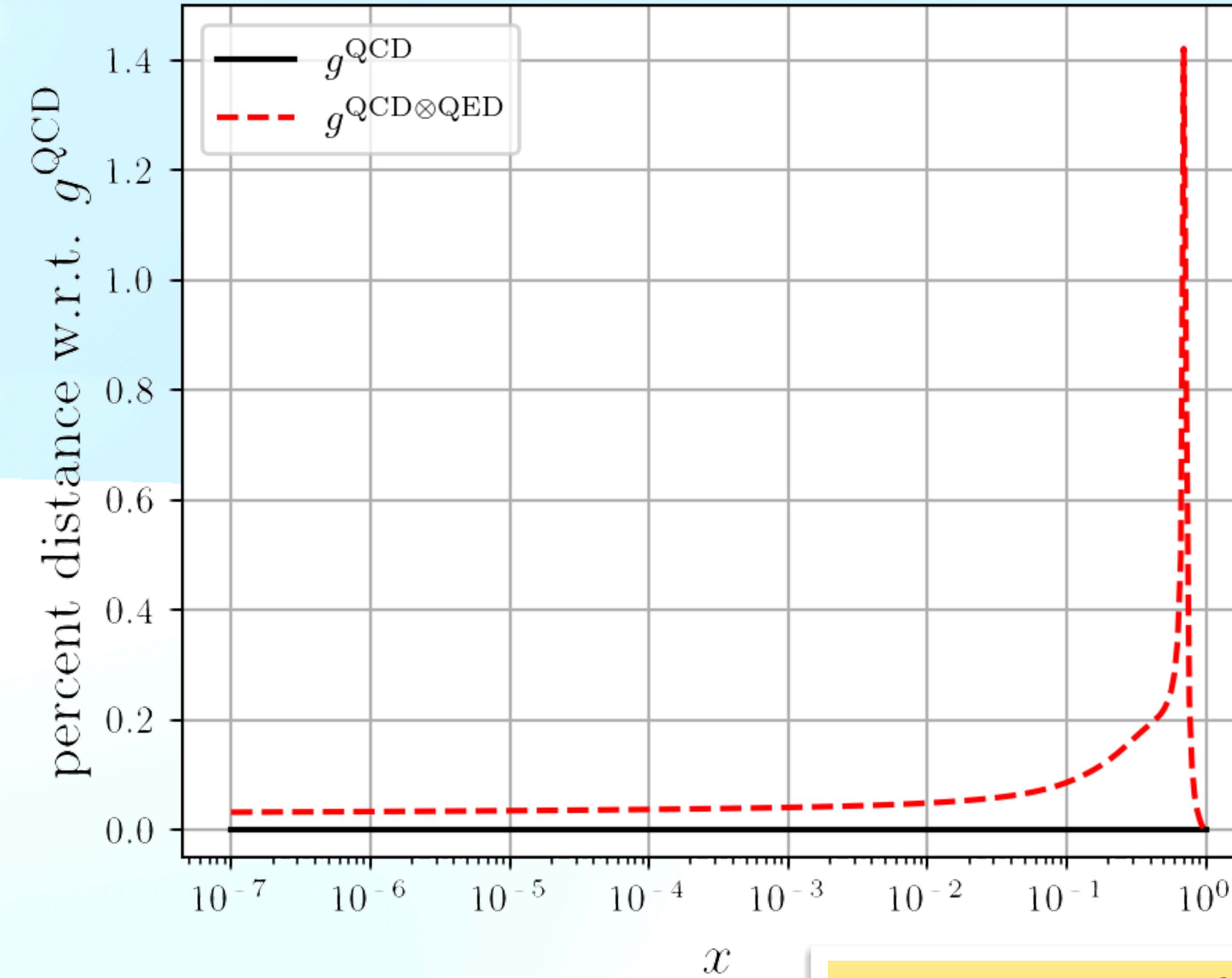
$$\mu^2 \frac{d}{d\mu^2} f_{ns,\pm}^{u/d} = \left(P_{ns,\pm} + \tilde{P}_{ns,\pm}^{u/d} \right) \otimes f_{ns,\pm}^{u/d}$$

$$f_{ns,\pm}^u = \begin{cases} u^\pm - c^\pm \\ u^\pm + c^\pm - 2t^\pm \end{cases} \quad f_{ns,\pm}^d = \begin{cases} d^\pm - s^\pm \\ d^\pm + s^\pm - 2b^\pm \end{cases}$$

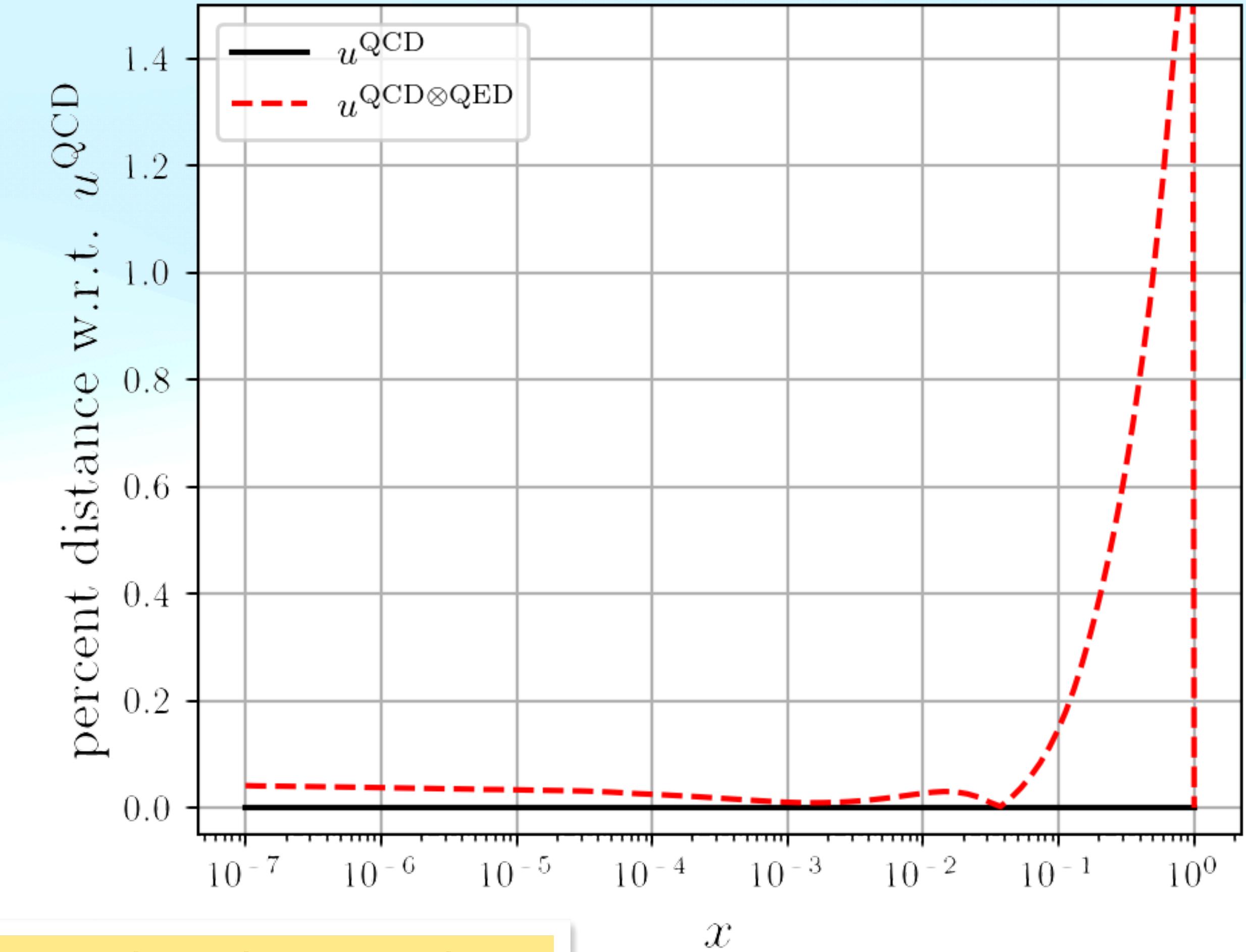
$$\Sigma_\Delta = \frac{n_d}{n_u} \sum_{i=1}^{n_u} u_i^+ - \sum_{i=1}^{n_d} d_i^+ \quad V_\Delta = \frac{n_d}{n_u} \sum_{i=1}^{n_u} u_i^- - \sum_{i=1}^{n_d} d_i^-$$

Numerical results

$g, Q_0=5 \text{ GeV} \rightarrow Q=100 \text{ GeV}$



$u, Q_0=5 \text{ GeV} \rightarrow Q=100 \text{ GeV}$



small correction for quark and gluon...but
needed for the evolution of the photon!

- * Photon PDF is obtained from LuxQED approach [Manohar, Nason, Salam, Zanderighi, 2016]

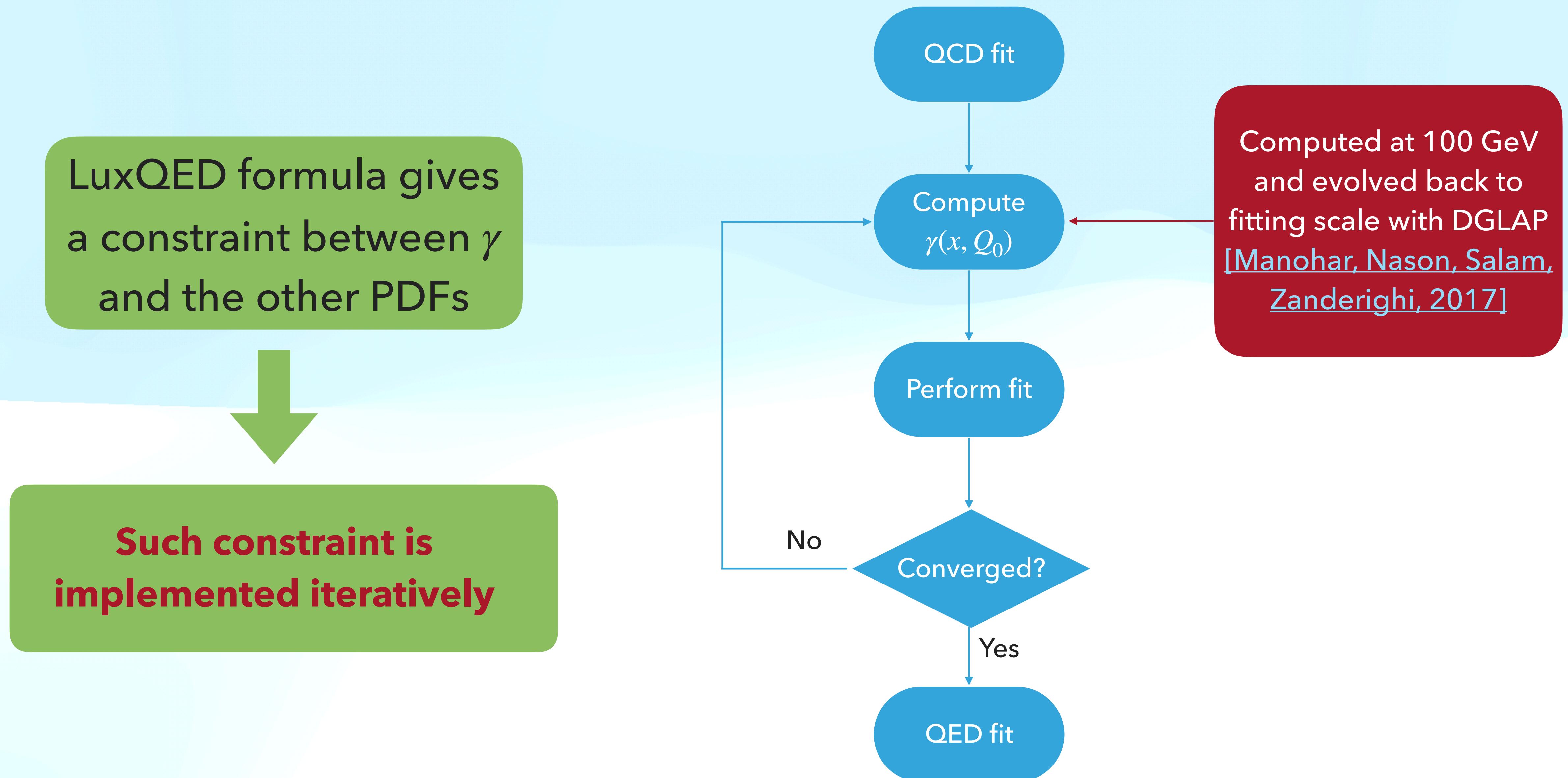
$$x\gamma(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{dz}{z} \left\{ \int_{\frac{m_p^2 x^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{dQ^2}{Q^2} \alpha^2(Q^2) \left[\left(zP_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L(x/z, Q^2) \right] \right. \\ \left. - \alpha^2(\mu^2) z^2 F_2(x/z, \mu^2) \right\}$$

- * γ modifies the momentum sum rules:

$$\int_0^1 dx x \left(\Sigma(x, Q^2) + g(x, Q^2) + \gamma(x, Q^2) \right) = 1$$

$$F_{2,L} = \sum_i C_{2,L,i} \otimes f_i$$

γ depends on the other PDFs!!



RESULTS OF THE FIT

No photon-initiated contributions in theory predictions

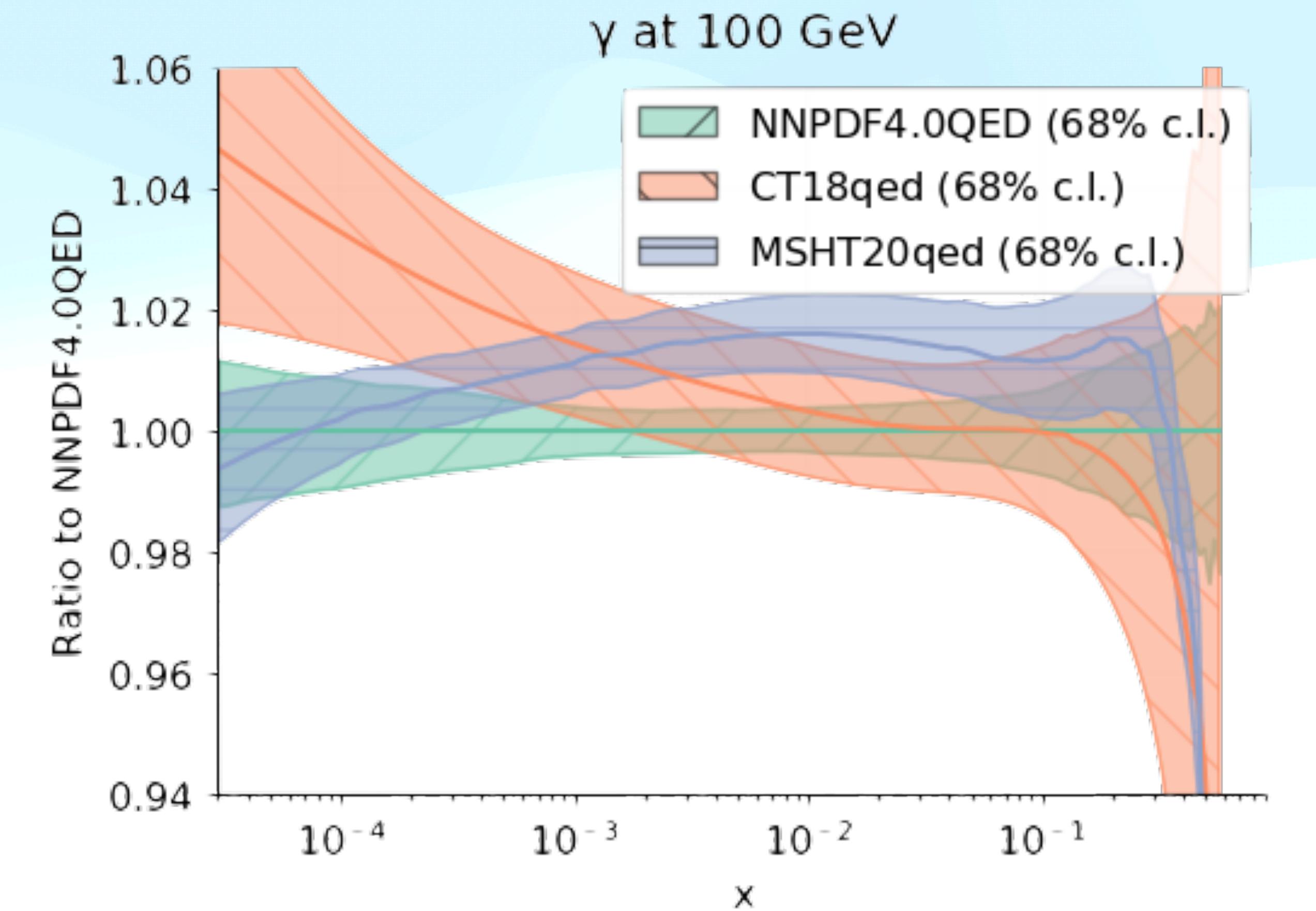
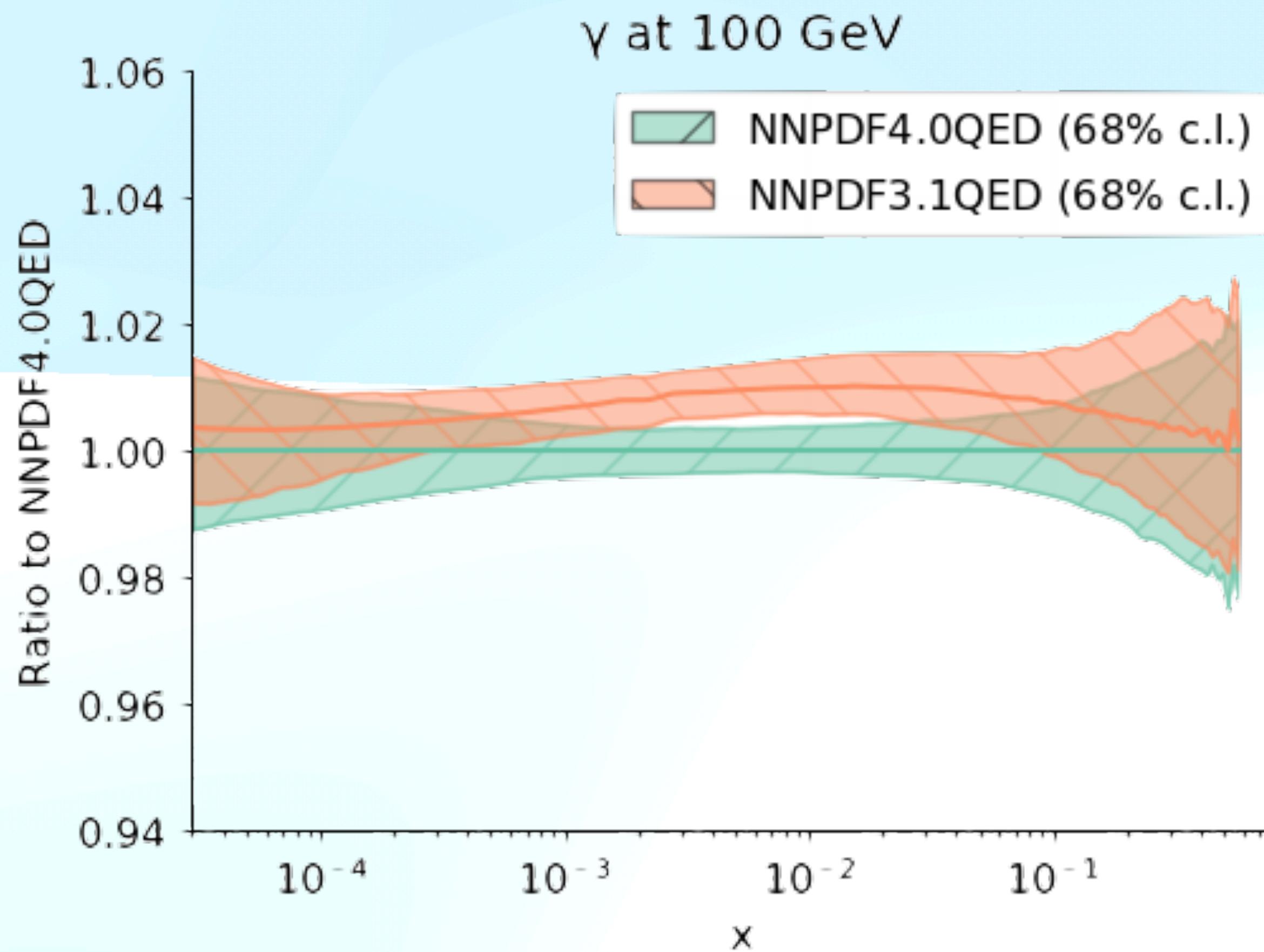
Chosen dataset cuts points in which they are important

QED corrections enter in the fit through momentum sum rule and DGLAP evolution

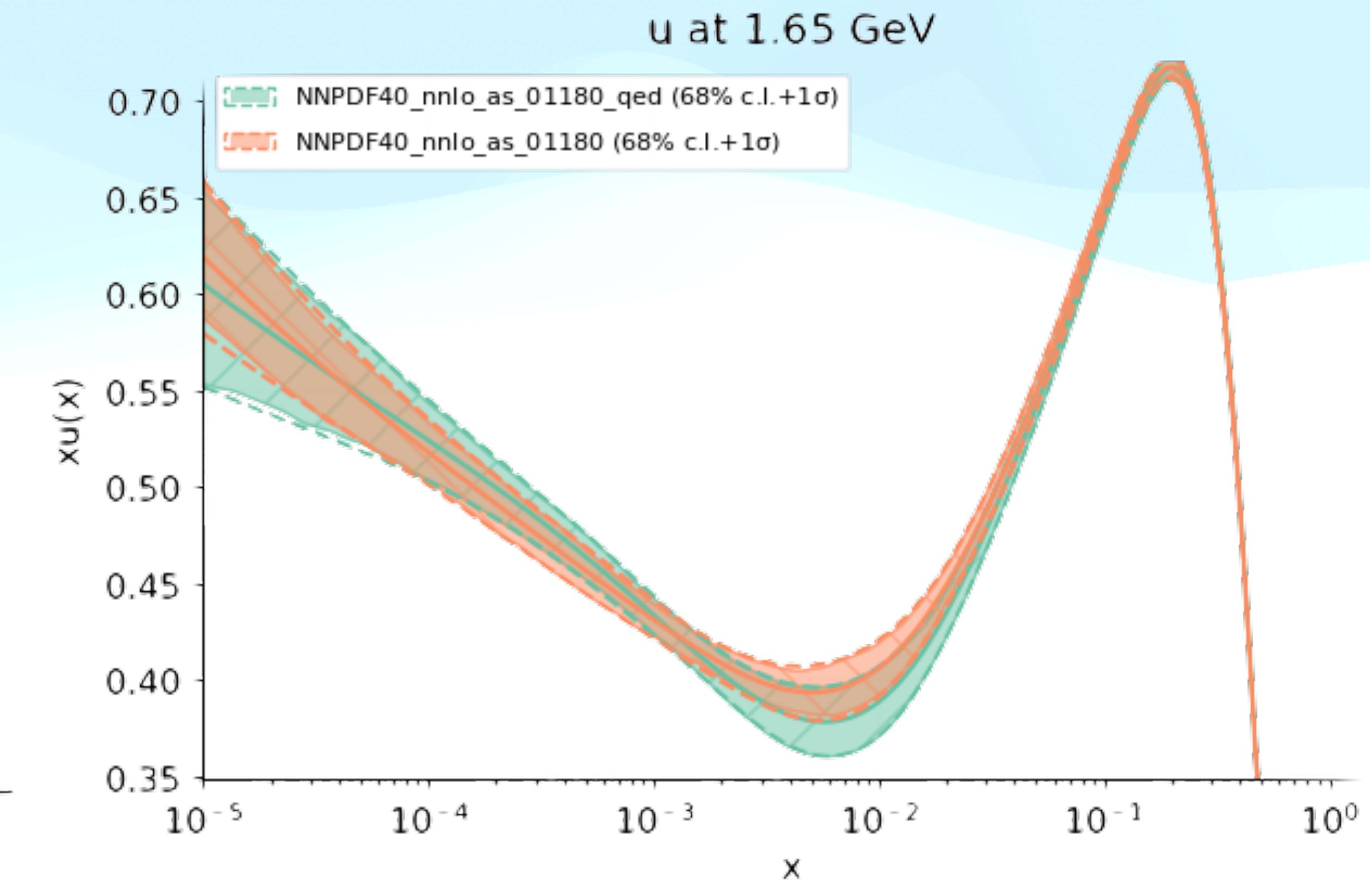
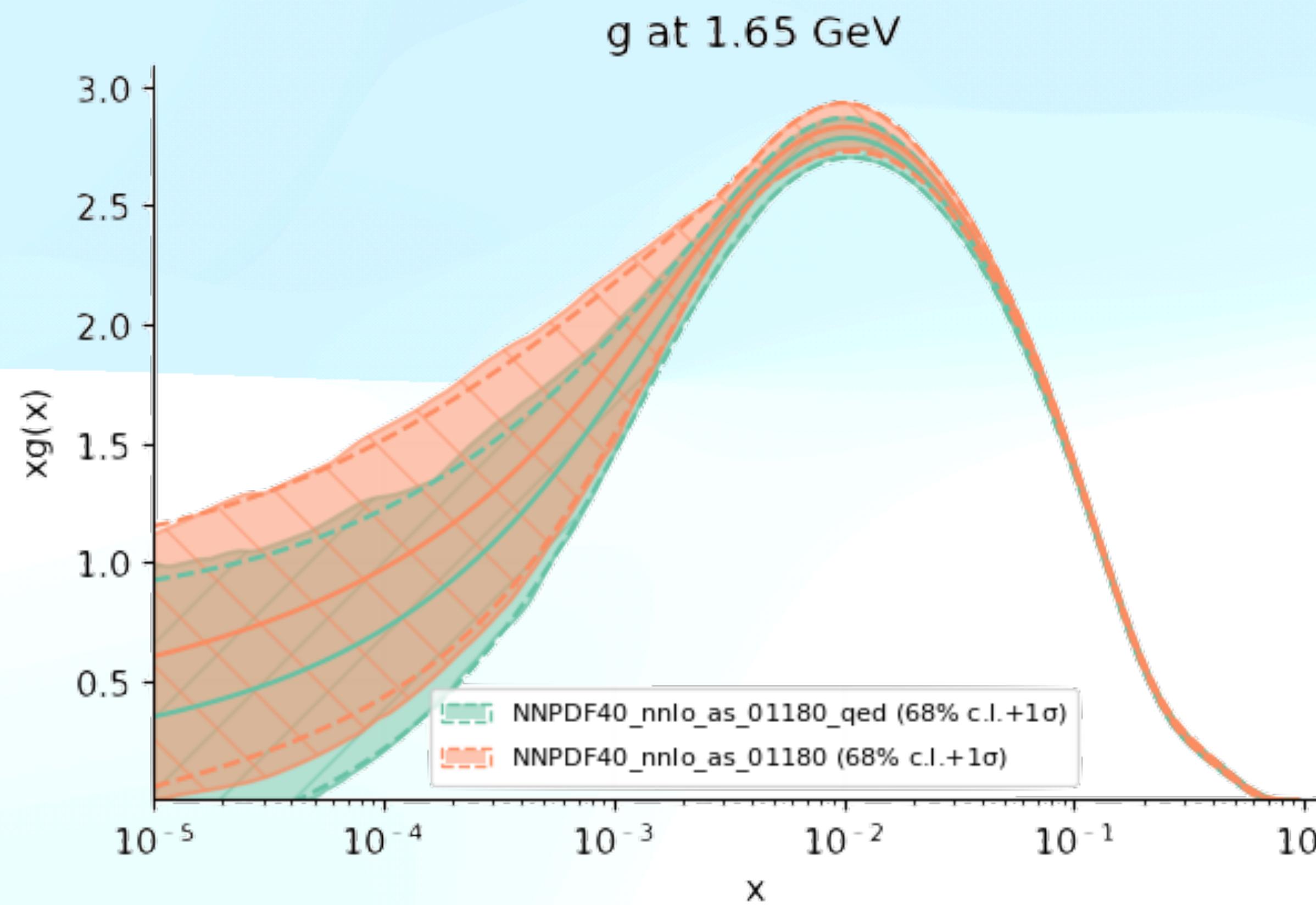
Future development

Add photon-initiated contributions and add data points in which they are important

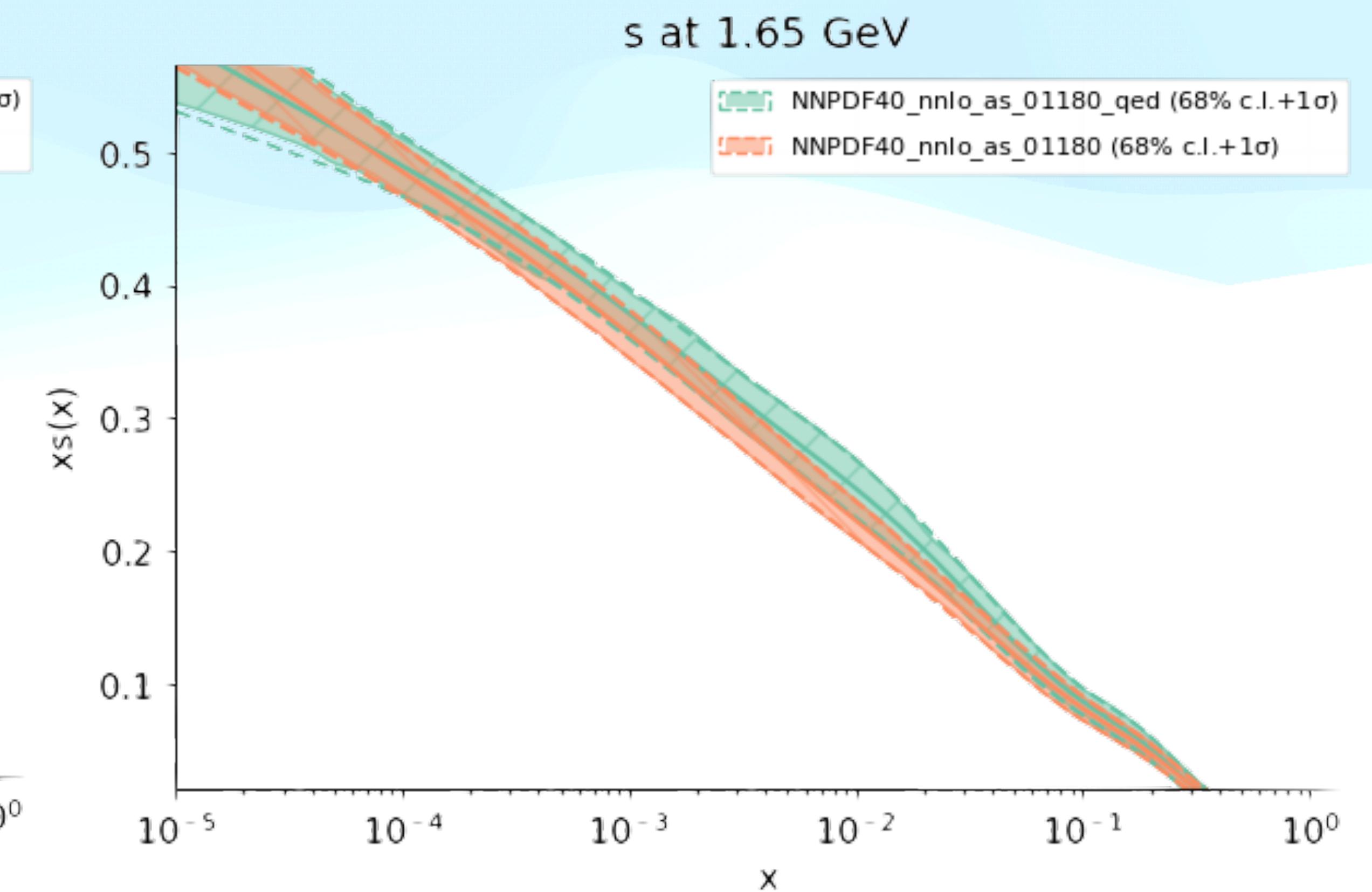
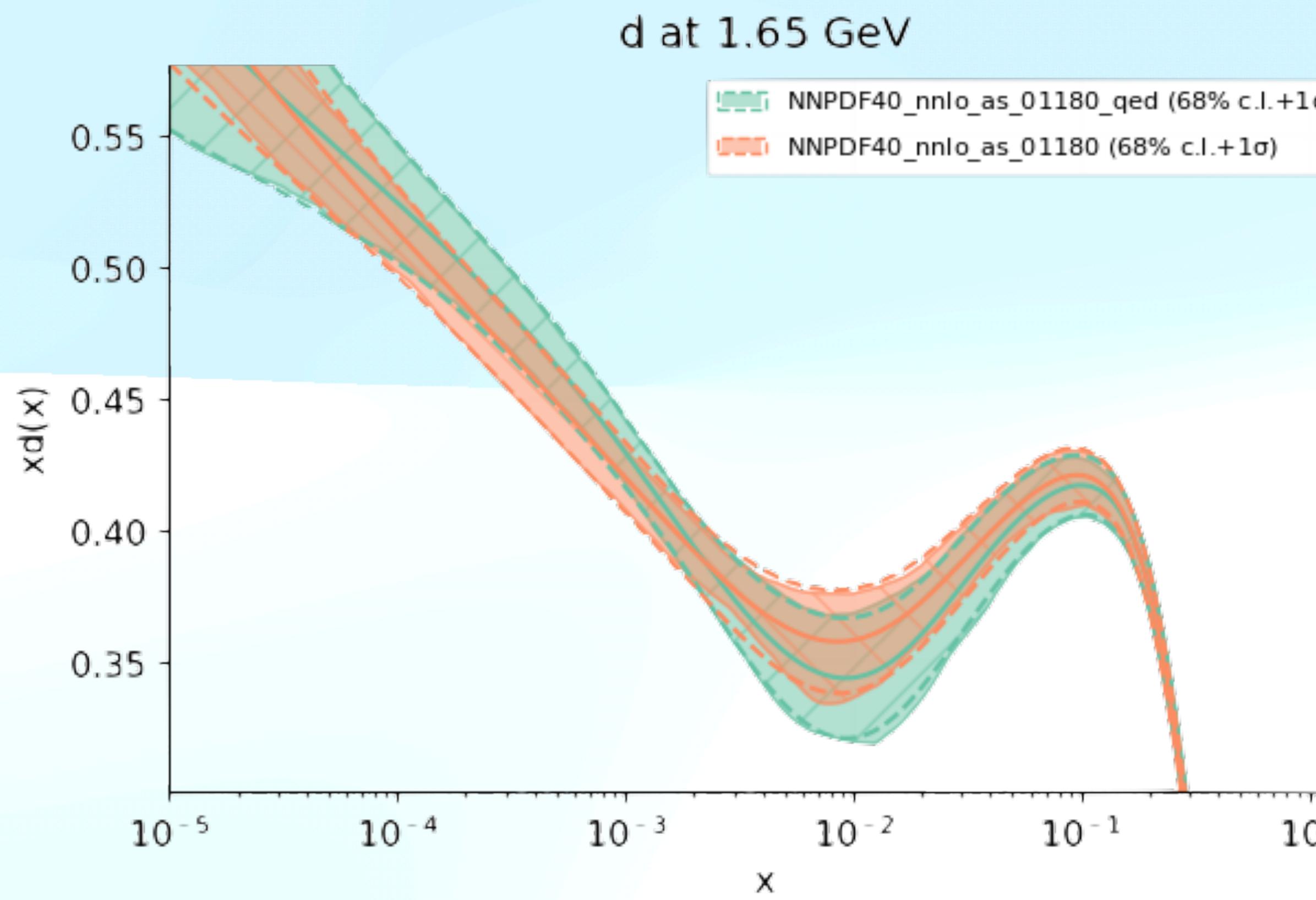
Comparison with other QED fits



Comparison with NNPDF4.0

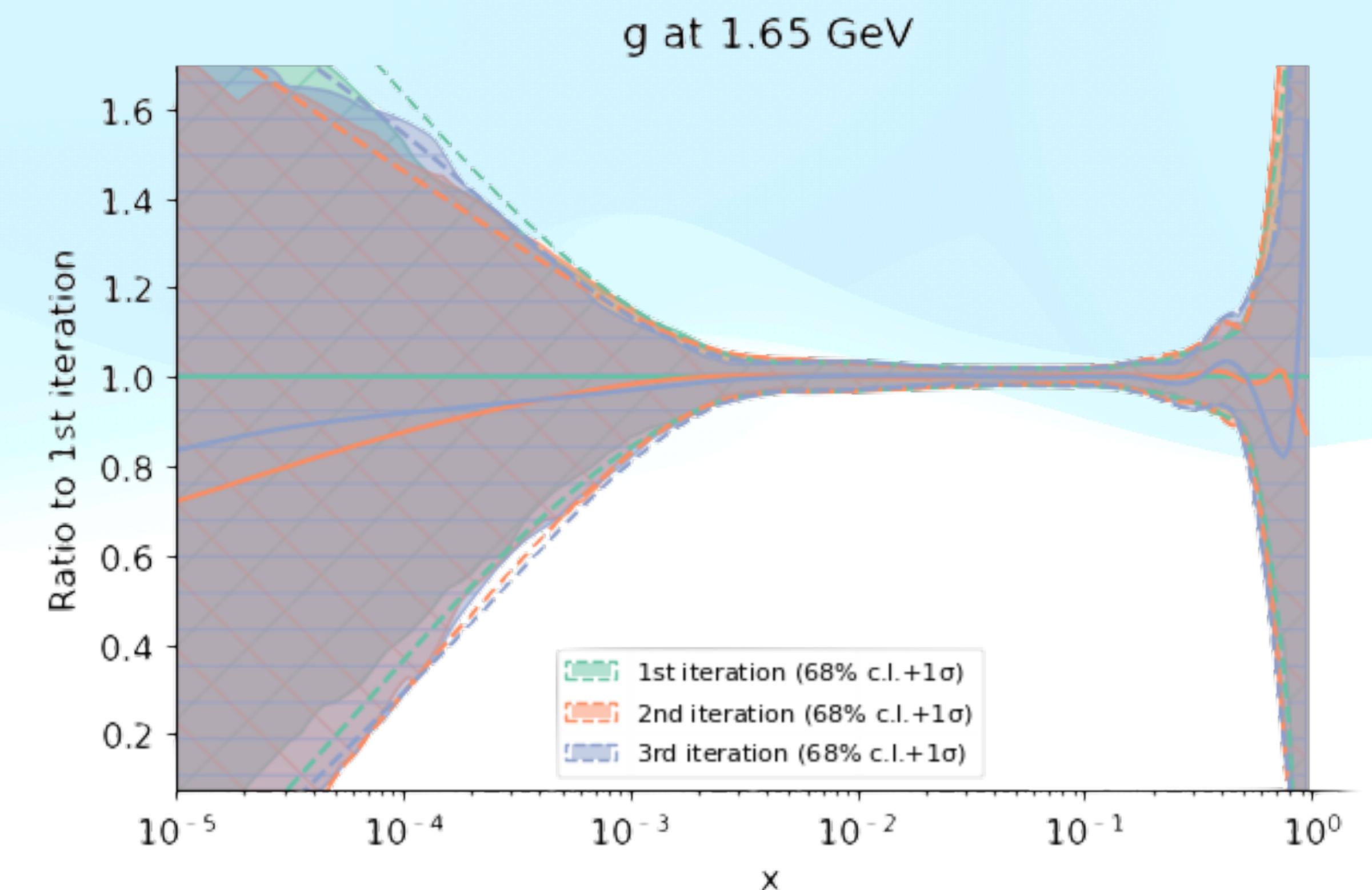
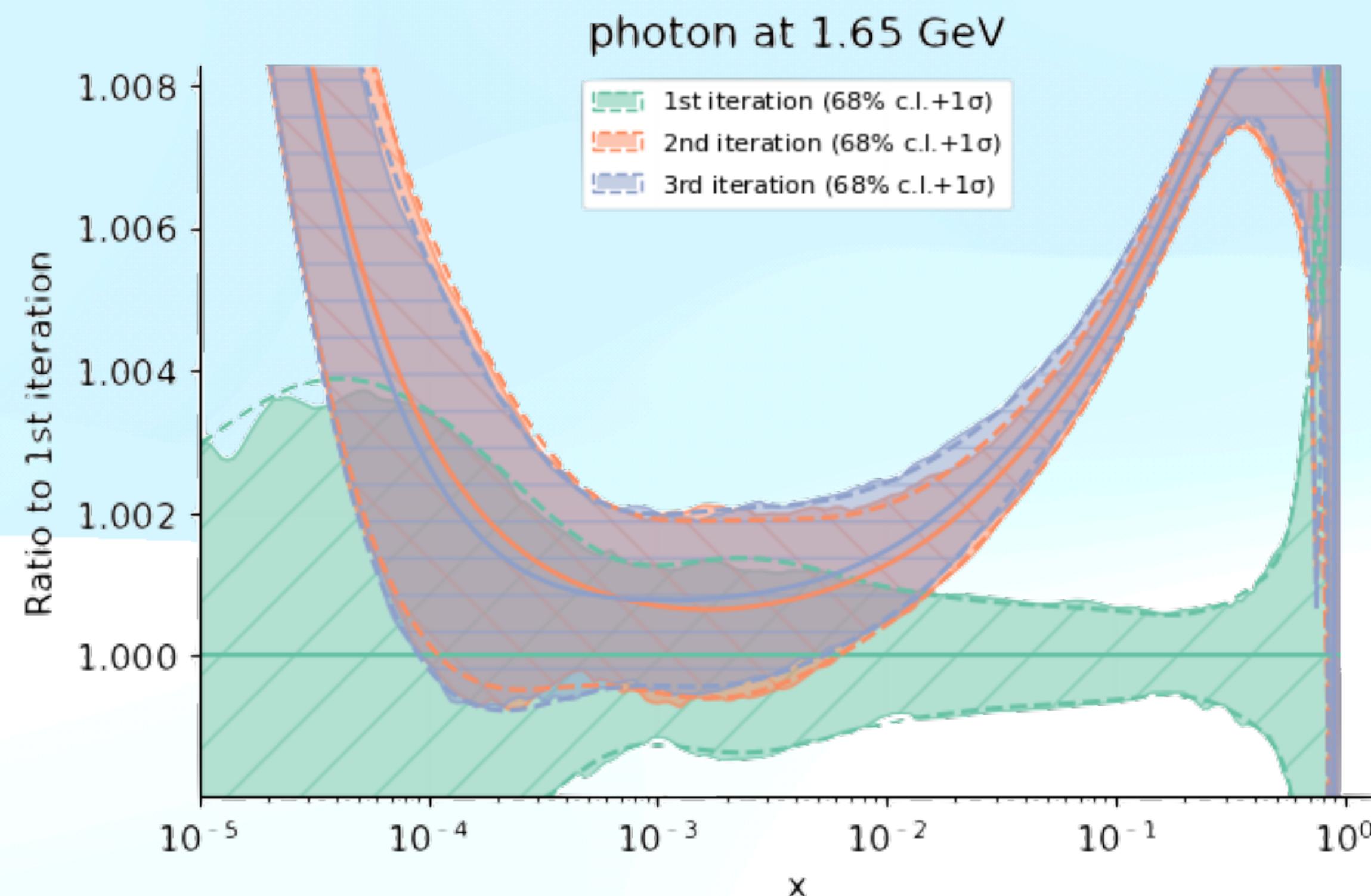


Comparison with NNPDF4.0



Results of the fit: iteration

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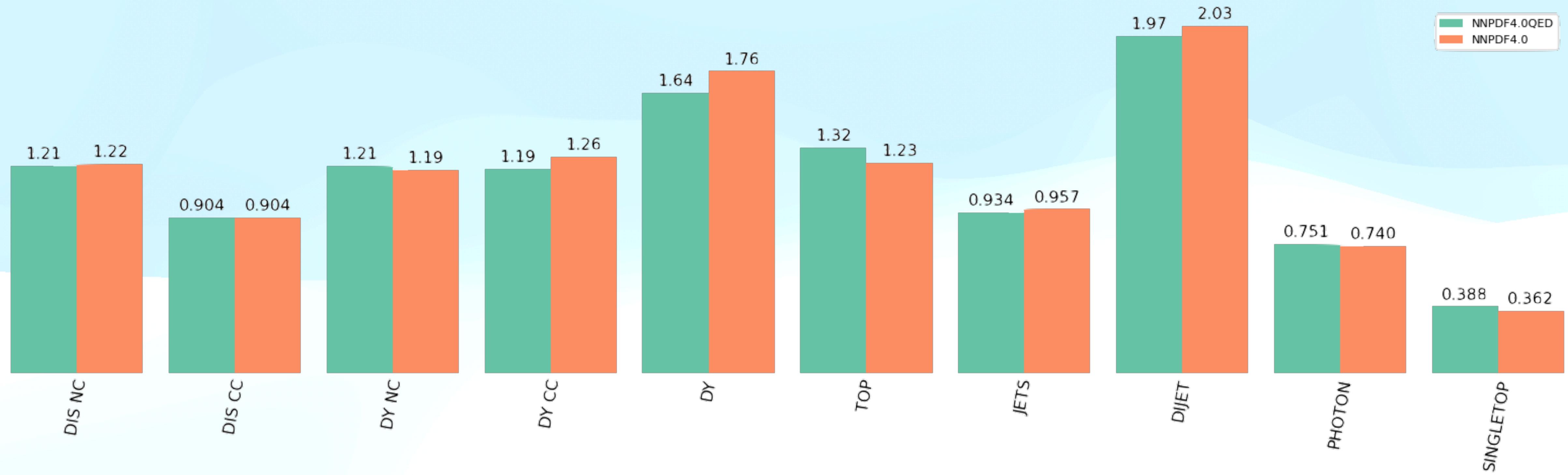


Two iterations are enough
for the fit to converge!

Results of the fit: fit quality

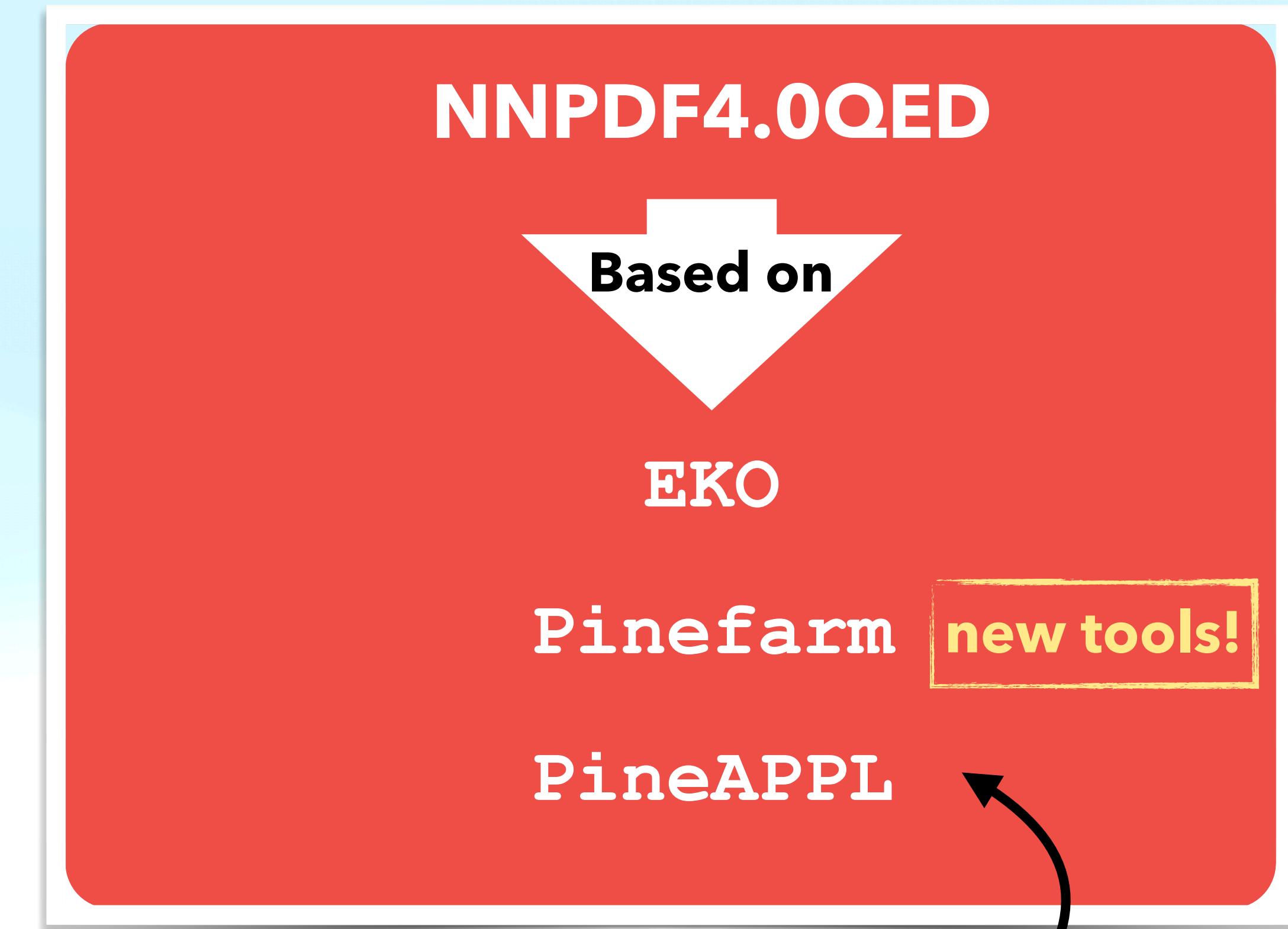
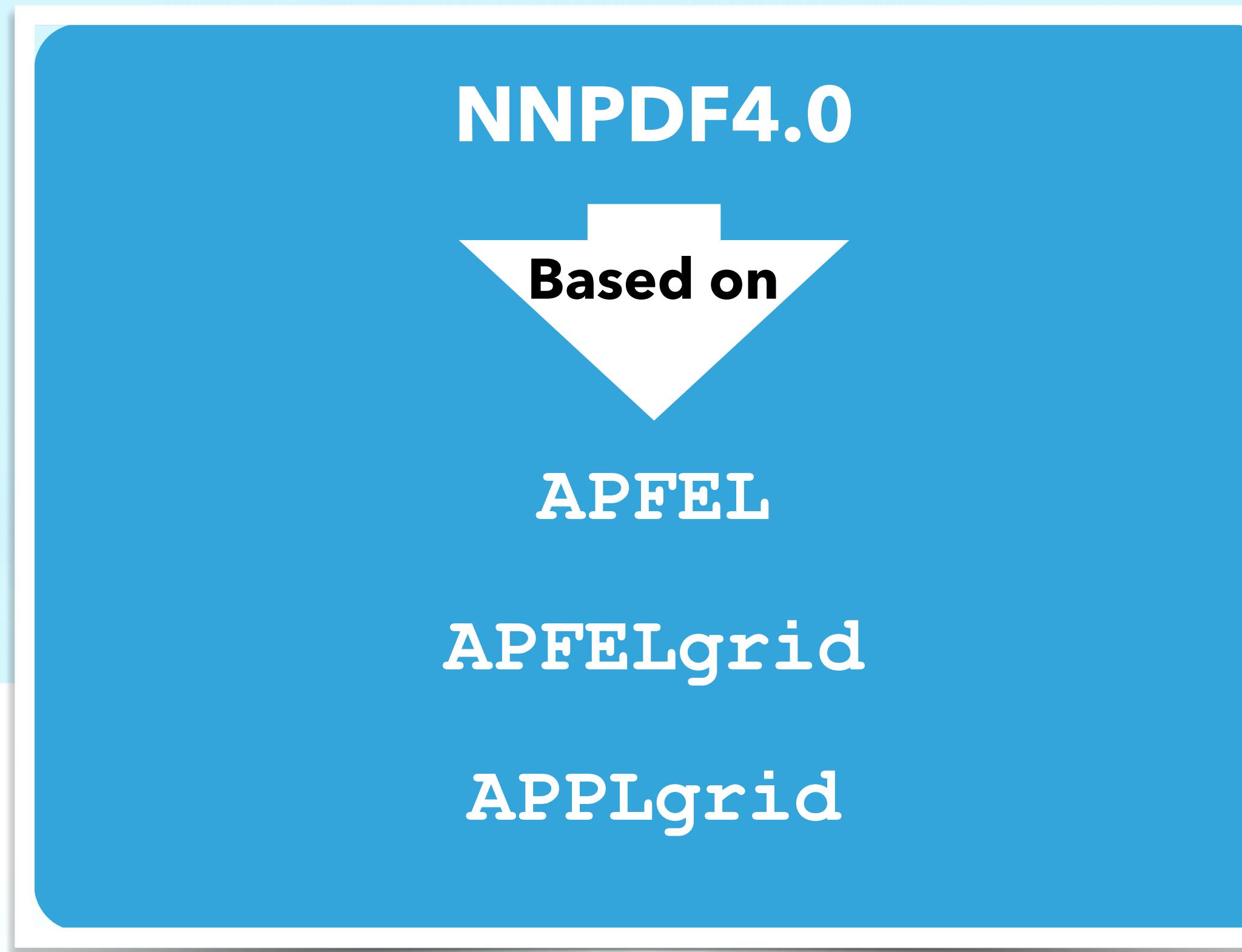
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χ^2 by processes:



Few words on a new pipeline

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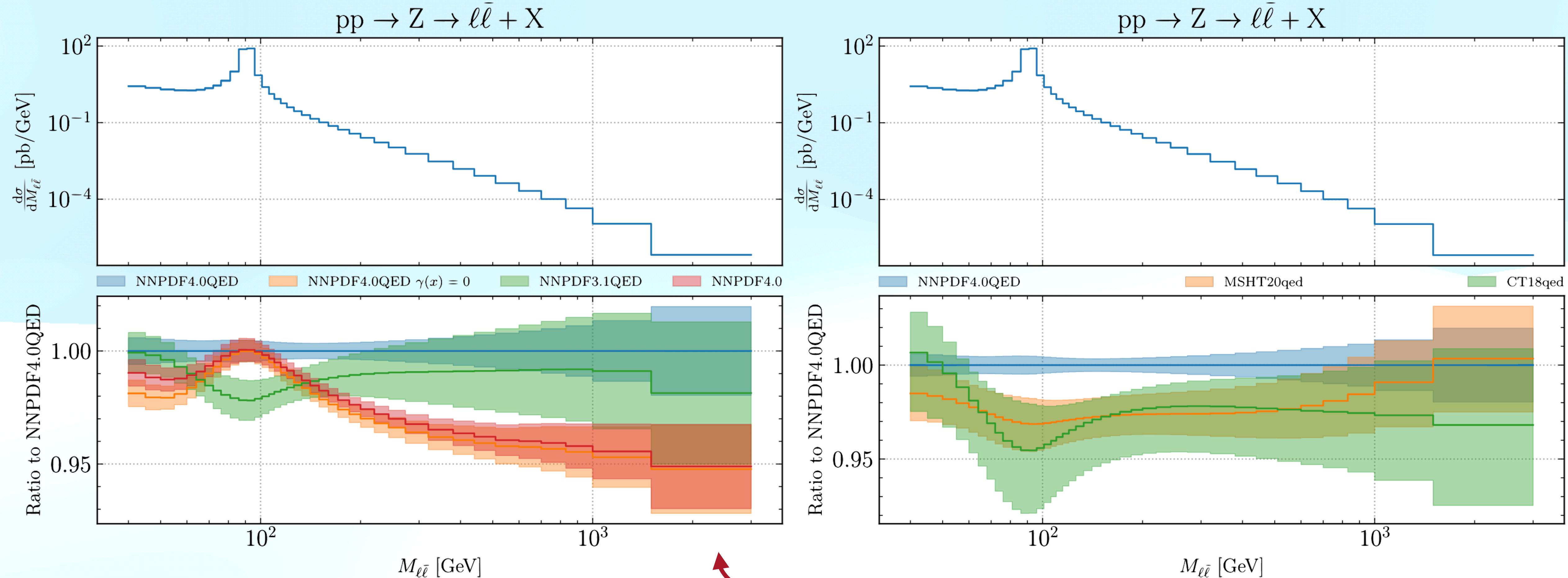
See "[Pineline: Industrialization of High-Energy Theory Predictions](#)" by A. Barontini

It will allow photon induced contributions in the theory predictions!

IMPACT ON PHENOMENOLOGY

Impact on phenomenology: inclusive Drell-Yan production

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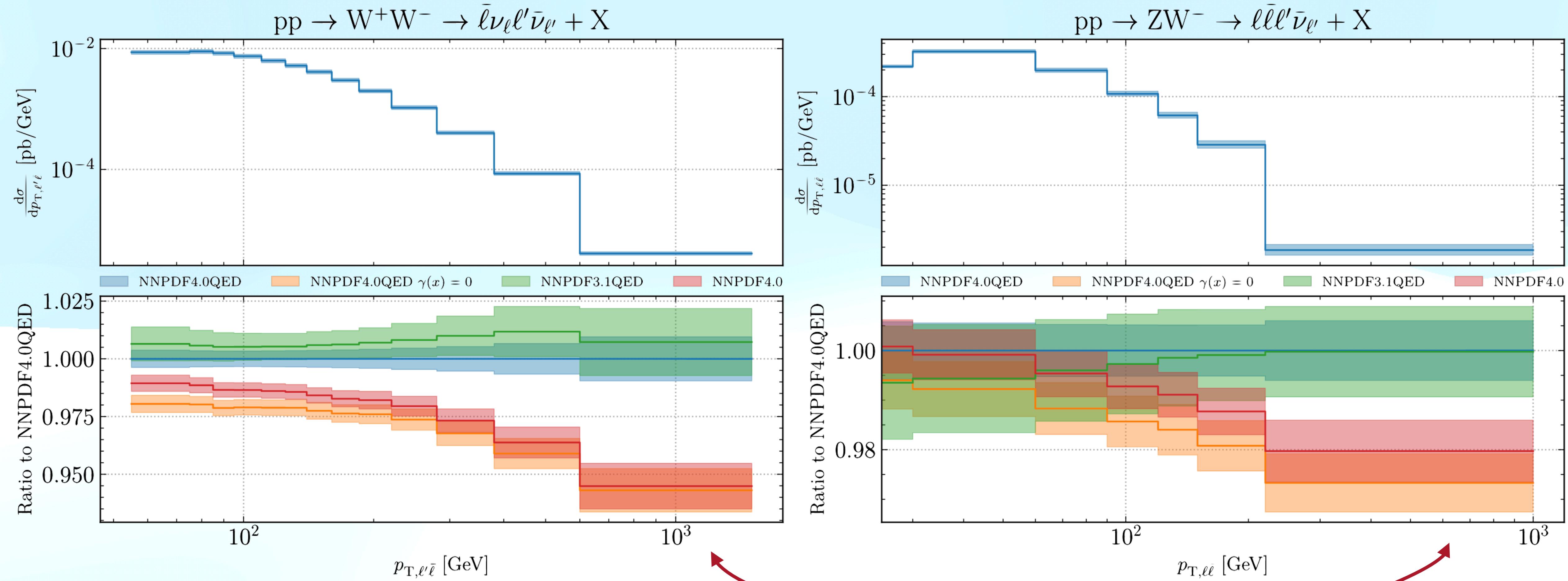


In this section photon-induced channels have been included

In the high invariant mass region QED corrections are not negligible!

Impact on phenomenology: weak boson production

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In the high p_T region QED corrections
are not negligible!

SUMMARY AND CONCLUSIONS

- We can add QED corrections to PDF fitting, getting a photon PDF
- The photon PDF is compatible with the most recent QED fits
- Quarks and gluon are almost unchanged (the photon PDF is small)
- There are processes in which photon initiated contributions are not negligible
- Soon we will be able to add such processes in our theory predictions

Thanks for your attention!!

BACKUP SLIDES

Solving DGLAP

Singlet and Valence sectors

$$\mathbf{P}_s = \begin{pmatrix} P_{gg} + \tilde{P}_{gg} & \tilde{P}_{g\gamma} & P_{gq} + \langle \tilde{P}_{gq} \rangle & \nu_u \tilde{P}_{g\Delta q} \\ \tilde{P}_{\gamma g} & \tilde{P}_{\gamma\gamma} & \langle \tilde{P}_{\gamma q} \rangle & \nu_u \tilde{P}_{\gamma\Delta q} \\ 2n_f(P_{qg} + \langle \tilde{P}_{qg} \rangle) & 2n_f \langle \tilde{P}_{q\gamma} \rangle & P_{qq} + \langle \tilde{P}_q^{ns,+} \rangle + \langle e_q^2 \rangle^2 \tilde{P}_{ps} & \nu_u \tilde{P}_{\Delta q}^{ns,+} + \nu_u e_{\Delta q}^2 \langle e_q^2 \rangle \tilde{P}_{ps} \\ 2n_f \nu_d \tilde{P}_{\Delta q g} & 2n_f \nu_d \tilde{P}_{\Delta q \gamma} & \nu_d \tilde{P}_{\Delta q}^{ns,+} + \nu_d e_{\Delta q}^2 \langle e_q^2 \rangle \tilde{P}_{ps} & P_{ns,+} + \{ \tilde{P}_q^{ns,+} \} + \nu_u \nu_d (e_{\Delta q}^2)^2 \tilde{P}_{ps} \end{pmatrix}$$

$$\mathbf{P}_v = \begin{pmatrix} P_{ns,V} + \langle \tilde{P}_q^{ns,-} \rangle & \nu_u \tilde{P}_{\Delta q}^{ns,-} \\ \nu_d \tilde{P}_{\Delta q}^{ns,-} & P_{ns-} + \{ \tilde{P}_q^{ns,-} \} \end{pmatrix}$$

$$\nu_{u/d} = \frac{n_{u/d}}{n_f}, \quad \langle \tilde{P}_q^{ns,\pm} \rangle = \nu_u \tilde{P}_u^{ns,\pm} + \nu_d \tilde{P}_d^{ns,\pm},$$

$$\{ \tilde{P}_q^{ns,\pm} \} = \nu_d \tilde{P}_u^{ns,\pm} + \nu_u \tilde{P}_d^{ns,\pm}, \quad \tilde{P}_{\Delta q}^{ns,\pm} = \tilde{P}_u^{ns,\pm} - \tilde{P}_d^{ns,\pm}$$

Solving DGLAP

Solution of the non-diagonal sectors

$$E_S(\mu^2 \leftarrow \mu_0^2) = \mathcal{P} \exp \left(- \int_{\log \mu_0^2}^{\log \mu^2} \gamma_S(\alpha_s(\mu'^2), \alpha(\mu'^2)) d \log \mu'^2 \right) \simeq \prod_{k=0}^{n-1} E_S(\mu^{2(k+1)} \leftarrow \mu^{2(k)})$$

$$\gamma(N) = - \int_0^1 dz z^{N-1} P(z)$$

$$E_S(\mu^{2(k+1)} \leftarrow \mu^{2(k)}) = \exp(-\gamma_S(\alpha_s(\mu^{2(k+1/2)}), \alpha(\mu^{2(k+1/2)})) \Delta \log \mu^{2(k)})$$

Solved in Mellin space

$$\log \mu^{2(k+1/2)} = \frac{\log \mu^{2(k+1)} + \log \mu^{2(k)}}{2}$$

$$\Delta \log \mu^{2(k)} = \log \mu^{2(k+1)} - \log \mu^{2(k)}$$

Computation of the photon

Why the LuxQED formula is used at 100 GeV?

LuxQED neglects
higher twist corrections

$$\mathcal{O}\left(\frac{\Lambda}{\mu}\right)$$

For low μ , the integral
is dominated by low Q^2
structure functions
non-perturbative!