Rescheduling the NBA regular season via Integer Programming

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JULY 2023



July 10-14 · SANTIAGO, CHILE















Impact in sport leagues around the world



UEFA Champions League Final (2020)



NBA Bubble (2019 - 2020)



Rescheduling matches pre and post COVID

Pre-COVID

COVID

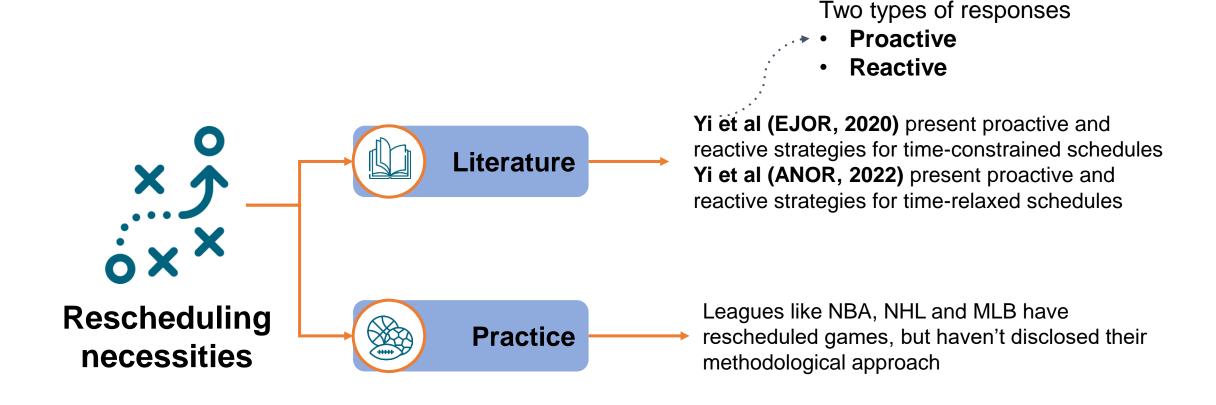
- Suspended matches are rare
- Suspensions are usually not related to each other

- Suspended matches are more common due to the health situation
- If multiple players become sick, consecutive games might be suspended

34%

Probability of a match being suspended in the NBA 2020-21 season, given than the previous match was suspended

Rescheduling in sports



The 2020 - 2021 NBA Season

The NBA applied the following contingency actions during the season:

Proactive scheduling strategy:

1. Schedule only the first half of the season (All-Star Game);

Q: Is there a way to see a breakdown of the schedule for 2020-21?

Yes, the 2020-21 regular season opponent matrix for each NBA team is available here. Full team-by-team schedules for the first half of 2020-21 are here.

- 1. Postpone games if a teams has insufficient players to the second half;
- 2. Generate a schedule for the second half + suspended games
- 3. Ad-hoc reschedule for games suspended during the second half.

72Games per team

5 Suspended games

3% Games suspended



Our approach: a reactive strategy

Definition

Each game in the executed timetable that is played before or after its scheduled round is considered a **disruption**. In our setup, each suspended game will therefore translate into a disruption that needs to be rescheduled in the remaining of the season schedule

Research Question

Can we systematically generate an *adjusted fixture* by rescheduling postponed games within the planned schedule?

Approach: a reactive strategy

- Consider as input the planned schedule for the entire season.
- Insert the disrupted matches onto the existing schedule, maintaining the original scheduled dates for non-disrupted matches
- We build a linear optimization model to find the best possible date for each disruption and, if we can't, we reschedule it after the end of the schedule's original date



Notations and Definitions

General

Set of teams: $S = \{1, \dots, m\}$

Set of original rounds: $T = \{1, ..., r\}$

Match between j and k: (j, k)

Scheduled game: Match between j

and k on round t: $\alpha = <(j, k), t>$

Schedule Rules

Scheduled games of team $i: R_i$

Disrupted games of team $i: R_i^{dis}$

Total disrupted games: $R^{dis} = \bigcup_{i \in S} R_i^{dis}$

Potential candidate variables dates for match $\alpha = T_{\alpha}^{free}$

Maximum number of games that a team can play within every window of $t_2 - t_1$ days: MG_{t_1,t_2}

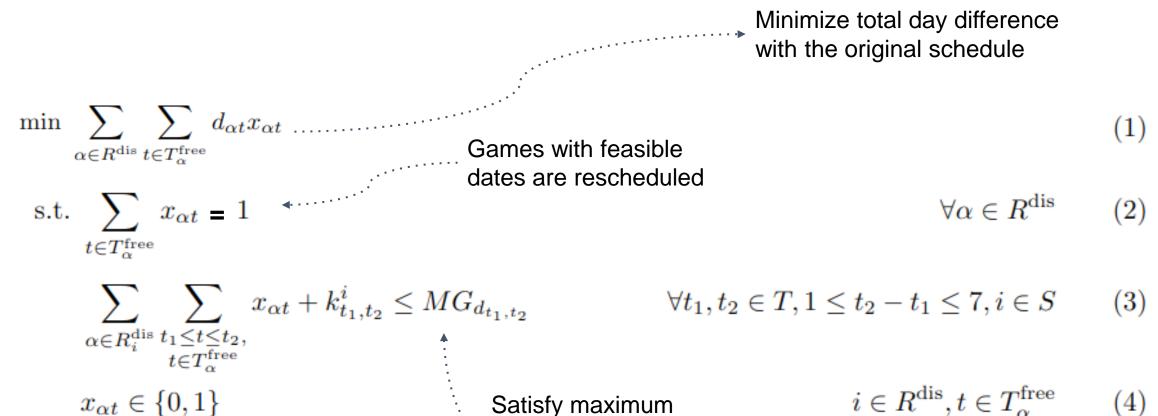
Number of non-disrupted games a team is playing between dates t_2 and t_1 : k_{t_1,t_2}^i

Decision variables

 $x_{\alpha t} = 1$ iff disrupted game α is rescheduled into round t



Mathematical Model (MinD)



Satisfy maximum $i \in R^{\mathrm{dis}}, t \in T_{\alpha}^{\mathrm{free}}$ number of games in $[\mathsf{t_1}, \mathsf{t_2}]$



Preliminary Experiments

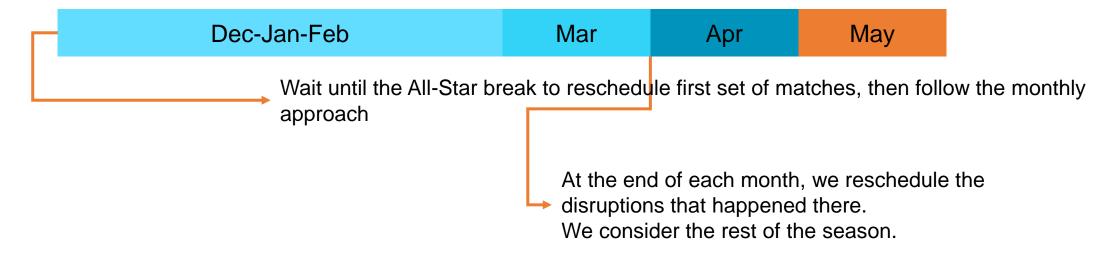
- Rescheduled dates for postponed games are not considered as part of the input schedule (except for some special configurations)
- We consider the following metrics:
 - Classical from scheduling: distance, breaks.
 - New: # of day added and # of games played after the end of the season in the planned schedule.
- Models and algorithms implemented in Python + CPLEX.

Rescheduling Strategy

 In order to get a better understanding of the performance of our solution we try to replicate the rescheduling process for the suspended games of the 2020-21 NBA season

Rescheduling methodology

Post All-Star



Post All Star*

Use the NBA's reschedules if they happened within the rescheduled window.



Main Results

Number of additional days needed after the end of the season

Metric	NBA exec	Post All Star	Post All Star*
Distance	-0.2%	0.03%	0.35%
Breaks	0.6%	0.3%	0.5%
# Dates Added	-	5	0
Games After	-	5	0
Exec. Time		5.98 min	5.62 min

Number of games scheduled after the end of the season



Key Takeouts

All differences are small (<1%)

The NBA's proactive approach has effects on the additional number of dates needed



Further Disruptions Scenarios

We consider instances stressing the number and timing of the disruptions:

• 15 more games: ~50% increase in the problem size

• 25 more games: ~80% increase in the problem size

• 15 more March games: Similar to a second COVID wave

Instance / Metric	Distance	Breaks	# dates added	Games after	Exec. Time
15 more games	3.4%	-0.7%	11	17	8.13 min
25 more games	5.1%	-0.6%	12	23	8.06 min
15 more games in March	1.3%	0.1%	9	20	7.61 min



Difference against the planned NBA schedule, post All-Star strategy



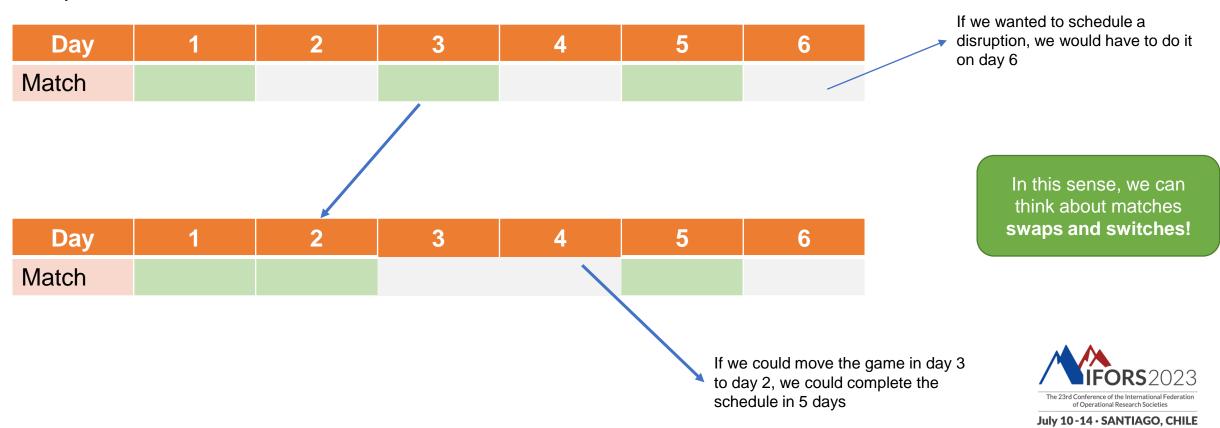
Effects on relevant KPIs is not negligible



How can we improve the existing solution

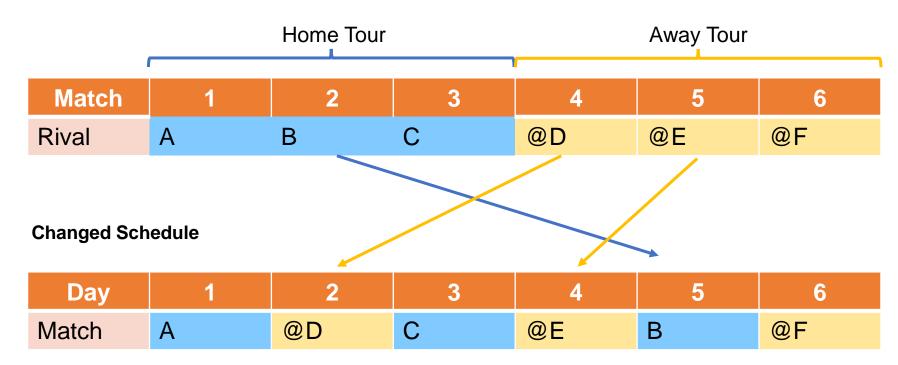
Given the current result, especially the effect on relevant KPIs of bigger instances, we might consider that a different approach is necessary:

Example



Beware of the modifications!

Example: Original Schedule



Our current approach might change the tour order, increasing the total distance travelled



How can we adapt the existing model?

Additional variables

- Non Disrupted Games of Team i: R_iND
- Set of rounds post-tournament: $TP = \{r + 1, ... r + 181\}$
- Maximum days of difference between match date and original date for non disruptions: d
- Original date for non disrupted match $\bar{\alpha}$: $\tau_{\bar{\alpha}}$
- Potential candidate dates for non disrupted match $\bar{\alpha}$: $T_{\bar{\alpha}}^{free} = \{\tau_{\bar{\alpha}} d, ... \tau_{\bar{\alpha}} + d\}$
- Tours of team $i: TO_i = \{TO_{i1}, TO_i\}$
- Tour n of team $i: TO_{i1} = \{\overline{\alpha_{n1}, \alpha_{n2}, ...}\}$
- Maximum non disruptions whose date can be modified within a tour: td
- Maximum non disruptions whose date can be modified within a window: md
- Variable that indicates that non disrupted match $\bar{\alpha}$ is scheduled on round $t: \bar{x}_{\alpha t}$
- Tour Start date of the tour that contains match $\bar{\alpha}$ of team $i: s_{\alpha i}$



$$\min \sum_{\alpha \in R^{DIS}} \sum_{t \in T_{\alpha}^{free}} d_{\alpha t} * x_{\alpha t} + \sum_{\alpha \in R^{DIS}} \sum_{t \in TP} 100 * d_{\alpha t} * x_{\alpha t}$$

$$s.t \sum_{t \in T_{\alpha}^{free}} x_{\alpha t} + \sum_{t \in TP} x_{\alpha t} = 1$$

$$\forall \alpha \in R^{DIS}$$

$$\sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} = 1$$

$$\forall \; \bar{\alpha} \; \in R^{ND}$$

$$\sum_{\substack{\alpha \in R_i^{DIS} \\ t_1 \leq t \leq t_2}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t_1 \leq t \leq t_2}} x_{\alpha t} + \sum_{\overline{\alpha} \in R_i^{ND}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t_1 \leq t \leq t_2}} \overline{x_{\alpha t}} \leq MG_{d_{t_1 t_2}}$$

$$\forall t_1, t_2 \in T \cup TP, 1 \le t_2 - t_1 \le 7, i \in S$$

$$\sum_{\overline{\alpha} \in TO_{in}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t \neq \tau_{\overline{\alpha}}}} \overline{x_{\alpha t}} \leq td$$

$$\forall \ n \ \in TO_i, i \ \in S$$

(10)

(11)

$$\sum_{\overline{\alpha}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t \neq \tau_{\overline{\alpha}}}} \overline{x_{\alpha t}} \leq md$$

$$\forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2$$

$$x_{\alpha t}, \overline{x_{\alpha t}} \in \{0; 1\}$$

 $\overline{x_{\alpha 1t1}} + \overline{x_{\alpha 2t2}} \le 1$

New mathematical m Minimize Day Difference Between Original and Final Date

$$\min \sum_{\alpha \in R^{DIS}} \sum_{t \in T_{\alpha}^{free}} d_{\alpha t} * x_{\alpha t} + \sum_{\alpha \in R^{DIS}} \sum_{t \in TP} 100 * d_{\alpha t} * x_{\alpha t}$$
(5)

$$s. t \sum_{t \in T_{\alpha}^{free}} x_{\alpha t} + \sum_{t \in TP} x_{\alpha t} = 1 \qquad \forall \alpha \in R^{DIS}$$

$$(6)$$

$$\sum_{t \in T_{\bar{\alpha}}^{free}} \overline{x_{\alpha t}} = 1 \qquad \forall \bar{\alpha} \in R^{ND}$$
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$$\sum_{\alpha \in R_i^{DIS}} \sum_{t \in T_{\overline{\alpha}}^{free}} x_{\alpha t} + \sum_{\overline{\alpha} \in R_i^{ND}} \sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} \leq MG_{d_{t_1 t_2}} \qquad \forall t_1, t_2 \in T \cup TP, 1 \leq t_2 - t_1 \leq 7, i \in S$$
 (8)

$$\sum_{\overline{\alpha} \in TO_{in}} \sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} \leq td \qquad \forall n \in TO_i, i \in S$$

$$(9)$$

$$\sum_{\overline{x}} \sum_{free} \overline{x_{\alpha t}} \le md \tag{10}$$

$$\frac{t \in T_{\overline{\alpha}}^{Iree}}{t \neq \tau_{\overline{\alpha}}}$$

$$\frac{t \neq \tau_{\overline{\alpha}}}{x_{\alpha 1t1}} + \overline{x_{\alpha 2t2}} \leq 1$$

$$\forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2$$
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$$\min \sum_{\alpha \in R^{DIS}} \sum_{t \in T_{\alpha}^{free}} d_{\alpha t} * x_{\alpha t} + \sum_{\alpha \in R^{DIS}} \sum_{t \in TP} 100 * d_{\alpha t} * x_{\alpha t}$$
All disruptions should be scheduled in existing or extra dates

$$s. t \sum_{t \in T_{\alpha}^{free}} x_{\alpha t} + \sum_{t \in TP} x_{\alpha t} = 1 \qquad \forall \alpha \in R^{DIS}$$

$$(6)$$

$$\sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} = 1 \qquad \forall \, \overline{\alpha} \in R^{ND}$$

$$\sum_{\alpha \in R_i^{DIS}} \sum_{t \in T_{\overline{\alpha}}^{free}} x_{\alpha t} + \sum_{\overline{\alpha} \in R_i^{ND}} \sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} \leq MG_{d_{t_1 t_2}} \qquad \forall t_1, t_2 \in T \cup TP, 1 \leq t_2 - t_1 \leq 7, i \in S$$
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$$\sum_{\overline{\alpha} \in TO_{in}} \sum_{t \in T^{free}} \overline{x_{\alpha t}} \leq td \qquad \forall n \in TO_i, i \in S$$

$$(9)$$

$$\sum_{\overline{x}} \sum_{f \neq \alpha} \overline{x_{\alpha t}} \leq md \tag{10}$$

$$\frac{t \in I_{\overline{\alpha}}}{t \neq \tau_{\overline{\alpha}}}$$

$$\overline{x_{\alpha 1t 1}} + \overline{x_{\alpha 2t 2}} \leq 1$$

$$\forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2$$

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$$x_{\alpha t}, \overline{x_{\alpha t}} \in \{0; 1\}$$



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$$\min \sum_{\alpha \in R^{DIS}} \sum_{t \in T_{\alpha}^{free}} d_{\alpha t} * x_{\alpha t} + \sum_{\alpha \in R^{DIS}} \sum_{t \in TP} 100 * d_{\alpha t} * x_{\alpha t}$$

$$\tag{5}$$

s.
$$t \sum_{t \in T_{\alpha}^{free}} x_{\alpha t} + \sum_{t \in TP} x_{\alpha t} = 1$$
 All non disruptions should be scheduled in possible dates

$$\sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} = 1 \qquad \forall \, \overline{\alpha} \in R^{ND}$$
 (7)

$$\sum_{\alpha \in R_i^{DIS}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t_1 \le t \le t_2}} x_{\alpha t} + \sum_{\overline{\alpha} \in R_i^{ND}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t_1 \le t \le t_2}} \overline{x_{\alpha t}} \le MG_{d_{t_1 t_2}} \qquad \forall t_1, t_2 \in T \cup TP, 1 \le t_2 - t_1 \le 7, i \in S$$

$$(8)$$

$$\sum_{\overline{\alpha} \in TO_{in}} \sum_{t \in T^{free}} \overline{x_{\alpha t}} \le td \qquad \forall n \in TO_i, i \in S$$

$$(9)$$

$$\sum_{\overline{\alpha}} \sum_{-free} \overline{x_{\alpha t}} \le md \tag{10}$$

$$\frac{t \neq \tau_{\bar{\alpha}}}{x_{\alpha 1 t 1} + x_{\alpha 2 t 2}} \leq 1 \qquad \forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2$$
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 $\forall \ \overline{\alpha} \in R^{ND}$ Schedule rules must be followe

Schedule rules must be followed

$$\sum_{\substack{\alpha \in R_i^{DIS} \\ t_1 \le t \le t_2}} \sum_{t \in T_{\overline{\alpha}}^{free}} x_{\alpha t} + \sum_{\overline{\alpha} \in R_i^{ND}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t_1 \le t \le t_2}} \overline{x_{\alpha t}} \leq MG_{d_{t_1 t_2}} \qquad \forall t_1, t_2 \in T \cup TP, 1 \le t_2 - t_1 \le 7, i \in S$$

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$$\sum_{\overline{\alpha} \in TO_{in}} \sum_{t \in T_{i}^{free}} \overline{x_{\alpha t}} \leq td \qquad \forall n \in TO_{i}, i \in S$$

$$(9)$$

$$\sum_{\overline{\alpha}} \sum_{-free} \overline{x_{\alpha t}} \le md \tag{10}$$

$$\frac{x_{\alpha 1}}{x_{\alpha 1}} + \frac{x_{\alpha 2}}{x_{\alpha 2}} \le 1 \qquad \forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2 \qquad (11)$$

$$x_{\alpha t}, \overline{x_{\alpha t}} \in \{0; 1\}$$



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$$\forall \ t_1, t_2 \in T \cup TP, 1 \leq t_2 - t_1 \leq 7, i \in S$$

$$\text{No more tan } \textit{td} \text{ non disruptions can be changed per tour}$$

$$\sum_{\overline{\alpha} \in TO_{in}} \sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} \leq td \qquad \forall n \in TO_i, i \in S$$

$$(9)$$

$$\sum_{\overline{x}} \sum_{\alpha t} \overline{x_{\alpha t}} \leq md \tag{10}$$

$$\frac{\alpha}{t \in T_{\overline{\alpha}}^{Tree}}$$

$$\frac{t \neq \tau_{\overline{\alpha}}}{x_{\alpha 1t1}} + \overline{x_{\alpha 2t2}} \leq 1$$

$$\forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2$$
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$$\sum_{\overline{\alpha}} \sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} \le md \tag{10}$$

$$\overline{x_{\alpha 1t1}} + \overline{x_{\alpha 2t2}} \le 1$$
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$$x_{\alpha t}, \overline{x_{\alpha t}} \in \{0; 1\}$$



(5)

(12)

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$\sum_{\overline{\alpha}} \sum_{\substack{t \in T_{\overline{\alpha}}^{free} \\ t \neq \tau_{\overline{\alpha}}}} \overline{x_{\alpha t}} \leq md$

Avoid tours being overlapped with modifiations

$$\overline{x_{\alpha 1t1}} + \frac{\alpha}{x_{\alpha 2t2}} \le 1$$

$$\forall \alpha 2, \alpha 1 \in R_i^{ND}, i \in S, s_{\alpha 1} > s_{\alpha 2}, t_1 < t_2$$

 $x_{\alpha t}, \overline{x_{\alpha t}} \in \{0, 1\}$

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$$\sum_{\overline{\alpha}} \sum_{t \in T_{\overline{\alpha}}^{free}} \overline{x_{\alpha t}} \le md \tag{10}$$

 $x_{\alpha t}, \overline{x_{\alpha t}} \in \{0; 1\} \tag{12}$

(5)

Effects on relevant KPIs

To get an understanding on the effect of this possible changes, let's analyze the results with a Post All Star scheduling strategy with our biggest instance: original disruptions + 25 new ones, where the maximum number of non-disruptions to be changed by window is 10:



^{*} Against original planned schedule

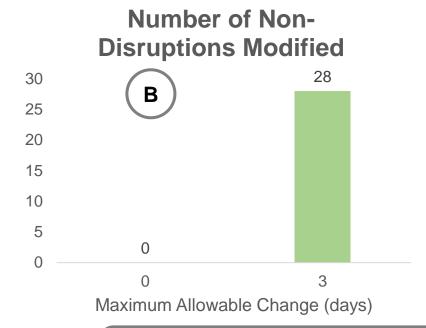
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Effects on relevant KPIs

To get an understanding on the effect of this possible changes, let's analyze the results with a Post All Star scheduling strategy with our biggest instance: original disruptions + 25 new ones, where the maximum number of non-disruptions to be changed by window is 10:



The possibility to reschedule more games increases complexity, although relationship is not clear



2% of the total games are being modified,

which is similar to the number of disruptions

of Operational Research Societies

^{*} Against original planned schedule

Summary

- We framed the problem of rescheduling in time-relaxed tournaments
- We evaluate different rescheduling strategies building on MIP models
- Initial results show we are obtaining similar results than the ones produced by the NBA
- More stressed disrupted scenarios have a considerable impact on relevant KPIs
- Schedule modifications may help reduce the impact of multiple disruptions on more stressed scenarios

Next steps

- Limit potential changes in order to find a good balance between additional dates needed to complete a schedule and total distance travelled
- Elaborate new model that enumerates potential tour changes and finds a schedule that generates the minimum distance.

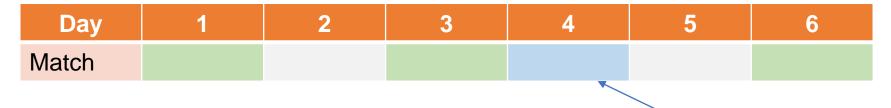


Next Steps

Tour – Sequence 1

Day	1	2	3	4	5	6
Match						

Tour – Sequence 2



Select the sequence that minimizes distance when rescheduling disruptions

Inserted disruption

Tour – Sequence 3

Day	1	2	3	4	5	6
Match						



ADVANCED ANALYTICS FOR A BETTER WORLD













