

BACKHAUL OPTIMIZATION

Consider the common backhaul scenarios shown in Figure I of the Appendix.

1. General form of Linear Programming (LP) Model for Backhauls (Empty Mile-based)

Method (1): Minimize $z = \sqrt{\text{dist}(a, d)^2 + \text{dist}(b, c)^2}$

Subject to:

$$\text{dist}(b, c) + \text{dist}(c, d) + \text{dist}(d, a) \geq \text{dist}(a, b)$$

$$\text{dist}(a, b), \text{dist}(b, c), \text{dist}(c, d), \text{dist}(a, d) \geq 0$$

Notes on Method (1):

- Considers **loaded miles** from $\text{dist}(a, b)$ and $\text{dist}(c, d)$ as a **value-added** service.
- Considers **empty miles** from $\text{dist}(a, d)$ and $\text{dist}(b, c)$ as a **non-value-added** service.
- This model seeks to minimize the non-value-added distance traveled (empty miles from (1) the destination to the pick-up location and (2) the drop-off location to the origin).

2. General form of Linear Programming (LP) Model for Backhauls (Distance-based)

Method (2): Minimize $z = \text{dist}(b, c) + \text{dist}(c, d) + \text{dist}(d, a) - \text{dist}(a, b)$

Subject to:

$$\text{dist}(b, c) + \text{dist}(c, d) + \text{dist}(d, a) \geq \text{dist}(a, b)$$

$$\text{dist}(c, d) \geq 100$$

$$\text{dist}(c, d) \geq 0.5 \times \text{dist}(a, b)$$

$$\text{dist}(a, b), \text{dist}(b, c), \text{dist}(c, d), \text{dist}(a, d) \geq 0$$

Notes on Method (2):

- This model aims to minimize the total round-trip distance by considering that the shortest possible return path would be if the following equation were true: $\text{dist}(b, c) + \text{dist}(c, d) + \text{dist}(d, a) = \text{dist}(a, b)$.
- The additional constraints handle cases where the backhaul pick-up and drop-off locations are along the same path as the actual return, but only make up a small portion of the journey back, resulting in excess empty miles traveled.

3. General form of Linear Programming (LP) Model for Backhauls (Cost-based)

Method (3): Minimize $z = \text{cpm}_1(\text{dist}(a, b) + \text{dist}(b, c) + \text{dist}(c, d) + \text{dist}(d, a)) - \text{cpm}_2(\text{dist}(c, d))$

Subject to:

$$\text{dist}(b, c) + \text{dist}(c, d) + \text{dist}(d, a) \geq \text{dist}(a, b)$$

$$\text{dist}(a, b), \text{dist}(b, c), \text{dist}(c, d), \text{dist}(a, d) \geq 0$$

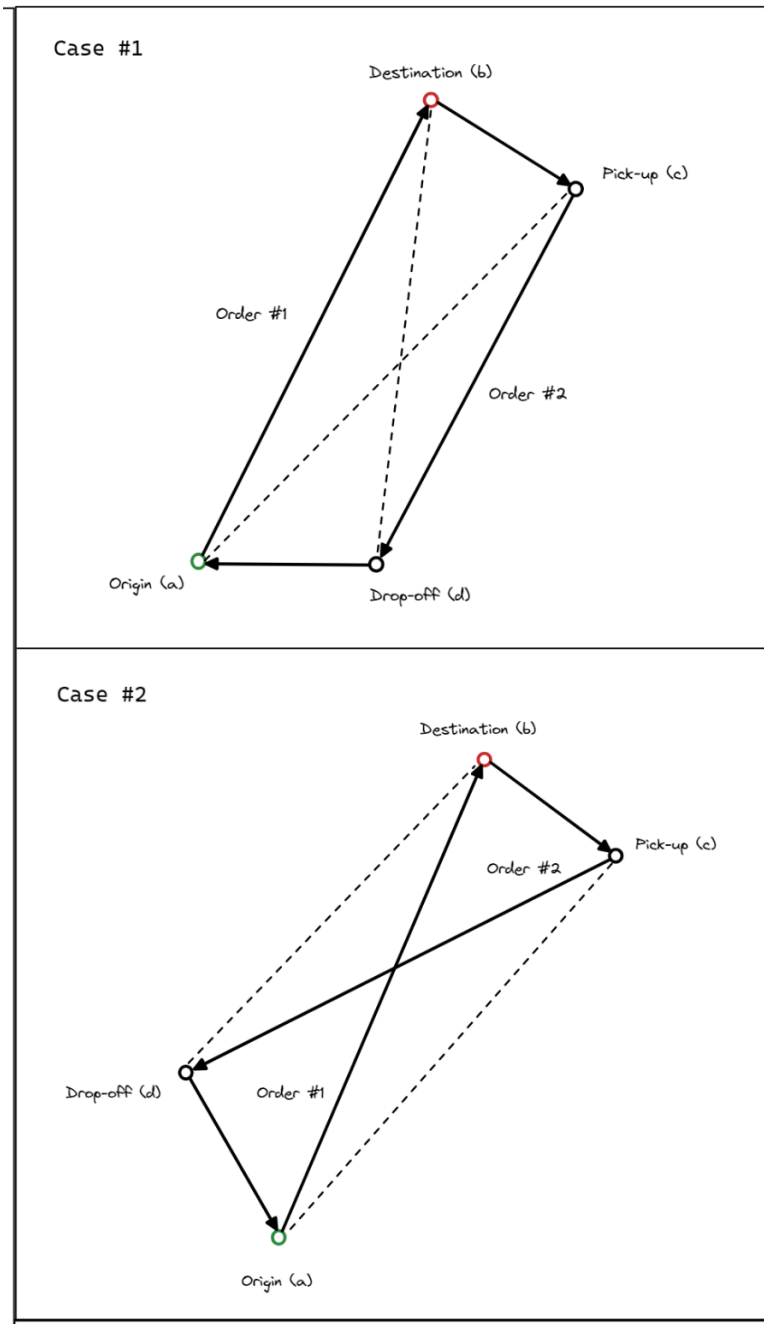
Where $\text{cpm}_1 = \text{cost per mile (standard)}$ and $\text{cpm}_2 = \text{revenue per mile (backhaul)}$

Notes on Method (3):

- This model seeks to minimize an estimate of the **total round-trip cost less backhaul revenue** using the straight-line distance between two locations.

APPENDIX

Figure I: Common Backhaul Scenarios



Cost Equations (Actual)

(1) *Actual OD Pair Cost = Round Trip Miles × CPM (standard) – Backhaul Revenue*

$$(2) \text{ Actual OD Pair CPM} = \frac{\text{Actual OD Pair Cost}}{\text{OD Pair Loaded Miles (one way)}}$$

Note: Miles are actual road miles driven.