

Father first (Father-Coach-Father):

The probability of winning two consecutive matches is $P_F(\{WWW, WWL, LWW\})$:

$$P_F(WWW) = 0.75 * 0.4 * 0.75 = 0.225$$

$$P_F(WWL) = 0.75 * 0.4 * 0.25 = 0.075$$

$$P_F(LWW) = 0.25 * 0.4 * 0.75 = 0.075$$

$$\begin{aligned} P_F(\{WWW, WWL, LWW\}) &= P_F(WWW) + P_F(WWL) + P_F(LWW) = \\ &= 0.225 + 0.075 + 0.075 = \mathbf{0.375} \end{aligned}$$

Coach first (Coach-Father-Coach):

The probability of winning two consecutive matches is $P_C(\{WWW, WWL, LWW\})$:

$$P_C(WWW) = 0.4 * 0.75 * 0.4 = 0.12$$

$$P_C(WWL) = 0.4 * 0.75 * 0.6 = 0.18$$

$$P_C(LWW) = 0.6 * 0.75 * 0.4 = 0.18$$

$$\begin{aligned} P_C(\{WWW, WWL, LWW\}) &= P_C(WWW) + P_C(WWL) + P_C(LWW) = \\ &= 0.12 + 0.18 + 0.18 = \mathbf{0.48} \end{aligned}$$

Since $P_C = 0.48 > 0.375 = P_F$, the order **Coach-Father-Coach** maximizes the chances of winning.

If the requirement for consecutive wins is removed then:

Father first (Father-Coach-Father):

The probability of winning two matches is $P_{F'}(\{WWW, WWL, LWW, WLW\}) = P_F + P_F(WLW)$:

$$P_F(WLW) = 0.75 * 0.6 * 0.75 = 0.3375$$

$$P_{F'}(\{WWW, WWL, LWW, WLW\}) = 0.375 + 0.3375 = \mathbf{0.7125}$$

Coach first (Coach-Father-Coach):

The probability of winning two matches is $P_{C'}(\{WWW, WWL, LWW, WLW\}) = P_C + P_C(WLW)$.

$$P_C(WLW) = 0.4 * 0.25 * 0.4 = 0.04$$

$$P_{C'}(\{WWW, WWL, LWW, WLW\}) = 0.48 + 0.04 = \mathbf{0.52}$$

In this case, since $P_{F'} = \mathbf{0.7125} > \mathbf{0.52} = P_{C'}$ the order **Father-Coach-Father** is preferred.