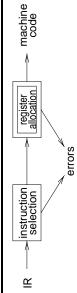
Register allocation



Register allocation:

- have value in a register when used
 - limited resources
- changes instruction choices
- can move loads and stores
- optimal allocation is difficult

 \Rightarrow NP-complete for $k \ge 1$ registers

Copyright © 2000 by Antony L. Hosking. Permission to make digital or hard copies of part or all of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and full citation on the first page. To copy otherwise, to republish, to post on servers, or to redistribute to lists, requires prior specific permission and/or fee. Request permission to publish from hosking@cs.purdue.edu.

_

Control flow analysis

Before performing liveness analysis, need to understand the control flow by building a control flow graph (CFG):

- nodes may be individual program statements or basic blocks
- edges represent potential flow of control

Out-edges from node n lead to successor nodes, succ[n] In-edges to node n come from predecessor nodes, pred[n]

Liveness analysis

Problem:

- IR contains an unbounded number of temporaries
 - machine has bounded number of registers

Approach:

- temporaries with disjoint live ranges can map to same register
- if not enough registers then spill some temporaries (i.e., keep them in memory)

The compiler must perform *liveness analysis* for each temporary:

It is *live* if it holds a value that may be needed in future

N

Example

$$a \leftarrow 0$$
 $L_1: b \leftarrow a+1$
 $c \leftarrow c+b$
 $a \leftarrow b \times 2$
if $a < N \text{ goto } L_1$
return c

Liveness analysis

Gathering liveness information is a form of data flow analysis operating over the CFG:

- liveness of variables "flows" around the edges of the graph
- assignments *define* a variable, ν :
- def(v) = set of graph nodes that define v
 - def[n] = set of variables defined by n
- occurrences of v in expressions use it:

- use(v) = set of nodes that use v

- use[n] = set of variables used in n

2

Liveness analysis

$$in[n]$$
 = variables live-in at n
 $out[n]$ = variables live-out at n

Then:

$$out[n] = \bigcup_{s \in SUCC(n)} in[s]$$

$$succ[n] = \phi \Rightarrow out[n] = \phi$$

Note:

$$in[n] \supseteq use[n]$$

 $in[n] \supseteq out[n] - def[n]$

use[n] and def[n] are constant (independent of control flow) Now, $v \in in[n]$ iff. $v \in use[n]$ or $v \in out[n] - def[n]$ Thus, $in[n] = use[n] \cup (out[n] - def[n])$

Definitions

 v is live on edge e if there is a directed path from e to a use of v that does not pass through any def(v)

v is live-in at node n if live on any of n's in-edges

v is live-out at n if live on any of n's out-edges

• $v \in use[n] \Rightarrow v \text{ live-in at } n$

• v live-in at $n \Rightarrow v$ live-out at all $m \in pred[n]$

• ν live-out at $n, \nu \not\in def[n] \Rightarrow \nu$ live-in at n

Iterative solution for liveness

foreach n

$$in[n] \leftarrow \phi$$

 $out[n] \leftarrow \phi$

repeat

 $in[n] \leftarrow use[n] \cup (out[n] - def[n])$ $out'[n] \leftarrow out[n];$ $in'[n] \leftarrow in[n];$ foreach n

 $\underline{\mathsf{until}} \; \mathit{in}'[n] = \mathit{in}[n] \; \land \; \mathsf{out'}[n] = \mathsf{out}[n], \forall n$ $out[n] \leftarrow \bigcup_{s \in Succ[n]} in[s]$

Notes

- should order computation of inner loop to follow the "flow"
- liveness flows backward along control-flow arcs, from out
- nodes can just as easily be basic blocks to reduce CFG
- could do one variable at a time, from uses back to defs, noting liveness along the way

တ

Least fixed points

There is often more than one solution for a given dataflow problem (see example).

Any solution to dataflow equations is a conservative approximation:

- v has some later use downstream from n ⇒ v ∈ out(n)
- but not the converse

Conservatively assuming a variable is live does not break the program; just means more registers may be needed.

Assuming a variable is dead when really live will break things.

Many possible solutions but we want the "smallest": the least fixpoint. The iterative algorithm computes this least fixpoint.

Iterative solution for liveness

Complexity: for input program of size N

- ≤ N nodes in CFG
- $\Rightarrow \leq N$ variables $\Rightarrow N$ elements per *in/out*
- \Rightarrow O(N) time per set-union
- for loop performs constant number of set operations per each iteration of repeat loop can only add to each set sets can contain at most every variable \Rightarrow O(N^2) time for for loop

 - \Rightarrow sizes of all in and out sets sum to $2N^2$, bounding the number of iterations of the **repeat** loop ordering can cut repeat loop down to 2-3 iterations \Rightarrow worst-case complexity of $O(N^4)$

 $\Rightarrow O(N)$ or $O(N^2)$ in practice

10