

**1. What is the probability of a CDO failing to pay out if it consists of 10 loans, each with independent failure probability of 0.1?**

$$\mathbb{P}(\text{"CDO fails to pay out"}) = \mathbb{P}(\text{"every loan fails"})$$

Since the probability of failure of each bond is independent and equal to 0.1:

$$\mathbb{P}(\text{"every loan fails"}) = (0.1)^{10} = 10^{-10} = 0.0000000001$$

The probability that the CDO fails to pay out is  $10^{-10}$ .

**2. How many independent subprime loans, each with failure probability 0.5, are needed to create a triple-A CDO (failure risk < 0.0012)?**

$$\text{failure risk} = \mathbb{P}(\text{"CDO fails to pay out"}) = (0.5)^n$$

where  $n$  is the number of loans.

$n = 9$  :

$$\text{failure risk} = (0.5)^9 = 0.00195$$

$n = 10$  :

$$\text{failure risk} = (0.5)^{10} = 0.000977$$

Therefore, at least 10 independent subprime loans are needed.