



浙江大学爱丁堡大学联合学院  
ZJU-UoE Institute

## Filters

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Nicola Romanò - [nicola.romano@ed.ac.uk](mailto:nicola.romano@ed.ac.uk)

- Define convolutional filters
- Explain their use in image analysis
- Implement basic filters in Python



# Types of pixel operations

Operations for manipulating pixel intensities

Two types of operations:

- Point operations - Change pixel intensity based only on its value -  $I'_{(x,y)} = f(I_{x,y})$  (see Lecture 3)
- **Neighborhood operations** - Change pixel intensity based on the intensity of the pixel and its neighbours.

Neighborhood operations, often called **filters** allow to modify an image in a way that is not possible with point operations.

- Detect simple structures such as edges, corners, lines, etc.
- Perform operations such as smoothing, sharpening, etc.
- Noise reduction

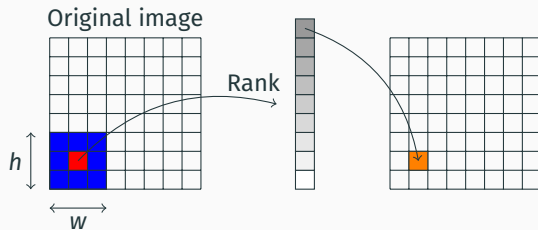
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Today we will look at:

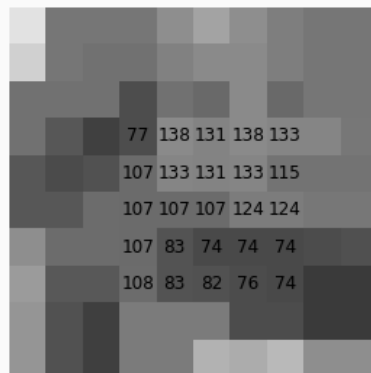
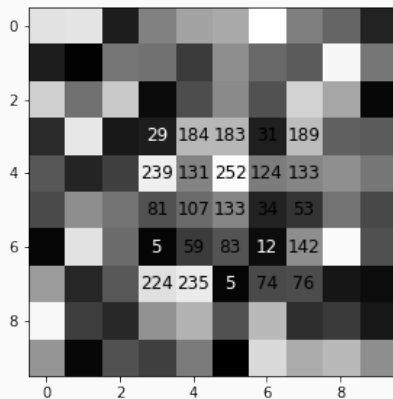
- **Rank filters** - the new pixel value is a function of the rank of the pixel values of the neighborhood
- **Convolutional filters** - the new pixel value is a weighted sum of the pixel values of the neighborhood

### Rank filters



- We decide on a window size  $w \times h$  (other non-rectangular shapes are possible)
- We traverse each pixel in the image and take its  $w \times h$  neighborhood
- We rank the intensity of each pixel in the neighborhood
- We take a specific value (e.g. minimum, maximum, mean, median) and set the output value to this value

## Example - median filter





## Rank filters in Scikit Image

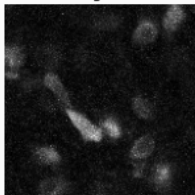
Rank filters are implemented in Scikit Image in the 'skimage.rank' module. These filters require a *footprint* of the pixel neighborhood, as a matrix of 0 and 1.

For example

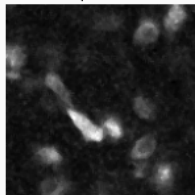
```
from skimage.rank import median

# 3x3 neighborhood
footprint = np.ones(3, 3)
img_median = median(img, selem=footprint)
```

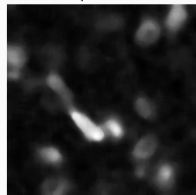
Original



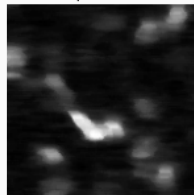
Footprint: 3x3



Footprint: 7x7



Footprint: 3x15

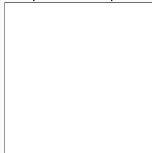


## Non-rectangular footprints

The footprint can be a *non-rectangular* matrix. For example, you can generate a footprint with a **circular** shape using the `skimage.morphology.disk` function or one with a **diamond** shape using the `skimage.morphology.diamond` function.

```
from skimage.morphology import disk,  
diamond  
  
dsk = disk(7) # A disk, radius 7  
dia = diamond(7) # A diamond, radius 7  
  
fig, ax = plt.subplots(1, 2)  
ax[0].imshow(dsk, cmap="gray")  
ax[1].imshow(dia, cmap="gray")
```

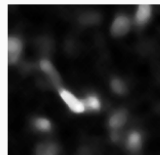
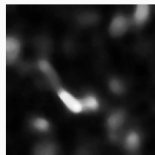
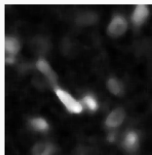
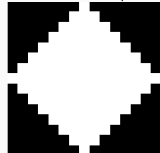
Square Footprint



Disk Footprint



Diamond Footprint



Rank filters are very simple, but have useful applications.

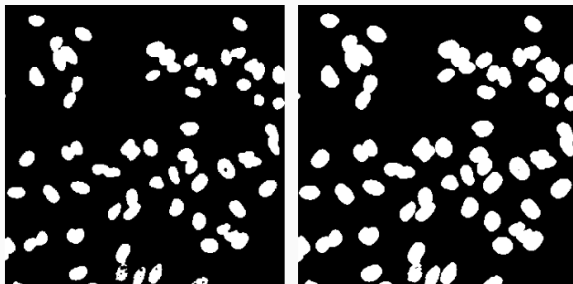
The **median and mean filter** are used to remove noise and to smooth images.

## Rank filters - use cases

Rank filters are very simple, but have useful applications.

The **median and mean filter** are used to remove noise and to smooth images.

The **maximum filter** can be used in binary images to remove small "holes". It is also a very common filter used in modern neural networks for image analysis.



The maximum filter can remove small holes in binary masks

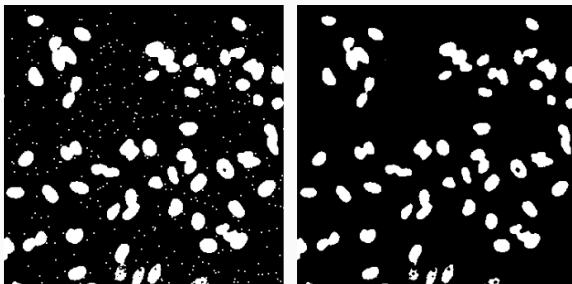
## Rank filters - use cases

Rank filters are very simple, but have useful applications.

The **median and mean filter** are used to remove noise and to smooth images.

The **maximum filter** can be used in binary images to remove small "holes". It is also a very common filter used in modern neural networks for image analysis.

The **minimum filter** can be used to remove small bright spots.



The minimum filter can remove small bright spots in binary masks