

Manual for the use of the optimization code

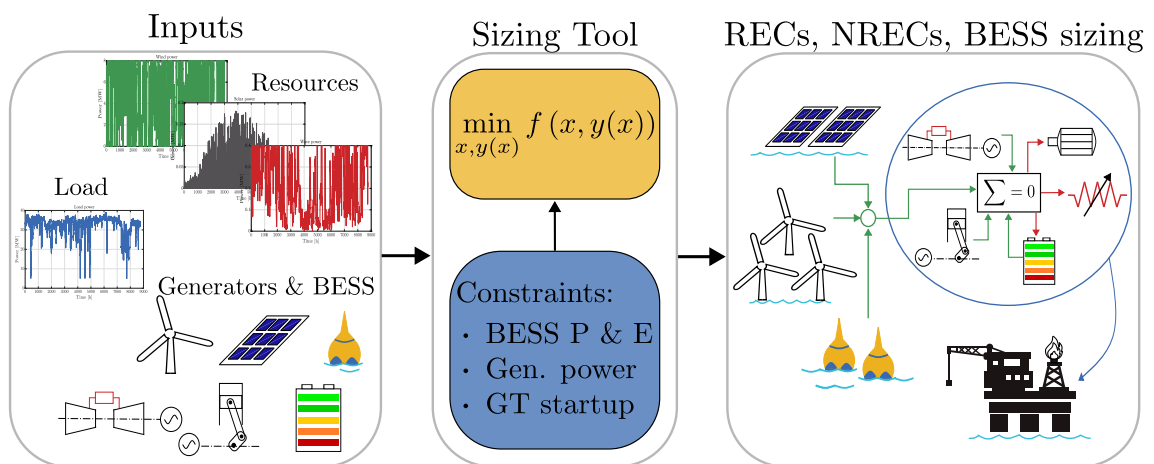
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Petronas-NTNU-IEL Collaboration within the SAFER Project

Energy Storage Sizing/Control for 100% Renewable Supplied Isolated Grids

Coordinated Converter Control for Stability and Power Quality in Inertia-less Grids



This manual and the related code is a work in progress, which is continuously improved by the authors. It is not a finished work and may therefore contain defects or “bugs” inherent to this type of development. For this reason the work is provided without warranties of any kind concerning the work, including without limitation merchantability, fitness for a particular purpose, absence of defects or errors, and accuracy.

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1 Code Capabilities

The focus of this manual is on the code capabilities and structure, so the reader can gain an understanding on how to use the code.

The code is developed requiring as input data series of the load and the environmental resources, the different type of assets (generators and storages) that can be installed, and their costs, and provides as output the optimal assets combination to support the load with the given specification. The code is able to perform parametric sweep of some user-defined parameters.

From the technical perspective the code builds and solves an optimization problem expressed as a Mixed Integer Linear Programming (MILP).

2 Prerequisites

The following Matlab products are required:

- Optimization toolbox
- Statistics and Machine Learning Toolbox
- Parallel Computing Toolbox
- Global Optimization Toolbox

2.1 Available assets

Management of the different devices: Battery Energy Storage System (BESS), Solar PV, Wind Turbine (WT), Diesel Generator (DG), Gas Turbine (GT), and potential extension to Hydrogen Fuel Cell.

2.2 Configurations

Different device configurations can be selected by the user before running the optimization (e.g. WT+DG, REC-U, REC-U+DG, REC-C+DG24).

2.3 Parameter Sweeps

It is possible to perform parameter sweep. Examples include risk-related variables, carbon tax, PV cost. When operating on parametric sweep it might time advantageous to parallelize the execution of the code.

3 Code Structure

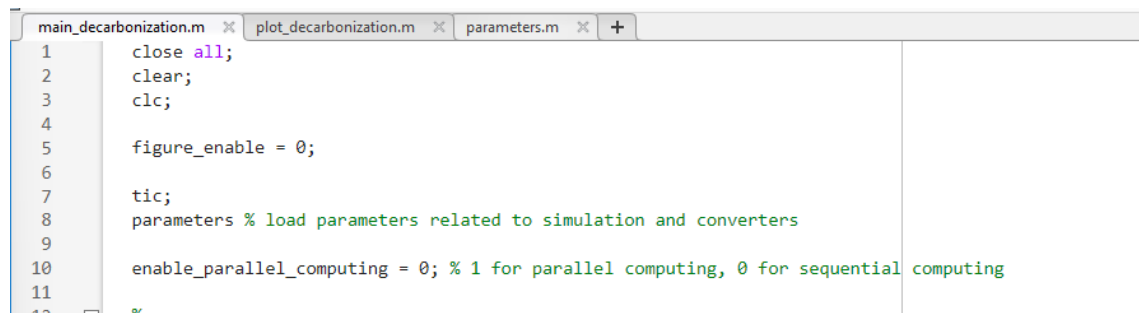
3.1 General Workflow

1. Data set import
2. Device definition
3. Optimization problem formulation
4. Post-processing
5. Results visualization

3.2 Initialization

Main file: `main_decarbonization.m`

Select parallel or sequential execution: `enable_parallel_computing` (Figure 1)

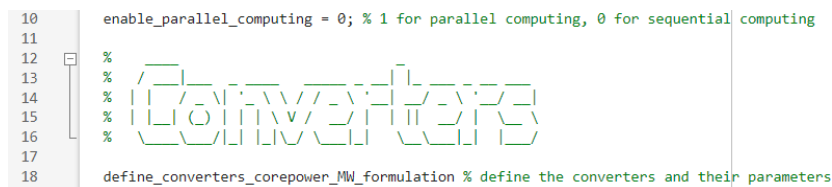


```
main_decarbonization.m x plot_decarbonization.m x parameters.m x +
1 close all;
2 clear;
3 clc;
4
5 figure_enable = 0;
6
7 tic;
8 parameters % load parameters related to simulation and converters
9
10 enable_parallel_computing = 0; % 1 for parallel computing, 0 for sequential computing
11
12
```

Figure 1: Main project file structure

3.3 Converters

Defined in `define_converters_corepower_MW_formulation` with all parameters Figure 2. Converters and storages are defined in classes Figure 3.



```
10 enable_parallel_computing = 0; % 1 for parallel computing, 0 for sequential computing
11
12 %
13 %
14 %
15 %
16 %
17
18 define_converters_corepower_MW_formulation % define the converters and their parameters
19
```

Figure 2: Converter definition

@BatteryX	5/23/2025 8:17 AM	File folder
@DataX	5/23/2025 8:17 AM	File folder
@DieselGeneratorX	5/23/2025 8:17 AM	File folder
@DumpLoadX	5/23/2025 8:17 AM	File folder
@ESSX	5/23/2025 8:17 AM	File folder
@GasTurbineX	5/23/2025 8:17 AM	File folder
@GridX	5/23/2025 8:17 AM	File folder
@LoadX	5/23/2025 8:17 AM	File folder
@PhotoVoltaicX	5/23/2025 8:17 AM	File folder
@REX	5/23/2025 8:17 AM	File folder
@VirtualPowerX	5/23/2025 8:17 AM	File folder
@WECX	5/23/2025 8:17 AM	File folder
@WindTurbineX	5/23/2025 8:17 AM	File folder

Figure 3: Class definitions for converters and storage

3.4 Dataset Import

`import_datasets_norway_1yr` loads the datasets of load and resources. Structure depends heavily on datasets in use, in the sense that the user has to tune the loading function according to the format of the available dataset Figure 4.

```

18 define_converters_corepower_MW_formulation % define the converters and their pa
19
20 %
21 %
22 %
23 %
24 %
25
26 import_datasets_norway_1yr % load the datasets of the different resources
27 % import_datasets_dulang_1yr % load the datasets of the different resources

```

Figure 4: Example dataset loading

3.5 Configuration Selection

`case_sim_vec` defines which devices are included in optimization. The user can specify which configuration to use among the listed ones Figure 5. If the user wants to add more configurations he/she has to start doing it from here.

3.6 Sweep Type Selection

Selection of sweep type. The sweep can be performed on the listed quantities:

- **None:** No sweep
- **beta:** Control parameter of the Conditional Value at Risk
- **LPSP:** Lost of Power Supply Probability (percentage)
- **PS:** Peak shaving (percentage)
- **Carbon_tax:** scaling factor for the nominal carbon tax

```

31 %
32 %
33 %
34 %
35 %
36 %
37
38 REC = RECX();
39 REC.WT = WT;
40 REC.PV = PV;
41 REC.WEC = WEC;
42 REC.DGv.DGv_obj = DGv_obj;
43 REC.DGv.n_NREC = 1;
44 REC.GT.GT_obj = GT_obj;
45 REC.GT.n_NREC = n_GT;
46 REC.DG.DG_obj = DG_obj;
47 REC.DG.n_NREC = n_DG;
48 %
49 %
50 %
51 %
52 %
53 %
54 %
55 %
56 %
57 %
58 %
59 %
60 %
61
62 case_sim_vec = {'WT+DG', 'REC-U', 'REC-U+DG', 'REC-C+DG24'};
63 case_sim_vec = {'WT+DG'};
64 num_sim = length(case_sim_vec);
65

```

Figure 5: Configuration selection

- PVCost: scaling factor for the nominal PV cost

```

66 %
67 %
68 %
69 %
70 %
71 %
72
73 %
74 %
75 %
76 %
77 %
78 %
79 %
80
81 sweep_type = 'None';
82 alpha_vec = 0.8; % [0.1, 0.5, 0.9];
83 num_alpha = size(alpha_vec, 2);
84 switch sweep_type
85 case 'None'
86     sweep_vec = 0;
87 case 'beta'
88     sweep_vec = [0:0.25:1];
89 case 'LPSP'
90     sweep_vec = [0:0.01:0.05]; % [0, 0.1, 0.5, 0.9];
91 case 'PS'
92     sweep_vec = [0:0.025:0.1];
93 case 'Carbon_tax'
94     sweep_vec = [1,10,100,1000];
95 case 'DGpower'
96     sweep_vec = [0.01,0.1,1/3,2/3,1,1.1,1.5,2:1:5,5.5:0.5:8,9,10];
97 case 'PVCost'
98     sweep_vec = [1,0.7,0.5];
99 otherwise
100     error('Unknown sweep type')
101 end
102 num_sweep = size(sweep_vec, 2);

```

Figure 6: Sweep type selection

3.7 Main Loop

Loop over configurations and sweeps Figure 7. Initially `do_power` computes generated power given the load series and converter models (Figure 8), then `optimization_setup` sets up the optimization parameters for the current case, and finally `CASE_optimization` builds and solves the optimization problem.

```

REC_obj(1:num_alpha,1:num_sweep) = REC;
scenario_mat(1:num_alpha,1:num_sweep) = scenario;
opt_parameters_vec(1:num_sim) = opt_parameters;
prob_sens = cell(num_alpha, num_sweep);
res_sens = cell(num_alpha, num_sweep);
load_sens = cell(num_alpha, num_sweep);
REC_tmp = cell(num_alpha, num_sweep);
load_scenarios = cell(num_alpha, num_sweep, num_sim);
time_sim = zeros(num_sweep);
seed_increment = zeros(num_sweep);
values_solution = cell(num_alpha, num_sweep, num_sim);
values_vector = cell(num_alpha, num_sweep, num_sim);
values_minvalue = cell(num_alpha, num_sweep, num_sim);
CO2_emitted = cell(num_alpha, num_sweep, num_sim);
for b = 1:num_sweep
    converged_a = false(num_alpha,1);
    for a = 1:num_alpha
        res_sens{a,b}{1} = wind.iniVec;
        res_sens{a,b}{2} = irradiance.iniVec;
        res_sens{a,b}{3} = reshape(met_data_swh, [], 1);
        res_sens{a,b}{4} = reshape(met_data_mwp, [], 1);
        load_scenarios.iniVec = LoadA.iniVec;
        load_sens{a,b} = load_scenarios;
        prob_sens{a,b} = 1/size(load_scenarios.iniVec, 2)*ones(size(load_scenarios.iniVec, 2), 1);

        [REC_tmp{a,b}] = do_power(REC_obj(a,b), res_sens{a,b});

    for i=1:num_sim
        tic;
        case_sim = case_sim_vec(i);

        % Optimization setup
        [REC_el, load_scenarios_el, opt_parameters_el, scenario_tmp] = optimization_setup('None', alpha_vec, sweep_type, sweep_vec, a, b, REC_tmp{a,b}, load_sens{a,b}, scenario_mat(a, b), opt_parameters_vec(i), 0, case_sim);

        % Run optimization
        [values_solution{a,b,i}, values_vector{a,b,i}, values_minvalue{a,b,i}, CO2_emitted{a,b,i}] = CASE_optimization(prob_sens{a,b}, REC_el, ESS, DL, load_scenarios_el, opt_parameters_el, scenario_tmp{a,b}, case_sim);

        % Track time and convergence
        time_sim{a,b,i} = toc;
        fprintf('Simulation, case=%s, a=%d, b=%d, time=%s.f [%i], stop due to %s\n, convergence=%5.2f\n', case_sim, alpha_vec(a), sweep_vec(b), time_sim{a,b,i}, values_solution{a,b,i}.min_info.message, values_solution{a,b,i}.min_info.relativegap);
    end
end
end

```

Figure 7: Main loop

```

res_sens{a,b}{1} = wind.iniVec;
res_sens{a,b}{2} = irradiance.iniVec;
res_sens{a,b}{3} = reshape(met_data_swh, [], 1);
res_sens{a,b}{4} = reshape(met_data_mwp, [], 1);
load_scenarios.iniVec = LoadA.iniVec;
load_sens{a,b} = load_scenarios;
prob_sens{a,b} = 1/size(load_scenarios.iniVec, 2)*ones(size(load_scenarios.iniVec, 2), 1);

[REC_tmp{a,b}] = do_power(REC_obj(a,b), res_sens{a,b});

```

Figure 8: Power computation from datasets

4 Optimization: CASE_optimization

4.1 General Notes

Optimization problem formulated as a *problem-based* approach¹.
Different cases handled via `switch` statements.

4.2 Structure

1. Extract information from input
2. Define variables
3. Define costs
4. Compose objective function
5. Define constraints
6. Solve optimization

¹<https://uk.mathworks.com/help/optim/problem-based-approach.html>

7. Post-process results

4.3 Information Extraction

Defines installed devices, load, and cost annualization factors Figure 9.

```
115
116 % Annualization-related variables
117 r = opt_parameters.r; % daily interest rate
118 L = opt_parameters.L; % investment lifetime
119 p = (365*24)*L/scenario.h_star; % recoupling period
120 T = scenario.T; % number of data in each scenario
121 W = size(Pload, 2); % number of scenarios (e.g. days)
122 AF.CRF = (r*(1 + r)^p)/((1 + r)^p - 1); % capital recovery factor (daily value
123 AF.gamma = scenario.h_star/scenario.h; % rescale the scenario to cost to dail
124 AF.YtD = scenario.d_o; % rescale from yearly to daily cost
```

Figure 9: Cost annualization factors

4.4 Variable Definition

Variables for each device defined in its own function Figure 10, as for example in the GT case in Figure 11:.

```
134 %
135 %
136 %
137 %
138 %
139
140 Pch = 0; % charging power of the battery
141 Pdc = 0; % discharging power of the battery
142 prob = optimproblem;
143 cvar_zeta = 0; % CVaR constraint
144 cvar_s = zeros([W, 1]); % CVaR constraint
145 P_REC_max = 0;
146 P_GT = 0;
147 Pbt = 0;
148
149 switch case_constraint
150 case {'GT24', 'GT365'} % Only GT
151     variable_def_GT;
152     variable_def_Pns_Pct;
153
154 case {'1GT+WT+DG', '2GT+WT+DG', '1GT+REC+DG', '2GT+REC+DG'} % 1/2 GT + REC + BESS
155     variable_def_GT;
156     x_GT = ones(REC.GT.n_NREC, 1); % impose the number of GTs
157     variable_def_REC;
158     variable_def_Pns_Pct;
159     if BESS_NL_model == 1
160         variable_def_BESS_NL_model;
161     else
162         variable_def_BESS;
163     end
164
165 case {'WT+DG', 'REC-U', 'REC-U+DG', 'REC-C+DG24', 'REC-C+DG365'} % REC + BESS
166     variable_def_REC;
167     variable_def_Pns_Pct;
168     if BESS_NL_model == 1
169         variable_def_BESS_NL_model;
170     else
171         variable_def_BESS;
172     end
173
174 case {'DG+REC24', 'DG+REC365'} % REC + BESS + DIESEL
175     variable_def_REC;
176     variable_def_DGv;
177     variable_def_Pns_Pct;
178     if BESS_NL_model == 1
179         variable_def_BESS_NL_model;
180     else
181         variable_def_BESS;
182     end
183
184 otherwise
185     error('Case name not implemented yet!\n');
186
187 end
188
```

Figure 10: Variable definitions

```

main_decarbonization.m | parameters.m | CASE_optimization.m | BESS_SOC_stationarity_NL_model.m | variable_def_GT.m | +
1 % Define the variables for the GT model
2
3 % x = [REC.GT.n_NREC]
4 x_GT = optimvar('x_GT', [REC.GT.n_NREC, 1], 'lowerBound', zeros(1, REC.GT.n_NREC), 'Type', 'integer', 'LowerBound', 0, 'UpperBound', 1);
5
6 % GT variables
7 P_GT = optimvar('P_GT', [T, W, REC.GT.n_NREC], 'LowerBound', 0, 'Type', 'continuous'); % power output of the GT
8 u_GT = optimvar('u_GT', [T, W, REC.GT.n_NREC], 'Type', 'integer', 'LowerBound', 0, 'UpperBound', 1); % ON/OFF status of the GT
9 z_GT = optimvar('z_GT', [T, W, REC.GT.n_NREC], 'Type', 'integer', 'LowerBound', 0, 'UpperBound', 1); % startup indicator of the GT
10 RR = optimvar('RR', [T, W, REC.GT.n_NREC], 'Type', 'continuous', 'LowerBound', 0); % absolute value of the ramping rate
11
12 z_help = optimvar('z_help', [T, W, REC.GT.n_NREC], 'Type', 'integer', 'LowerBound', 0, 'UpperBound', 1); % helper variable for removing the nonlinearity
13
14 delta_GT_Pmax = optimvar('delta_GT_Pmax', [T, W, REC.GT.n_NREC], 'Type', 'integer', 'LowerBound', 0, 'UpperBound', 1);
15
16 x0.x_GT = ones([REC.GT.n_NREC, 1]);
17 x0.P_GT = zeros([T, W, REC.GT.n_NREC]);
18 x0.u_GT = zeros([T, W, REC.GT.n_NREC]);
19 x0.z_GT = zeros([T, W, REC.GT.n_NREC]);
20 x0.RR = zeros([T, W, REC.GT.n_NREC]);
21 x0.z_help = zeros([T, W, REC.GT.n_NREC]);
22 x0.delta_GT_Pmax = zeros([T, W, REC.GT.n_NREC]);

```

Figure 11: Gas Turbine variables

4.5 Cost Definition

Costs defined per asset in stage 1 and stage 2, in separate functions as shown in Figure 12, and visible in the GT example Figure 13. Afterwards, they are composed as in Figure 14.

```

main_decarbonization.m | parameters.m | CASE_optimization.m | BESS_SOC_stationarity_NL_model.m | +
193 %
194 % [Diagram: A box labeled 'GT' with inputs 'P_GT' and 'u_GT' and output 'P_GT * u_GT']
195 %
196 % [Diagram: A box labeled 'BESS' with inputs 'P_REC' and 'P_REC_max' and output 'P_REC * P_REC_max']
197 %
198 %
199 cTx_BESS = 0;
200 cTx_GT = 0;
201 cTx_REC = 0;
202 cTx_DG = 0;
203 cTx_Dv = 0;
204 qTy_xc_GT = 0;
205 qTy_xc_BESS = 0;
206 qTy_xc_DG = 0;
207 qTy_xc_Dv = 0;
208 qTy_xc_Dv = 0;
209 wTz = 0;
210 PRec_vec = zeros(T, W); % vector power of the RECs
211
212 % build case constraint
213 case ('GT24', 'GT24S') % Only GT
214 [cTx_GT, qTy_xc_GT] = cost_GT(Obj, Af, REC.GT.n_NREC, P_GT, u_GT, z_GT, RR, x_GT, T, W); % cost related to the GTs
215 Pbt = zeros(T, W);
216
217 case ('1GT+1WT+DG', '2GT+1WT+DG') % 1/2 GT + WT + BESS
218 [cTx_GT, qTy_xc_GT] = cost_GT(Obj, Af, REC.GT.n_NREC, P_GT, u_GT, z_GT, RR, x_GT, T, W); % cost related to the GTs
219 REC_obj = (WT);
220 REC_obj = reshape_REC_power(REC_obj, Pload);
221 [cTx_REC, P_REC_max, PRec_vec] = cost_REC(REC_obj, Af, n_REC, x_REC);
222 [cTx_BESS, qTy_xc_BESS] = cost_BESS(BAT, Af, x_ESS_IV, x_ESS_IVV);
223
224 case ('1GT+REC+DG', '2GT+REC+DG') % 1/2 GT + REC + BESS
225 [cTx_GT, qTy_xc_GT] = cost_GT(Obj, Af, REC.GT.n_NREC, P_GT, u_GT, z_GT, RR, x_GT, T, W); % cost related to the GTs
226 REC_obj = (PV, WT, REC);
227 REC_obj = reshape_REC_power(REC_obj, Pload);
228 [cTx_REC, P_REC_max, PRec_vec] = cost_REC(REC_obj, Af, n_REC, x_REC);
229 [cTx_BESS, qTy_xc_BESS] = cost_BESS(BAT, Af, x_ESS_IV, x_ESS_IVV);
230
231 case ('WT+DG') % only WT + BESS
232 REC_obj = (WT);
233 REC_obj = reshape_REC_power(REC_obj, Pload);
234 [cTx_REC, P_REC_max, PRec_vec] = cost_REC(REC_obj, Af, n_REC, x_REC);
235 [cTx_BESS, qTy_xc_BESS] = cost_BESS(BAT, Af, x_ESS_IV, x_ESS_IVV);
236
237 case ('REC+U', 'REC+U+DG', 'REC+C+DG24', 'REC+C+DG365') % REC + BESS
238 REC_obj = (PV, WT, REC);
239 REC_obj = reshape_REC_power(REC_obj, Pload);
240 [cTx_REC, P_REC_max, PRec_vec] = cost_REC(REC_obj, Af, n_REC, x_REC);
241 [cTx_BESS, qTy_xc_BESS] = cost_BESS(BAT, Af, x_ESS_IV, x_ESS_IVV);
242
243 case ('DG+REC24', 'DG+REC365') % REC + BESS + DIESEL
244 REC_obj = (PV, WT, REC);
245 REC_obj = reshape_REC_power(REC_obj, Pload);
246 [cTx_REC, P_REC_max, PRec_vec] = cost_REC(REC_obj, Af, n_REC, x_REC);
247 % [cTx_DG, qTy_xc_DG] = cost_DG_linear(DG_obj, Af, REC.DG.n_NREC, P_DG, x_DG, T, W);
248 [cTx_BESS, qTy_xc_BESS] = cost_BESS(BAT, Af, x_ESS_IV, x_ESS_IVV);

```

Figure 12: Cost definitions

4.6 Constraints

Constraints are imposed according to the utilized devices as in Figure 15. For example, for the GT they are as in Figure 16.

4.7 Solving

After having defined costs and constraints, the problem is solved as in Figure 17.

```

main_decarbonization.m | parameters.m | CASE_optimization.m | BESS_SOC_stationarity_NL_model.m | cost_GT.m | +
1 function [cTx, qTy_w] = cost_GT(GT_obj, AF, n_GT, P_GT, u_GT, z_GT, RR, x_GT, T, W)
2 % cost related to the GTs
3
4 % 1st stage variable cost
5 c = zeros(n_GT, 1);
6 for g = 1:n_GT
7     c(g) = GT_obj{g}.C_I;
8 end
9
10 % 2nd stage variable cost
11 % cost associated with the GTs
12 for g = 1:n_GT
13     qTg = [GT_obj{g}.C_per_watt*ones(T, 1); GT_obj{g}.C_on*ones(T, 1); GT_obj{g}.C_start*ones(T, 1); GT_obj{g}.C_RR*ones(T, 1)];
14     y_G(1,1:W,g) = qTg*[P_GT(:,g);u_GT(:,g);z_GT(:,g);RR(:,g)];
15 end
16
17 cTx = AF.CRF*c'*x_GT;
18 qTy_w = sum(y_G, 3);
19 end
20

```

Figure 13: Gas Turbine cost function

```

253
254 % fast_constraint;
255
256 [qTy_w_Pns_Pct] = cost_Pns_Pct(Pns, Pct, T, Pload_obj);
257 [cTy_Pv, qTy_w_Pv] = cost_DGv(AF, P_DGv, T, P_DGv_max_inst, REC.DGv.DGv_obj{1}); % virtual power (i.e. diesel cost without intercept)
258
259 cTx = cTx_GT + cTx_BESS + cTx_REC + cTx_DG + cTx_Pv; % Total 1st stage cost
260 qTy_w = qTy_w_GT + qTy_w_BESS + qTy_w_Pns_Pct + qTy_w_DG + qTy_w_DR + qTy_w_Pv; % Total 2nd stage cost
261
262 f = cTx + AF.gamma*qTy_w*LscensProbVec_N;
263 if num_ESS > 0
264     [wTz] = cost_soft_constraint(BAT, AF, epsilon_bat);
265     f = f + wTz; % add soft constraint in case of presence of the BESS
266 end
267
268 cvar = cvar_zeta + (1/(1 - cvar_alpha))*sum(LscensProbVec_N.*cvar_s);
269 F = (1 - cvar_beta)*f + cvar_beta*cvar;
270 prob.Objective = F;
271

```

Figure 14: Cost composition

```

main_decarbonization.m | parameters.m | CASE_optimization.m | BESS_SOC_stationarity_NL_model.m | cost_GT.m | +
272 %
273 %
274 % Constraints
275 %
276 %
277 Pload_PS = load_PS(Pload, Pps_rem, Pps_add);
278
279 switch case_constraint
280 case {'GT24', 'GT365'} % Only GT
281     P_gen_tot = sum(P_GT, 3);
282     prob = GT_constraints(prob, REC.GT.n_NREC, T, W, GT_obj, u_GT, z_GT, x_GT, P_GT, RR, z_help, case_constraint);
283
284 case {'1GT+WT+DG', '2GT+WT+DG', '1GT+REC+DG', '2GT+REC+DG'} % GT + REC + BESS
285 % GT
286     P_gen_tot = P_res + sum(P_GT, 3);
287     prob = GT_constraints(prob, REC.GT.n_NREC, T, W, GT_obj, u_GT, z_GT, x_GT, P_GT, RR, z_help, case_constraint);
288
289 % REC
290     prob = REC_constraints(prob, P_res, P_REC_max, n_REC, REC_obj, x_REC);
291
292 % BESS
293     prob = BESS_constraints(prob, BESS_NL_model, E0, Ebt, Pch, Pdc, Pbt, Uch, Udc, PchNch, PdcNdc, BAT, x_ESS_IV, x_ESS_NIV, epsilon_bat);
294
295 case {'WT+DG', 'REC+DG24', 'REC+DG365'} % G -> WT + BESS
296     % I -> REC + BESS
297
298 % REC
299     P_gen_tot = P_res;
300     prob = REC_constraints(prob, P_res, P_REC_max, n_REC, REC_obj, x_REC);
301
302 % BESS
303     prob = BESS_constraints(prob, BESS_NL_model, E0, Ebt, Pch, Pdc, Pbt, Uch, Udc, PchNch, PdcNdc, BAT, x_ESS_IV, x_ESS_NIV, epsilon_bat);
304
305 case {'REC+DG'} % REC + BESS w/o plant size constraints and possibility to use Pv
306 % REC
307     P_gen_tot = P_res;
308     prob = max_power(prob, 'REC_max_power', P_res, P_REC_max); % Maximum power produced by the REC
309
310 % BESS
311     prob = BESS_constraints(prob, BESS_NL_model, E0, Ebt, Pch, Pdc, Pbt, Uch, Udc, PchNch, PdcNdc, BAT, x_ESS_IV, x_ESS_NIV, epsilon_bat);
312
313 case {'REC-U'} % REC + BESS w/o plant size constraints
314 % REC
315     P_gen_tot = P_res;
316     prob = max_power(prob, 'REC_max_power', P_res, P_REC_max); % Maximum power produced by the REC
317
318 % BESS
319     prob = BESS_constraints(prob, BESS_NL_model, E0, Ebt, Pch, Pdc, Pbt, Uch, Udc, PchNch, PdcNdc, BAT, x_ESS_IV, x_ESS_NIV, epsilon_bat);
320
321 % Virtual power
322     prob.Constraints.Pv_zero = P_DGv == 0;
323
324 case {'DG+REC24', 'DG+REC365'} % REC + BESS + DIESEL
325 % Total generated power
326     P_gen_tot = P_res + sum(P_DG, 3);
327

```

Figure 15: General constraints

```

main_decarbonization.m  parameters.m  CASE_optimization.m  BESS_SOC_stationarity_NL_model.m  cost_GT.m  GT_constraints.m  +
1  function prob = GT_constraints(prob, n_GT, T, W, GT_obj, u_GT, z_GT, x_GT, P_GT, RR, z_help, case_constraint)
2      % Constraints related to the GT
3
4      switch case_constraint
5          case {'GT24','GT365'}
6              prob = GT_offtime(prob, n_GT, T, W, GT_obj, u_GT);
7              prob = GT_startUP(prob, n_GT, T, W, z_GT, u_GT);
8              prob = GT_P_minmax(prob, n_GT, T, W, P_GT, x_GT, GT_obj, u_GT, z_help);
9              prob = GT_rump_UP(prob, n_GT, T, W, P_GT, GT_obj);
10             prob = GT_rump_UP_cost_constraint(prob, n_GT, T, W, P_GT, RR);
11
12             case {'1GT+WT+DG', '2GT+WT+DG', '1GT+REC+DG', '2GT+REC+DG'}
13                 prob = GT_offtime(prob, n_GT, T, W, GT_obj, u_GT);
14                 prob = GT_startUP(prob, n_GT, T, W, z_GT, u_GT);
15                 prob = GT_P_minmax_fix_GT_number(prob, n_GT, T, W, P_GT, GT_obj, u_GT);
16                 prob = GT_rump_UP(prob, n_GT, T, W, P_GT, GT_obj);
17                 prob = GT_rump_UP_cost_constraint(prob, n_GT, T, W, P_GT, RR);
18
19             end
20
21         end

```

Figure 16: Gas Turbine constraints

```

370  %
371  % SOLUTION
372  %
373  %
374  %
375
376  fprintf('Start solution\n')
377
378  % prob.Constraints.tmp1 = x_REC == 1;
379  % prob.Constraints.tmp2 = x_ESS_IV == 4e6;
380  % prob.Constraints.tmp2 = x_ESS_NIV == 4;
381
382  opt = optimoptions('intlinprog', 'Display', 'iter', 'AbsoluteGapTolerance', abs_gap_tol, 'RelativeGapTolerance', rel_gap_tol, 'IntegerTolerance', 1e-3, 'MaxTime', 2*3600, 'Heur');
383  prob.ObjectiveSense = 'minimize';
384  [values_solution, values_minvalue, tmp, min_info] = solve(prob, 'Options', opt);
385
386  values_solution.min_info = min_info;
387  values_solution.values_minvalue = values_minvalue;
388
389  fprintf('Solution ended\n')
390
391  if ~isempty(queue)
392      % write the messages to be sent to the queue
393      tmp_message.case_constraint = case_constraint;
394      tmp_message.values_minvalue = values_minvalue;
395
396      send(queue, tmp_message)
397  end
398

```

Figure 17: Solving the optimization problem

4.8 Post-Processing

Computes costs including already installed devices, CO₂ emissions, installed power as shown in Figure 18.

```

399 %
400 %
401 %
402 %
403 %
404 %
405 %
406 % Check that the battery does not charge and discharge at the same time
407 if isfield(values_solution, 'Pch')
408     check_charging(values_solution);
409 end
410 % Reshape values in a vector
411 values_n_REC = n_REC;
412 [values_vector, values_solution] = reshape_data(values_solution, Pload, Pres_vec, BAT);
413 %
414 %
415 %
416 % Compute the capacity factors
417 % values_vector = capacity_factor(values_vector, values_vector, PV, WT, WEC, BAT, W, T);
418 %
419 % Compute the emitted CO2
420 compute_CO2
421 %
422 % compute the installed power
423 compute_installed_power;
424 %
425 % Evaluate the costs
426 compute_final_costs;
427 %
428 % Compute the CVaR
429 values_solution.CVaR = values_solution.cvar_zeta + (1/(1 - cvar_alpha))*LscnsProbVec_N*values_solution.cvar_s;
430 %
431 % Effective LPSP
432 values_solution.LPSP_eff = sum(values_vector.Pns)/sum(Pload, 'all');
433 %
434 end

```

Figure 18: Post-processing results

5 Results and Plots

The results can be displayed using `plot_decarbonization` (Figure 19), for producing plots like the one in Figure 20, Figure 21, and Figure 22.

```

150 end
151 end
152 %
153 %
154 %
155 %
156 %
157 %
158 %
159 %
160 %
161 close all;
162 plot_decarbonization

```

Figure 19: Example plot layout

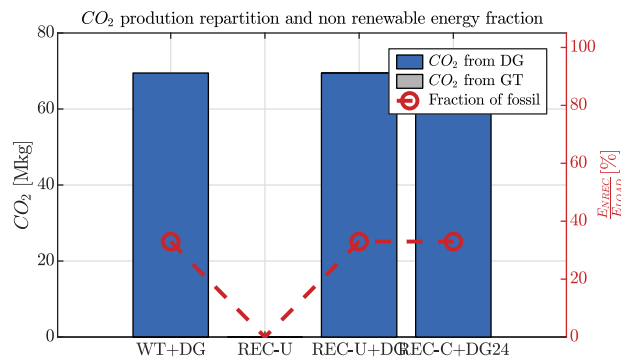


Figure 20: CO_2 fraction

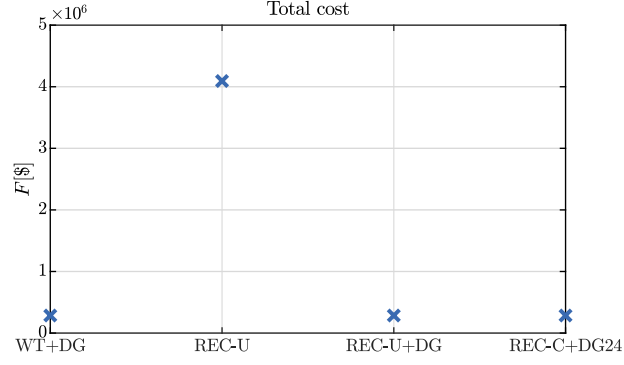


Figure 21: Total cost

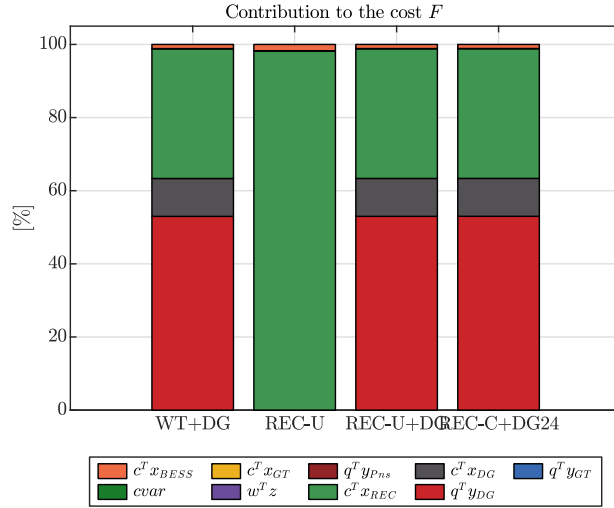


Figure 22: Cost fraction breakdown