Introduction to data-science with Python

Nicolas Jouvin

M2 data science Évry 2022

Outline

Python?









Singularity



Singularity



Shitty visualization



Singularity



Shitty visualization



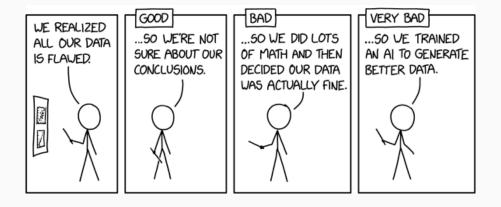
WTF Google Image ?!

```
import numpy as np
def predict(X, y):
    0.00
    Documentation
    0.00
    # Do something clever
res = predict(X, y)
res.plot()
```

Definition

Machine learning = statistics + scientific programming.

XKCD¹ always has the final words...



¹https://xkcd.com/



Organization

Course dates

Teaching material On https://github.com/nicolasJouvin/introduction_python

4 sessions, 3h each. Each session is a mix of slides + practical session (+ breaks)

Important Form groups if you need

- 2 student/group max ideally
- one machine per group (minimum)
- heterogeneous levels in Python (collaboration)

The dates are on the master's agenda

Evaluation Final exam on machine Check the course's website for news about this.

Practicalities

Software requirement

Mandatory For next session every machine should at least have

- Python > 3.8 : if possible, use the Anaconda distribution
- · A dedicated **Python environment**
 - 1. `\$pip install -r requirement.txt` executed
 - 2. **`\$jupyter notebook`** running in your default browser

Advised

- Python IDE: VSCode or PyCharm Community (free)
- Git (not covered during this course)

Who is familiar with Python programming? (not necessarily Machine Learning)

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Today's program Python syntax, data structure and types

Basics of Python

High-level (like R or Matlab), *i.e.* not a compiled language (C/C++) Question: good or bad ?

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Versatile not dedicated to statistics/machine learning but many scientific libraries

- Numpy (matrix)
- Pandas (data manipulation)
- Matplotlib (plotting/visualization)
- · Scikit-learn, tensorflow, pytorch, etc.

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Trendy nowadays

Our first Hello World!

Open some text editor (VSCode/PyCharm are better)

Save a new file as helloworld.py with the following lines

```
# This is a comment
print('Hello World !')
```

Open

- · Windows Conda bash
- · Linux or MacOS bash

Type \$python helloworld.py

The Python interpreter

No magic Python is installed somewhere on your machine \$python --version

You can even have co-existing versions of Python (environments)

- · Pros: flexibility on versions, manage clean project
- \cdot Cons: source of errors! \longrightarrow always know which python you are using!

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Homework

Create an environment named "M2Evry" with Python 3.9 **Hint:** follow this tutorial

Interactive mode

In this course we will alternate between three ways of using Python

1. Command line (Bash \$python -options my_script.py)

Interactive mode

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- 1. Command line (Bash \$python -options my_script.py)
- 2. Python Shell

```
(M2Evry) nicolas@admininrae-Precision-3561:~$ python
Python 3.10.4 (main, Mar 31 2022, 08:41:55) [GCC 7.5.0] on linux
Type "help", "copyright", "credits" or "license" for more information.
>>> x = 2
>>> x+1
3
>>> ■
```

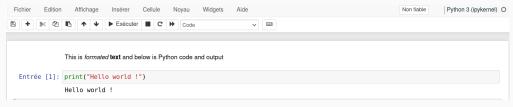
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- 1. Command line (Bash \$python -options my_script.py)
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>>> ■
```

3. Jupyter notebooks: mix of formated text and Python code (\sim Rmarkdown \cdot Rmd)



Frequent types and data

structure

Objects, types and variables

Objects

- Python manipulates objects
- · each object has a type
 - · specify the possible values
 - specify the possible operations
- · example
 - · 1 is an int
 - · 1.3 is a float
 - · "abcd" is a str
 - False is a bool

Variables

- · objects can be named
- a variable is a name for an object
- Affectation = setting/binding a name
 - variable = object
- Names are replaced by the object in expressions
- x = 2
 - 2 * x

Maths

Difference between int and float

```
x = 2
print(type(x))
x_f = 2.0
print(type(x_f))
```

Maths

```
Difference between int and float
```

```
x = 2
print(type(x))
x_f = 2.0
print(type(x_f))
Python knows how to add, multiply, exponentiate
v = 3
print(x)
print(x+y)
print(x*y)
print(x ** y)
```

Maths

print(x*y)
print(x ** y)

Difference between int and float

```
x = 2
print(type(x))
x_f = 2.0
print(type(x_f))

Python knows how to add, multiply, exponentiate
y = 3
print(x)
print(x+y)
```

Question: what is the expected type of 2.0 * 2?

Booleans

```
Three keywords: True, False and not
x = True
y = not x
print(x, y)
print(int(x), int(y))
If... Else statements
if x:
    print("I'm True")
else:
    print("I'm False")
```

Logical conditions

- Equals: a == b
- Not Equals: a != b
- Less than: a < b
- Less than or equal to: a <= b
- Greater than: a > b
- Greater than or equal to: a >= b

Output is a float

Exercise

Write a program that prints the maximum of two floats a and b

Lists

Lists are collection of objects with different types \longrightarrow **ubiquitous** in Python

```
l = [1, 2.3, 'a']
print(l)
print(type(l)) # a list
print(len(l)) # number of elts
print(l[0]) # first elt
```

Indexation starts at 0 !!

```
# Some really un-pythonic way to browse a list...
for i in range(len(l)):
    print(i, l[i])
```

Lists (cont'd)

- [content] is the litteral value, and [] is the empty list
- n=len(1) is the length, indexes vary in $0, \ldots, n-1$
- \cdot l[-i] access the *i*-th element starting from the **end**
- Lists are iterable objects

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- · Lists are iterable objects

```
# only run through elements
for element in l:
    print(element)
```

```
# keep the index information
for idx, elt in enumerate(l):
    print(idx, elt)
```

Lists (cont'd)

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# only run through elements
for element in l:
    print(element)
```

```
# keep the index information
for idx, elt in enumerate(l):
    print(idx, elt)
```

Exercise

```
Let l = [-1, 3, -2.3, 7.6, 0.6]. Write a program creating a list with
```

- 1. the non-negative values of l
- 2. their indexes

Hint: Use the append() method \rightarrow -clist.append(<something</pre>)

Lists (cont'd 2)

Lists are objects² in Python \longrightarrow several *methods* exists

- append(x) create a slot at the end of the list and add x.
- \cdot insert(i, x) insert x at position i
- \cdot pop(i) delete the *i*-th element and returns it.
- count(x) number of occurences of x in the list.
- reverse() reverse the order of elements.
- extend(12) add 12 in the end of the calling list
- And more...

²Python use a dot to link objects and methods: **object.method()**

Lists (cont'd 2)

Lists are objects² in Python \longrightarrow several *methods* exists

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- pop(i) delete the *i*-th element and returns it.
- · count(x) number of occurences of x in the list.
- reverse() reverse the order of elements.
- extend(l2) add l2 in the end of the calling list
- And more...

Exercise

Reverse the order of element of l without using l.reverse()

²Python use a dot to link objects and methods: **object.method()**

Slices

Some Python objects, including lists, can be indexed with [] and sliced with:

- numbering always starts at 0
- negative ordering \leftrightarrow reverse ordering
- · l[i:j]
 - 1. from i to j-1
 - 2. missing i means a start at 0
 - missing j means an end at len(l)-1

```
l[:3]  # compare to l[0:3]
l[2:len(l)] # compare to l[2:len(l)]
l[2:4]
```

Comprehension

List comprehension is the combination of **for** loop with **list** syntax

- · great way to make your code more *Pythonic*
- · apply to other data structure such as dictionaries (cf. later)

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General syntax: [expression for variable in iterable]

The three following lines are thus equivalent

```
l = [-2, -1, 0, 1, 2]
l = [elt for elt in range(-2, 3)]
l = list(range(-2, 3))
```

```
pos_l = [x for x in l if x > 0] # you can even add conditions !
```

Comprehension

List comprehension is the combination of **for** loop with **list** syntax

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```

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pos_l = [x for x in l if x > 0] # you can even add conditions!
```

Exercise

Use list comprehension to return the index of positive elements in 1 Hint: enumerate returns an iterable

Nested comprehension

```
We can chain for inside list comprehension ←→ nested for loops
Example:
l = [i + j for i in range(3) for j in [2,5,10]]
is equivalent to
l = []
for i in range(3):
    for j in [2, 5, 10]:
        l.append(i+j)
```

Nested comprehension

```
We can chain for inside list comprehension \longleftrightarrow nested for loops Example:

l = [i + j for i in range(3) for j in [2,5,10]] is equivalent to
```

Exercise

Rewrite as nested loops

```
\cdot [x - y for x in range(4) for y in range(x + 2) if x != y]
```

```
\cdot [[x / 2 for x in range(y)] for y in range(2, 5)]
```

Be careful: references & copies

In Python variable = object, remember?

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However, Python manipulates object by reference

- The content of the variable is the **adress** of the object in memory
- It's like an ID or a phone number!

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```
In Python variable = object, remember?
```

However, Python manipulates object by reference

- The content of the variable is the **adress** of the object in memory
- It's like an ID or a phone number!

Warning: it's a VERY frequent type of mistakes

Workaround: use 12 = 11.copy() to create a new list

Strings

```
Litteral: s = "A String" or p = "another string" / Type is str(string)
Strings are iterable and behave like lists
```

Lots of methods for str

- upper() upper cases whole string: 'Help!'.upper()
- · lower() upper cases whole string: 'Help!'.lower()
- · Many more...

Comprehension [char for char in s+p if char.isupper()]

Exercise

```
Create a sub-string only only from alphabet letter of s="No57$9i74s0:!y"
Hint: Use ''.join(list) and .isalpha()
```

Dictionaries

Dictionaries are basically lists indexed by a **key**

```
d = {'mykey': 1, 'foo': 2.3, 'bar': 'a'} # dict
Try d[0], what happens?
```

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```
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Important: dictionaries are indexed keys not integers: d['bar']

Built-in methods returning an iterable

- Keys: d.keys()
- Values: d.values()
- Both: d.items()

Exercise

Write a program that prints the keys and values of a dictionary.

Dict comprehension

```
for key, val in d.items():
    print(d[key] == val)

General syntax: {key:expression for variable in iterable}

The two following lines are thus equivalent

d = {'1':0, '2':1, '3':2}
 d = {str(i+1):i for i in range(3)}

d2 = {key:val for key, val in d.items() if val >=1} # conditions
```

Dict comprehension

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for key, val in d.items():
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General syntax: {key:expression for variable in iterable}
The two following lines are thus equivalent
d = \{'1':0, '2':1, '3':2\}
d = \{str(i+1): i \text{ for } i \text{ in } range(3)\}
d2 = {key:val for key, val in d.items() if val >=1} # conditions
```

Exercise

```
Let d = {str(i+1):i/2 for i in range(10)}.
Use list comprehension to create a new dict with only integer values of d
Hint: Use isinstance(val, int) to test if val is an int
```

Tuples are non-modifiable lists

```
t = (1, 2.3, 'a') # tuple
Try t[0] = 2, what happens?
```

Important: tuples are immutable, they cannot me modified.

Tuples are non-modifiable lists

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Packing & unpacking: the Pythonic way

$$x, y, z = t$$
 # unpacking $x, y, z = 1, 2.3, 'a'$ # together

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Packing & unpacking: the Pythonic way

Quizz: we have already seen unpacking, can you guess when?

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Packing & unpacking: the Pythonic way

Quizz: we have already seen unpacking, can you guess when ?
for i, val in enumerate(l): returns an iterable on tuples (idx, value)
Each iteration there is an unpacking: i, val = idx, value

Again: references & copy

Same warning as for lists applies for dict

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Same warning as for lists applies for dict

```
d = {'a':2, 'b':'astring'}
d2 = d
d2['a'] = 'modified!'
print(d)
```

Workaround: use d.copy()

Functions

A first example

A function allows

- to manipulate objects with more than operators +, *, etc.
- to organize our program in small, simple blocks
- to reduce code repetition

Example: parity of an integer (modulo operator in python %)

```
def is_even(x):
    val = False
    if x%2==0:
        val = True
    return val
is_even(2) # returns True
is_even(3) # returns False
```

```
def my function(argt_1, ..., argt_n):
    0.00
    This is a Python docstring: a long comment used to
    document functions.
    . . .
    instructions 1
    instructions m
    return something
val = my function(argt 1= δ,..., argt n= δ) # a function call
Important keywords
  • def: initiate a function definition
```

• return: ends the function and define its value

Scope (1)

Python code is organized in blocks an sub-blocks, defining scope

```
def func():
    # this is the function body, z only exists here (locally)
    z = 2
    print(x + z)

x = 2 #    x exists globally
func()
```

In this example there are two types of scope

- **global** scope: contains all the names defined in the top level Hence, x is available everywhere in the script, even if not passed as an argument.
- local scope: contains the names defined inside the function only
 Hence, z is only available inside func() block. Try print(z) outside of func()?

Variables can be redefined in the local scope.

 \implies we can use the same name for different variable in *global* and *local* scopes.

```
def func(x):
    z = 2
    print(x + z)

x = 2
func(3)
print(x)
```

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Unrolling what happens here

1. Variables **x** and **func** are created in the global scope

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- 6. We get outside the function, local scope is erased.

```
def func(x):
    z = 2
    print(x + z)

x = 2
func(3)
```

print(x)

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 \implies we can use the same name for different variable in *global* and *local* scopes.

def func(x): z = 2 print(x + z) x = 2 func(3) print(x)

- 1. Variables **x** and **func** are created in the global scope
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- 4. The local **x** wins over the global one
- 5. The body of func is executed with x = 3
- 6. We get outside the function, local scope is erased.
- print(x) uses the global x since it is the only one existing.

Function value

The return any value can be

- · Nothing: **return None** or no return
- · Numerical, string, list
- · Another function
- Basically any object

```
def exponentiate(n):
    def power(x):
        return x**n
    return power
x = 2
power_2 = exponentiate(2)
power_2(x)
[exponentiate(n)(x) for n in range(10)]
```

Lambda functions

Python onliner for short, simple functions \longrightarrow avoid using $\operatorname{\textbf{def}}$

The created function has no name (anonymous)

```
def anonymous_func(x):
    f = lambda x: x**2
    f(2)
    f(3)
    f(3)
    def anonymous_func(x):
        return x**2
    f = anonymous_func
    f(2)
    f(3)
```

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    f(2)
    f(3)
    f(3)
    def anonymous_func(x):
        return x**2
    f = anonymous_func
    f(2)
    f(3)
```

Exercise

Rewrite the exponentiate function from previous slide using lambda

Default argument & function calls option

```
Some argument may be set to default values \longrightarrow ease the use Used everywhere in built-in functions, e.g. list.sort(reverse=True) Syntax: def f(a, b=2): return a + b f(1) f(1,3)
```

Default argument & function calls option

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```

Syntax:

```
def f(a, b=2):
    return a + b

f(1)
f(1,3)
```

Possible ways of calling:

- 1. Positional arguments: $f(1, 3) \longrightarrow Python$ assign according to order
- 2. Keywords arguments: $f(b=3, a=1) \rightarrow Python assign by their names$
- 3. Positional then named: f(1, b=3)

Named then positional is not possible, e.g. f(a=1, 2) returns an error!

Function as argument

```
Functions are objects, e.g. f = lambda x : x+1 and print(type(f))
Thus, g=f and g(1) returns 2
Why? Same reason as for list, etc. f (and g) only store the reference toward the function
Ok... But why is it interesting? Well, because f can be passed as an argument to another
function
def filter negative(f, l):
     return [x for x in l if f(x) < 0]
filter negative(f, range(-4, 5))
The functools module implements some utilities based on this mechanism
```

· map(f, ite) - Apply f to every item of iter and return a list of the results.

from functools import map, filter

• filter(f, ite) - Construct a list from elements of ite for which f returns true.

Some exercises

Exercise 1 (easy)

Try to re-implement the function map(f, ite)

Exercise 2 (intermediary)

Let l be a list, sort l according to the values of the **square** of its elements.

E.g.: if l=list(range(-2, 3)), the program should return [0, -1, 1, -2, 2]

Hint: Use the key argument of l.sort(key=f) for some function f you should write.

Exercise 3 (difficult)

Search on the web for reduce() of the functools module Using only two lines, write $sum_int(n)$ that computes the sum of the n first integers $\sum_{i=0}^{n} i$ without using the formula n(n+1)/2

Modules

Extending Python

So far, Python seems cool but...

What if i ask you to

- randomly generate items between 0 and 1?
- compute AB for two conform matrices A and B?
- compute descriptive statistics (mean, sd, etc.) for a given dataset?

Extending Python

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What if i ask you to

- randomly generate items between 0 and 1?
- compute AB for two conform matrices A and B?
- · compute descriptive statistics (mean, sd, etc.) for a given dataset ?

Luckily, smart people have implemented these things in Python modules

A module need to be **imported** to access its names

- 1. import module gives access to module.name
- 2. import module as mod: gives alias bla, so we access via mod.name

Objects

A first example

In Python, almost anything is an *object* with a *class*. We can create classes.

```
class Animal:
    """Class names are CamelCase by convention."""
   def __init__(self, type, name):
        self.name = name
        self.type = type
   def present(self):
        print(self.name, "is a", self.type)
    foo = Animal("dog", "medor")
    foo.present()
    print(foo.type, foo.name)
```

Object oriented programming in Python

A class can have

- attributes any object: str, int, list, anything
 Access via object.attribute, e.g. foo.type
- methods e.g. functions for object
 Call via object.method(a_1, ..., a_n), e.g. foo.present()

Special keywords & methods:

- self reference to the object itself must be used as an argument to a method (default first argument)
- def __init__(self, ...): the constructor, it tells Python how to create an object of the class.

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 Call via object.method(a_1, ..., a_n), e.g. foo.present()

Special keywords & methods:

- self reference to the object itself must be used as an argument to a method (default first argument)
- def __init__(self, ...): the constructor, it tells Python how to create an object of the class.

Exercise

Create a class 2DPoint that represent a point in $(x, y) \in \mathbb{R}^2$ with x and y coordinates. This class will have a method distance() that computes the distance to the origin.

```
class Parrot(Animal):
    """Class names are CamelCase by convention."""
   def init (self, name, message):
       # super() is a special function to call constructor from
       # the mother class Animal
       super(). init (type='Bird', name=name)
       self.message = message
   def repeat(self):
       print(self.name, "(a " + self.type + "):", self.message)
coco = Parrot("coco", "#!@%*") # an object of class Parrot
coco.repeat() # call the method repeat()
coco.present() # the method present is inherited
```

In-place modification

Warning: be careful with attribute (passed by reference) class ListModifier(): def init (self, l): self.l = 1def append(self, x): self.l.append(x)l = [0, 1]obj = ListModifier(l) obj.append("a") print(obj.l) # atribute is modified print(l) # l was also modified !

Exercises

Exercise 1

Create the **Vector** class that has

- as attribute the list of coordinate of a vector $x \in \mathbb{R}^n$.
- a method **norm** that compute and returns the euclidean norm of the vector. Hint: use the function sum

Exercise 2

Create the classe ValueTable which has

- · attributes: a function f of one argument, a minimum and maximum values min & max.
- a method compute(step) that computes the list of tuples (x, f(x)) for x ranging between min and max with steps of size step. The list must be stored in an attribute table.

Exercises (cont'd)

Exercise 3

Create the Model class that has

- · attributes:
 - · name the name of the model
 - · dtype the input data type (binary, discrete, continuous)
 - · ddim the dimension of input data
 - pdim the dimension of parameter space
 - · llhood the likelihood function
- a method describe() that prints a description of the model.

Exercise (cont'd)

Exercise 4 (inheritance)

Create the class Bernoulli inheriting from Model and store the following model

$$p \in [0, 1], x_i \in \{0, 1\}, \quad x_i \sim \mathcal{B}(p),$$

$$L(x_1, \dots, x_n; p) = \sum_{i=1}^n x_i \log p + (1 - x_i) \log(1 - p)$$
(1)

Create the $ml_est(x)$ method that takes as input a list of n binary observations and returns the max-likelihood estimate $\hat{p} = \sum_i x_i/n$

References & useful ressources

Fabrice Rossi teaching materials on his website https://apiacoa.org/teaching/python/index.fr.html

Stackoverflow Q&A forum: https://stackoverflow.com/

Fun-mooc courses:

- Python programming https://www.fun-mooc.fr/fr/cours/apprendre-a-coder-avec-python/
- ML with scikit-learn https://www.fun-mooc.fr/fr/cours/machine-learning-python-scikit-learn/