# Numpy & Matplotlib

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This exercise sheet gets you accointed with NumPy and Matplotlib modules.

## 1 NumPy

## Lecture notes

First, take a look at the NumPy warmup notebook on the website.

From the notebook, we now that NumPy is an implementation of arrays in Python (vector, matrices, tensor). It comes with many built-in methods functions for the np.array type. It also allows for random number generation via the np.random submodule and linear algebra via the cousin scipy module.

## 1.1 Some basics

## Question 1 (Operations)

Compute

- 1. the sum of all elements of x and A using the dedicated method.
- 2. the row-wise and column-wise sum of elements of A.
- 3. the product Ax. What is the expected shape?

### Question 2 (Array creation)

Create an array with

- 1. integers from 0 to 9
- 2. a linearly spaced sequence of the following 13 floats between 0 and  $2\pi$ :  $\{0, \pi/6, \pi/3, ..., 2\pi\} = \{k\pi/6, k = 0, ..., 12\}$
- 3. A  $5 \times 5$  diagonal matrix with only 23 on its diagonal.

### Question 3 (Indexing & slicing)

Create

```
X = np.arange(100).reshape(50, 2)
Use slicing: to get
```

- 1. the whole second column of X & the whole 5th of X
- 2. The first 7 rows
- 3. The rows from 3rd to 7th (included)
- 4. The last 5 rows
- 5. One every 3 rows of X starting from the second one

#### Use boolean indexing to

- 1. get the elements of X greater or equal to 30.
- 2. get the elements of X in [25, 45]
- 3. fill C = np.zeros((5, 5)) of 1 on every two rows and one every two columns (une colonne sur deux et une ligne sur deux).

```
[[1. 0. 1. 0. 1.]
[0. 0. 0. 0. 0.]
[1. 0. 1. 0. 1.]
[0. 0. 0. 0. 0.]
[1. 0. 1. 0. 1.]]
```

## Question 4 (Random number generation)

Create a NUmPy random number generator with seed set to 42. Then, draw

- 1. 100 samples from a  $\mathcal{N}(-3,2)$
- 2. 50 samples uniformly from the list ['a', 'b', 'c']
- 3. a  $85 \times 5$  matrix of samples from  $\mathcal{U}([-3.5, 6e^2])$
- 4. a  $42 \times 3$  matrix of samples from a Poisson  $\mathcal{P}(3)$

### Question 5 (Universal function (ufunc))

Compute

```
1. \sin(x_i) for x \in \{0, \pi/6, \pi/3, ..., 2\pi\}
2. \exp(-x^2) for x \in \{-4, -3, ..., 3, 4\}
```

3.  $c_i = \tan(a_i) \times b_i - a_i^{b_i}$  with a = rng.random(100) and b = rng.random(100)

## Lecture notes

NumPy has built-in function and methods that operates on arrays. For example, the np.min() and np.max() function return the maximum element of an array. In addition, the np.argmin() and np.argmax() return the indice(s) of the minimum (resp. maximum) element of the array.

They have an argument axis that allow to specify the axis among which the min (resp. max) should be computed.

## Question 6 (Advanced operations)

Let

```
a = rng.random(size=(100,))
target = 0.23
```

- 1. find the maximum element of a
- 2. find the closest value to target in array a. What if a is 2-D? e.g. a = rng.random(size=(100,10)). Hint: look at the np.unravel\_index function documentation.

- 3. when a is 2-D, find the maximum for each column and the maximum for each row.
- 4. Read the documentation of np.unique() and its arguments. Then, count the number of unique elements in x = rng.choice(np.arange(10), size = 100).

#### Lecture notes

The SciPy module is built for NumPy arrays. It is organized in many submodules for signal processing, statistics, etc. Its scipy.linalg submodule provides advanced linear algebra tools such as norm computations (possibly with axis specification) and eigen decomposition.

```
import scipy.linalg as spla
help(spla.norm)
help(spla.eig)
help(spla.inv)
```

## Question 7 (Linear algebra)

```
Let X = rng.random(shape=(20, 5))
```

- 1. compute the two symmetric matrices  $A = XX^{\top}$  and  $B = X^{\top}X$
- 2. check that the euclidean norms of A and B (seen a vectors in  $\mathbb{R}^{100}$ ) are equal
- 3. compute the row-wise  $l_1$  norm of A
- 4. get P and D from the eigen decomposition of  $A = PDP^{-1}$
- 5. compute  $P^{-1}$
- 6. use np.allclose to check if  $PDP^{-1}$  is equal (up to a  $10^{-7}$  absolute tolerance) to A
- 7. use np.isclose to extract the non-zero eigenvalues of A.
- 8. check that the non-zero eigenvalues of A and B are the same
- 9. check that the sum of eigenvalues of A (or B) is (up to a  $10^{-7}$  absolute tolerance) equal to the sum of the diagonal element of A (or B).

## Lecture notes

NumPy uses array broadcasting to simplify operation on arrays like X + 1 or x \* y. In order to work, shapes must match and the operation is done element by element. Otherwise, NumPy will automatically try to detect in which way the operation can be done by extending the shape of the smaller array. We say that the smaller array is broadcast across the bigger array.

For example the following code tries to normalize the row of X by its rowsum. It will return a broadcasting error.

```
X = rng.random(size=(20, 5)
X = X / X.sum(axis=1) # return a broadcasting error
```

Indeed, the shape (20, 5) and shape (20,) are not compatible. The shape must be (20, 1) to be extended. In this example it can be achieved vie the keepdims arguments or the np.newaxis trick to created a new "dimension" for our 1D array

```
X = rng.random(size=(20, 5))

X = X / X.sum(axis=1, keepdims=True) # the column dimension is preserved with keepdims <math>X = X / X.sum(axis=1)[:, np.newaxis] # equivalent
```

## Question 8 (Broadcasting)

Let X be as before

```
X = rng.random(size=(20, 5))
```

Use array broadcasting to

- 1. Normalize the rows of X in the sense of euclidean norm. Sanity check :  $diag(XX^{\top}) = I_{20}$  up to an small absolute tolerance.
- 2. Normalize the columns of X in the sense of euclidean norm. Sanity check :  $diag(X^{\top}X) = I_5$  up to an small absolute tolerance.
- 3. multiply column j by j + 1, *i.e.* column 1 by 2, column 2 by 3, etc.
- 4. multiply row i by i + 2, i.e. row 1 by 3, row 2 by 4, etc.

## 2 Matplotlib

#### Lecture notes

The matplotlib.pyplot module provides basic plotting functionalities to draw points, lines with titles.

The basic object is a Figure. We open a new Figure with plt.figure() where we can provide argument such as the size, etc.

```
import matplotlib.pyplot as plt
plt.figure()
plt.plot([1, 3, 4, 6], [2, 3, 5, 1])
plt.scatter([1, 3, 4, 6], np.array([2, 3, 5, 1]) + 1)
plt.show()
```

When a figure is open, matplotlib will draw on it by default. There are several plotting functions such as

- plt.plot() : line plot (draw a line between points)
- plt.scatter(): scatter plot (draw only the points)

Important: However, in order to show the figure in the screen we need to call plt.show().

Note: plt.show() closes the current figure, the latter being "lost". However, figures may be saved with plt.savefig(). It is important to keep them when running script with python my\_script.py in bash or anaconda prompt, otherwise they will be lost.

```
plt.figure()
plt.plot([1, 3, 4, 6], [2, 3, 5, 1])
plt.scatter([1, 3, 4, 6], np.array([2, 3, 5, 1]) + 1)
plt.savefig('my-first-plot.pdf')
```

#### Question 1 (Basic plotting)

Plot  $\sin(t)$  for  $t \in [-2\pi, 2\pi]$  (discretized in 100 linearly spaced points). Add label "t" and " $\sin(t)$ " for x-axis and y-axis. Finally add the title "Sinus function". Save the plot to a file named ' $\sin$ -plot.pdf'. Your plot should look like Figure 1.

### Question 2 (Setting x and y limits)

Change the x and y axis limits to [-8, 10] and [-0.9, 2] respectively.

## Question 3 (Playing with graphical arguments)

Look at the plt.plot documentation or this webpage and try changing the plot to have

- 1. a red, dashed line
- 2. a green, dash-dot line with width 4

## Question 4 (Adding another plot)

On the same plot, add  $\cos(t)$  as a orange scatter plot with x-shaped point markers of size 12.

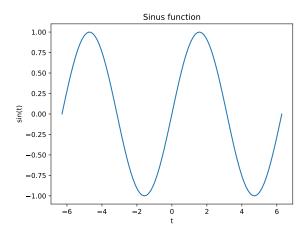


Figure 1: Question 1