Team notebook

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Contents

1 1. Template

1.1 1 template

```
#include <bits/stdc++.h>
using namespace std;

#define pb push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))

template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;
template<class T> using pqg = priority_queue<T>;

using ll = long long;
using ld = long double;
using pi = pair<int, int>;
using pl = pair<ll, ll>;
using ti = tuple<long long, long long, long long>;
using vi = vector<int>;
using vb = vector<bool>;
using vl = vector<ll>;
using vs = vector<string>;
using vvl = vector<vl>;
using vpl = vector<pl>;

const ll INF = INT64_MAX;
const int inf = INT32_MAX;
const ld PI = acos(-1);
const int MOD = 1e9 + 7;
const int DX[4]{1,0,-1,0}, DY[4]{0,1,0,-1};

void init();
```

```
void test_case();

int main() {
    ios::sync_with_stdio(0);
    cin.tie(0);
    cout.tie(0);
    init();
    int T;
    T = 1;
    // cin >> T;
    while (T--) {
        test_case();
    }
    return 0;
}

void init() {

}

void test_case() {

}


// Pablo va por ti
// Efe C
```

1.2 CLIONmain

```
// Practice Every Day :)
#include <bits/stdc++.h>
using namespace std;

#define pb push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sortn(x, n) sort((x), (x) + (n))
#define sq(a) ((a) * (a))
#define MP make_pair
#define each(x, xs) for (auto &x : (xs))
#define rep(i, be, en) for (__typeof(en) i = (be) - ((be) > (en)); i !=
    (en) - ((be) > (en)); i += 1 - 2 * ((be) > (en)))
// old loops
#define FOR(i, a, b) for (int (i) = (a); (i) < (b); (i)++)
#define ROF(i, a, b) for (int (i) = (a); (i) >= (b); (i)--)
#define REP(i, a, b) for (int (i) = (a); (i) <= (b); (i)++)
#define EACH(a, x) for (auto &(a) : (x))

using ll = long long;
using ld = long double;
using pi = pair<int, int>;
using pl = pair<ll, ll>;
using ti = tuple<long long, long long, long long>;
using vi = vector<int>;
using vb = vector<bool>;
using vl = vector<ll>;
using vs = vector<string>;
using vvl = vector<vl>;
using vpl = vector<pl>;
template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;
template<class T> using pqg = priority_queue<T>;

// >>>>>>>>>> debugging >>>>>>>>>>
#ifdef DEBUG_NICO
#include "debug.h"
#define LINE cout << "--------------------" << endl;
#else
#define deb(x...)
#define LINE
#endif
// <<<<<<<<<< debugging <<<<<<<<<<

void cfgIO() {
#ifdef NICOLAS
    freopen("../input.txt", "r", stdin);
    freopen("../output.txt", "w", stdout);
//    freopen("../error.txt", "w", stderr);
#endif
    ios::sync_with_stdio(0);
    cin.tie(0);
    cout.tie(0);
}
// END DEBUG
```

```
void solve();
void init();

int testId = 0;
int main() {
    cfgIO();
    init();
//    int t; cin >> t; while (t--)
//        cout << "Case #" << ++testId << ": ",
    solve(), ++testId;
}
const int N = 1e5 + 10;

void init(){}

void solve() {}
```

1.3 CMakeLists

```
cmake_minimum_required(VERSION 3.22)
project(competitive)

set(CMAKE_CXX_STANDARD 11) # This could different

set(A main.cpp C.cpp) # Add file names here
foreach(X IN LISTS A)
    add_executable("${X}" "${X}")
    target_compile_definitions("${X}" PRIVATE NICOLAS=1) # add ENV_VAR
    target_compile_definitions("${X}" PRIVATE DEBUG_NICO=1)
endforeach()
```

1.4 debug

```
#include <bits/stdc++.h>
using namespace std;

#ifndef DEBUG_H
#define DEBUG_H

void __print(int x)                 {cerr << x;}
void __print(long x)                {cerr << x;}
void __print(long long x)           {cerr << x;}
void __print(unsigned x)            {cerr << x;}
void __print(unsigned long x)       {cerr << x;}
void __print(unsigned long long x) {cerr << x;}
void __print(float x)               {cerr << x;}
void __print(double x)              {cerr << x;}
void __print(long double x)         {cerr << x;}
void __print(char x)                {cerr << '\'' << x << '\'';}
void __print(const char *x)         {cerr << '\"' << x << '\"';}
void __print(const string &x)       {cerr << '\"' << x << '\"';}
void __print(bool x)                {cerr << (x ? "true" : "false");}

template<typename T>
void __print(priority_queue<T> xs)
{cerr << "[ "; while (xs.size()) {__print(xs.top()); xs.pop(); cerr << '
    '; }cerr << ']';}

template<typename T, typename V>
void __print(const pair<T, V> &x)
{__print(x.first); cerr << ':'; __print(x.second);}

template<typename T> // for data structures (vector, set, map, etc)
void __print(const T &xs)
{cerr << "[ "; for (auto &x : xs) {__print(x);cerr << ' ';}cerr << ']';}

void _print()
{cerr << "]" << endl;}

template <typename T, typename... V>
void _print(T t, V... v)
{__print(t); if (sizeof...(v)) cerr << ", "; _print(v...);}

#define deb(x...) cerr << "[" << #x << "] = [", _print(x)

#endif /* DEBUG_H */
```

2 2. math

2.1 Chinease Remainder

```
ll x, y;
/// O(log(max(a, b)))
```

```
ll euclid(ll a, ll b) {
    if(b == 0) { x = 1; y = 0; return a; }
    ll d = euclid(b, a%b);
    ll aux = x;
    x = y;
    y = aux - a/b*y;
    return d;
}

pair<ll, ll> crt(vector<ll> A, vector<ll> M) {
    ll n = A.size(), ans = A[0], lcm = M[0];
    for (int i = 1; i < n; i++) {
        ll d = euclid(lcm, M[i]);
        if ((A[i] - ans) % d) return {-1, -1};
        ll mod = lcm / d * M[i];
        ans = (ans + x * (A[i] - ans) / d % (M[i] / d) * lcm) % mod;
        if (ans < 0) ans += mod;
        lcm = mod;
    }
    return {ans, lcm};
}
```

2.2 Combinatorics

```
// if k == 0 then 1
// if k negative or no enough choices then 0
// O(min(n, n -k)) lineal
ll nck(ll n, ll k) {
    if (k < 0 || n < k) return 0;
    k = min(k, n-k);
    ll ans = 1;
    for (int i = 1; i <= k; i++) {
        ans = ans * (n-i+1) / i;
    }
    return ans;
}
```

2.3 Count$primes$

```
// sprime.count_primes(n);
// O(n^{2/3})
```

```
// PI(n) = Count prime numbers until n inclusive

struct count_primers_struct {
    vector<int> primes;
    vector<int> mnprimes;
    ll ans;
    ll y;
    vector<pair<pair<ll, int>, char>> queries;

    ll count_primes(ll n) {
        // this y is actually n/y
        // also no logarithms, welcome to reality, this y is the best for
            n=10^12 or n=10^13
        y = pow(n, 0.64);
        if (n < 100) y = n;

        // linear sieve
        primes.clear();
        mnprimes.assign(y + 1, -1);
        ans = 0;
        for (int i = 2; i <= y; ++i) {
            if (mnprimes[i] == -1) {
                mnprimes[i] = primes.size();
                primes.push_back(i);
            }
            for (int k = 0; k < primes.size(); ++k) {
                int j = primes[k];
                if (i * j > y) break;
                mnprimes[i * j] = k;
                if (i % j == 0) break;
            }
        }
        if (n < 100) return primes.size();
        ll s = n / y;

        for (int p : primes) {
            if (p > s) break;
            ans++;
        }
        // pi(n / y)
        int ssz = ans;

        // F with two pointers
        int ptr = primes.size() - 1;
        for (int i = ssz; i < primes.size(); ++i) {
```

```
        while (ptr >= i && (ll)primes[i] * primes[ptr] > n)
            --ptr;
        if (ptr < i) break;
        ans -= ptr - i + 1;
    }

    // phi, store all queries
    phi(n, ssz - 1);

    sort(queries.begin(), queries.end());
    int ind = 2;
    int sz = primes.size();

    // the order in fenwick will be reversed, because prefix sum in a
        fenwick is just one query
    fenwick fw(sz);
    for (auto qq : queries) {
        auto na = qq.F;
        auto sign = qq.S;
        auto n = na.F;
        auto a = na.S;
        while (ind <= n)
            fw.add(sz - 1 - mnprimes[ind++], 1);
        ans += (fw.ask(sz - a - 2) + 1) * sign;
    }
    queries.clear();
    return ans - 1;
}

void phi(ll n, int a, int sign = 1) {
    if (n == 0) return;
    if (a == -1) {
        ans += n * sign;
        return;
    }
    if (n <= y) {
        queries.emplace_back(make_pair(n, a), sign);
        return;
    }
    phi(n, a - 1, sign);
    phi(n / primes[a], a - 1, -sign);
}

struct fenwick {
    vector<int> tree;
    int n;

    fenwick(int n = 0) : n(n) {
        tree.assign(n, 0);
    }

    void add(int i, int k) {
        for (; i < n; i = (i | (i + 1)))
            tree[i] += k;
    }

    int ask(int r) {
        int res = 0;
        for (; r >= 0; r = (r & (r + 1)) - 1)
            res += tree[r];
        return res;
    }
};
} ;

count_primers_struct sprime;
```

2.4 Erdős–Szekeres$_{theorem}$

```
Suppose a,b in N, n=ab+1, and x_1, ..., x_n is a sequence of n real
    numbers. Then this sequence contains a monotonic increasing
    (decreasing) subsequence of a+1 terms or a monotonic decreasing
    (increasing) subsequence of b+1 terms. Dilworth's lemma is a
    generalization of this theorem.
```

2.5 Extended Euclides

```
// It finds X and Y in equation:
// a * X + b * Y = gcd(a, b)

int x, y;

int euclid(int a, int b) {
       if (b == 0) {
              x = 1;
              y = 0;
```

```
            return a;
        }
        int aux = x;
        x = y;
        y = aux - a/b*y;
        return euclid(b, a % b);
}
```

2.6 FFT

```
// FFT multiplies polinomial 'a' and 'b' in nlogn

using cd = complex<long double>;
void fft(vector<cd> & a, bool invert) {
    ll n = a.size();

    for (ll i = 1, j = 0; i < n; i++) {
        ll bit = n >> 1;
        for (; j & bit; bit >>= 1)
            j ^= bit;
        j ^= bit;

        if (i < j)
            swap(a[i], a[j]);
    }

    for (ll len = 2; len <= n; len <<= 1) {
        long double ang = 2 * PI / len * (invert ? -1 : 1);
        cd wlen(cos(ang), sin(ang));
        for (ll i = 0; i < n; i += len) {
            cd w(1);
            for (ll j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
    }

    if (invert) {
        for (cd & x : a)
            x /= n;
    }
}

vector<ll> multiply(vector<ll> const& a, vector<ll> const& b) {
    vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
    ll n = 1;
    while (n < a.size() + b.size())
        n <<= 1;
    fa.resize(n);
    fb.resize(n);

    fft(fa, false);
    fft(fb, false);
    for (ll i = 0; i < n; i++)
        fa[i] *= fb[i];
    fft(fa, true);

    vector<ll> result(n);
    for (ll i = 0; i < n; i++)
        result[i] = round(fa[i].real());
    return result;
}
```

2.7 Floor$_{sum}$

```
// from atcoder
// floor_sum(n,m,a,b) = sum{0}to{n-1} [(a*i+b)/m]
// O(log m), mod 2^64, n<2^32, m<2^32

constexpr long long safe_mod(long long x, long long m) {
    x %= m;
    if (x < 0) x += m;
    return x;
}

unsigned long long floor_sum_unsigned(unsigned long long n,
                                      unsigned long long m,
                                      unsigned long long a,
                                      unsigned long long b) {
    unsigned long long ans = 0;
    while (true) {
        if (a >= m) {
```

```
            ans += n * (n - 1) / 2 * (a / m);
            a %= m;
        }
        if (b >= m) {
            ans += n * (b / m);
            b %= m;
        }

        unsigned long long y_max = a * n + b;
        if (y_max < m) break;
        // y_max < m * (n + 1)
        // floor(y_max / m) <= n
        n = (unsigned long long)(y_max / m);
        b = (unsigned long long)(y_max % m);
        swap(m, a);
    }
    return ans;
}

long long floor_sum(long long n, long long m, long long a, long long b) {
    assert(0 <= n && n < (1LL << 32));
    assert(1 <= m && m < (1LL << 32));
    unsigned long long ans = 0;
    if (a < 0) {
        unsigned long long a2 = safe_mod(a, m);
        ans -= 1ULL * n * (n - 1) / 2 * ((a2 - a) / m);
        a = a2;
    }
    if (b < 0) {
        unsigned long long b2 = safe_mod(b, m);
        ans -= 1ULL * n * ((b2 - b) / m);
        b = b2;
    }
    return ans + floor_sum_unsigned(n, m, a, b);
}
```

2.8 Greatest Common Divisor

```
// Alternative: __gcd(a, b);
// O(log(max(a, b)))

ll gcd(ll a, ll b) {
        return b == 0 ? a : gcd(b, a % b);
}
```

2.9 Lowest Common Multiple

```
// O(log(max(a, b)))
int lcm(int a, int b) {
        return a/gcd(a, b) * b;
}
```

2.10 MatrixExponentiation

```
// For Linear recurenses DP in O(log(N)*M^3)

typedef ll T;
const int M = 2;
struct Matrix {
    T a[M][M] = {0};
    Matrix() {}

    Matrix (vector<vector<T>> o) {
        for (int i = 0; i < M; i++)
            for (int j = 0; j < M; j++)
                a[i][j] = o[i][j];
    }

    Matrix operator * (const Matrix &o) {
        Matrix ans;
        for (int i = 0; i < M; i++)
        for (int j = 0; j < M; j++)
        for (int k = 0; k < M; k++)
            ans.a[i][j] += a[i][k] * o.a[k][j]
            //,ans.a[i][j] %= MOD
            ;
        return ans;
    }
};

Matrix matrixPower(Matrix a, ll power) {
    Matrix ans;
    for (int i = 0; i < M; i++) ans.a[i][i] = 1;
```

```
    while (power) {
        if (power & 1) {
            ans = ans * a;
        }

        a = a * a;
        power >>= 1;
    }

    return ans;
}

void test_case() {
    ll n;
    cin >> n;
    Matrix m({
        {1, 1},
        {1, 0}
    });

    auto ans = matrixPower(m, n);
    cout << ans.a[0][1] << "\n";
}
```

2.11 Modular Aritmethics

Modular Aritmethics.cpp

```
ll sum(ll a, ll b) {
    ll c = a + b;
    if (c >= m) c -=m;
    return c;
}

ll sub(ll a, ll b) {
    ll c = a - b;
    if (c < 0) c += m;
    return c;
}

ll mul(__int128 a, __int128 b) {
    return (a * b) % m;
}

ll modexp(ll a, ll n) {
    if (n == 0) return 1;
    ll p = modexp(a, n / 2);
    ll res = mul(p, p);
    if (n & 1) {
        res = mul(res, a);
    }
    return res;
}

// O(sqrt n)
ll phi(ll n) {
    ll ans = n;
    for (int p = 2; p <= n/p; ++p) {
        if (n % p == 0) ans -= ans / p;
        while (n % p == 0) n /= p;
    }
    if (n > 1) ans -= ans / n;
    return ans;
}

ll x, y;
/// O(log(max(a, b)))
ll euclid(ll a, ll b) {
    if(b == 0) { x = 1; y = 0; return a; }
    ll d = euclid(b, a%b);
    ll aux = x;
    x = y;
    y = aux - a/b*y;
    return d;
}

ll invmod(ll a) {
    ll d = euclid(a, m);
    if (d > 1) return -1;
    return (x % m + m) % m;
}

ll divv(ll a, ll b) {
    ll inv = invmod(b);
    if (inv == -1) return -1;
    ll res = mul(a, inv);
    return res;
```

```
}


// a * (b^{euler(m) - 1})
// for primes: a * b ^ (P - 2)
ll divv2(ll a, ll b) {
    if (__gcd(b, m) != 1) return -1;
    ll ex = modexp(b, euler - 1);
    ll res = mul(a, ex);
    return res;
}
```

2.12 Modular Combinatorics

```
// NCK nck(maxN, primeMod)
// ^nC_k How many ways you can choose k items from an array of n items.

struct NCK {
    ll MAX_N;
    ll MOD;
    vl fact;

    explicit NCK(ll maxN, ll mod) : MAX_N(maxN), MOD(mod) {
        fact.resize(MAX_N + 1, 1);
        fact[0] = 1;
        REP(i, 1, MAX_N) {
            fact[i] = fact[i - 1] * (i % MOD);
            fact[i] %= MOD;
        }
    }

    ll inv(ll a){
        return powmod(a, MOD-2); // MOD is prime, otherwise use powmod(a,
             eulerPhi(mod) - 1)
    }

    ll powmod(ll a, ll b){
        if (b == 0) return 1;
        ll mid = powmod(a, b / 2);
        ll ans = (mid * mid) % MOD;
        if (b & 1) {
            ans *= a;
            ans %= MOD;
        }
        return ans;
    }

    ll nCk(ll n, ll k){
        ll nOverK = (fact[n] * inv(fact[k])) % MOD;
        return (nOverK * inv(fact[n-k])) % MOD;
    }
};
```

2.13 Ternary Search

```
// this is for find minimum point in a parabolic
// O(log3(n))
ll left = 0;
ll right = n - 1;
while (left + 3 < right) {
    ll mid1 = left + (right - left) / 3;
    ll mid2 = right - (right - left) / 3;
    if (f(b, lines[mid1]) <= f(b, lines[mid2])) {
        right = mid2;
    } else {
        left = mid1;
    }
}
ll target = -4 * a * c;
ll ans = -1; // find the answer, in this case any works.
for (ll mid = left; mid <= right; mid++) {
    if (f(b, lines[mid]) + target < 0) {
        ans = mid;
    }
}
```

2.14 catalan

```
static int MAX = 30;
static long catalan[] = new long[MAX+1];

static void catalanNumbers(){
        catalan[0] = 1;
        for(int i = 1; i <= MAX; i++){
```

```
            catalan[i] = (long)(catalan[i-1]*((double)(2*((2 * i)-
                1))/(i + 1)));
        }
}
```

2.15 factorization

```
// Polar rho, miller rabin
// O(log^3(n))
// But I get TLE once in 1e7
ll expmod(ll b, ll e, ll m) {
    ll ans = 1;
    while (e) {
        if (e&1) ans = (1ll*ans*b) % m;
        b = (1ll*b*b) % m;
        e /= 2;
    }
    return ans;
}

ll mulmod(ll a, ll b, ll m) {
    ll r = a*b-(ll)((long double)a*b/m+.5)*m;
    return r < 0 ? r+m : r;
}

/// O(log^3(n))
bool test(ll n, int a) {
    if (n == a) return true;
    ll s = 0, d = n-1;
    while (d%2 == 0) s++, d /= 2;
    ll x = expmod(a, d, n);
    if (x == 1 || x+1 == n) return true;
    for (int i = 0; i < s-1; i++) {
        x = mulmod(x, x, n);
        if (x == 1) return false;
        if (x+1 == n) return true;
    }
    return false;
}

ll gcd(ll a, ll b) { return a ? gcd(b%a, a) : b; }

ll rho(ll n) {
    if (!(n&1)) return 2;
    ll x = 2, y = 2, d = 1;
    ll c = rand() % n + 1;
    while (d == 1) {
        x = (mulmod(x, x, n) + c) % n;
        y = (mulmod(y, y, n) + c) % n;
        y = (mulmod(y, y, n) + c) % n;
        d = gcd(abs(x-y), n);
    }
    return d == n ? rho(n) : d;
}

bool is_prime(ll n) {
    if (n == 1) return false;
    int ar[] = {2,3,5,7,11,13,17,19,23};
    for (auto &p : ar) if (!test(n, p)) return false;
    return true;
}

/// O(log(n)^3) aprox
void fact(ll n, map<ll, int> &f) {
    if (n == 1) return;
    if (is_prime(n)) { f[n]++; return; }
    ll q = rho(n);
    fact(q, f); fact(n/q, f);
}

// ###############################################################
// Normal algorithm with precomputing primes
// O(sqrt(MAX_N)/log(sqrt(MAX_N)), it worked for 1e9 for me
const ll MAX_N = 1e7;
vl primes;
void init() {
    ll N = sqrt(MAX_N) + 1;
    vector<bool> sieve(N + 1);
    for (ll i = 2; i <= N; i++) {
        if (!sieve[i]) {
            for (ll j = i*i; j <= N; j+=i) {
                sieve[j] = true;
            }
        }
    }
    for (ll i = 2; i <= N; i++) {
        if (!sieve[i]) primes.pb(i);
    }
```

```
}

vl fact(ll n) {
    vl ans;
    ll rest = n;
    for (auto &p : primes) {
        if (p * p > n) break;
        if (rest % p == 0) {
            ans.pb(p);
            while (rest % p == 0) rest/=p;
        }
    }
    if (rest != 1) {
        ans.pb(rest);
    }
    return ans;
}

// ###################################################
// Modification of sieve erathostenes
// From CF Faster than previous, but needs more memory
const int N = int(1e7) + 5;
int mind[N];
void init() {
    for (int i = 0; i < N; i++)
                mind[i] = i;

        for (int p = 2; p < N; p++) {
                if (mind[p] != p)
                        continue;
                for (int d = 2 * p; d < N; d += p)
                        mind[d] = min(mind[d], p);
        }
}

vector<int> getPrimes(int v) {
        vector<int> ps;
        while (v > 1) {
                if (ps.empty() || ps.back() != mind[v])
                        ps.push_back(mind[v]);
                v /= mind[v];
        }
        return ps;
}
```

2.16 fermat

```
// ll fermatFactors(ll n) {
//     ll a = ceil(sqrt(n)) ;
//     if(a * a == n){
//         return a;
//     }
//     ll b;
//     while(true) {
//         ll b1 = a * a - n ;
//         b = (ll)sqrt(b1) ;

//         if(b * b == b1)
//             break;
//         else
//             a += 1;
//     }
//     return min(a - b, a + b);
// }
```

2.17 fraction$_{m}odular$

```
const ll MOD = 998244353;

struct frac : public pair<ll, ll> {
    using pair<ll, ll>::pair;

    frac simplify() {
        if (first == 0) {
            return frac(0, 1);
        }
        ll gcd_val = __gcd(first, second);
        return frac(first / gcd_val, second / gcd_val);
    }

    frac operator*(const frac &other) {
        // a * invmod(b) = a / b
        // a * invmod(b) * a2 * invmod(b2) = (a * a2) / (b * b2)
        return frac((first * other.first) % MOD , (second * other.second)
            % MOD ).simplify();
    }

    frac operator+(const frac &other) {
```

```
        // opertaor + with module
        // a * invmod(b) + a2 * invmod(b2) = (a * b2 + a2 * b) / (b * b2)
        ll up = (first * other.second) % MOD + (other.first * second) %
            MOD;
        ll down = (second * other.second) % MOD;
        // TODO: check if simplify should be here
        return frac(up, down).simplify();
    }
};

// Expected Value is the sum of all the possible values multiplied by
    their probability
// Geometrica is reversed.
```

2.18 primes

```
// O(sqrt(n))
bool isPrime(int x) {
    for (int d = 2; d * d <= x; d++) {
        if (x % d == 0)
            return false;
    }
    return true;
}

// O(nloglogn)
// sieve[X] == 0 if it is prime
int const N = 1e6;
bool sieve[N + 1];
vector<int> primes;

void calculate() {
    for (int p = 2; p <= N; p++) {
        if (sieve[p]) continue;
        primes.PB(p);
        for (ll i = 1ll*p*p; i <= N; i += p)
            sieve[i] = true;
    }
}


// For 64-bit integers
// O((ln n)^2)
// 32 bits bases: 2, 3, 5, 7.
// 64 bits bases: 2 ... 37

using u64 = uint64_t;
using u128 = __uint128_t;

u64 binpower(u64 base, u64 e, u64 mod) {
    u64 result = 1;
    base %= mod;
    while (e) {
        if (e & 1)
            result = (u128)result * base % mod;
        base = (u128)base * base % mod;
        e >>= 1;
    }
    return result;
}

bool check_composite(u64 n, u64 a, u64 d, int s) {
    u64 x = binpower(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (int r = 1; r < s; r++) {
        x = (u128)x * x % n;
        if (x == n - 1)
            return false;
    }
    return true;
}

bool MillerRabin(u64 n) {
    if (n < 2)
        return false;

    int r = 0;
    u64 d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        r++;
    }

    for (int a : {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}) {
        if (n == a)
            return true;
        if (check_composite(n, a, d, r))
```

```
            return false;
    }
    return true;
}
```

2.19 triple$_m odular_e xp$

```
// calcula a^b^c % MOD

ll pou(ll a, ll b, ll m) {
    ll ans = 1;
    while (b) {
        if (b&1) ans *= a, ans%=m;
        a*=a;
        a%=m;
        b/=2;
    }
    return ans;
}

void test_case() {
    ll a, b, c;
    cin >> a >> b >> c;
    // fermat theorem
    // a^(p-1) = 1 (mod p)
    b = pou(b, c, MOD - 1);
    a = pou(a, b, MOD);

    cout << a << "\n";
}
```

3 3. graph

3.1 1 - DFS

```
const int n = 1e6;
vector<int> adj[n + 1];
bool visited[n + 1];

void dfs(int x) {
        if (visited[x]) return;
        visited[x] = true;
        for (int &a : adj[x]) {
                dfs(x);
        }
}
```

3.2 2 - BFS

```
2. BFS

vector<int> adj[n + 1];
bool visited[n + 1];

void bfs() {
        queue<int> q;
        q.push(0); // initial node
        visited[0] = true;
        while(q.size() > 0) {
                int c = q.front();
                q.pop();
                for (int a : adj[c]) {
                        if (visited[a]) continue;
                        q.push(a);
                        visited[a] = true;
                }
        }
}
```

3.3 3 - Dijkstra

```
3. Dijkstra

const int inf = 1e9;
vector<pair<int, int>> adj[n];
bool processed[n];
ll distance[n];

void dijkstra() {
        priority_queue<pair<int, int>> q;
        for (int i = 0; i < n; i++) {
```

```
            distance[i] = inf;
        }
        distance[start] = 0;
        q.push({0, start});
        while (q.size() > 0) {
            int c = q.top().second;
            q.pop();
            if (processed[c]) continue;
            processed[c] = true;
            for (auto& a : adj[c]) {
                int u = a.first;
                int w = a.second;
                if (distance[c] + w < distance[u]) {
                    distance[u] = distance[c] + w;
                    q.push({-distance[u], u});
                }
            }
        }
}
```

3.4 4 - BellmanFord

```
4. BellmanFord

const int inf = 1e9;
vector<tuple<int, int, int>> edges;
ll distance[n];


void bellmanFord() {
    for (int i = 0; i < n; i++) {
        distance[i] = inf;
    }
    distance[start] = 0;
    for (int i = 0; i < n - 1; i++) {
        //bool changed = false; add one iteration (i < n) to
            valide negative cicles
        for (auto& edge : edges) {
            int a, b, w;
            tie(a, b, w) = edge;
            if (distance[a] + w < distance[b]) {
                distance[b] = distance[a] + w;
                //changed = true;
            }
        }
    }
}
```

3.5 5 - Floyd Warshall

```
5. Floyd Warshall

const int inf = 1e9;
vector<pair<int, int>> adj[n];
ll distance[n][n];

void floydWarshall() {
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            distance[i][j] = inf;
        }
    }
    for (int i = 0; i < n; i++) {
        for (auto p : adj[i]) {
            int b = p.first;
            int w = p.second;
            distance[i][b] = w;
        }
    }
    for (int k = 0; k < n; k++) {
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                distance[i][j] = min(distance[i][j],
                    distance[i][k] + distance[k][j]);
            }
        }
    }
}
```

3.6 6 - Euler Path and Cycle

```
6. Euler Path and Cycle

// TODO
```

3.7 7 - Topological Sort

```
7. Topological Sort

stack<int> topo;
vector<int> adj[n + 1];
bool visited[n + 1];

void dfs(int x) {
	if (visited[x]) return;
	visited[x] = true;
	for (int a : adj[x]) {
		dfs(a);
	}
	topo.push(x);
}
```

3.8 8 - Transitive Closure

```
8. Transitive Closure

const int inf = 1e9;
vector<int> adj[n];
ll distance[n][n];

void floydWarshall() {
	for (int i = 0; i < n; i++) {
		for (int j = 0; j < n; j++) {
			distance[i][j] = false;
		}
	}
	for (int i = 0; i < n; i++) {
		for (int b : adj[i]) {
			distance[i][b] = true;
		}
	}
	for (int k = 0; k < n; k++) {
		for (int i = 0; i < n; i++) {
			for (int j = 0; j < n; j++) {
				distance[i][j] |= distance[i][k] &
				    distance[k][j];
			}
		}
	}
}
```

3.9 9 - Kruskal

```
// 9. Kruskal
// Finds the max/min spanning tree of an undirected graph
// provide the undirected edges with its costs vector<{cost(a, b), a, b}>
// and the size

struct union_find {
    vl p;
    union_find(int n) : p(n,-1) {}

    ll find(ll x) {
        if (p[x] == -1) return x;
        return p[x] = find(p[x]);
    }

    bool group(ll a, ll b) {
        a = find(a);
        b = find(b);
        if (a == b) return false;
        p[a] = b;
        return true;
    }
};

ll kruskal(vector<tuple<ll,ll,ll>> &edges, ll nodes) {
    union_find uf(nodes+1);
    sort(all(edges));
    reverse(all(edges)); // for max
    ll answer = 0;
    for (auto edge : edges) {
        ll cost, a, b;
        tie(cost, a, b) = edge;
        if (uf.group(a, b))
            answer += cost;
    }
    return answer;
}
```

3.10 A - Union Find

10. Union Find

```
struct union_find {
    vi link;
    vi score;
    vi size;
    int n;
    void init(int nn) {
        link.resize(nn);
        score.resize(nn);
        size.resize(nn);
        this->n = nn;
        for (int i = 0; i < n; i++) {
            link[i] = i;
            score[i] = 0;
            size[i] = 1;
        }
    }
    int find(int x) {
        if (link[x] == x) return x;
        return (link[x] = find(link[x]));
    }
    void group(int a, int b) {
        int pa = find(a);
        int pb = find(b);
        if (pa != pb) {
            if (score[pa] >= score[pb]) {
                link[pb] = pa;
                size[pa] += size[pb];
                if (score[pa] == score[pb]) score[pa]++;
            } else {
                link[pa] = pb;
                size[pb] += size[pa];
            }
        }
    }
};
```

3.11 B - SCC

Dado un grafo dirigido halla las componentes fuertemente conexas (SCC).

```
const int inf = 1e9;
const int MX = 1e5+5; //Cantidad maxima de nodos
vector<int> g[MX]; //Lista de adyacencia
stack<int> st;
int low[MX], pre[MX], cnt;
int comp[MX]; //Almacena la componente a la que pertenece cada nodo
int SCC; //Cantidad de componentes fuertemente conexas
int n, m; //Cantidad de nodos y aristas

void tarjan(int u) {
    low[u] = pre[u] = cnt++;
    st.push(u);

    for (auto &v : g[u]) {
        if (pre[v] == -1) tarjan(v);
        low[u] = min(low[u], low[v]);
    }
    if (low[u] == pre[u]) {
        while (true) {
            int v = st.top(); st.pop();
            low[v] = inf;
            comp[v] = SCC;
            if (u == v) break;
        }
        SCC++;
    }
}

void init() {
    cnt = SCC = 0;
    for (int i = 0; i <= n; i++) {
        g[i].clear();
        pre[i] = -1; //no visitado
    }
}

// example
void test_case() {
    cin >> n >> m;
    init();
    rep(i, 0, m) {
        int x, y;
        cin >> x >> y;
        g[x].pb(y);
```

```
    }
    rep(i, 1, n + 1) {
        if (pre[i] == -1) {
            tarjan(i);
        }
    }
}
```

3.12 C-Cycle$_{D}$etection

```
const int N = 1e5 + 10;
vpl adj[N];
int vis[N];
vpl res;
vpl edge;

void dfs(int x) {
    if (vis[x] == 2) return;
    vis[x] = 1;
    each(z, adj[x]) {
        int y, i;
        tie(y, i) = z;
        if (vis[y] == 1) {
            pl a = {-1, -1};
            if (edge[i] == a) {
                edge[i] = {y, x};
            }
        } else {
            pl a = {-1, -1};
            if (edge[i] == a) {
                edge[i] = {x, y};
            }
        }
        if (vis[y] == 0) dfs(y);
    }
    vis[x] = 2;
}



void test_case() {
    int n, m;
    cin >> n >> m;
    edge = vpl(m);
    rep(i, 0, m) {
        int x, y;
        cin >> x >> y;
        adj[x].pb({y, i});
        adj[y].pb({x, i});
        edge[i] = {-1, -1};
    }
    rep(i, 1, n + 1) {
        dfs(i);
    }
    each(r, edge) {
        cout << r.F << " " << r.S << "\n";
    }
}
```

3.13 Z-Extra-OrStatements2Sat

```
// Return the smaller lexicographic array of size n that satities a_i |
    a_j = z
// a_i | a_i = z is allowed.
// there must exists a solution.
vector<ll> f(ll n, vector<tuple<ll,ll,ll>> &statements) {
    ll m = statements.size();
    vector<vector<pair<ll,ll>>> adj(n + 1);
    const ll bits = 30;
    vector<ll> taken(n+1, (1 << bits) - 1), answer(n+1, (1 << bits) - 1);
    for (int i = 0; i < m; i++) {
        ll x, y, z;
        tie(x, y, z) = statements[i];

        answer[x] &= z;
        answer[y] &= z;
        if (x == y) {
            taken[x] = 0;
            continue;
        }
        taken[x] &= z;
        taken[y] &= z;
        adj[x].pb({y, z});
        adj[y].pb({x, z});
    }
    for (int x = 1; x <= n; x++) {
```

```
        for (int i = 0; i < bits; i++) {
            if (!((taken[x] >> i) & 1)) continue;
            ll allHave = true;
            for (auto y : adj[x]) {
                if ((y.S >> i) & 1) {
                    allHave &= ((taken[y.F] >> i) & 1) || ((answer[y.F] >>
                        i) & 1);
                }
            }
            taken[x] -= 1 << i;
            if (allHave) {
                answer[x] -= 1 << i;
                for (auto y : adj[x]) {
                    if ((y.S >> i) & 1) {
                        taken[y.F] |= 1 << i;
                        taken[y.F] ^= 1 << i;
                    }
                }
            }
        }
    }
    answer.erase(answer.begin());
    return answer;
}
```

4 4. dp

4.1 Traveling Sales Man

```
// Given directed weighted graph, gets the minimun halmilton cycle.
// Use dfs(0, 1), if 1e9 then it impossible, otherwise get the min.
const int MAX_SIZE = 15;
const ll IMPOSSIBLE = 1e9;
ll INITIAL = 0; // initial node
vpl adj[MAX_SIZE];
vvl dp(MAX_SIZE, vl(1 << MAX_SIZE, -1));
ll n, m;
ll target; // init as (1 << n) - 1, full visited

ll dfs(ll x, ll mask) {
    if (dp[x][mask] != -1) {
        return dp[x][mask];
    }
    if (mask == target) {
        each(yy, adj[x]) {
            if (yy.F == INITIAL) {
                return yy.S;
            }
        }
        return dp[x][mask] = IMPOSSIBLE;
    }
    ll ans = IMPOSSIBLE;
    each(yy, adj[x]) {
        ll y, d;
        tie(y, d) = yy;
        if ((mask >> y) & 1) continue;
        ll actual = dfs(y, mask | (1 << y)) + d;
        ans = min(ans, actual);
    }
    return dp[x][mask] = ans;
}
```

4.2 coin$_c$*hange*

```
// infinite number of coins
// Get the minimum number of coins that sum a value.
void test_case() {
    ll n, x;
    cin >> n >> x;
    vl dp(x + 1, inf - 1);
    vl coin(n);
    rep(i, 0, n) cin >> coin[i];
    dp[0] = 0;
    rep(i, 0, x) {
        each(c, coin) {
            if (c + i > x) continue;
            dp[i + c] = min(dp[i + c], dp[i] + 1);
        }
    }
    if (dp[x] + 1== inf) {
        cout << "-1\n";
    } else {
        cout << dp[x] << "\n";
    }
}
```

4.3 edit$_d$istance

```
// editDistance(a, b, a.size(), b.size());

// Cuantas operaciones, (insert, remove, remplazar) necesito
// para que string a y b sean iguales.
int editDistance(string a, string b, int m, int n)
{
    if (m == 0) return n;
    if (n == 0) return m;
    if (a[m - 1] == b[n - 1])
        return editDistance(a, b, m - 1, n - 1);

    return 1 + min({editDistance(a, b, m, n - 1), // Insert
                    editDistance(a, b, m - 1, n), // Remove
                    editDistance(a, b, m - 1, n - 1) // Replace
                });
}

// My own
ll editDistance(string &s, string &t) {
    ll n = s.size();
    ll m = t.size();
    vvl dp(n+1, vl(m+1, 0));
    for (int i = 0; i <= n; i++) {
        for (int j = 0; j <= m; j++) {
            if (min(i, j) == 0) dp[i][j] = max(i, j);
            else if (s[i-1] == t[j-1]) dp[i][j] = dp[i-1][j-1];
            else dp[i][j] = min(dp[i-1][j], min(dp[i][j-1], dp[i-1][j-1]))
                + 1;
        }
    }
    return dp[n][m];
}
```

4.4 eleverator$_p$roblem

```
// Given n <= 20 persons, print the minimum number of travels
// to move everyone in a elevator with capacity k.

ll n, k;
vl nums;
vector<pair<ll,ll>> dp;

// minimum travels, last travel with minimum weight.
// use f((1 << n) - 1).F
pair<ll,ll> f(ll mask) {
    if (dp[mask] != make_pair(-1ll, -1ll)) {
        return dp[mask];
    }
    if (mask == 0) {
        return dp[mask] = {0, k};
    }
    dp[mask] = {n + 1, 0}; // one person in a travel, or use popcount.
    for (int i = 0; i < n; i++) {
        // person i is the last to enter to elevator.
        if ((mask >> i) & 1) {
            auto actual = f(mask ^ (1 << i)); // best option without this
                last person.
            if (actual.S + nums[i] <= k) {
                actual.S += nums[i];
                // what happened if there are a better minimum.
                // well in that case the last person should be other one.
                // so we are trying all options that last person will be
                    better.
            } else {
                actual.S = nums[i];
                actual.F++;
            }
            dp[mask] = min(dp[mask], actual);
        }
    }
    return dp[mask];
}


// Iterative
void test_case() {
    ll n, k;
    cin >> n >> k;
    vl nums(n);
    vector<pair<ll,ll>> dp(1 << n, {n+1, 0});
    for (int i =0; i < n; i++) cin >> nums[i];
    dp[0] = {0, k};
    for (int i = 1; i < (1 << n); i++) {
        for (int j = 0; j < n; j++) {
            if (i& (1 << j)) {
                auto actual = dp[i ^ (1 << j)];
```

```
            if (actual.S + nums[j] <= k) {
                actual.S += nums[j];
            } else {
                actual.F++;
                actual.S = nums[j];
            }
            dp[i] = min(dp[i], actual);
        }
    }
  }
  cout << dp[(1 << n) -1].F << "\n";
}
```

4.5 lcs

```
const int M_MAX = 20;
const int N_MAX = 20;
int m, n;
string X;
string Y;
int memo[M_MAX + 1][N_MAX + 1];


// Encuetra el Longest Common Subsequence de string X e Y. m y n son sus
    tamaos
// lcs de abfgh aeeeeiiiiigh = agh
int lcs (int m, int n) {
  for (int i = 0; i <= m; i++) {
    for (int j = 0; j <= n; j++) {
      if (i == 0 || j == 0) memo[i][j] = 0;
      else if (X[i - 1] == Y[j - 1]) memo[i][j] = memo[i - 1][j - 1] + 1;
      else memo[i][j] = max(memo[i - 1][j], memo[i][j - 1]);
    }
  }
  return memo[m][n];
}
```

4.6 lcs3

```
string X = "AGGT12";
string Y = "12TXAYB";
string Z = "12XBA";
bool calc[100][100][100];
int dp[100][100][100];
//lcsOf3(X.size() - 1, Y.size() - 1, Z.size() - 1);
int lcsOf3(int i, int j,int k) {
    if(i==-1||j==-1||k==-1) // outbounds
        return 0;
    if(calc[i][j][k]) //memo
        return dp[i][j][k];
    calc[i][j][k] = true;
    if(X[i]==Y[j] && Y[j]==Z[k]) // same
        return dp[i][j][k] = 1+lcsOf3(i-1,j-1,k-1);
    else // best of reducine any
        return dp[i][j][k] = max(max(lcsOf3(i-1,j,k),
                            lcsOf3(i,j-1,k)),lcsOf3(i,j,k-1));
}
```

4.7 lis

```
// TODO: O(n^2)

// nlog(n)
// 1 2 3 5 10 2 -1 100 500
// 1 2 3 5 10 100 500
int lis(vi& v) {
    if (v.size() == 0) // boundary case
        return 0;

    vi tail(v.size(), 0);
    int length = 1; // always points empty slot in tail

    tail[0] = v[0];

    for (int i = 1; i < v.size(); i++) {

        // Do binary search for the element in
        // the range from begin to begin + length
        auto start = tail.begin(), end = tail.begin() + length;
        auto it = lower_bound(start, end, v[i]);

        // If not present change the tail element to v[i]
        if (it == tail.begin() + length)
            tail[length++] = v[i];
```

```
        else
            *it = v[i];
    }

    return length;
}

// My own LIS
int lis(vl &nums) {
    vl best;
    int n = nums.size();
    for (int i = 0; i < n; i++) {
        // For non-decreasing
        // int idx = upper_bound(all(best), nums[i]) - best.begin();

        // For increasing
        int idx = lower_bound(all(best), nums[i]) - best.begin();
        if (idx == best.size()) {
            best.pb(nums[i]);
        } else {
            best[idx] = min(best[idx], nums[i]);
        }
    }

    return best.size();
}

// Also LIS with Segment Tree
```

4.8 $\max_s um_3 d$

```
long long a=20, b=20, c=20;
long long acum[a][b][c];
long long INF = -100000000007;

long long max_range_3D(){
       for(int x=0; x<a; x++){
              for(int y = 0; y<b; y++){
                     for(int z = 0; z<c; z++){
                            if(x>0) acum[x][y][z] += acum[x-1][y][z];
                            if(y>0) acum[x][y][z] += acum[x][y-1][z];
                            if(z>0) acum[x][y][z] += acum[x][y][z-1];
                            if(x>0 && y>0) acum[x][y][z] -=
                                acum[x-1][y-1][z];
                            if(x>0 && z>0) acum[x][y][z] -=
                                acum[x-1][y][z-1];
                            if(y>0 && z>0) acum[x][y][z] -=
                                acum[x][y-1][z-1];
                            if(x>0 && y>0 && z>0) acum[x][y][z] +=
                                acum[x-1][y-1][z-1];
                     }
              }
       }
long long max_value = INF;
for(int x=0; x<a; x++){
       for(int y = 0; y<b; y++){
              for(int z = 0; z<c; z++){
                     for(int h = x; h<a; h++){
                            for(int k = y; k<b; k++){
                                   for(int l = z; l<c; l++){
                                          long long aux =
                                              acum[h][k][l];
                                          if(x>0) aux -=
                                              acum[x-1][k][l];
                                          if(y>0) aux -=
                                              acum[h][y-1][l];
                                          if(z>0) aux -=
                                              acum[x][k][z-1];
                                          if(x>0 && y>0) aux +=
                                              acum[x-1][y-1][l];
                                          if(x>0 && z>0) aux +=
                                              acum[x-1][k][z-1];
                                          if(z>0 && y>0) aux +=
                                              acum[h][y-1][z-1];
                                          if(x>0 && y>0 && z>0)
                                              aux -=
                                              acum[x-1][y-1][z-1];
                                          max_value =
                                              max(max_value,
                                              aux);
                                   }
                            }
                     }
              }
       }
}
return max_value;
```

```
}
```

4.9 max$_s$um$_a$rray

```
int maxRangeSum(vector<int> a){
       int sum = 0, ans = 0;
       for (int i = 0; i < a.size(); i++){
              if (sum + a[i] >= 0) {
                     sum += a[i];
               ans = max(ans, sum);
         } else sum = 0;
       }
       return ans;
}
```

4.10 max$_s$um$_a$rray2d

```
int INF = -100000007; // minimo valor
int n, m; //filas y columnas
const int MAX_N = 105, MAX_M = 105;
int values[MAX_N][MAX_M];

int max_range_sum2D(){
       for(int i=0; i<n;i++){
              for(int j=0; j<m; j++){
                     if(i>0) values[i][j] += values[i-1][j];
                     if(j>0) values[i][j] += values[i][j-1];
                     if(i>0 && j>0) values[i][j] -= values[i-1][j-1];
              }
       }
       int max_mat = INF;
       for(int i=0; i<n;i++){
              for(int j=0; j<m; j++){
                     for(int h = i; h<n; h++){
                            for(int k = j; k<m; k++){
                                   int sub_mat = values[h][k];
                                   if(i>0) sub_mat -= values[i-1][k];
                                   if(j>0) sub_mat -= values[h][j-1];
                                   if(i>0 && j>0) sub_mat +=
                                       values[i-1][j-1];
                                   max_mat = max(sub_mat, max_mat);
                            }
                     }
              }
       }
       return max_mat;
}
```

5 5. tree

5.1 1 K-th Parent

```
1. K-th Parent.cpp

class TreeAncestor {
    int LOG = 20;
    int up[50000][20];
public:
    TreeAncestor(int n, vector<int>& parent) {
        memset(up, -1, 50000 * LOG * 4);
        for (int i = 0; i < n; i++) {
            up[i][0] = parent[i];
        }
        for (int k = 1; k < LOG; k++) {
            for (int i = 0; i < n; i++) {
                if (up[i][k-1] != -1)
                    up[i][k] = up[up[i][k-1]][k-1];
            }
        }
    }

    int getKthAncestor(int node, int k) {
        for (int i = 0; i < LOG; i++) {
            if (k & 1<<i) {
                node = up[node][i];
            }
            if (node == -1) return -1;
        }
        return node;
    }
};
```

5.2 Nearest$_S$elected$_N$odes$_P$roblem

```
// Given an order of selected nodes in a tree, you should print the
    miminum distance between two selected nodes after each operation.

// O(nlogn or n*sqrt(n)); n <= 2*10^5, 2.7 seconds.
// adj is the adjacency list, order is the selected nodes in order
// n is the numeber of nodes, returns the minimum after each operation
// note that operation 0 answer is 1e9
vl f(vvl &adj, vl &order, ll n) {
    vl answer;
    vl dist(n + 1, 1e9);
    ll best = 1e9;
    vl q(n + 1);
    ll sz = 0;
    for (int i = 0; i < n; i++) {
        best = min(best, dist[order[i]]);
        sz = 0;
        dist[order[i]] = 0;
        q[sz++] = order[i];
        ll idx = 0;
        while (idx < sz) {
            ll x = q[idx++];
            if (dist[x] + 1 >= best) break;
            for (auto &y : adj[x]) {
                if (dist[x] + 1 < dist[y]) {
                    dist[y] = dist[x] + 1;
                    q[sz++] = y;
                }
            }
        }
        answer.pb(best);
    }
    return answer;
}
```

5.3 Two$_P$ieces$_o$n$_T$ree

```
// In a tree with 'n' nodes where 2 pieces starting from root 1
// must go to certain nodes each one and must not exceed 'd' between
// the two pieces, after they have to return to root 1
// two_pieces_on_tree() find the minimum quantity of moves
// My submittion in CF:
    https://codeforces.com/contest/1774/submission/189071201

ll n, d; // quantity of nodes, maximum distance between pieces
vvl children; // tree
vector<int> a, b; // nodes that must visit first and second piecesS

void dfs(ll x, vl &route) {
    route.pb(x);
    ll kParent = 1; //route
    if (route.size() - 1 >= d) {
        kParent = route[route.size() - 1 - d];
    }
    b[kParent] |= a[x];
    a[kParent] |= b[x];
    each(y, children[x]) {
        dfs(y, route);
        a[x] |= a[y];
        b[x] |= b[y];
    }
    route.pop_back();
}

ll two_pieces_on_tree() {
    ll root = 1;
    vl emptyRoute = vl();
    dfs(root, emptyRoute);
    ll total = 0;
    for (int i = 1; i <= n; i++) {
        total += a[i] + b[i];
    }
    return total * 2 - 4;
}
```

5.4 lca

```
#include<bits/stdc++.h>
//#include<cmath>
//#include<bitset>

using namespace std;

#define MP make_pair
```

```cpp
#define MT make_tuple
#define PB push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sortn(x, n) sort((x), (x) + (n));
#define SQ(a) ((a) * (a))
#define max3(a, b, c) max((a), max((b), (c)))
#define max4(a, b, c, d) max(max3(a, b, c), d)
#define min3(a, b, c) min((a), min((b), (c)))
#define min4(a, b, c, d) min(min3(a, b, c), d)
#define fastIO() cin.tie(0); ios::sync_with_stdio(0);

// loops
#define FOR(i, a, b) for (int (i) = (a); (i) < (b); (i)++)
#define ROF(i, a, b) for (int (i) = (a); (i) >= (b); (i)--)
#define REP(i, a, b) for (int (i) = (a); (i) <= (b); (i)++)
#define EACH(a, x) for (auto &(a) : (x))

typedef long long ll;
typedef pair<int, int> pii;
typedef tuple<long long, long long, long long> tiii;
typedef pair<long long, long long> pll;
typedef unsigned long long ull;
typedef long double ld;
typedef vector<int> vi;
typedef vector<bool> vb;
typedef vector<ll> vl;
typedef vector<string> vs;

const int dx[4]{1,0,-1,0}, dy[4]{0,1,0,-1};
const int MOD = 1e9 + 7;

template <typename... V>
void funcDebug(string vars, V... v) {
    cout << vars << " = ";
    string delim = "";
    (..., (cout << delim << v, delim = ", "));
    cout << endl;
}

// #define ONLINE_JUDGE
#ifndef ONLINE_JUDGE
    #define deb(x...) funcDebug(#x, x);
    #define debug(x) (cout << #x << ": " << x << endl);
    #define LINE cout << "--------------------" << endl;
    #define LINE2 cout << "~ ~ ~ ~ ~ ~ ~ ~ ~ ~" << endl;
    #define LINE3 cout << "- - - - - - - -" << endl;
    #define debugA(x, n) cout << #x << ": "; for (int zabz = 0; zabz < n;
        zabz++) cout << (x)[zabz] << " "; cout << endl;
    #define debugI(x) cout << #x << ": "; EACH(y, (x)) cout << y << " ";
        cout << endl;
#else
    #define deb(x...)
    #define debug(x)
    #define debugA(x, n)
    #define LINE
    #define LINE2
    #define LINE3
    #define debugI(x)
#endif

const ll infl = INT64_MAX;
const int inf = INT32_MAX;


// const int N = 1e5 + 10;

// const int LOG = 16;


const int N = 50000;
const int LOG = 16;

vector<pii> children[N];
int up[N][LOG];
int dist[N][LOG];
int depth[N];
bool visited[N];


void dfs(int x, int level = 0) {
    if (visited[x]) return;
    visited[x] = true;
    depth[x] = level;
    EACH(y, children[x]) {
        if (!visited[y.F]) {
            up[y.F][0] = x;
            dist[y.F][0] = y.S;
```

```
            dfs(y.F, level + 1);
        }
    }
}

int query(int x, int y) {
    if (depth[y] > depth[x]) swap(x, y);
    int toUp = depth[x] - depth[y];
    int bit = 0;
    int res = 0;
    while (toUp) {
        if (toUp & 1) res += dist[x][bit], x = up[x][bit];
        bit++;
        toUp >>=1;
    }
    if (x == y) return res;
    ROF(i, LOG - 1, 0) {
        if (up[x][i] != up[y][i]) {
            res += dist[x][i] + dist[y][i];
            x = up[x][i];
            y = up[y][i];
        }
    }
    return dist[x][0] + dist[y][0] + res;
}

void solve() {
    int n;
    cin >> n;
    FOR(i, 0, n - 1) {
        int a, b, w;
        cin >> a >> b >> w;
        children[a].PB({b, w});
        children[b].PB({a, w});
    }
    int root = 0;
    dfs(root);
    FOR(i, 1, LOG) {
        FOR(j, 0, n) {
            int ancestor = up[j][i - 1];
            up[j][i] = up[ancestor][i - 1];
            dist[j][i] = dist[ancestor][i - 1] + dist[j][i - 1];
        }
    }
    int q;
    cin >> q;
    while (q--) {
        int a, b;
        cin >> a >> b;
        cout << query(a, b) << "\n";
    }
}


int main() {
    fastIO();
    solve();
}
```

5.5 moetree

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vi;
typedef vector<vi> vvi;

map<int, int> getID;
map<int, int>::iterator it;

const int LOGN = 20;
int id, bs, N;
int counter[50050];
int A[50050], P[100050];
int res[100050];
int st[50050], ed[50050];
int DP[20][50050], level[50050];
bool flag[50050];
bool seen[50050];
vvi edges;

struct Q {
   int l, r, p, id;
   bool operator < (const Q& other) const {
      return (l / bs < other.l / bs || (l / bs == other.l / bs && r <
          other.r));
   }//operator <
} q[100050];
```

```
void DFS0(const int u) {
   seen[u] = 1;
   P[id] = u;
   st[u] = id++;
   for (auto& e : edges[u]) {
      if (!seen[e]) {
         DP[0][e] = u;
         level[e] = level[u] + 1;
         DFS0(e);
      }//if
   }//for
   P[id] = u;
   ed[u] = id++;
}//DFS0

void prep(const int r) {
   level[r] = 0;
   for (int i = 0; i < LOGN; i++)
      DP[i][r] = r;
   id = 0;
   DFS0(r);
   for (int i = 1; i < LOGN; i++)
      for (int j = 1; j <= N; j++)
         DP[i][j] = DP[i - 1][DP[i - 1][j]];
}//prep

int LCA(int a, int b) {
   if (level[a] > level[b])
      swap(a, b);
   int diff = level[b] - level[a];
   for (int i = 0; i < LOGN; i++)
      if (diff & (1 << i))
         b = DP[i][b]; //move 2^i parents upwards
   if (a == b)
      return a;
   for (int i = LOGN - 1; i >= 0; i--)
      if (DP[i][a] != DP[i][b])
         a = DP[i][a], b = DP[i][b];
   return DP[0][a];
}//LCA

int main() {
   int Q, n1, n2, L, R, a, v = 1, tot;
   scanf("%d %d", &N, &Q);
   edges.assign(N + 5, vi());
   bs = sqrt(N);
   for (int i = 1; i <= N; i++) {
      scanf("%d", &a);
      A[i] = ((it = getID.find(a)) != getID.end()) ? it->second :
          (getID[a] = v++);
   }//for
   for (int i = 0; i < N - 1; i++) {
      scanf("%d %d", &n1, &n2);
      edges[n1].push_back(n2);
      edges[n2].push_back(n1);
   }//for
   prep(1);
   for (int i = 0; i < Q; i++) {
      scanf("%d %d", &n1, &n2);
      if (st[n1] > st[n2])
         swap(n1, n2);
      q[i].p = LCA(n1, n2);
      if (q[i].p == n1)
         q[i].l = st[n1], q[i].r = st[n2];
      else
         q[i].l = ed[n1], q[i].r = st[n2];
      q[i].id = i;
   }//for
   sort(q, q + Q);
   L = 0; R = -1; tot = 0;
   for (int i = 0; i < Q; i++) {
      while (R < q[i].r) {
         if (!flag[P[++R]])
            tot += (++counter[A[P[R]]] == 1);
         else
            tot -= (--counter[A[P[R]]] == 0);
         flag[P[R]] = !flag[P[R]];
      }//while
      while (R > q[i].r) {
         if (!flag[P[R]])
            tot += (++counter[A[P[R]]] == 1);
         else
            tot -= (--counter[A[P[R]]] == 0);
         flag[P[R]] = !flag[P[R]];
         R--;
      }//while
      while (L < q[i].l) {
         if (!flag[P[L]])
            tot += (++counter[A[P[L]]] == 1);
         else
```

```
          tot -= (--counter[A[P[L]]] == 0);
        flag[P[L]] = !flag[P[L]];
        L++;
      }//while
      while (L > q[i].l) {
        if (!flag[P[--L]])
          tot += (++counter[A[P[L]]] == 1);
        else
          tot -= (--counter[A[P[L]]] == 0);
        flag[P[L]] = !flag[P[L]];
      }//while
      res[q[i].id] = tot + (q[i].p != P[q[i].l] && !counter[A[q[i].p]]);
   }//for
   for (int i = 0; i < Q; i++)
      printf("%d\n", res[i]);
   return 0;
}//main
```

5.6 simple-lca

```
// view: https://cses.fi/problemset/task/1688/
vector<vector<ll>> children;
vector<vector<ll>> up;
const int LOG = 18; // 2e5
vector<ll> depth;

void dfs(ll x, ll d =0) {
    depth[x] = d;
    for (auto y : children[x]) {
        dfs(y, d + 1);
    }
}

ll kParent(ll x, ll k) {
    ll i = 0;
    while (k) {
        if (k & 1) {
            x = up[i][x];
        }
        k >>= 1;
        i++;
    }
    return x;
}

ll query(ll x, ll y) {
    if (depth[x] < depth[y]) {
        swap(x, y);
    }

    x = kParent(x, depth[x] - depth[y]);
    if (x == y) {
        return x;
    }
    for (int i = LOG - 1; i >= 0; i--) {
        if (up[i][x] != up[i][y]) {
            x = up[i][x];
            y = up[i][y];
        }
    }
    return up[0][x];
}

void test_case() {
    ll n, q;
    cin >> n >> q;
    children = vector<vector<ll>>(n);
    up = vector<vector<ll>>(LOG, vector<ll>(n, 0));
    depth = vector<ll>(n);
    for (int i = 1; i < n; i++) {
        ll p;
        cin >> p;
        p--;
        children[p].pb(i);
        up[0][i] = p;
    }
    dfs(0);
    for (int i = 1; i < LOG; i++) {
        for (int j = 0; j < n; j++) {
            up[i][j] = up[i-1][up[i-1][j]];
        }
    }
    for (int i = 0; i < q; i++) {
        ll x, y;
        cin >> x >> y;
        x--,y--;
        cout << query(x, y) + 1<< "\n";
    }
```

```
}
```

6 6. flows

6.1 Hungarian

```
Halla el mximo match en un grafo bipartito con pesos (min cost) O(V ^ 3)

typedef ll T;
const T inf = 1e18;

struct hung {
    int n, m;
    vector<T> u, v; vector<int> p, way;
    vector<vector<T>> g;

    hung(int n, int m):
        n(n), m(m), g(n+1, vector<T>(m+1, inf-1)),
        u(n+1), v(m+1), p(m+1), way(m+1) {}

    void set(int u, int v, T w) { g[u+1][v+1] = w; }

    T assign() {
        for (int i = 1; i <= n; ++i) {
            int j0 = 0; p[0] = i;
            vector<T> minv(m+1, inf);
            vector<char> used(m+1, false);
            do {
                used[j0] = true;
                int i0 = p[j0], j1; T delta = inf;
                for (int j = 1; j <= m; ++j) if (!used[j]) {
                    T cur = g[i0][j] - u[i0] - v[j];
                    if (cur < minv[j]) minv[j] = cur, way[j] = j0;
                    if (minv[j] < delta) delta = minv[j], j1 = j;
                }
                for (int j = 0; j <= m; ++j)
                    if (used[j]) u[p[j]] += delta, v[j] -= delta;
                    else minv[j] -= delta;
                j0 = j1;
            } while (p[j0]);
            do {
                int j1 = way[j0]; p[j0] = p[j1]; j0 = j1;
            } while (j0);
        }
        return -v[0];
    }
};
```

6.2 MaxFlow

```
// N <= 5000, M <= 30000, C <= 1e9, 300ms

const int INF = INT32_MAX;

struct flowEdge{
    ll to, rev, f, cap;
};


struct max_flow {

    vector<vector<flowEdge>> G;

    max_flow(int n) : G(n) {
        nodes = n;
    }

    // Aade arista (st -> en) con su capacidad
    void addEdge(int st, int en, int cap) {
        flowEdge A = {en, (int)G[en].size(), 0, cap};
        flowEdge B = {st, (int)G[st].size(), 0, 0};
        G[st].pb(A);
        G[en].pb(B);
    }

    ll nodes, S, T; // asignar estos valores al armar el grafo G
                // nodes = nodos en red de flujo. Hacer G.clear();
                    G.resize(nodes);
    vl work, lvl;


    bool bfs() {
        int qt = 0;
        queue<ll> q;
        q.push(S);
```

```
        lvl.assign(nodes, -1);
        lvl[S] = 0;
        while (q.size()) {
            int v = q.front(); q.pop();
            for (flowEdge &e : G[v]) {
                int u = e.to;
                if (e.cap <= e.f || lvl[u] != -1) continue;
                lvl[u] = lvl[v] + 1;
                q.push(u);
            }
        }
        return lvl[T] != -1;
    }

    ll dfs(ll v, ll f) {
        if (v == T || f == 0) return f;
        for (ll &i = work[v]; i < G[v].size(); i++) {
            flowEdge &e = G[v][i];
            ll u = e.to;
            if (e.cap <= e.f || lvl[u] != lvl[v] + 1) continue;
            ll df = dfs(u, min(f, e.cap - e.f));
            if (df) {
                e.f += df;
                G[u][e.rev].f -= df;
                return df;
            }
        }
        return 0;
    }

    ll maxFlow(ll s, ll t) {
        S = s;
        T = t;
        ll flow = 0;
        while (bfs()) {
            work.assign(nodes, 0);
            while (true) {
                ll df = dfs(S, INF);
                if (df == 0) break;
                flow += df;
            }
        }
        return flow;
    }
};
```

6.3 $\max_{f}low$

```
struct Dinitz{
    const int INF = 1e9 + 7;
    Dinitz(){}
    Dinitz(int n, int s, int t) {init(n, s, t);}

    void init(int n, int s, int t)
    {
        S = s, T = t;
        nodes = n;
        G.clear(), G.resize(n);
        Q.resize(n);
    }
    struct flowEdge
    {
        int to, rev, f, cap;
    };

    vector<vector<flowEdge> > G;

    // Aade arista (st -> en) con su capacidad
    void addEdge(int st, int en, int cap) {
        flowEdge A = {en, (int)G[en].size(), 0, cap};
        flowEdge B = {st, (int)G[st].size(), 0, 0};
        G[st].pb(A);
        G[en].pb(B);
    }

    int nodes, S, T; // asignar estos valores al armar el grafo G
                     // nodes = nodos en red de flujo. Hacer G.clear();
                         G.resize(nodes);
    vi work, lvl;
    vi Q;

    bool bfs() {
        int qt = 0;
        Q[qt++] = S;
        lvl.assign(nodes, -1);
        lvl[S] = 0;
        for (int qh = 0; qh < qt; qh++) {
            int v = Q[qh];
            for (flowEdge &e : G[v]) {
                int u = e.to;
                if (e.cap <= e.f || lvl[u] != -1) continue;
```

```
                lvl[u] = lvl[v] + 1;
                Q[qt++] = u;
            }
        }
        return lvl[T] != -1;
    }

    int dfs(int v, int f) {
        if (v == T || f == 0) return f;
        for (int &i = work[v]; i < G[v].size(); i++) {
            flowEdge &e = G[v][i];
            int u = e.to;
            if (e.cap <= e.f || lvl[u] != lvl[v] + 1) continue;
            int df = dfs(u, min(f, e.cap - e.f));
            if (df) {
                e.f += df;
                G[u][e.rev].f -= df;
                return df;
            }
        }
        return 0;
    }

    int maxFlow() {
        int flow = 0;
        while (bfs()) {
            work.assign(nodes, 0);
            while (true) {
                int df = dfs(S, INF);
                if (df == 0) break;
                flow += df;
            }
        }
        return flow;
    }
};
```

6.4 $\min_{cost}{}_{flow}$

```
// O(min(E^2 V ^2,   EVFLOW  ))
// Min Cost Max Flow Dinits
struct CheapDinitz{
    const int INF = 1e9 + 7;

    CheapDinitz() {}
    CheapDinitz(int n, int s, int t) {init(n, s, t);}

    int nodes, S, T;
    vi dist;
    vi pot, curFlow, prevNode, prevEdge, Q, inQue;

    struct flowEdge{
        int to, rev, flow, cap, cost;
    };
    vector<vector<flowEdge>> G;
    void init(int n, int s, int t)
    {
        nodes = n, S = s, T = t;
        curFlow.assign(n, 0), prevNode.assign(n, 0), prevEdge.assign(n, 0);
        Q.assign(n, 0), inQue.assign(n, 0);
        G.clear();
        G.resize(n);
    }

    void addEdge(int s, int t, int cap, int cost)
    {
        flowEdge a = {t, (int)G[t].size(), 0, cap, cost};
        flowEdge b = {s, (int)G[s].size(), 0, 0, -cost};
        G[s].pb(a);
        G[t].pb(b);
    }

    void bellmanFord()
    {
        pot.assign(nodes, INF);
        pot[S] = 0;
        int qt = 0;
        Q[qt++] = S;
        for (int qh = 0; (qh - qt) % nodes != 0; qh++)
        {
            int u = Q[qh % nodes];
            inQue[u] = 0;
            for (int i = 0; i < (int)G[u].size(); i++)
            {
                flowEdge &e = G[u][i];
                if (e.cap <= e.flow) continue;
                int v = e.to;
                int newDist = pot[u] + e.cost;
```

```
            if (pot[v] > newDist)
            {
                pot[v] = newDist;
                if (!inQue[v])
                {
                    Q[qt++ % nodes] = v;
                    inQue[v] = 1;
                }
            }
        }
    }
}

ii MinCostFlow()
{
    bellmanFord();
    int flow = 0;
    int flowCost = 0;
    while (true) // always a good start for an algorithm :v
    {
        set<ii> s;
        s.insert({0, S});
        dist.assign(nodes, INF);
        dist[S] = 0;
        curFlow[S] = INF;
        while (s.size() > 0)
        {
            int u = s.begin() -> s;
            int actDist = s.begin() -> f;
            s.erase(s.begin());
            if (actDist > dist[u]) continue;
            for (int i = 0; i < (int)G[u].size(); i++)
            {
                flowEdge &e = G[u][i];
                int v = e.to;
                if (e.cap <= e.flow) continue;
                int newDist = actDist + e.cost + pot[u] - pot[v];
                if (newDist < dist[v])
                {
                    dist[v] = newDist;
                    s.insert({newDist, v});
                    prevNode[v] = u;
                    prevEdge[v] = i;
                    curFlow[v] = min(curFlow[u], e.cap - e.flow);
                }
            }
        }
        if (dist[T] == INF)
            break;
        for (int i = 0; i < nodes; i++)
            pot[i] += dist[i];
        int df = curFlow[T];
        flow += df;
        for (int v = T; v != S; v = prevNode[v])
        {
            flowEdge &e = G[prevNode[v]][prevEdge[v]];
            e.flow += df;
            G[v][e.rev].flow -= df;
            flowCost += df * e.cost;
        }
    }
    return {flow, flowCost};
}
};
```

7 7. query

7.1 1 - Segment Tree

```
1. Segment Tree

const int N = 1e6 + 1;

int tree[N * 4 + 4];
int nums[N + 1];

void build(int i, int l, int r) {
        if (l == r) {
                tree[i] = nums[r];
        } else {
                int mid = (l + r) / 2;
                build(i * 2 + 1, l, mid);
                build(i * 2 + 2, mid + 1, r);
                tree[i] = tree[i * 2 + 1] + tree[i * 2 + 2];
                // tree[i] = compare(tree[i * 2 + 1], tree[i * 2 + 2]);
        }
}
```

```
void update(int i, int l, int r, int pos, int diff) {
	if (l <= pos && pos <= r) {
		if (l == r) { // leaf
			tree[i] += diff;
		} else { // node
			int mid = (l + r) / 2;
			update(i * 2 + 1, l, mid, pos, diff);
			update(i * 2 + 2, mid + 1, r, pos, diff);
			tree[i] = tree[i * 2 + 1] + tree[i * 2 + 2];
			// tree[i] = compare(...)
		}
	}
}

int query(int i, int sl, int sr, int l, int r) {
	if (l <= sl && sr <= r) { // overlap
		return tree[i];
	} else if (sr < l || r < sl) { // no overlap
		return 0;
	} else { // partially over lap
		int mid = (sl + sr) / 2;
		return query(i * 2 + 1, sl, mid, l, r) + query(i * 2 + 2,
		    mid + 1, sr, l, r);
		// return compare(a, b);
	}
}
```

7.2 2D$_{F}enwick$

```
/* C++ program to implement 2D Binary Indexed Tree

2D BIT is basically a BIT where each element is another BIT.
Updating by adding v on (x, y) means it's effect will be found
throughout the rectangle [(x, y), (max_x, max_y)],
and query for (x, y) gives you the result of the rectangle
[(0, 0), (x, y)], assuming the total rectangle is
[(0, 0), (max_x, max_y)]. So when you query and update on
this BIT,you have to be careful about how many times you are
subtracting a rectangle and adding it. Simple set union formula
works here.

So if you want to get the result of a specific rectangle
[(x1, y1), (x2, y2)], the following steps are necessary:

Query(x1,y1,x2,y2) = getSum(x2, y2)-getSum(x2, y1-1) -
                                    getSum(x1-1, y2)+getSum(x1-1, y1-1)

Here 'Query(x1,y1,x2,y2)' means the sum of elements enclosed
in the rectangle with bottom-left corner's co-ordinates
(x1, y1) and top-right corner's co-ordinates - (x2, y2)

Constraints -> x1<=x2 and y1<=y2

       /\
y |
       |              --------(x2,y2)
       |              |      |
       |              |      |
       |              |      |
       |              ---------
       |       (x1,y1)
       |
       |____________________________
(0, 0)                         x-->

In this program we have assumed a square matrix. The
program can be easily extended to a rectangular one. */

#include<bits/stdc++.h>
using namespace std;

#define N 4 // N-->max_x and max_y

// A structure to hold the queries
struct Query
{
	int x1, y1; // x and y co-ordinates of bottom left
	int x2, y2; // x and y co-ordinates of top right
};

// A function to update the 2D BIT
void updateBIT(int BIT[][N+1], int x, int y, int val)
{
	for (; x <= N; x += (x & -x))
	{
		// This loop update all the 1D BIT inside the
		// array of 1D BIT = BIT[x]
```

```
                for (int yy=y; yy <= N; yy += (yy & -yy))
                        BIT[x][yy] += val;
        }
        return;
}

// A function to get sum from (0, 0) to (x, y)
int getSum(int BIT[][N+1], int x, int y)
{
        int sum = 0;

        for(; x > 0; x -= x&-x)
        {
                // This loop sum through all the 1D BIT
                // inside the array of 1D BIT = BIT[x]
                for(int yy=y; yy > 0; yy -= yy&-yy)
                {
                        sum += BIT[x][yy];
                }
        }
        return sum;
}

// A function to create an auxiliary matrix
// from the given input matrix
void constructAux(int mat[][N], int aux[][N+1])
{
        // Initialise Auxiliary array to 0
        for (int i=0; i<=N; i++)
                for (int j=0; j<=N; j++)
                        aux[i][j] = 0;

        // Construct the Auxiliary Matrix
        for (int j=1; j<=N; j++)
                for (int i=1; i<=N; i++)
                        aux[i][j] = mat[N-j][i-1];

        return;
}

// A function to construct a 2D BIT
void construct2DBIT(int mat[][N], int BIT[][N+1])
{
        // Create an auxiliary matrix
        int aux[N+1][N+1];

        constructAux(mat, aux);

        // Initialise the BIT to 0
        for (int i=1; i<=N; i++)
                for (int j=1; j<=N; j++)
                        BIT[i][j] = 0;

        for (int j=1; j<=N; j++)
        {
                for (int i=1; i<=N; i++)
                {
                        // Creating a 2D-BIT using update function
                        // everytime we/ encounter a value in the
                        // input 2D-array
                        int v1 = getSum(BIT, i, j);
                        int v2 = getSum(BIT, i, j-1);
                        int v3 = getSum(BIT, i-1, j-1);
                        int v4 = getSum(BIT, i-1, j);

                        // Assigning a value to a particular element
                        // of 2D BIT
                        updateBIT(BIT, i, j, aux[i][j]-(v1-v2-v4+v3));
                }
        }

        return;
}

// A function to answer the queries
void answerQueries(Query q[], int m, int BIT[][N+1])
{
        for (int i=0; i<m; i++)
        {
                int x1 = q[i].x1 + 1;
                int y1 = q[i].y1 + 1;
                int x2 = q[i].x2 + 1;
                int y2 = q[i].y2 + 1;

                int ans = getSum(BIT, x2, y2)-getSum(BIT, x2, y1-1)-
                                getSum(BIT, x1-1, y2)+getSum(BIT, x1-1,
                                    y1-1);

                printf ("Query(%d, %d, %d, %d) = %d\n",
                                q[i].x1, q[i].y1, q[i].x2, q[i].y2, ans);
        }
```

```
        return;
}

// Driver program
int main()
{
        int mat[N][N] = {{1, 2, 3, 4},
                                    {5, 3, 8, 1},
                                    {4, 6, 7, 5},
                                    {2, 4, 8, 9}};

        // Create a 2D Binary Indexed Tree
        int BIT[N+1][N+1];
        construct2DBIT(mat, BIT);

        /* Queries of the form - x1, y1, x2, y2
        For example the query- {1, 1, 3, 2} means the sub-matrix-
        y
        /\
3 |     1 2 3 4       Sub-matrix
2 |     5 3 8 1       {1,1,3,2}     --->   3 8 1
1 |     4 6 7 5
    6 7 5
0 |     2 4 8 9
        |
--|------ 0 1 2 3 ----> x
        |

        Hence sum of the sub-matrix = 3+8+1+6+7+5 = 30

        */

        Query q[] = {{1, 1, 3, 2}, {2, 3, 3, 3}, {1, 1, 1, 1}};
        int m = sizeof(q)/sizeof(q[0]);

        answerQueries(q, m, BIT);

        return(0);
}
```

7.3 Merge$_{S}ort_{T}ree$

```
// usage
// vector<node*> nodes;
// tree.query(l, r, nodes);

// returns log(n) sorted segments in a range (l, r)

struct node {
    ll l, r;
    vl nums;
    vl prefix;
};

struct segtree {
    int n;
    vector<node> tree;
    void init(int nn, vl& nodes) {
        tree.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        tree.resize(size * 2);
        build(0, 0, n - 1, nodes);
    }


    void query(ll i, ll sl, ll sr, ll l, ll r, vector<node*> &ans) {
        if (l <= sl && sr <= r) {
            ans.pb(&tree[i]);
        } else if (sr < l || r < sl) {

        } else {
            int mid = (sl + sr) >> 1;
            query(i * 2 + 1, sl, mid, l, r, ans);
            query(i * 2 + 2, mid + 1, sr, l, r, ans);
        }
    }

    void query(ll l, ll r, vector<node*> &ans) {
        return query(0, 0, n - 1, l, r, ans);
    }

    void build(int nodei, int l, int r, vl &nums) {
        if (l == r) {
            tree[nodei].nums = { nums[l] };
```

```
            tree[nodei].prefix = {nums[l]};
            tree[nodei].l = l;
            tree[nodei].r = r;
        } else {
            ll mid = (l + r) >> 1;
            build(nodei * 2 + 1, l, mid, nums);
            build(nodei * 2 + 2, mid + 1, r, nums);
            ll a = tree[nodei*2+1].nums.size();
            ll b = tree[nodei*2+2].nums.size();
            tree[nodei].nums.reserve(a + b);
            tree[nodei].prefix.resize(a+b);
            ll i = 0;
            ll j = 0;
            while (i < a && j < b) {
                ll simon = tree[nodei*2+1].nums[i];
                ll simon2 = tree[nodei*2+2].nums[j];
                if (simon <= simon2) {
                    tree[nodei].nums.pb(simon);
                    i++;
                } else {
                    tree[nodei].nums.pb(simon2);
                    j++;
                }
            }
            while (i < a) {
                tree[nodei].nums.pb(tree[nodei*2+1].nums[i]);
                i++;
            }
            while (j < b) {
                tree[nodei].nums.pb(tree[nodei*2+2].nums[j]);
                j++;
            }
            tree[nodei].prefix[0] = tree[nodei].nums[0];
            for (int i = 1; i < a + b; i++) {
                tree[nodei].prefix[i] = tree[nodei].prefix[i - 1] +
                    tree[nodei].nums[i];
            }
            tree[nodei].l = l;
            tree[nodei].r = r;
        }
    }
};
```

7.4 Min Segment Tree

```
// Max segment tree
struct segtree {
    int n;
    vl tree;

    void init(int nn) {
        tree.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        tree.resize(size * 2);
    }

    void update(int i, int sl, int sr, int pos, ll diff) {
        if (sl <= pos && pos <= sr) {
            if (sl == sr) {
                tree[i] += diff;
            } else {
                int mid = (sl + sr) / 2;
                update(i * 2 + 1, sl, mid, pos, diff);
                update(i * 2 + 2, mid + 1, sr, pos, diff);
                tree[i] = max(tree[i * 2 + 1], tree[i * 2 + 2]);
            }
        }
    }

    void update(int pos, ll diff) {
        update(0, 0, n - 1, pos, diff);
    }

    ll query(int i, int sl, int sr, int l, int r) {
        if (l <= sl && sr <= r) {
            return tree[i];
        } else if(sr < l || r < sl) {
            return INT64_MIN;
        } else {
            int mid = (sl + sr) / 2;
            auto a = query(i * 2 + 1, sl, mid, l, r);
            auto b = query(i * 2 + 2, mid + 1, sr, l, r);
            return max(a, b);
        }
```

```
    }

    ll query(int l, int r) {
        return query(0, 0, n - 1, l, r);
    }
};
```

7.5 Mo's

```
const int BLOCK_SIZE = 430; // 1e5=310 2e5=430

struct query {
    int l, r, idx;

    bool operator <(query &other) const {
        return MP(l / BLOCK_SIZE, r) < MP(other.l / BLOCK_SIZE, other.r);
    }
};


void add(int idx);
void remove(int idx);
ll getAnswer();

vector<ll> mo(vector<query> queries) {
    vector<ll> answers(queries.size());
    int l = 0;
    int r = -1;
    sort(all(queries));
    EACH(q, queries) {
        while (q.l < l) add(--l);
        while (r < q.r) add(++r);
        while (l < q.l) remove(l++);
        while (q.r < r) remove(r--);
        answers[q.idx] = getAnswer();
    }
    return answers;
}

vl nums; //init
ll ans = 0;
int cnt[1000001];
void add(int idx) {}
void remove(int idx) {}
ll getAnswer() {
    return ans;
}
```

7.6 SegTree Max Sum sub arrays

```
// Segmentree to calculate the maximum sum of all possible sub arrays.
// assing value is the initial default value
// set the values with modif
// get the answer with tree.query(0, n - 1).val

struct DynamicMaxSubarraySum {
    struct node {
        ll pref, suf, val, sum;
    };
    int N;
    ll neutral;
    vector<node> t;
    DynamicMaxSubarraySum(int _N, ll assign_value) {
        neutral = assign_value;
        N = _N;
        t.resize(4 * N);
        FOR(i, 0, 4 * N) t[i] = {0, 0, 0, 0};
        build(1, 0, N - 1);
    }
    void build(int i, int l, int r) {
        if(l == r) {
            t[i].pref = t[i].suf = t[i].val = t[i].sum = neutral;
            return;
        }
        int mid = (l + r) >> 1;
        build(2 * i, l, mid);
        build(2 * i + 1, mid + 1, r);
        t[i] = merge(t[2 * i], t[2 * i + 1]);
    }
    node merge(node a, node b) {
        node c;
        c.pref = max(a.pref, a.sum + b.pref);
        c.suf = max(b.suf, b.sum + a.suf);
        c.val = max({a.val, b.val, a.suf + b.pref});
        c.sum = a.sum + b.sum;
        return c;
```

```
    }

    void modif(int i, int l, int r, int pos, ll val) {
        if(l > pos || r < pos) return;
        if(l == pos && r == pos) {
            t[i].pref = t[i].suf = t[i].val = t[i].sum = val;
            return;
        }
        int mid = (l + r) >> 1;
        modif(2 * i, l, mid, pos, val);
        modif(2 * i + 1, mid + 1, r, pos, val);
        t[i] = merge(t[2 * i], t[2 * i + 1]);
    }
    node query(int i, int l, int r, int tl, int tr) {
        if(l > tr || r < tl) return {0, 0, 0, 0};
        if(l >= tl && r <= tr) return t[i];
        int mid = (l + r) >> 1;
        return merge(query(2 * i, l, mid, tl, tr), query(2 * i + 1, mid +
            1, r, tl, tr));
    }

    void modif(int pos, ll val) {
        modif(1, 0, N - 1, pos, val);
    }
    node query(int l, int r) {
        return query(1, 0, N - 1, l, r);
    }
    node query(int pos) {
        return query(1, 0, N - 1, pos, pos);
    }
};
```

7.7 fenwicktree

```
struct FenwickTree {
    vector<int> bit;
    int n;

    FenwickTree(int n) {
        this->n = n;
        bit.assign(n, 0);
    }

    FenwickTree(vector<int> a) : FenwickTree(a.size()) {
        for (size_t i = 0; i < a.size(); i++)
            add(i, a[i]);
    }

    int sum(int r) {
        int ret = 0;
        for (; r >= 0; r = (r & (r + 1)) - 1)
            ret += bit[r];
        return ret;
    }

    int sum(int l, int r) {
        return sum(r) - sum(l - 1);
    }

    void add(int idx, int delta) {
        for (; idx < n; idx = idx | (idx + 1))
            bit[idx] += delta;
    }
};
```

7.8 general$_s$egtree

```
// >>>>>>> Implement
// Example of a Segment tree of Xor
struct Node {
    ll a = 0;
};

Node e() {
    Node node;
    return node;
}

Node op(Node a, Node b) {
    Node node;
    node.a = a.a ^ b.a;
    return node;
}
// >>>>>>>> Implement
```

```
struct segtree {
    vector<Node> nodes;
    ll n;

    void init(int n) {
        auto a = vector<Node>(n, e());
        init(a);
    }

    void init(vector<Node>& initial) {
        nodes.clear();
        n = initial.size();
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        nodes.resize(size * 2);
        build(0, 0, n-1, initial);
    }

    void build(int i, int sl, int sr, vector<Node>& initial) {
        if (sl == sr) {
            nodes[i] = initial[sl];
        } else {
            ll mid = (sl + sr) >> 1;
            build(i*2+1, sl, mid, initial);
            build(i*2+2, mid+1,sr,initial);
            nodes[i] = op(nodes[i*2+1], nodes[i*2+2]);
        }
    }

    void update(int i, int sl, int sr, int pos, Node node) {
        if (sl <= pos && pos <= sr) {
            if (sl == sr) {
                nodes[i] = node;
            } else {
                int mid = (sl + sr) >> 1;
                update(i * 2 + 1, sl, mid, pos, node);
                update(i * 2 + 2, mid + 1, sr, pos, node);
                nodes[i] = op(nodes[i*2+1], nodes[i*2+2]);
            }
        }
    }

    void update(int pos, Node node) {
        update(0, 0, n - 1, pos, node);
    }

    Node query(int i, int sl, int sr, int l, int r) {
        if (l <= sl && sr <= r) {
            return nodes[i];
        } else if(sr < l || r < sl) {
            return e();
        } else {
            int mid = (sl + sr) / 2;
            auto a = query(i * 2 + 1, sl, mid, l, r);
            auto b = query(i * 2 + 2, mid + 1, sr, l, r);
            return op(a, b);
        }
    }

    Node query(int l, int r) {
        return query(0, 0, n - 1, l, r);
    }

    Node get(int i) {
        return query(i, i);
    }
};
```

7.9 $\mathbf{min}_{s}parse_{t}able$

```
using Type = int;

struct min_sparse {

    int log;
    vector<vector<Type>> sparse;

    void init(vector<Type> &nums) {
        int n = nums.size();
        log = 0;
        while (n) log++, n/=2;
        n = nums.size();
        sparse.assign(n, vector<Type>(log, 0));
        for (int i = 0; i < n; i++) sparse[i][0] = nums[i];
        for (int l = 1; l < log; l++) {
            for (int j = 0; j + (1 << l) - 1 < n; j++) {
```

```
            sparse[j][l] = min(sparse[j][l-1], sparse[j+(1 <<
                (l-1))][l-1]);
        }
    }
}

Type query(int x, int y) {
    int n = y - x + 1;
    int logg = -1;
    while (n) logg++, n/=2;
    return min(sparse[x][logg], sparse[y-(1 << logg)+1][logg]);
}
};
```

7.10 struct lazy tree

```
struct lazytree {
    int n;
    vl sum;
    vl lazySum;

    void init(int nn) {
        sum.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        sum.resize(size * 2);
        lazySum.resize(size * 2);
    }

    void update(int i, int sl, int sr, int l, int r, ll diff) {
        if (lazySum[i]) {
            sum[i] += (sr - sl + 1) * lazySum[i];
            if (sl != sr) {
                lazySum[i * 2 + 1] += lazySum[i];
                lazySum[i * 2 + 2] += lazySum[i];
            }
            lazySum[i] = 0;
        }
        if (l <= sl && sr <= r) {
            sum[i] += (sr - sl + 1) * diff;
            if (sl != sr) {
                lazySum[i * 2 + 1] += diff;
                lazySum[i * 2 + 2] += diff;
            }
        } else if (sr < l || r < sl) {
        } else {
            int mid = (sl + sr) >> 1;
            update(i * 2 + 1, sl, mid, l, r, diff);
            update(i * 2 + 2, mid + 1, sr, l, r, diff);
            sum[i] = sum[i * 2 + 1] + sum[i * 2 + 2];
        }
    }

    void update(int l, int r, ll diff) {
        assert(l <= r);
        assert(r < n);
        update(0, 0, n - 1, l, r, diff);
    }

    ll query(int i, int sl, int sr, int l, int r) {
        if (lazySum[i]) {
            sum[i] += lazySum[i] * (sr - sl + 1);
            if (sl != sr) {
                lazySum[i * 2 + 1] += lazySum[i];
                lazySum[i * 2 + 2] += lazySum[i];
            }
            lazySum[i] = 0;
        }
        if (l <= sl && sr <= r) {
            return sum[i];
        } else if (sr < l || r < sl) {
            return 0;
        } else {
            int mid = (sl + sr) >> 1;
            return query(i * 2 + 1, sl, mid, l, r) + query(i * 2 + 2, mid
                + 1, sr, l, r);
        }
    }

    ll query(int l, int r) {
        assert(l <= r);
        assert(r < n);
        return query(0, 0, n - 1, l, r);
    }
};
```

7.11 struct segment tree

```
// Segment Tree for Sum in ranges, also gives you the quantity of numbers
    greater than zero (present numbers)

// segtree tree;
// tree.init(N);
// update values
// uses queries

struct segtree {
    int n;
    vl sum;
    vl present;

    void init(int nn) {
        sum.clear();
        present.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        sum.resize(size * 2);
        present.resize(size * 2);
    }

    void update(int i, int sl, int sr, int pos, ll diff) {
        if (sl <= pos && pos <= sr) {
            if (sl == sr) {
                sum[i] += diff;
                present[i] = sum[i] > 0;
            } else {
                int mid = (sl + sr) / 2;
                update(i * 2 + 1, sl, mid, pos, diff);
                update(i * 2 + 2, mid + 1, sr, pos, diff);
                sum[i] = sum[i * 2 + 1] + sum[i * 2 + 2];
                present[i] = present[i * 2 + 1] + present[i * 2 + 2];
            }
        }
    }

    void update(int pos, ll diff) {
        update(0, 0, n - 1, pos, diff);
    }

    pl query(int i, int sl, int sr, int l, int r) {
        if (l <= sl && sr <= r) {
            return {sum[i], present[i]};
        } else if(sr < l || r < sl) {
            return {0, 0};
        } else {
            int mid = (sl + sr) / 2;
            auto a = query(i * 2 + 1, sl, mid, l, r);
            auto b = query(i * 2 + 2, mid + 1, sr, l, r);
            return {a.F + b.F, a.S + b.S};
        }
    }

    pl query(int l, int r) {
        return query(0, 0, n - 1, l, r);
    }
};
```

7.12 $\text{sum}_{s}parse_{t}able$

8 8. geometry

8.1 area

```
// Glass Area
// p is the height of water
// r2 the small radio of base
// r3 the big radio of water ceil
((p * PI)*(sq(r1) + sq(r2) + r1 * r2))/3
```

8.2 convex-hull

```
// lineal or nlogn
struct pt {
    ll x, y;
```

```
    pt operator - (pt p) { return {x-p.x, y-p.y}; }

    bool operator == (pt b) { return x == b.x && y == b.y; }
    bool operator != (pt b) { return !((*this) == b); }
    bool operator < (const pt &o) const { return y < o.y || (y == o.y &&
        x < o.x); }
};

ll cross(pt a, pt b) { return a.x*b.y - a.y*b.x; } // x = 180 -> sin = 0
ll orient(pt a, pt b, pt c) { return cross(b-a,c-a); }// clockwise = -
ld norm(pt a) { return a.x*a.x + a.y*a.y; }
ld abs(pt a) { return sqrt(norm(a)); }


struct polygon {
    vector<pt> p;
    polygon(int n) : p(n) {}

    void delete_repetead() {
        vector<pt> aux;
        sort(p.begin(), p.end());
        for(pt &i : p)
            if(aux.empty() || aux.back() != i)
              aux.push_back(i);
        p.swap(aux);
    }

    int top = -1, bottom = -1;
    void normalize() { /// polygon is CCW
        bottom = min_element(p.begin(), p.end()) - p.begin();
        vector<pt> tmp(p.begin()+bottom, p.end());
        tmp.insert(tmp.end(), p.begin(), p.begin()+bottom);
        p.swap(tmp);
        bottom = 0;
        top = max_element(p.begin(), p.end()) - p.begin();
    }

    void convex_hull() {
        sort(p.begin(), p.end());
        vector<pt> ch;
        ch.reserve(p.size()+1);
        for(int it = 0; it < 2; it++) {
            int start = ch.size();
            for(auto &a : p) {
                /// if colineal are needed, use < and remove repeated
                    points
                while(ch.size() >= start+2 && orient(ch[ch.size()-2],
                    ch.back(), a) <= 0)
                   ch.pop_back();
                ch.push_back(a);
            }
            ch.pop_back();
            reverse(p.begin(), p.end());
        }
        if(ch.size() == 2 && ch[0] == ch[1]) ch.pop_back();
        /// be careful with CH of size < 3
        p.swap(ch);
    }

    ld perimeter() {
        ld per = 0;
        for(int i = 0, n = p.size(); i < n; i++)
          per += abs(p[i] - p[(i+1)%n]);
        return per;
    }
};
```

8.3 heron formula

```
ld triangle_area(ld a, ld b, ld c) {
    ld s = (a + b + c) / 2;
    return sqrtl(s * (s - a) * (s - b) * (s - c));
}
```

8.4 segment-intersection

```
// LINE they are parallel
// They never be touched because
// other wise provise the point
// The correct name is segment
struct line {
    ld a, b;
    ld x, y;
```

```
    ld m() {
        return (a - x)/(b - y);
    }

    bool horizontal() {
        return b == y;
    }

    bool vertical() {
        return a == x;
    }

    void intersects(line &o) {


        if (horizontal() && o.horizontal()) {
            if (y == o.y) {
                cout << "LINE\n";
            } else {
                cout << "NONE\n";
            }
            return;
        }

        if (vertical() && o.vertical()) {
            if (x == o.x) {
                cout << "LINE\n";
            } else {
                cout << "NONE\n";
            }
            return;
        }

        if (!horizontal() && !o.horizontal()) {
            ld ma = m();
            ld mb = o.m();

            if (ma == mb) {
                ld someY = (o.x - x)/ma + y;
                if (abs(someY - o.y) <= 0.000001) {
                    cout << "LINE\n";
                } else {
                    cout << "NONE\n";
                }
            } else {
                ld xx = (x*mb - o.x*ma + ma*mb*(o.y - y))/(mb - ma);
                ld yy = (xx - x)/ma + y;
                cout << "POINT " << fixed << setprecision(2) << xx << " "
                     << yy << "\n";
            }
        } else {
            if (!horizontal()) {
                ld xx;
                if (x == a) {
                    xx = x;
                } else {
                    xx = (o.y - y)/m() + x;
                }
                ld yy = o.y;
                cout << "POINT "<< fixed << setprecision(2) << xx << " "
                     << yy << "\n";
            } else {
                ld xx;
                if (x == a) {
                    xx = x;
                } else {
                    xx = (y - o.y)/o.m() + o.x;
                }
                ld yy = y;
                cout << "POINT "<< fixed << setprecision(2) << xx << " "
                     << yy << "\n";
            }
        }

    }

};

void test_case() {
    line l[2];
    for (int i = 0; i < 2; i++) {
        ld x, y, a, b;
        cin >> x >> y >> a >> b;
        l[i].a = x;
        l[i].b = y;
        l[i].x = a;
        l[i].y = b;
    }

    l[0].intersects(l[1]);
```

```
}
```

8.5 sin cos law

```
a/senA == b/senB == c/senC

c^2 = a^2 + b^2 - 2abcosC
```

9 9. string

9.1 1 - KMP

```
1. KMP.cpp

struct KMP {
    int kmp(vector<ll> &s, vector<ll> &p) {
        int n = s.size(), m = p.size(), cnt = 0;
        vector<int> pf = prefix_function(p);
        for(int i = 0, j = 0; i < n; i++) {
            while(j && s[i] != p[j]) j = pf[j-1];
            if(s[i] == p[j]) j++;
            if(j == m) {
                cnt++;
                j = pf[j-1];
            }
        }
        return cnt;
    }

    vector<int> prefix_function(vector<ll> &s) {
        int n = s.size();
        vector<int> pf(n);
        pf[0] = 0;
        for (int i = 1, j = 0; i < n; i++) {
            while (j && s[i] != s[j]) j = pf[j-1];
            if (s[i] == s[j]) j++;
            pf[i] = j;
        }
        return pf;
    }
};
```

9.2 Hashing

```
ll pot(ll b, ll e , ll m) {
    ll res = 1;
    while (e > 0) {
        if (e&1) res = res * b % m;
        e >>= 1;
        b = b * b % m;
    }
    return res;
}

struct Hash
{
        int p = 997, m[2], in[2];
        vector<int> h[2], inv[2];
        Hash(string s)
        {
                m[0] = 998244353, m[1] = 1000000009;
                for(int i = 0; i < 2; i++)
                {
                        in[i] = pot(p, m[i]-2, m[i]);
                        h[i].resize(s.size() + 1);
                        inv[i].resize(s.size() + 1);
                        ll acu = 1;
                        h[i][0] = 0, inv[i][0] = 1;
                        for(int j = 0; j < s.size(); j++)
                        {
                                h[i][j + 1] = (h[i][j] + acu * s[j]) % m[i];
                                inv[i][j + 1] = (1ll * inv[i][j] * in[i]) %
                                    m[i];
                                acu = (acu * p) % m[i];
                        }
                }
        }

        // Return the hash of the the substring of 's' from index 'b' to
            'e' inclusive.
        // Note that ABCABC, the hash of 0 to 2 is the same as 3 to 5.
        ll get(int b, int e)
        {
```

```
            e++; // Important to make this inclusive
            ll ha[2];
            for(int i = 0; i < 2; i++)
                ha[i] = ((((h[i][e] - h[i][b]) * (ll)inv[i][b]) %
                    m[i]) + m[i]) % m[i];
            return((ha[0] << 32) | ha[1]) ;
        }
};
```

10 A. util

10.1 PI

```
const ld PI = acos(-1);
```

10.2 custom$_h$ash

```
struct custom_hash {
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            chrono::steady_clock::now().time_since_epoch().count();
        x ^= FIXED_RANDOM;
        return x ^ (x >> 16);
    }
};

struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }

    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
```

10.3 custom$_h$ash$_p$air

```
// Use: unordered_set<pair<ll,ll>, HASH> exists;

struct HASH{
  size_t operator()(const pair<ll,ll>&x)const{
    return hash<ll>()(((ll)x.first)^(((ll)x.second)<<32));
  }
};
```

10.4 exponential$_n$otation

```
// O(n) convert numbers to Exponential Notation
// (e.g 0102.150 -> 1.0215E2)
// only float numbers > 0
string exponential_notation(string s) {
    int firstPos = find_if(all(s), [&](char c) {
        return c != '0' && c != '.';
    }) - s.begin();
    int dotPos = find(all(s), '.') - s.begin();
    ll base = dotPos - (firstPos+(firstPos <= dotPos));
    s.erase(dotPos, 1);
    for (int i = 0; i < 2; i++) { //erase traveling zeros
        while (s.back() == '0') s.pop_back();
        reverse(all(s));
    }
    if (s.size() > 1) s.insert(1, ".");
    if (base != 0) s+= "E" + to_string(base);
    return s;
}
```

10.5 io-int128

```
__int128 read() {
    __int128 x = 0, f = 1;
    char ch = getchar();
    while (ch < '0' || ch > '9') {
```

```
        if (ch == '-') f = -1;
        ch = getchar();
    }
    while (ch >= '0' && ch <= '9') {
        x = x * 10 + ch - '0';
        ch = getchar();
    }
    return x * f;
}
void print(__int128 x) {
    if (x < 0) {
        putchar('-');
        x = -x;
    }
    if (x > 9) print(x / 10);
    putchar(x % 10 + '0');
}

void print(__int128 x) {
    if (x < 0) {
        cout << "-";
        x = -x;
    }
    if (x > 9) print(x / 10);
    cout << char((int)(x % 10) + '0');
}
```

10.6 macros

```
#define MP make_pair
#define MT make_tuple
#define PB push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sortn(x, n) sort((x), (x) + (n));
#define SQ(a) ((a) * (a))
#define max3(a, b, c) max((a), max((b), (c)))
#define max4(a, b, c, d) max(max3(a, b, c), d)
#define min3(a, b, c) min((a), min((b), (c)))
#define min4(a, b, c, d) min(min3(a, b, c), d)
#define fastIO() cin.tie(0); ios::sync_with_stdio(0);

// loops
#define FOR(i, a, b) for (ll (i) = (a); (i) < (b); (i)++)
#define ROF(i, a, b) for (ll (i) = (a); (i) >= (b); (i)--)
#define REP(i, a, b) for (ll (i) = (a); (i) <= (b); (i)++)
#define EACH(a, x) for (auto &(a) : (x))

typedef long long ll;
typedef pair<int, int> pii;
typedef tuple<long long, long long, long long> tiii;
typedef pair<long long, long long> pll;
typedef unsigned long long ull;
typedef long double ld;
typedef vector<int> vi;
typedef vector<bool> vb;
typedef vector<ll> vl;
typedef vector<pll> vpll;
typedef vector<vl> vvl;
typedef vector<vi> vvi;
typedef vector<string> vs;
typedef vector<ld> vld;

template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;
template<class T> using pqg = priority_queue<T>;

const ld DINF=1e100;
const ld EPS = 1e-9;
const ld PI = acos(-1);
const ll infl = INT64_MAX;
const int inf = INT32_MAX;
const int dx[4]{1,0,-1,0}, dy[4]{0,1,0,-1};
const int MOD = 1e9 + 7;
```

10.7 multi$_o$set

```
#include <bits/stdc++.h>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/assoc_container.hpp>

using namespace __gnu_pbds;

struct multiordered_set {
    tree<ll,
```

```
    null_type,
    less_equal<ll>, // this is the trick
    rb_tree_tag,
    tree_order_statistics_node_update> oset;

//this function inserts one more occurrence of (x) into the set.
void insert(ll x) {
    oset.insert(x);
}

//this function checks weather the value (x) exists in the set or not.
bool exists(ll x) {
    auto it = oset.upper_bound(x);
    if (it == oset.end()) {
        return false;
    }
    return *it == x;
}

//this function erases one occurrence of the value (x).
void erase(ll x) {
    if (exists(x)) {
        oset.erase(oset.upper_bound(x));
    }
}

//this function returns the value at the index (idx)..(0 indexing).
ll find_by_order(ll pos) {
    return *(oset.find_by_order(pos));
}

//this function returns the first index of the value (x)..(0
    indexing).
int first_index(ll x) {
    if (!exists(x)) {
        return -1;
    }
    return (oset.order_of_key(x));
}

//this function returns the last index of the value (x)..(0 indexing).
int last_index(ll x) {
    if (!exists(x)) {
        return -1;
    }
    if (find_by_order(size() -1) == x) {
        return size() - 1;
    }
    return first_index(*oset.lower_bound(x)) -1;
}

//this function returns the number of occurrences of the value (x).
int count(ll x) {
    if (!exists(x)) {
        return -1;
    }
    return last_index(x) - first_index(x) + 1;
}

//this function clears all the elements from the set.
void clear() {
    oset.clear();
}

//this function returns the size of the set.
ll size() {
    return (ll)oset.size();
}
};
```

10.8 oset

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

#define oset tree<ll, null_type,less<ll>,
    rb_tree_tag,tree_order_statistics_node_update>
//find_by_order(k) order_of_key(k)
```

10.9 polinomios

```
A(x) = Sum i=0 to n ( a_i * x^i ) y B(x) Sum i=0 to m ( b_i * x^i)

A(x)*B(x) Sum i=0 to (n+m) Sum j=0 to (n+m) (a_j)*(b_i-j))x^i
```

10.10 pragmas

```
//#pragma GCC target("popcnt")
//It's worth noting that after adding __builtin_popcount() is replaced to
    corresponding machine instruction (look at the difference). In my
    test this maked x2 speed up. bitset::count() use __builtin_popcount()
    call in implementation, so it's also affected by this.
#pragma GCC target ("avx2")
#pragma GCC optimization ("O3")
#pragma GCC optimization ("unroll-loops")
#pragma GCC target("popcnt")
#pragma GCC target("avx,avx2,sse3,ssse3,sse4.1,sse4.2,tune=native")
#pragma GCC optimize(3)
#pragma GCC optimize("O3")
#pragma GCC optimize("inline")
#pragma GCC optimize("-fgcse")
#pragma GCC optimize("-fgcse-lm")
#pragma GCC optimize("-fipa-sra")
#pragma GCC optimize("-ftree-pre")
#pragma GCC optimize("-ftree-vrp")
#pragma GCC optimize("-fpeephole2")
#pragma GCC optimize("-fsched-spec")
#pragma GCC optimize("-falign-jumps")
#pragma GCC optimize("-falign-loops")
#pragma GCC optimize("-falign-labels")
#pragma GCC optimize("-fdevirtualize")
#pragma GCC optimize("-fcaller-saves")
#pragma GCC optimize("-fcrossjumping")
#pragma GCC optimize("-fthread-jumps")
#pragma GCC optimize("-freorder-blocks")
#pragma GCC optimize("-fschedule-insns")
#pragma GCC optimize("inline-functions")
#pragma GCC optimize("-ftree-tail-merge")
#pragma GCC optimize("-fschedule-insns2")
#pragma GCC optimize("-fstrict-aliasing")
#pragma GCC optimize("-falign-functions")
#pragma GCC optimize("-fcse-follow-jumps")
#pragma GCC optimize("-fsched-interblock")
#pragma GCC optimize("-fpartial-inlining")
#pragma GCC optimize("no-stack-protector")
#pragma GCC optimize("-freorder-functions")
#pragma GCC optimize("-findirect-inlining")
#pragma GCC optimize("-fhoist-adjacent-loads")
#pragma GCC optimize("-frerun-cse-after-loop")
#pragma GCC optimize("inline-small-functions")
#pragma GCC optimize("-finline-small-functions")
#pragma GCC optimize("-ftree-switch-conversion")
#pragma GCC optimize("-foptimize-sibling-calls")
#pragma GCC optimize("-fexpensive-optimizations")
#pragma GCC optimize("inline-functions-called-once")
#pragma GCC optimize("-fdelete-null-pointer-checks")
```

10.11 priority$_{q}ueue$

```
template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;//
    less
template<class T> using pqg = priority_queue<T>; // greater
```

10.12 random

```
mt19937 mt_rng(chrono::steady_clock::now().time_since_epoch().count());
// also for ll exists mt19937_64
ll randint(ll a, ll b) {
    return uniform_int_distribution<ll>(a, b)(mt_rng);
}
```

10.13 util bultin functions

```
# Sum the values of a iterable
# Very important to put 0ll to avoid overflows
accumulate(v.begin(),v.end(),0ll)/n;
```