Team notebook

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Contents

1 1. Template

1.1 CLIONmain

```
// Practice Every Day :)
#include <bits/stdc++.h>
using namespace std;

#define pb push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sortn(x, n) sort((x), (x) + (n))
#define sq(a) ((a) * (a))
#define MP make_pair

#define each(x, xs) for (auto &x : (xs))
#define rep(i, be, en) for (__typeof(en) i = (be) - ((be) > (en)); i !=
    (en) - ((be) > (en)); i += 1 - 2 * ((be) > (en)))
// old loops
#define FOR(i, a, b) for (int (i) = (a); (i) < (b); (i)++)
#define ROF(i, a, b) for (int (i) = (a); (i) >= (b); (i)--)
#define REP(i, a, b) for (int (i) = (a); (i) <= (b); (i)++)
#define EACH(a, x) for (auto &(a) : (x))

using ll = long long;
using ld = long double;
using pi = pair<int, int>;
using pl = pair<ll, ll>;
using ti = tuple<long long, long long, long long>;
using vi = vector<int>;
using vb = vector<bool>;
using vl = vector<ll>;
using vs = vector<string>;
using vvl = vector<vl>;
using vpl = vector<pl>;
template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;
template<class T> using pqg = priority_queue<T>;

// >>>>>>>>>> debugging >>>>>>>>>>
#ifdef DEBUG_NICO
#include "debug.h"
#define LINE cout << "--------------------" << endl;
```

```
#else
#define deb(x...)
#define LINE
#endif
// <<<<<<<<<< debugging <<<<<<<<<<

void cfgIO() {
#ifdef NICOLAS
    freopen("../input.txt", "r", stdin);
    freopen("../output.txt", "w", stdout);
//    freopen("../error.txt", "w", stderr);
#endif
    ios::sync_with_stdio(0);
    cin.tie(0);
    cout.tie(0);
}
// END DEBUG

void solve();
void init();

int testId = 0;
int main() {
    cfgIO();
    init();
//    int t; cin >> t; while (t--)
//        cout << "Case #" << ++testId << ": ",
    solve(), ++testId;
}
const int N = 1e5 + 10;

void init(){}

void solve() {}
```

1.2 CMakeLists

```
cmake_minimum_required(VERSION 3.22)
project(competitive)

set(CMAKE_CXX_STANDARD 11) # This could different

set(A main.cpp C.cpp) # Add file names here

foreach(X IN LISTS A)
    add_executable("${X}" "${X}")
    target_compile_definitions("${X}" PRIVATE NICOLAS=1) # add ENV_VAR
    target_compile_definitions("${X}" PRIVATE DEBUG_NICO=1)
endforeach()
```

1.3 debug

```
#include <bits/stdc++.h>
using namespace std;

#ifndef DEBUG_H
#define DEBUG_H

void __print(int x)                {cerr << x;}
void __print(long x)               {cerr << x;}
void __print(long long x)          {cerr << x;}
void __print(unsigned x)           {cerr << x;}
void __print(unsigned long x)      {cerr << x;}
void __print(unsigned long long x) {cerr << x;}
void __print(float x)              {cerr << x;}
void __print(double x)             {cerr << x;}
void __print(long double x)        {cerr << x;}
void __print(char x)               {cerr << '\'' << x << '\'';}
void __print(const char *x)        {cerr << '\"' << x << '\"';}
void __print(const string &x)      {cerr << '\"' << x << '\"';}
void __print(bool x)               {cerr << (x ? "true" : "false");}

template<typename T>
void __print(priority_queue<T> xs)
{cerr << "[ "; while (xs.size()) {__print(xs.top()); xs.pop(); cerr << '
    '; }cerr << ']';}

template<typename T, typename V>
void __print(const pair<T, V> &x)
{__print(x.first); cerr << ':'; __print(x.second);}

template<typename T> // for data structures (vector, set, map, etc)
void __print(const T &xs)
{cerr << "[ "; for (auto &x : xs) {__print(x);cerr << ' ';}cerr << ']';}

void _print()
{cerr << "]" << endl;}
```

```
template <typename T, typename... V>
void _print(T t, V... v)
{__print(t); if (sizeof...(v)) cerr << ", "; _print(v...);}

#define deb(x...) cerr << "[" << #x << "] = [", _print(x)

#endif /* DEBUG_H */
```

1.4 vscode-template

```
#include <bits/stdc++.h>
using namespace std;

#define pb push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sq(a) ((a) * (a))

#define each(x, xs) for (auto &x : (xs))
#define rep(i, be, en) for (__typeof(en) i = (be) - ((be) > (en)); i !=
    (en) - ((be) > (en)); i += 1 - 2 * ((be) > (en)))
#define FOR(i, a, b) for (ll (i) = (a); (i) < (b); (i)++)

using ll = long long;
using ld = long double;
using pi = pair<int, int>;
using pl = pair<ll, ll>;
using ti = tuple<long long, long long, long long>;
using vi = vector<int>;
using vb = vector<bool>;
using vl = vector<ll>;
using vs = vector<string>;
using vvl = vector<vl>;
using vpl = vector<pl>;
template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;
template<class T> using pqg = priority_queue<T>;

// >>>>>>>>>> debugging >>>>>>>>>>
// Change this part to local file or put the debug here
#ifndef ONLINE_JUDGE
    #include "/home/fundacion/templates/debug.h"
    #define LINE cerr << "-------------------" << endl;
#else
    #define deb(x...)
    #define LINE
#endif
// <<<<<<<<<< debugging <<<<<<<<<<

void test_case();


const ll INF = INT64_MAX;
const int inf = INT32_MAX;
const ld PI = acos(-1);
const int MOD = 1e9 + 7;
const int DX[4]{1,0,-1,0}, DY[4]{0,1,0,-1};

int testId;
int main() {
    ios::sync_with_stdio(0);
    cin.tie(0);
    cout.tie(0);
    int T;
    T = 1;
    cin >> T;// if one test case, comment this line
    rep (t, 0, T) { testId++; test_case(); }

    return 0;
}

void test_case() {

}
```

2 dp

2.1 Traveling Sales Man

```
// Given directed weighted graph, gets the minimun halmilton cycle.
// Use dfs(0, 1), if 1e9 then it impossible, otherwise get the min.
const int MAX_SIZE = 15;
const ll IMPOSSIBLE = 1e9;
```

```
ll INITIAL = 0; // initial node
vpl adj[MAX_SIZE];
vvl dp(MAX_SIZE, vl(1 << MAX_SIZE, -1));
ll n, m;
ll target; // init as (1 << n) - 1, full visited

ll dfs(ll x, ll mask) {
    if (dp[x][mask] != -1) {
        return dp[x][mask];
    }
    if (mask == target) {
        each(yy, adj[x]) {
            if (yy.F == INITIAL) {
                return yy.S;
            }
        }
        return dp[x][mask] = IMPOSSIBLE;
    }
    ll ans = IMPOSSIBLE;
    each(yy, adj[x]) {
        ll y, d;
        tie(y, d) = yy;
        if ((mask >> y) & 1) continue;
        ll actual = dfs(y, mask | (1 << y)) + d;
        ans = min(ans, actual);
    }
    return dp[x][mask] = ans;
}
```

2.2 coin$_c$hange

```
// infinite number of coins
// Get the minimum number of coins that sum a value.
void test_case() {
    ll n, x;
    cin >> n >> x;
    vl dp(x + 1, inf - 1);
    vl coin(n);
    rep(i, 0, n) cin >> coin[i];
    dp[0] = 0;
    rep(i, 0, x) {
        each(c, coin) {
            if (c + i > x) continue;
            dp[i + c] = min(dp[i + c], dp[i] + 1);
        }
    }
    if (dp[x] + 1== inf) {
        cout << "-1\n";
    } else {
        cout << dp[x] << "\n";
    }
}
```

2.3 edit$_d$istance

```
// editDistance(a, b, a.size(), b.size());

// Cuantas operaciones, (insert, remove, remplazar) necesito
// para que string a y b sean iguales.
int editDistance(string a, string b, int m, int n)
{
    if (m == 0) return n;
    if (n == 0) return m;
    if (a[m - 1] == b[n - 1])
        return editDistance(a, b, m - 1, n - 1);

    return 1 + min({editDistance(a, b, m, n - 1), // Insert
                    editDistance(a, b, m - 1, n), // Remove
                    editDistance(a, b, m - 1, n - 1) // Replace
                });
}

// My own
ll editDistance(string &s, string &t) {
    ll n = s.size();
    ll m = t.size();
    vvl dp(n+1, vl(m+1, 0));
    for (int i = 0; i <= n; i++) {
        for (int j = 0; j <= m; j++) {
            if (min(i, j) == 0) dp[i][j] = max(i, j);
            else if (s[i-1] == t[j-1]) dp[i][j] = dp[i-1][j-1];
            else dp[i][j] = min(dp[i-1][j], min(dp[i][j-1], dp[i-1][j-1]))
                + 1;
        }
    }
    return dp[n][m];
```

```
}
```

2.4 eleverator$_{problem}$

```
// Given n <= 20 persons, print the minimum number of travels
// to move everyone in a elevator with capacity k.

ll n, k;
vl nums;
vector<pair<ll,ll>> dp;

// minimum travels, last travel with minimum weight.
// use f((1 << n) - 1).F
pair<ll,ll> f(ll mask) {
    if (dp[mask] != make_pair(-1ll, -1ll)) {
        return dp[mask];
    }
    if (mask == 0) {
        return dp[mask] = {0, k};
    }
    dp[mask] = {n + 1, 0}; // one person in a travel, or use popcount.
    for (int i = 0; i < n; i++) {
        // person i is the last to enter to elevator.
        if ((mask >> i) & 1) {
            auto actual = f(mask ^ (1 << i)); // best option without this
                last person.
            if (actual.S + nums[i] <= k) {
                actual.S += nums[i];
                // what happened if there are a better minimum.
                // well in that case the last person should be other one.
                // so we are trying all options that last person will be
                    better.
            } else {
                actual.S = nums[i];
                actual.F++;
            }
            dp[mask] = min(dp[mask], actual);
        }
    }
    return dp[mask];
}
```

```
// Iterative
void test_case() {
    ll n, k;
    cin >> n >> k;
    vl nums(n);
    vector<pair<ll,ll>> dp(1 << n, {n+1, 0});
    for (int i =0; i < n; i++) cin >> nums[i];
    dp[0] = {0, k};
    for (int i = 1; i < (1 << n); i++) {
        for (int j = 0; j < n; j++) {
            if (i& (1 << j)) {
                auto actual = dp[i ^ (1 << j)];
                if (actual.S + nums[j] <= k) {
                    actual.S += nums[j];
                } else {
                    actual.F++;
                    actual.S = nums[j];
                }
                dp[i] = min(dp[i], actual);
            }
        }
    }
    cout << dp[(1 << n) -1].F << "\n";
}
```

2.5 lcs

```
const int M_MAX = 20;
const int N_MAX = 20;
int m, n;
string X;
string Y;
int memo[M_MAX + 1][N_MAX + 1];


// Encuetra el Longest Common Subsequence de string X e Y. m y n son sus
    tamaos
// lcs de abfgh aeeeeiiiiigh = agh
int lcs (int m, int n) {
  for (int i = 0; i <= m; i++) {
    for (int j = 0; j <= n; j++) {
      if (i == 0 || j == 0) memo[i][j] = 0;
      else if (X[i - 1] == Y[j - 1]) memo[i][j] = memo[i - 1][j - 1] + 1;
```

```
      else memo[i][j] = max(memo[i - 1][j], memo[i][j - 1]);
    }
  }
  return memo[m][n];
}
```

2.6 lcs3

```
string X = "AGGT12";
string Y = "12TXAYB";
string Z = "12XBA";
bool calc[100][100][100];
int dp[100][100][100];
//lcsOf3(X.size() - 1, Y.size() - 1, Z.size() - 1);
int lcsOf3(int i, int j,int k) {
    if(i==-1||j==-1||k==-1) // outbounds
        return 0;
    if(calc[i][j][k]) //memo
        return dp[i][j][k];
    calc[i][j][k] = true;
    if(X[i]==Y[j] && Y[j]==Z[k]) // same
        return dp[i][j][k] = 1+lcsOf3(i-1,j-1,k-1);
    else // best of reducine any
        return dp[i][j][k] = max(max(lcsOf3(i-1,j,k),
                        lcsOf3(i,j-1,k)),lcsOf3(i,j,k-1));
}
```

2.7 lis

```
// TODO: O(n^2)

// nlog(n)
// 1 2 3 5 10 2 -1 100 500
// 1 2 3 5 10 100 500
int lis(vi& v) {
    if (v.size() == 0) // boundary case
        return 0;

    vi tail(v.size(), 0);
    int length = 1; // always points empty slot in tail

    tail[0] = v[0];

    for (int i = 1; i < v.size(); i++) {

        // Do binary search for the element in
        // the range from begin to begin + length
        auto start = tail.begin(), end = tail.begin() + length;
        auto it = lower_bound(start, end, v[i]);

        // If not present change the tail element to v[i]
        if (it == tail.begin() + length)
            tail[length++] = v[i];
        else
            *it = v[i];
    }

    return length;
}

// My own LIS
int lis(vl &nums) {
    vl best;
    int n = nums.size();
    for (int i = 0; i < n; i++) {
        // For non-decreasing
        // int idx = upper_bound(all(best), nums[i]) - best.begin();

        // For increasing
        int idx = lower_bound(all(best), nums[i]) - best.begin();
        if (idx == best.size()) {
            best.pb(nums[i]);
        } else {
            best[idx] = min(best[idx], nums[i]);
        }
    }

    return best.size();
}

// Also LIS with Segment Tree
```

2.8 $\max_s um_3 d$

```
long long a=20, b=20, c=20;
long long acum[a][b][c];
long long INF = -100000000007;

long long max_range_3D(){
	for(int x=0; x<a; x++){
		for(int y = 0; y<b; y++){
			for(int z = 0; z<c; z++){
				if(x>0) acum[x][y][z] += acum[x-1][y][z];
				if(y>0) acum[x][y][z] += acum[x][y-1][z];
				if(z>0) acum[x][y][z] += acum[x][y][z-1];
				if(x>0 && y>0) acum[x][y][z] -=
				    acum[x-1][y-1][z];
				if(x>0 && z>0) acum[x][y][z] -=
				    acum[x-1][y][z-1];
				if(y>0 && z>0) acum[x][y][z] -=
				    acum[x][y-1][z-1];
				if(x>0 && y>0 && z>0) acum[x][y][z] +=
				    acum[x-1][y-1][z-1];
			}
		}
	}
	long long max_value = INF;
	for(int x=0; x<a; x++){
		for(int y = 0; y<b; y++){
			for(int z = 0; z<c; z++){
				for(int h = x; h<a; h++){
					for(int k = y; k<b; k++){
						for(int l = z; l<c; l++){
							long long aux =
							    acum[h][k][l];
							if(x>0) aux -=
							    acum[x-1][k][l];
							if(y>0) aux -=
							    acum[h][y-1][l];
							if(z>0) aux -=
							    acum[x][k][z-1];
							if(x>0 && y>0) aux +=
							    acum[x-1][y-1][l];
							if(x>0 && z>0) aux +=
							    acum[x-1][k][z-1];
							if(z>0 && y>0) aux +=
							    acum[h][y-1][z-1];
							if(x>0 && y>0 && z>0)
							    aux -=
							    acum[x-1][y-1][z-1];
							max_value =
							    max(max_value,
							    aux);
						}
					}
				}
			}
		}
	}
	return max_value;
}
```

2.9 $\max_s um_a rray$

```
int maxRangeSum(vector<int> a){
	int sum = 0, ans = 0;
	for (int i = 0; i < a.size(); i++){
		if (sum + a[i] >= 0) {
			sum += a[i];
		  ans = max(ans, sum);
		} else sum = 0;
	}
	return ans;
}
```

2.10 $\max_s um_a rray2d$

```
int INF = -100000007; // minimo valor
int n, m; //filas y columnas
const int MAX_N = 105, MAX_M = 105;
int values[MAX_N][MAX_M];

int max_range_sum2D(){
	for(int i=0; i<n;i++){
		for(int j=0; j<m; j++){
			if(i>0) values[i][j] += values[i-1][j];
			if(j>0) values[i][j] += values[i][j-1];
			if(i>0 && j>0) values[i][j] -= values[i-1][j-1];
		}
	}
```

```
        int max_mat = INF;
        for(int i=0; i<n;i++){
                for(int j=0; j<m; j++){
                        for(int h = i; h<n; h++){
                                for(int k = j; k<m; k++){
                                        int sub_mat = values[h][k];
                                        if(i>0) sub_mat -= values[i-1][k];
                                        if(j>0) sub_mat -= values[h][j-1];
                                        if(i>0 && j>0) sub_mat +=
                                            values[i-1][j-1];
                                        max_mat = max(sub_mat, max_mat);
                                }
                        }
                }
        }
        return max_mat;
}
```

3 flows

3.1 Hungarian

```
Halla el mximo match en un grafo bipartito con pesos (min cost) O(V ^ 3)

typedef ll T;
const T inf = 1e18;

struct hung {
    int n, m;
    vector<T> u, v; vector<int> p, way;
    vector<vector<T>> g;

    hung(int n, int m):
        n(n), m(m), g(n+1, vector<T>(m+1, inf-1)),
        u(n+1), v(m+1), p(m+1), way(m+1) {}

    void set(int u, int v, T w) { g[u+1][v+1] = w; }

    T assign() {
        for (int i = 1; i <= n; ++i) {
            int j0 = 0; p[0] = i;
            vector<T> minv(m+1, inf);
            vector<char> used(m+1, false);
            do {
                used[j0] = true;
                int i0 = p[j0], j1; T delta = inf;
                for (int j = 1; j <= m; ++j) if (!used[j]) {
                    T cur = g[i0][j] - u[i0] - v[j];
                    if (cur < minv[j]) minv[j] = cur, way[j] = j0;
                    if (minv[j] < delta) delta = minv[j], j1 = j;
                }
                for (int j = 0; j <= m; ++j)
                    if (used[j]) u[p[j]] += delta, v[j] -= delta;
                    else minv[j] -= delta;
                j0 = j1;
            } while (p[j0]);
            do {
                int j1 = way[j0]; p[j0] = p[j1]; j0 = j1;
            } while (j0);
        }
        return -v[0];
    }
};
```

3.2 MaxFlow

```
// N <= 5000, M <= 30000, C <= 1e9, 300ms

const int INF = INT32_MAX;

struct flowEdge{
    ll to, rev, f, cap;
};


struct max_flow {

    vector<vector<flowEdge>> G;

    max_flow(int n) : G(n) {
        nodes = n;
    }

    // Aade arista (st -> en) con su capacidad
    void addEdge(int st, int en, int cap) {
```

```
    flowEdge A = {en, (int)G[en].size(), 0, cap};
    flowEdge B = {st, (int)G[st].size(), 0, 0};
    G[st].pb(A);
    G[en].pb(B);
}

ll nodes, S, T; // asignar estos valores al armar el grafo G
            // nodes = nodos en red de flujo. Hacer G.clear();
                G.resize(nodes);
vl work, lvl;


bool bfs() {
    int qt = 0;
    queue<ll> q;
    q.push(S);
    lvl.assign(nodes, -1);
    lvl[S] = 0;
    while (q.size()) {
        int v = q.front(); q.pop();
        for (flowEdge &e : G[v]) {
            int u = e.to;
            if (e.cap <= e.f || lvl[u] != -1) continue;
            lvl[u] = lvl[v] + 1;
            q.push(u);
        }
    }
    return lvl[T] != -1;
}

ll dfs(ll v, ll f) {
    if (v == T || f == 0) return f;
    for (ll &i = work[v]; i < G[v].size(); i++) {
        flowEdge &e = G[v][i];
        ll u = e.to;
        if (e.cap <= e.f || lvl[u] != lvl[v] + 1) continue;
        ll df = dfs(u, min(f, e.cap - e.f));
        if (df) {
            e.f += df;
            G[u][e.rev].f -= df;
            return df;
        }
    }
    return 0;
}
```

```
    ll maxFlow(ll s, ll t) {
        S = s;
        T = t;
        ll flow = 0;
        while (bfs()) {
            work.assign(nodes, 0);
            while (true) {
                ll df = dfs(S, INF);
                if (df == 0) break;
                flow += df;
            }
        }
        return flow;
    }
};
```

3.3 $\max_flow$

```
struct Dinitz{
    const int INF = 1e9 + 7;
    Dinitz(){}
    Dinitz(int n, int s, int t) {init(n, s, t);}

    void init(int n, int s, int t)
    {
        S = s, T = t;
        nodes = n;
        G.clear(), G.resize(n);
        Q.resize(n);
    }
    struct flowEdge
    {
        int to, rev, f, cap;
    };

    vector<vector<flowEdge> > G;

    // Aade arista (st -> en) con su capacidad
    void addEdge(int st, int en, int cap) {
        flowEdge A = {en, (int)G[en].size(), 0, cap};
        flowEdge B = {st, (int)G[st].size(), 0, 0};
        G[st].pb(A);
```

```
    G[en].pb(B);
}

int nodes, S, T; // asignar estos valores al armar el grafo G
                 // nodes = nodos en red de flujo. Hacer G.clear();
                     G.resize(nodes);
vi work, lvl;
vi Q;

bool bfs() {
    int qt = 0;
    Q[qt++] = S;
    lvl.assign(nodes, -1);
    lvl[S] = 0;
    for (int qh = 0; qh < qt; qh++) {
        int v = Q[qh];
        for (flowEdge &e : G[v]) {
            int u = e.to;
            if (e.cap <= e.f || lvl[u] != -1) continue;
            lvl[u] = lvl[v] + 1;
            Q[qt++] = u;
        }
    }
    return lvl[T] != -1;
}

int dfs(int v, int f) {
    if (v == T || f == 0) return f;
    for (int &i = work[v]; i < G[v].size(); i++) {
        flowEdge &e = G[v][i];
        int u = e.to;
        if (e.cap <= e.f || lvl[u] != lvl[v] + 1) continue;
        int df = dfs(u, min(f, e.cap - e.f));
        if (df) {
            e.f += df;
            G[u][e.rev].f -= df;
            return df;
        }
    }
    return 0;
}

int maxFlow() {
    int flow = 0;
    while (bfs()) {
        work.assign(nodes, 0);
        while (true) {
            int df = dfs(S, INF);
            if (df == 0) break;
            flow += df;
        }
    }
    return flow;
}
};
```

3.4 $\min_{c}ost_{f}low$

```
// O(min(E^2 V ^2,   EVFLOW  ))
struct CheapDinitz{
    const int INF = 1e9 + 7;

    CheapDinitz() {}
    CheapDinitz(int n, int s, int t) {init(n, s, t);}

    int nodes, S, T;
    vi dist;
    vi pot, curFlow, prevNode, prevEdge, Q, inQue;

    struct flowEdge{
        int to, rev, flow, cap, cost;
    };
    vector<vector<flowEdge>> G;
    void init(int n, int s, int t)
    {
        nodes = n, S = s, T = t;
        curFlow.assign(n, 0), prevNode.assign(n, 0), prevEdge.assign(n, 0);
        Q.assign(n, 0), inQue.assign(n, 0);
        G.clear();
        G.resize(n);
    }

    void addEdge(int s, int t, int cap, int cost)
    {
        flowEdge a = {t, (int)G[t].size(), 0, cap, cost};
        flowEdge b = {s, (int)G[s].size(), 0, 0, -cost};
        G[s].pb(a);
        G[t].pb(b);
```

```
}

void bellmanFord()
{
    pot.assign(nodes, INF);
    pot[S] = 0;
    int qt = 0;
    Q[qt++] = S;
    for (int qh = 0; (qh - qt) % nodes != 0; qh++)
    {
        int u = Q[qh % nodes];
        inQue[u] = 0;
        for (int i = 0; i < (int)G[u].size(); i++)
        {
            flowEdge &e = G[u][i];
            if (e.cap <= e.flow) continue;
            int v = e.to;
            int newDist = pot[u] + e.cost;
            if (pot[v] > newDist)
            {
                pot[v] = newDist;
                if (!inQue[v])
                {
                    Q[qt++ % nodes] = v;
                    inQue[v] = 1;
                }
            }
        }
    }
}

ii MinCostFlow()
{
    bellmanFord();
    int flow = 0;
    int flowCost = 0;
    while (true) // always a good start for an algorithm :v
    {
        set<ii> s;
        s.insert({0, S});
        dist.assign(nodes, INF);
        dist[S] = 0;
        curFlow[S] = INF;
        while (s.size() > 0)
        {
            int u = s.begin() -> s;
            int actDist = s.begin() -> f;
            s.erase(s.begin());
            if (actDist > dist[u]) continue;
            for (int i = 0; i < (int)G[u].size(); i++)
            {
                flowEdge &e = G[u][i];
                int v = e.to;
                if (e.cap <= e.flow) continue;
                int newDist = actDist + e.cost + pot[u] - pot[v];
                if (newDist < dist[v])
                {
                    dist[v] = newDist;
                    s.insert({newDist, v});
                    prevNode[v] = u;
                    prevEdge[v] = i;
                    curFlow[v] = min(curFlow[u], e.cap - e.flow);
                }
            }
        }
        if (dist[T] == INF)
            break;
        for (int i = 0; i < nodes; i++)
            pot[i] += dist[i];
        int df = curFlow[T];
        flow += df;
        for (int v = T; v != S; v = prevNode[v])
        {
            flowEdge &e = G[prevNode[v]][prevEdge[v]];
            e.flow += df;
            G[v][e.rev].flow -= df;
            flowCost += df * e.cost;
        }
    }
    return {flow, flowCost};
}
};
```

4 geometry

4.1 area

```
// Glass Area
// p is the height of water
// r2 the small radio of base
// r3 the big radio of water ceil
((p * PI)*(sq(r1) + sq(r2) + r1 * r2))/3
```

4.2 convex-hull

```
// lineal or nlogn
struct pt {
    ll x, y;

    pt operator - (pt p) { return {x-p.x, y-p.y}; }

    bool operator == (pt b) { return x == b.x && y == b.y; }
    bool operator != (pt b) { return !((*this) == b); }
    bool operator < (const pt &o) const { return y < o.y || (y == o.y &&
        x < o.x); }
};

ll cross(pt a, pt b) { return a.x*b.y - a.y*b.x; } // x = 180 -> sin = 0
ll orient(pt a, pt b, pt c) { return cross(b-a,c-a); }// clockwise = -
ld norm(pt a) { return a.x*a.x + a.y*a.y; }
ld abs(pt a) { return sqrt(norm(a)); }


struct polygon {
    vector<pt> p;
    polygon(int n) : p(n) {}

    void delete_repetead() {
        vector<pt> aux;
        sort(p.begin(), p.end());
        for(pt &i : p)
            if(aux.empty() || aux.back() != i)
              aux.push_back(i);
        p.swap(aux);
    }

    int top = -1, bottom = -1;
    void normalize() { /// polygon is CCW
        bottom = min_element(p.begin(), p.end()) - p.begin();
        vector<pt> tmp(p.begin()+bottom, p.end());
        tmp.insert(tmp.end(), p.begin(), p.begin()+bottom);
        p.swap(tmp);
        bottom = 0;
        top = max_element(p.begin(), p.end()) - p.begin();
    }

    void convex_hull() {
        sort(p.begin(), p.end());
        vector<pt> ch;
        ch.reserve(p.size()+1);
        for(int it = 0; it < 2; it++) {
            int start = ch.size();
            for(auto &a : p) {
                /// if colineal are needed, use < and remove repeated
                    points
                while(ch.size() >= start+2 && orient(ch[ch.size()-2],
                    ch.back(), a) <= 0)
                   ch.pop_back();
                ch.push_back(a);
            }
            ch.pop_back();
            reverse(p.begin(), p.end());
        }
        if(ch.size() == 2 && ch[0] == ch[1]) ch.pop_back();
        /// be careful with CH of size < 3
        p.swap(ch);
    }

    ld perimeter() {
        ld per = 0;
        for(int i = 0, n = p.size(); i < n; i++)
          per += abs(p[i] - p[(i+1)%n]);
        return per;
    }
};
```

4.3 heron formula

```
ld triangle_area(ld a, ld b, ld c) {
    ld s = (a + b + c) / 2;
    return sqrtl(s * (s - a) * (s - b) * (s - c));
}
```

4.4 segment-intersection

```
// LINE they are parallel
// They never be touched because
// other wise provise the point
// The correct name is segment
struct line {
    ld a, b;
    ld x, y;


    ld m() {
        return (a - x)/(b - y);
    }

    bool horizontal() {
        return b == y;
    }

    bool vertical() {
        return a == x;
    }

    void intersects(line &o) {


        if (horizontal() && o.horizontal()) {
            if (y == o.y) {
                cout << "LINE\n";
            } else {
                cout << "NONE\n";
            }
            return;
        }

        if (vertical() && o.vertical()) {
            if (x == o.x) {
                cout << "LINE\n";
            } else {
                cout << "NONE\n";
            }
            return;
        }

        if (!horizontal() && !o.horizontal()) {
            ld ma = m();
            ld mb = o.m();

            if (ma == mb) {
                ld someY = (o.x - x)/ma + y;
                if (abs(someY - o.y) <= 0.000001) {
                    cout << "LINE\n";
                } else {
                    cout << "NONE\n";
                }
            } else {
                ld xx = (x*mb - o.x*ma + ma*mb*(o.y - y))/(mb - ma);
                ld yy = (xx - x)/ma + y;
                cout << "POINT " << fixed << setprecision(2) << xx << " "
                     << yy << "\n";
            }
        } else {
            if (!horizontal()) {
                ld xx;
                if (x == a) {
                    xx = x;
                } else {
                    xx = (o.y - y)/m() + x;
                }
                ld yy = o.y;
                cout << "POINT "<< fixed << setprecision(2) << xx << " "
                     << yy << "\n";
            } else {
                ld xx;
                if (x == a) {
                    xx = x;
                } else {
                    xx = (y - o.y)/o.m() + o.x;
                }
                ld yy = y;
                cout << "POINT "<< fixed << setprecision(2) << xx << " "
                     << yy << "\n";
            }
        }

    }

};

void test_case() {
```

```
    line l[2];
    for (int i = 0; i < 2; i++) {
        ld x, y, a, b;
        cin >> x >> y >> a >> b;
        l[i].a = x;
        l[i].b = y;
        l[i].x = a;
        l[i].y = b;
    }

    l[0].intersects(l[1]);
}
```

4.5 sin cos law

```
a/senA == b/senB == c/senC

c^2 = a^2 + b^2 - 2abcosC
```

5 graph

5.1 1 - DFS

```
const int n = 1e6;
vector<int> adj[n + 1];
bool visited[n + 1];

void dfs(int x) {
        if (visited[x]) return;
        visited[x] = true;
        for (int &a : adj[x]) {
                dfs(x);
        }
}
```

5.2 2 - BFS

```
2. BFS

vector<int> adj[n + 1];
bool visited[n + 1];

void bfs() {
        queue<int> q;
        q.push(0); // initial node
        visited[0] = true;
        while(q.size() > 0) {
                int c = q.front();
                q.pop();
                for (int a : adj[c]) {
                        if (visited[a]) continue;
                        q.push(a);
                        visited[a] = true;
                }
        }
}
```

5.3 3 - Dijkstra

```
3. Dijkstra

const int inf = 1e9;
vector<pair<int, int>> adj[n];
bool processed[n];
ll distance[n];

void dijkstra() {
        priority_queue<pair<int, int>> q;
        for (int i = 0; i < n; i++) {
                distance[i] = inf;
        }
        distance[start] = 0;
        q.push({0, start});
        while (q.size() > 0) {
                int c = q.top().second;
                q.pop();
                if (processed[c]) continue;
                processed[c] = true;
                for (auto& a : adj[c]) {
                        int u = a.first;
                        int w = a.second;
```

```
                        if (distance[c] + w < distance[u]) {
                                distance[u] = distance[c] + w;
                                q.push({-distance[u], u});
                        }
                }
        }
}
```

5.4 4 - BellmanFord

```
4. BellmanFord

const int inf = 1e9;
vector<tuple<int, int, int>> edges;
ll distance[n];


void bellmanFord() {
        for (int i = 0; i < n; i++) {
                distance[i] = inf;
        }
        distance[start] = 0;
        for (int i = 0; i < n - 1; i++) {
                //bool changed = false; add one iteration (i < n) to
                    valide negative cicles
                for (auto& edge : edges) {
                        int a, b, w;
                        tie(a, b, w) = edge;
                        if (distance[a] + w < distance[b]) {
                                distance[b] = distance[a] + w;
                                //changed = true;
                        }
                }
        }
}
```

5.5 5 - Floyd Warshall

```
5. Floyd Warshall

const int inf = 1e9;
vector<pair<int, int>> adj[n];
ll distance[n][n];

void floydWarshall() {
        for (int i = 0; i < n; i++) {
                for (int j = 0; j < n; j++) {
                        distance[i][j] = inf;
                }
        }
        for (int i = 0; i < n; i++) {
                for (auto p : adj[i]) {
                        int b = p.first;
                        int w = p.second;
                        distance[i][b] = w;
                }
        }
        for (int k = 0; k < n; k++) {
                for (int i = 0; i < n; i++) {
                        for (int j = 0; j < n; j++) {
                                distance[i][j] = min(distance[i][j],
                                    distance[i][k] + distance[k][j]);
                        }
                }
        }
}
```

5.6 6 - Euler Path and Cycle

```
6. Euler Path and Cycle

// TODO
```

5.7 7 - Topological Sort

```
7. Topological Sort

stack<int> topo;
vector<int> adj[n + 1];
bool visited[n + 1];

void dfs(int x) {
```

```
        if (visited[x]) return;
        visited[x] = true;
        for (int a : adj[x]) {
                dfs(a);
        }
        topo.push(x);
}
```

5.8 8 - Transitive Closure

```
8. Transitive Closure

const int inf = 1e9;
vector<int> adj[n];
ll distance[n][n];

void floydWarshall() {
        for (int i = 0; i < n; i++) {
                for (int j = 0; j < n; j++) {
                        distance[i][j] = false;
                }
        }
        for (int i = 0; i < n; i++) {
                for (int b : adj[i]) {
                        distance[i][b] = true;
                }
        }
        for (int k = 0; k < n; k++) {
                for (int i = 0; i < n; i++) {
                        for (int j = 0; j < n; j++) {
                                distance[i][j] |= distance[i][k] &
                                    distance[k][j];
                        }
                }
        }
}
```

5.9 9 - Kruskal

```
9. Kruskal

vector<tuple<int, int, int> edges;


void kruskal() {
        ll res = 0;
        sort(edges.begin(), edges.end());// sorted by weight
        for (auto edge : edges) {
                int a, b, w;
                tie(w, a, b) = edge;
                if (find(a) != find(b)) {
                        group(a, b);
                        res += w;
                }
        }
}
```

5.10 A - Union Find

```
10. Union Find

struct union_find {
    vi link;
    vi score;
    vi size;
    int n;
    void init(int nn) {
        link.resize(nn);
        score.resize(nn);
        size.resize(nn);
        this->n = nn;
        for (int i = 0; i < n; i++) {
            link[i] = i;
            score[i] = 0;
            size[i] = 1;
        }
    }
    int find(int x) {
        if (link[x] == x) return x;
        return (link[x] = find(link[x]));
    }
    void group(int a, int b) {
        int pa = find(a);
        int pb = find(b);
```

```
        if (pa != pb) {
            if (score[pa] >= score[pb]) {
                link[pb] = pa;
                size[pa] += size[pb];
                if (score[pa] == score[pb]) score[pa]++;
            } else {
                link[pa] = pb;
                size[pb] += size[pa];
            }
        }
    }
};
```

5.11 B - SCC

Dado un grafo dirigido halla las componentes fuertemente conexas (SCC).

```
const int inf = 1e9;
const int MX = 1e5+5; //Cantidad maxima de nodos
vector<int> g[MX]; //Lista de adyacencia
stack<int> st;
int low[MX], pre[MX], cnt;
int comp[MX]; //Almacena la componente a la que pertenece cada nodo
int SCC; //Cantidad de componentes fuertemente conexas
int n, m; //Cantidad de nodos y aristas

void tarjan(int u) {
    low[u] = pre[u] = cnt++;
    st.push(u);

    for (auto &v : g[u]) {
        if (pre[v] == -1) tarjan(v);
        low[u] = min(low[u], low[v]);
    }
    if (low[u] == pre[u]) {
        while (true) {
            int v = st.top(); st.pop();
            low[v] = inf;
            comp[v] = SCC;
            if (u == v) break;
        }
        SCC++;
    }
}

void init() {
    cnt = SCC = 0;
    for (int i = 0; i <= n; i++) {
        g[i].clear();
        pre[i] = -1; //no visitado
    }
}

// example
void test_case() {
    cin >> n >> m;
    init();
    rep(i, 0, m) {
        int x, y;
        cin >> x >> y;
        g[x].pb(y);
    }
    rep(i, 1, n + 1) {
        if (pre[i] == -1) {
            tarjan(i);
        }
    }
}
```

5.12 C-Cycle$_{D}$*etection*

```
const int N = 1e5 + 10;
vpl adj[N];
int vis[N];
vpl res;
vpl edge;

void dfs(int x) {
    if (vis[x] == 2) return;
    vis[x] = 1;
    each(z, adj[x]) {
        int y, i;
        tie(y, i) = z;
        if (vis[y] == 1) {
            pl a = {-1, -1};
            if (edge[i] == a) {
```

```
                edge[i] = {y, x};
            }
        } else {
            pl a = {-1, -1};
            if (edge[i] == a) {
                edge[i] = {x, y};
            }
        }
        if (vis[y] == 0) dfs(y);
    }
    vis[x] = 2;
}



void test_case() {
    int n, m;
    cin >> n >> m;
    edge = vpl(m);
    rep(i, 0, m) {
        int x, y;
        cin >> x >> y;
        adj[x].pb({y, i});
        adj[y].pb({x, i});
        edge[i] = {-1, -1};
    }
    rep(i, 1, n + 1) {
        dfs(i);
    }
    each(r, edge) {
        cout << r.F << " " << r.S << "\n";
    }
}
```

5.13 Z-Extra-OrStatements2Sat

```
// Return the smaller lexicographic array of size n that satities a_i |
    a_j = z
// a_i | a_i = z is allowed.
// there must exists a solution.
vector<ll> f(ll n, vector<tuple<ll,ll,ll>> &statements) {
    ll m = statements.size();
    vector<vector<pair<ll,ll>>> adj(n + 1);
    const ll bits = 30;
    vector<ll> taken(n+1, (1 << bits) - 1), answer(n+1, (1 << bits) - 1);
    for (int i = 0; i < m; i++) {
        ll x, y, z;
        tie(x, y, z) = statements[i];

        answer[x] &= z;
        answer[y] &= z;
        if (x == y) {
            taken[x] = 0;
            continue;
        }
        taken[x] &= z;
        taken[y] &= z;
        adj[x].pb({y, z});
        adj[y].pb({x, z});
    }
    for (int x = 1; x <= n; x++) {
        for (int i = 0; i < bits; i++) {
            if (!((taken[x] >> i) & 1)) continue;
            ll allHave = true;
            for (auto y : adj[x]) {
                if ((y.S >> i) & 1) {
                    allHave &= ((taken[y.F] >> i) & 1) || ((answer[y.F] >>
                        i) & 1);
                }
            }
            taken[x] -= 1 << i;
            if (allHave) {
                answer[x] -= 1 << i;
                for (auto y : adj[x]) {
                    if ((y.S >> i) & 1) {
                        taken[y.F] |= 1 << i;
                        taken[y.F] ^= 1 << i;
                    }
                }
            }
        }
    }
    answer.erase(answer.begin());
    return answer;
}
```

6 math

6.1 Chinease Remainder

```
ll x, y;
/// O(log(max(a, b)))
ll euclid(ll a, ll b) {
    if(b == 0) { x = 1; y = 0; return a; }
    ll d = euclid(b, a%b);
    ll aux = x;
    x = y;
    y = aux - a/b*y;
    return d;
}

pair<ll, ll> crt(vector<ll> A, vector<ll> M) {
    ll n = A.size(), ans = A[0], lcm = M[0];
    for (int i = 1; i < n; i++) {
        ll d = euclid(lcm, M[i]);
        if ((A[i] - ans) % d) return {-1, -1};
        ll mod = lcm / d * M[i];
        ans = (ans + x * (A[i] - ans) / d % (M[i] / d) * lcm) % mod;
        if (ans < 0) ans += mod;
        lcm = mod;
    }
    return {ans, lcm};
}
```

6.2 Combinatorics

```
// if k == 0 then 1
// if k negative or no enough choices then 0
// O(min(n, n -k)) lineal
ll nck(ll n, ll k) {
    if (k < 0 || n < k) return 0;
    k = min(k, n-k);
    ll ans = 1;
    for (int i = 1; i <= k; i++) {
        ans = ans * (n-i+1) / i;
    }
    return ans;
}
```

6.3 Count$primes$

```
// sprime.count_primes(n);
// O(n^{2/3})
// PI(n) = Count prime numbers until n inclusive

struct count_primers_struct {
    vector<int> primes;
    vector<int> mnprimes;
    ll ans;
    ll y;
    vector<pair<pair<ll, int>, char>> queries;

    ll count_primes(ll n) {
        // this y is actually n/y
        // also no logarithms, welcome to reality, this y is the best for
            n=10^12 or n=10^13
        y = pow(n, 0.64);
        if (n < 100) y = n;

        // linear sieve
        primes.clear();
        mnprimes.assign(y + 1, -1);
        ans = 0;
        for (int i = 2; i <= y; ++i) {
            if (mnprimes[i] == -1) {
                mnprimes[i] = primes.size();
                primes.push_back(i);
            }
            for (int k = 0; k < primes.size(); ++k) {
                int j = primes[k];
                if (i * j > y) break;
                mnprimes[i * j] = k;
                if (i % j == 0) break;
            }
        }
        if (n < 100) return primes.size();
        ll s = n / y;

        for (int p : primes) {
            if (p > s) break;
            ans++;
        }
        // pi(n / y)
        int ssz = ans;
```

```
    // F with two pointers
    int ptr = primes.size() - 1;
    for (int i = ssz; i < primes.size(); ++i) {
        while (ptr >= i && (ll)primes[i] * primes[ptr] > n)
            --ptr;
        if (ptr < i) break;
        ans -= ptr - i + 1;
    }

    // phi, store all queries
    phi(n, ssz - 1);

    sort(queries.begin(), queries.end());
    int ind = 2;
    int sz = primes.size();

    // the order in fenwick will be reversed, because prefix sum in a
        fenwick is just one query
    fenwick fw(sz);
    for (auto qq : queries) {
        auto na = qq.F;
        auto sign = qq.S;
        auto n = na.F;
        auto a = na.S;
        while (ind <= n)
            fw.add(sz - 1 - mnprimes[ind++], 1);
        ans += (fw.ask(sz - a - 2) + 1) * sign;
    }
    queries.clear();
    return ans - 1;
}

void phi(ll n, int a, int sign = 1) {
    if (n == 0) return;
    if (a == -1) {
        ans += n * sign;
        return;
    }
    if (n <= y) {
        queries.emplace_back(make_pair(n, a), sign);
        return;
    }
    phi(n, a - 1, sign);
    phi(n / primes[a], a - 1, -sign);
}

    struct fenwick {
        vector<int> tree;
        int n;

        fenwick(int n = 0) : n(n) {
            tree.assign(n, 0);
        }

        void add(int i, int k) {
            for (; i < n; i = (i | (i + 1)))
                tree[i] += k;
        }

        int ask(int r) {
            int res = 0;
            for (; r >= 0; r = (r & (r + 1)) - 1)
                res += tree[r];
            return res;
        }
    };
} ;

count_primers_struct sprime;
```

6.4 Erdős–Szekeres$_{theorem}$

```
Suppose a,b in N, n=ab+1, and x_1, ..., x_n is a sequence of n real
    numbers. Then this sequence contains a monotonic increasing
    (decreasing) subsequence of a+1 terms or a monotonic decreasing
    (increasing) subsequence of b+1 terms. Dilworth's lemma is a
    generalization of this theorem.
```

6.5 Extended Euclides

```
// It finds X and Y in equation:
// a * X + b * Y = gcd(a, b)

int x, y;
```

```
int euclid(int a, int b) {
       if (b == 0) {
              x = 1;
              y = 0;
              return a;
       }
       int aux = x;
       x = y;
       y = aux - a/b*y;
       return euclid(b, a % b);
}
```

6.6 FFT

```
// FFT multiplies polinomial 'a' and 'b' in nlogn

using cd = complex<long double>;
void fft(vector<cd> & a, bool invert) {
    ll n = a.size();

    for (ll i = 1, j = 0; i < n; i++) {
        ll bit = n >> 1;
        for (; j & bit; bit >>= 1)
            j ^= bit;
        j ^= bit;

        if (i < j)
            swap(a[i], a[j]);
    }

    for (ll len = 2; len <= n; len <<= 1) {
        long double ang = 2 * PI / len * (invert ? -1 : 1);
        cd wlen(cos(ang), sin(ang));
        for (ll i = 0; i < n; i += len) {
            cd w(1);
            for (ll j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
    }
    if (invert) {
        for (cd & x : a)
            x /= n;
    }
}

vector<ll> multiply(vector<ll> const& a, vector<ll> const& b) {
    vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
    ll n = 1;
    while (n < a.size() + b.size())
        n <<= 1;
    fa.resize(n);
    fb.resize(n);

    fft(fa, false);
    fft(fb, false);
    for (ll i = 0; i < n; i++)
        fa[i] *= fb[i];
    fft(fa, true);

    vector<ll> result(n);
    for (ll i = 0; i < n; i++)
        result[i] = round(fa[i].real());
    return result;
}
```

6.7 Floor$_{sum}$

```
// from atcoder
// floor_sum(n,m,a,b) = sum{0}to{n-1} [(a*i+b)/m]
// O(log m), mod 2^64, n<2^32, m<2^32

constexpr long long safe_mod(long long x, long long m) {
    x %= m;
    if (x < 0) x += m;
    return x;
}

unsigned long long floor_sum_unsigned(unsigned long long n,
                                      unsigned long long m,
                                      unsigned long long a,
```

```
                                unsigned long long b) {
    unsigned long long ans = 0;
    while (true) {
        if (a >= m) {
            ans += n * (n - 1) / 2 * (a / m);
            a %= m;
        }
        if (b >= m) {
            ans += n * (b / m);
            b %= m;
        }

        unsigned long long y_max = a * n + b;
        if (y_max < m) break;
        // y_max < m * (n + 1)
        // floor(y_max / m) <= n
        n = (unsigned long long)(y_max / m);
        b = (unsigned long long)(y_max % m);
        swap(m, a);
    }
    return ans;
}

long long floor_sum(long long n, long long m, long long a, long long b) {
    assert(0 <= n && n < (1LL << 32));
    assert(1 <= m && m < (1LL << 32));
    unsigned long long ans = 0;
    if (a < 0) {
        unsigned long long a2 = safe_mod(a, m);
        ans -= 1ULL * n * (n - 1) / 2 * ((a2 - a) / m);
        a = a2;
    }
    if (b < 0) {
        unsigned long long b2 = safe_mod(b, m);
        ans -= 1ULL * n * ((b2 - b) / m);
        b = b2;
    }
    return ans + floor_sum_unsigned(n, m, a, b);
}
```

6.8 Greatest Common Divisor

```
// Alternative: __gcd(a, b);
// O(log(max(a, b)))

ll gcd(ll a, ll b) {
       return b == 0 ? a : gcd(b, a % b);
}
```

6.9 Lowest Common Multiple

```
// O(log(max(a, b)))
int lcm(int a, int b) {
       return a/gcd(a, b) * b;
}
```

6.10 MatrixExponentiation

```
// For Linear recurenses DP in O(log(N)*M^3)

typedef ll T;
const int M = 2;
struct Matrix {
    T a[M][M] = {0};
    Matrix() {}

    Matrix (vector<vector<T>> o) {
        for (int i = 0; i < M; i++)
            for (int j = 0; j < M; j++)
                a[i][j] = o[i][j];
    }

    Matrix operator * (const Matrix &o) {
        Matrix ans;
        for (int i = 0; i < M; i++)
        for (int j = 0; j < M; j++)
        for (int k = 0; k < M; k++)
            ans.a[i][j] += a[i][k] * o.a[k][j]
            //,ans.a[i][j] %= MOD
            ;
        return ans;
    }
};
```

```
Matrix matrixPower(Matrix a, ll power) {
    Matrix ans;
    for (int i = 0; i < M; i++) ans.a[i][i] = 1;

    while (power) {
        if (power & 1) {
            ans = ans * a;
        }

        a = a * a;
        power >>= 1;
    }

    return ans;
}

void test_case() {
    ll n;
    cin >> n;
    Matrix m({
        {1, 1},
        {1, 0}
    });

    auto ans = matrixPower(m, n);
    cout << ans.a[0][1] << "\n";
}
```

6.11 Modular Aritmethics

Modular Aritmethics.cpp

```
ll sum(ll a, ll b) {
    ll c = a + b;
    if (c >= m) c -=m;
    return c;
}

ll sub(ll a, ll b) {
    ll c = a - b;
    if (c < 0) c += m;
    return c;
}

ll mul(__int128 a, __int128 b) {
    return (a * b) % m;
}

ll modexp(ll a, ll n) {
    if (n == 0) return 1;
    ll p = modexp(a, n / 2);
    ll res = mul(p, p);
    if (n & 1) {
        res = mul(res, a);
    }
    return res;
}

// O(sqrt n)
ll phi(ll n) {
    ll ans = n;
    for (int p = 2; p <= n/p; ++p) {
        if (n % p == 0) ans -= ans / p;
        while (n % p == 0) n /= p;
    }
    if (n > 1) ans -= ans / n;
    return ans;
}

ll x, y;
/// O(log(max(a, b)))
ll euclid(ll a, ll b) {
    if(b == 0) { x = 1; y = 0; return a; }
    ll d = euclid(b, a%b);
    ll aux = x;
    x = y;
    y = aux - a/b*y;
    return d;
}

ll invmod(ll a) {
    ll d = euclid(a, m);
    if (d > 1) return -1;
    return (x % m + m) % m;
}

ll divv(ll a, ll b) {
```

```
    ll inv = invmod(b);
    if (inv == -1) return -1;
    ll res = mul(a, inv);
    return res;
}


// a * (b^{euler(m) - 1})
// for primes: a * b ^ (P - 2)
ll divv2(ll a, ll b) {
    if (__gcd(b, m) != 1) return -1;
    ll ex = modexp(b, euler - 1);
    ll res = mul(a, ex);
    return res;
}
```

6.12 Modular Combinatorics

```
// NCK nck(maxN, primeMod)
// ^nC_k How many ways you can choose k items from an array of n items.

struct NCK {
    ll MAX_N;
    ll MOD;
    vl fact;

    explicit NCK(ll maxN, ll mod) : MAX_N(maxN), MOD(mod) {
        fact.resize(MAX_N + 1, 1);
        fact[0] = 1;
        REP(i, 1, MAX_N) {
            fact[i] = fact[i - 1] * (i % MOD);
            fact[i] %= MOD;
        }
    }

    ll inv(ll a){
        return powmod(a, MOD-2); // MOD is prime, otherwise use powmod(a,
            eulerPhi(mod) - 1)
    }

    ll powmod(ll a, ll b){
        if (b == 0) return 1;
        ll mid = powmod(a, b / 2);
        ll ans = (mid * mid) % MOD;
        if (b & 1) {
            ans *= a;
            ans %= MOD;
        }
        return ans;
    }

    ll nCk(ll n, ll k){
        ll nOverK = (fact[n] * inv(fact[k])) % MOD;
        return (nOverK * inv(fact[n-k])) % MOD;
    }
};
```

6.13 Ternary Search

```
// this is for find minimum point in a parabolic
// O(log3(n))
ll left = 0;
ll right = n - 1;
while (left + 3 < right) {
    ll mid1 = left + (right - left) / 3;
    ll mid2 = right - (right - left) / 3;
    if (f(b, lines[mid1]) <= f(b, lines[mid2])) {
        right = mid2;
    } else {
        left = mid1;
    }
}
ll target = -4 * a * c;
ll ans = -1; // find the answer, in this case any works.
for (ll mid = left; mid <= right; mid++) {
    if (f(b, lines[mid]) + target < 0) {
        ans = mid;
    }
}
```

6.14 catalan

```
static int MAX = 30;
static long catalan[] = new long[MAX+1];
```

```
static void catalanNumbers(){
       catalan[0] = 1;
       for(int i = 1; i <= MAX; i++){
              catalan[i] = (long)(catalan[i-1]*((double)(2*((2 * i)-
                  1))/(i + 1)));
       }
}
```

6.15 factorization

```
// Polar rho, miller rabin
// O(log^3(n))
// But I get TLE once in 1e7
ll expmod(ll b, ll e, ll m) {
    ll ans = 1;
    while (e) {
        if (e&1) ans = (1ll*ans*b) % m;
        b = (1ll*b*b) % m;
        e /= 2;
    }
    return ans;
}

ll mulmod(ll a, ll b, ll m) {
    ll r = a*b-(ll)((long double)a*b/m+.5)*m;
    return r < 0 ? r+m : r;
}

/// O(log^3(n))
bool test(ll n, int a) {
    if (n == a) return true;
    ll s = 0, d = n-1;
    while (d%2 == 0) s++, d /= 2;
    ll x = expmod(a, d, n);
    if (x == 1 || x+1 == n) return true;
    for (int i = 0; i < s-1; i++) {
        x = mulmod(x, x, n);
        if (x == 1) return false;
        if (x+1 == n) return true;
    }
    return false;
}

ll gcd(ll a, ll b) { return a ? gcd(b%a, a) : b; }

ll rho(ll n) {
    if (!(n&1)) return 2;
    ll x = 2, y = 2, d = 1;
    ll c = rand() % n + 1;
    while (d == 1) {
        x = (mulmod(x, x, n) + c) % n;
        y = (mulmod(y, y, n) + c) % n;
        y = (mulmod(y, y, n) + c) % n;
        d = gcd(abs(x-y), n);
    }
    return d == n ? rho(n) : d;
}

bool is_prime(ll n) {
    if (n == 1) return false;
    int ar[] = {2,3,5,7,11,13,17,19,23};
    for (auto &p : ar) if (!test(n, p)) return false;
    return true;
}

/// O(log(n)^3) aprox
void fact(ll n, map<ll, int> &f) {
    if (n == 1) return;
    if (is_prime(n)) { f[n]++; return; }
    ll q = rho(n);
    fact(q, f); fact(n/q, f);
}

// ###########################################################
// Normal algorithm with precomputing primes
// O(sqrt(MAX_N)/log(sqrt(MAX_N)), it worked for 1e9 for me
const ll MAX_N = 1e7;
vl primes;
void init() {
    ll N = sqrt(MAX_N) + 1;
    vector<bool> sieve(N + 1);
    for (ll i = 2; i <= N; i++) {
        if (!sieve[i]) {
            for (ll j = i*i; j <= N; j+=i) {
                sieve[j] = true;
            }
        }
```

```
    }
    for (ll i = 2; i <= N; i++) {
        if (!sieve[i]) primes.pb(i);
    }
}

vl fact(ll n) {
    vl ans;
    ll rest = n;
    for (auto &p : primes) {
        if (p * p > n) break;
        if (rest % p == 0) {
            ans.pb(p);
            while (rest % p == 0) rest/=p;
        }
    }
    if (rest != 1) {
        ans.pb(rest);
    }
    return ans;
}

// ###################################################
// Modification of sieve erathostenes
// From CF Faster than previous, but needs more memory
const int N = int(1e7) + 5;
int mind[N];
void init() {
    for (int i = 0; i < N; i++)
                mind[i] = i;

        for (int p = 2; p < N; p++) {
                if (mind[p] != p)
                        continue;
                for (int d = 2 * p; d < N; d += p)
                        mind[d] = min(mind[d], p);
        }
}

vector<int> getPrimes(int v) {
        vector<int> ps;
        while (v > 1) {
                if (ps.empty() || ps.back() != mind[v])
                        ps.push_back(mind[v]);
                v /= mind[v];
        }
        return ps;
}
```

6.16 fermat

```
// ll fermatFactors(ll n) {
//     ll a = ceil(sqrt(n)) ;
//     if(a * a == n){
//         return a;
//     }
//     ll b;
//     while(true) {
//         ll b1 = a * a - n ;
//         b = (ll)sqrt(b1) ;

//         if(b * b == b1)
//             break;
//         else
//             a += 1;
//     }
//     return min(a - b, a + b);
// }
```

6.17 primes

```
// O(sqrt(n))
bool isPrime(int x) {
    for (int d = 2; d * d <= x; d++) {
        if (x % d == 0)
            return false;
    }
    return true;
}

// O(nloglogn)
// sieve[X] == 0 if it is prime
int const N = 1e6;
bool sieve[N + 1];
vector<int> primes;
```

```
void calculate() {
    for (int p = 2; p <= N; p++) {
        if (sieve[p]) continue;
        primes.PB(p);
        for (ll i = 1ll*p*p; i <= N; i += p)
            sieve[i] = true;
    }
}


// For 64-bit integers
// O((ln n)^2)
// 32 bits bases: 2, 3, 5, 7.
// 64 bits bases: 2 ... 37

using u64 = uint64_t;
using u128 = __uint128_t;

u64 binpower(u64 base, u64 e, u64 mod) {
    u64 result = 1;
    base %= mod;
    while (e) {
        if (e & 1)
            result = (u128)result * base % mod;
        base = (u128)base * base % mod;
        e >>= 1;
    }
    return result;
}

bool check_composite(u64 n, u64 a, u64 d, int s) {
    u64 x = binpower(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (int r = 1; r < s; r++) {
        x = (u128)x * x % n;
        if (x == n - 1)
            return false;
    }
    return true;
}

bool MillerRabin(u64 n) {
    if (n < 2)
        return false;
    int r = 0;
    u64 d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        r++;
    }

    for (int a : {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}) {
        if (n == a)
            return true;
        if (check_composite(n, a, d, r))
            return false;
    }
    return true;
}
```

7 query

7.1 1 - Segment Tree

```
1. Segment Tree

const int N = 1e6 + 1;

int tree[N * 4 + 4];
int nums[N + 1];

void build(int i, int l, int r) {
        if (l == r) {
                tree[i] = nums[r];
        } else {
                int mid = (l + r) / 2;
                build(i * 2 + 1, l, mid);
                build(i * 2 + 2, mid + 1, r);
                tree[i] = tree[i * 2 + 1] + tree[i * 2 + 2];
                // tree[i] = compare(tree[i * 2 + 1], tree[i * 2 + 2]);
        }
}

void update(int i, int l, int r, int pos, int diff) {
        if (l <= pos && pos <= r) {
```

```
            if (l == r) { // leaf
                tree[i] += diff;
            } else { // node
                int mid = (l + r) / 2;
                update(i * 2 + 1, l, mid, pos, diff);
                updaet(i * 2 + 2, mid + 1, r, pos, diff);
                tree[i] = tree[i * 2 + 1] + tree[i * 2 + 2];
                // tree[i] = compare(...)
            }
        }
}

int query(int i, int sl, int sr, int l, int r) {
        if (l <= sl && sr <= r) { // overlap
            return tree[i];
        } else if (sr < l || r < sl) { // no overlap
            return 0;
        } else { // partially over lap
            int mid = (sl + sr) / 2;
            return query(i * 2 + 1, sl, mid, l, r) + query(i * 2 + 2,
                mid + 1, sr, l, r);
            // return compare(a, b);
        }
}
```

7.2 Merge$_S$ort$_T$ree

```
// usage
// vector<node*> nodes;
// tree.query(l, r, nodes);

// returns log(n) sorted segments in a range (l, r)

struct node {
    ll l, r;
    vl nums;
    vl prefix;
};

struct segtree {
    int n;
    vector<node> tree;
    void init(int nn, vl& nodes) {
        tree.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        tree.resize(size * 2);
        build(0, 0, n - 1, nodes);
    }


    void query(ll i, ll sl, ll sr, ll l, ll r, vector<node*> &ans) {
        if (l <= sl && sr <= r) {
            ans.pb(&tree[i]);
        } else if (sr < l || r < sl) {

        } else {
            int mid = (sl + sr) >> 1;
            query(i * 2 + 1, sl, mid, l, r, ans);
            query(i * 2 + 2, mid + 1, sr, l, r, ans);
        }
    }

    void query(ll l, ll r, vector<node*> &ans) {
        return query(0, 0, n - 1, l, r, ans);
    }

    void build(int nodei, int l, int r, vl &nums) {
        if (l == r) {
            tree[nodei].nums = { nums[l] };
            tree[nodei].prefix = {nums[l]};
            tree[nodei].l = l;
            tree[nodei].r = r;
        } else {
            ll mid = (l + r) >> 1;
            build(nodei * 2 + 1, l, mid, nums);
            build(nodei * 2 + 2, mid + 1, r, nums);
            ll a = tree[nodei*2+1].nums.size();
            ll b = tree[nodei*2+2].nums.size();
            tree[nodei].nums.reserve(a + b);
            tree[nodei].prefix.resize(a+b);
            ll i = 0;
            ll j = 0;
            while (i < a && j < b) {
                ll simon = tree[nodei*2+1].nums[i];
```

```
            ll simon2 = tree[nodei*2+2].nums[j];
            if (simon <= simon2) {
                tree[nodei].nums.pb(simon);
                i++;
            } else {
                tree[nodei].nums.pb(simon2);
                j++;
            }
        }
        while (i < a) {
            tree[nodei].nums.pb(tree[nodei*2+1].nums[i]);
            i++;
        }
        while (j < b) {
            tree[nodei].nums.pb(tree[nodei*2+2].nums[j]);
            j++;
        }
        tree[nodei].prefix[0] = tree[nodei].nums[0];
        for (int i = 1; i < a + b; i++) {
            tree[nodei].prefix[i] = tree[nodei].prefix[i - 1] +
                tree[nodei].nums[i];
        }
        tree[nodei].l = l;
        tree[nodei].r = r;
    }
  }
};
```

7.3 Min Segment Tree

```
// Max segment tree
struct segtree {
    int n;
    vl tree;

    void init(int nn) {
        tree.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        tree.resize(size * 2);
    }

    void update(int i, int sl, int sr, int pos, ll diff) {
        if (sl <= pos && pos <= sr) {
            if (sl == sr) {
                tree[i] += diff;
            } else {
                int mid = (sl + sr) / 2;
                update(i * 2 + 1, sl, mid, pos, diff);
                update(i * 2 + 2, mid + 1, sr, pos, diff);
                tree[i] = max(tree[i * 2 + 1], tree[i * 2 + 2]);
            }
        }
    }

    void update(int pos, ll diff) {
        update(0, 0, n - 1, pos, diff);
    }

    ll query(int i, int sl, int sr, int l, int r) {
        if (l <= sl && sr <= r) {
            return tree[i];
        } else if(sr < l || r < sl) {
            return INT64_MIN;
        } else {
            int mid = (sl + sr) / 2;
            auto a = query(i * 2 + 1, sl, mid, l, r);
            auto b = query(i * 2 + 2, mid + 1, sr, l, r);
            return max(a, b);
        }
    }

    ll query(int l, int r) {
        return query(0, 0, n - 1, l, r);
    }
};
```

7.4 Mo's

```
const int BLOCK_SIZE = 430; // 1e5=310 2e5=430

struct query {
    int l, r, idx;
```

```
    bool operator <(query &other) const {
        return MP(l / BLOCK_SIZE, r) < MP(other.l / BLOCK_SIZE, other.r);
    }
};


void add(int idx);
void remove(int idx);
ll getAnswer();

vector<ll> mo(vector<query> queries) {
    vector<ll> answers(queries.size());
    int l = 0;
    int r = -1;
    sort(all(queries));
    EACH(q, queries) {
        while (q.l < l) add(--l);
        while (r < q.r) add(++r);
        while (l < q.l) remove(l++);
        while (q.r < r) remove(r--);
        answers[q.idx] = getAnswer();
    }
    return answers;
}

vl nums; //init
ll ans = 0;
int cnt[1000001];
void add(int idx) {}
void remove(int idx) {}
ll getAnswer() {
    return ans;
}
```

7.5 SegTree Max Sum sub arrays

```
// Segmentree to calculate the maximum sum of all possible sub arrays.
// assing value is the initial default value
// set the values with modif
// get the answer with tree.query(0, n - 1).val

struct DynamicMaxSubarraySum {
    struct node {
        ll pref, suf, val, sum;
    };
    int N;
    ll neutral;
    vector<node> t;
    DynamicMaxSubarraySum(int _N, ll assign_value) {
        neutral = assign_value;
        N = _N;
        t.resize(4 * N);
        FOR(i, 0, 4 * N) t[i] = {0, 0, 0, 0};
        build(1, 0, N - 1);
    }
    void build(int i, int l, int r) {
        if(l == r) {
            t[i].pref = t[i].suf = t[i].val = t[i].sum = neutral;
            return;
        }
        int mid = (l + r) >> 1;
        build(2 * i, l, mid);
        build(2 * i + 1, mid + 1, r);
        t[i] = merge(t[2 * i], t[2 * i + 1]);
    }
    node merge(node a, node b) {
        node c;
        c.pref = max(a.pref, a.sum + b.pref);
        c.suf = max(b.suf, b.sum + a.suf);
        c.val = max({a.val, b.val, a.suf + b.pref});
        c.sum = a.sum + b.sum;
        return c;
    }

    void modif(int i, int l, int r, int pos, ll val) {
        if(l > pos || r < pos) return;
        if(l == pos && r == pos) {
            t[i].pref = t[i].suf = t[i].val = t[i].sum = val;
            return;
        }
        int mid = (l + r) >> 1;
        modif(2 * i, l, mid, pos, val);
        modif(2 * i + 1, mid + 1, r, pos, val);
        t[i] = merge(t[2 * i], t[2 * i + 1]);
    }
    node query(int i, int l, int r, int tl, int tr) {
        if(l > tr || r < tl) return {0, 0, 0, 0};
```

```
        if(l >= tl && r <= tr) return t[i];
        int mid = (l + r) >> 1;
        return merge(query(2 * i, l, mid, tl, tr), query(2 * i + 1, mid +
            1, r, tl, tr));
    }

    void modif(int pos, ll val) {
        modif(1, 0, N - 1, pos, val);
    }
    node query(int l, int r) {
        return query(1, 0, N - 1, l, r);
    }
    node query(int pos) {
        return query(1, 0, N - 1, pos, pos);
    }
};
```

7.6 fenwicktree

```
struct FenwickTree {
    vector<int> bit;
    int n;

    FenwickTree(int n) {
        this->n = n;
        bit.assign(n, 0);
    }

    FenwickTree(vector<int> a) : FenwickTree(a.size()) {
        for (size_t i = 0; i < a.size(); i++)
            add(i, a[i]);
    }

    int sum(int r) {
        int ret = 0;
        for (; r >= 0; r = (r & (r + 1)) - 1)
            ret += bit[r];
        return ret;
    }

    int sum(int l, int r) {
        return sum(r) - sum(l - 1);
    }

    void add(int idx, int delta) {
        for (; idx < n; idx = idx | (idx + 1))
            bit[idx] += delta;
    }
};
```

7.7 $\min_{s}parse_{t}able$

```
using Type = int;

struct min_sparse {

    int log;
    vector<vector<Type>> sparse;

    void init(vector<Type> &nums) {
        int n = nums.size();
        log = 0;
        while (n) log++, n/=2;
        n = nums.size();
        sparse.assign(n, vector<Type>(log, 0));
        for (int i = 0; i < n; i++) sparse[i][0] = nums[i];
        for (int l = 1; l < log; l++) {
            for (int j = 0; j + (1 << l) - 1 < n; j++) {
                sparse[j][l] = min(sparse[j][l-1], sparse[j+(1 <<
                    (l-1))][l-1]);
            }
        }
    }

    Type query(int x, int y) {
        int n = y - x + 1;
        int logg = -1;
        while (n) logg++, n/=2;
        return min(sparse[x][logg], sparse[y-(1 << logg)+1][logg]);
    }
};
```

7.8 struct lazy tree

```
struct lazytree {
    int n;
    vl sum;
    vl lazySum;

    void init(int nn) {
        sum.clear();
        n = nn;
        int size = 1;
        while (size < n) {
            size *= 2;
        }
        sum.resize(size * 2);
        lazySum.resize(size * 2);
    }

    void update(int i, int sl, int sr, int l, int r, ll diff) {
        if (lazySum[i]) {
            sum[i] += (sr - sl + 1) * lazySum[i];
            if (sl != sr) {
                lazySum[i * 2 + 1] += lazySum[i];
                lazySum[i * 2 + 2] += lazySum[i];
            }
            lazySum[i] = 0;
        }
        if (l <= sl && sr <= r) {
            sum[i] += (sr - sl + 1) * diff;
            if (sl != sr) {
                lazySum[i * 2 + 1] += diff;
                lazySum[i * 2 + 2] += diff;
            }
        } else if (sr < l || r < sl) {
        } else {
            int mid = (sl + sr) >> 1;
            update(i * 2 + 1, sl, mid, l, r, diff);
            update(i * 2 + 2, mid + 1, sr, l, r, diff);
            sum[i] = sum[i * 2 + 1] + sum[i * 2 + 2];
        }
    }

    void update(int l, int r, ll diff) {
        assert(l <= r);
        assert(r < n);
        update(0, 0, n - 1, l, r, diff);
    }

    ll query(int i, int sl, int sr, int l, int r) {
        if (lazySum[i]) {
            sum[i] += lazySum[i] * (sr - sl + 1);
            if (sl != sr) {
                lazySum[i * 2 + 1] += lazySum[i];
                lazySum[i * 2 + 2] += lazySum[i];
            }
            lazySum[i] = 0;
        }
        if (l <= sl && sr <= r) {
            return sum[i];
        } else if (sr < l || r < sl) {
            return 0;
        } else {
            int mid = (sl + sr) >> 1;
            return query(i * 2 + 1, sl, mid, l, r) + query(i * 2 + 2, mid
                + 1, sr, l, r);
        }
    }

    ll query(int l, int r) {
        assert(l <= r);
        assert(r < n);
        return query(0, 0, n - 1, l, r);
    }
};
```

7.9 struct segment tree

```
// Segment Tree for Sum in ranges, also gives you the quantity of numbers
    greater than zero (present numbers)

// segtree tree;
// tree.init(N);
// update values
// uses queries

struct segtree {
    int n;
    vl sum;
    vl present;
```

```
void init(int nn) {
    sum.clear();
    present.clear();
    n = nn;
    int size = 1;
    while (size < n) {
        size *= 2;
    }
    sum.resize(size * 2);
    present.resize(size * 2);
}

void update(int i, int sl, int sr, int pos, ll diff) {
    if (sl <= pos && pos <= sr) {
        if (sl == sr) {
            sum[i] += diff;
            present[i] = sum[i] > 0;
        } else {
            int mid = (sl + sr) / 2;
            update(i * 2 + 1, sl, mid, pos, diff);
            update(i * 2 + 2, mid + 1, sr, pos, diff);
            sum[i] = sum[i * 2 + 1] + sum[i * 2 + 2];
            present[i] = present[i * 2 + 1] + present[i * 2 + 2];
        }
    }
}

void update(int pos, ll diff) {
    update(0, 0, n - 1, pos, diff);
}

pl query(int i, int sl, int sr, int l, int r) {
    if (l <= sl && sr <= r) {
        return {sum[i], present[i]};
    } else if(sr < l || r < sl) {
        return {0, 0};
    } else {
        int mid = (sl + sr) / 2;
        auto a = query(i * 2 + 1, sl, mid, l, r);
        auto b = query(i * 2 + 2, mid + 1, sr, l, r);
        return {a.F + b.F, a.S + b.S};
    }
}

pl query(int l, int r) {
    return query(0, 0, n - 1, l, r);
}
};
```

7.10 $\text{sum}_s parse_t able$

8 string

8.1 1 - KMP

1. KMP.cpp

```
struct KMP {
    int kmp(vector<ll> &s, vector<ll> &p) {
        int n = s.size(), m = p.size(), cnt = 0;
        vector<int> pf = prefix_function(p);
        for(int i = 0, j = 0; i < n; i++) {
            while(j && s[i] != p[j]) j = pf[j-1];
            if(s[i] == p[j]) j++;
            if(j == m) {
                cnt++;
                j = pf[j-1];
            }
        }
        return cnt;
    }

    vector<int> prefix_function(vector<ll> &s) {
        int n = s.size();
        vector<int> pf(n);
        pf[0] = 0;
        for (int i = 1, j = 0; i < n; i++) {
            while (j && s[i] != s[j]) j = pf[j-1];
            if (s[i] == s[j]) j++;
            pf[i] = j;
        }
        return pf;
    }
};
```

8.2 Hashing

```
ll pot(ll b, ll e , ll m) {
    ll res = 1;
    while (e > 0) {
        if (e&1) res = res * b % m;
        e >>= 1;
        b = b * b % m;
    }
    return res;
}

struct Hash
{
        int p = 997, m[2], in[2];
        vector<int> h[2], inv[2];
        Hash(string s)
        {
                m[0] = 998244353, m[1] = 1000000009;
                for(int i = 0; i < 2; i++)
                {
                        in[i] = pot(p, m[i]-2, m[i]);
                        h[i].resize(s.size() + 1);
                        inv[i].resize(s.size() + 1);
                        ll acu = 1;
                        h[i][0] = 0, inv[i][0] = 1;
                        for(int j = 0; j < s.size(); j++)
                        {
                                h[i][j + 1] = (h[i][j] + acu * s[j]) % m[i];
                                inv[i][j + 1] = (1ll * inv[i][j] * in[i]) %
                                    m[i];
                                acu = (acu * p) % m[i];
                        }
                }
        }

        // Return the hash of the the substring of 's' from index 'b' to
            'e' inclusive.
        // Note that ABCABC, the hash of 0 to 2 is the same as 3 to 5.
        ll get(int b, int e)
        {
                e++; // Important to make this inclusive
                ll ha[2];
                for(int i = 0; i < 2; i++)
                        ha[i] = ((((h[i][e] - h[i][b]) * (ll)inv[i][b]) %
                            m[i]) + m[i]) % m[i];
                return((ha[0] << 32) | ha[1]) ;
        }
};
```

9 tree

9.1 1 K-th Parent

```
1. K-th Parent.cpp

class TreeAncestor {
    int LOG = 20;
    int up[50000][20];
public:
    TreeAncestor(int n, vector<int>& parent) {
        memset(up, -1, 50000 * LOG * 4);
        for (int i = 0; i < n; i++) {
            up[i][0] = parent[i];
        }
        for (int k = 1; k < LOG; k++) {
            for (int i = 0; i < n; i++) {
                if (up[i][k-1] != -1)
                    up[i][k] = up[up[i][k-1]][k-1];
            }
        }
    }

    int getKthAncestor(int node, int k) {
        for (int i = 0; i < LOG; i++) {
            if (k & 1<<i) {
                node = up[node][i];
            }
            if (node == -1) return -1;
        }
        return node;
    }
};
```

9.2 Nearest$_S$elected$_N$odes$_P$roblem

```
// Given an order of selected nodes in a tree, you should print the
    miminum distance between two selected nodes after each operation.

// O(nlogn or n*sqrt(n)); n <= 2*10^5, 2.7 seconds.
// adj is the adjacency list, order is the selected nodes in order
// n is the numeber of nodes, returns the minimum after each operation
// note that operation 0 answer is 1e9
vl f(vvl &adj, vl &order, ll n) {
    vl answer;
    vl dist(n + 1, 1e9);
    ll best = 1e9;
    vl q(n + 1);
    ll sz = 0;
    for (int i = 0; i < n; i++) {
        best = min(best, dist[order[i]]);
        sz = 0;
        dist[order[i]] = 0;
        q[sz++] = order[i];
        ll idx = 0;
        while (idx < sz) {
            ll x = q[idx++];
            if (dist[x] + 1 >= best) break;
            for (auto &y : adj[x]) {
                if (dist[x] + 1 < dist[y]) {
                    dist[y] = dist[x] + 1;
                    q[sz++] = y;
                }
            }
        }
        answer.pb(best);
    }
    return answer;
}
```

9.3 Two$_P$ieces$_o$n$_T$ree

```
// In a tree with 'n' nodes where 2 pieces starting from root 1
// must go to certain nodes each one and must not exceed 'd' between
// the two pieces, after they have to return to root 1
// two_pieces_on_tree() find the minimum quantity of moves
// My submittion in CF:
    https://codeforces.com/contest/1774/submission/189071201

ll n, d; // quantity of nodes, maximum distance between pieces
vvl children; // tree
vector<int> a, b; // nodes that must visit first and second piecesS

void dfs(ll x, vl &route) {
    route.pb(x);
    ll kParent = 1; //route
    if (route.size() - 1 >= d) {
        kParent = route[route.size() - 1 - d];
    }
    b[kParent] |= a[x];
    a[kParent] |= b[x];
    each(y, children[x]) {
        dfs(y, route);
        a[x] |= a[y];
        b[x] |= b[y];
    }
    route.pop_back();
}

ll two_pieces_on_tree() {
    ll root = 1;
    vl emptyRoute = vl();
    dfs(root, emptyRoute);
    ll total = 0;
    for (int i = 1; i <= n; i++) {
        total += a[i] + b[i];
    }
    return total * 2 - 4;
}
```

9.4 lca

```
#include<bits/stdc++.h>
//#include<cmath>
//#include<bitset>

using namespace std;

#define MP make_pair
```

```cpp
#define MT make_tuple
#define PB push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sortn(x, n) sort((x), (x) + (n));
#define SQ(a) ((a) * (a))
#define max3(a, b, c) max((a), max((b), (c)))
#define max4(a, b, c, d) max(max3(a, b, c), d)
#define min3(a, b, c) min((a), min((b), (c)))
#define min4(a, b, c, d) min(min3(a, b, c), d)
#define fastIO() cin.tie(0); ios::sync_with_stdio(0);

// loops
#define FOR(i, a, b) for (int (i) = (a); (i) < (b); (i)++)
#define ROF(i, a, b) for (int (i) = (a); (i) >= (b); (i)--)
#define REP(i, a, b) for (int (i) = (a); (i) <= (b); (i)++)
#define EACH(a, x) for (auto &(a) : (x))

typedef long long ll;
typedef pair<int, int> pii;
typedef tuple<long long, long long, long long> tiii;
typedef pair<long long, long long> pll;
typedef unsigned long long ull;
typedef long double ld;
typedef vector<int> vi;
typedef vector<bool> vb;
typedef vector<ll> vl;
typedef vector<string> vs;

const int dx[4]{1,0,-1,0}, dy[4]{0,1,0,-1};
const int MOD = 1e9 + 7;

template <typename... V>
void funcDebug(string vars, V... v) {
    cout << vars << " = ";
    string delim = "";
    (..., (cout << delim << v, delim = ", "));
    cout << endl;
}

// #define ONLINE_JUDGE
#ifndef ONLINE_JUDGE
    #define deb(x...) funcDebug(#x, x);
    #define debug(x) (cout << #x << ": " << x << endl);
    #define LINE cout << "--------------------" << endl;
    #define LINE2 cout << "~ ~ ~ ~ ~ ~ ~ ~ ~ ~" << endl;
    #define LINE3 cout << "- - - - - - - -" << endl;
    #define debugA(x, n) cout << #x << ": "; for (int zabz = 0; zabz < n;
        zabz++) cout << (x)[zabz] << " "; cout << endl;
    #define debugI(x) cout << #x << ": "; EACH(y, (x)) cout << y << " ";
        cout << endl;
#else
    #define deb(x...)
    #define debug(x)
    #define debugA(x, n)
    #define LINE
    #define LINE2
    #define LINE3
    #define debugI(x)
#endif

const ll infl = INT64_MAX;
const int inf = INT32_MAX;


// const int N = 1e5 + 10;

// const int LOG = 16;


const int N = 50000;
const int LOG = 16;

vector<pii> children[N];
int up[N][LOG];
int dist[N][LOG];
int depth[N];
bool visited[N];


void dfs(int x, int level = 0) {
    if (visited[x]) return;
    visited[x] = true;
    depth[x] = level;
    EACH(y, children[x]) {
        if (!visited[y.F]) {
            up[y.F][0] = x;
            dist[y.F][0] = y.S;
```

```
            dfs(y.F, level + 1);
        }
    }
}

int query(int x, int y) {
    if (depth[y] > depth[x]) swap(x, y);
    int toUp = depth[x] - depth[y];
    int bit = 0;
    int res = 0;
    while (toUp) {
        if (toUp & 1) res += dist[x][bit], x = up[x][bit];
        bit++;
        toUp >>=1;
    }
    if (x == y) return res;
    ROF(i, LOG - 1, 0) {
        if (up[x][i] != up[y][i]) {
            res += dist[x][i] + dist[y][i];
            x = up[x][i];
            y = up[y][i];
        }
    }
    return dist[x][0] + dist[y][0] + res;
}

void solve() {
    int n;
    cin >> n;
    FOR(i, 0, n - 1) {
        int a, b, w;
        cin >> a >> b >> w;
        children[a].PB({b, w});
        children[b].PB({a, w});
    }
    int root = 0;
    dfs(root);
    FOR(i, 1, LOG) {
        FOR(j, 0, n) {
            int ancestor = up[j][i - 1];
            up[j][i] = up[ancestor][i - 1];
            dist[j][i] = dist[ancestor][i - 1] + dist[j][i - 1];
        }
    }
    int q;
    cin >> q;
    while (q--) {
        int a, b;
        cin >> a >> b;
        cout << query(a, b) << "\n";
    }
}


int main() {
    fastIO();
    solve();
}
```

10 util

10.1 PI

```
const ld PI = acos(-1);
```

10.2 custom$_{h}ash$

```
struct custom_hash {
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            chrono::steady_clock::now().time_since_epoch().count();
        x ^= FIXED_RANDOM;
        return x ^ (x >> 16);
    }
};

struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }
```

```
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
            chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
```

10.3 custom$_{h}ash_{p}air$

```
// Use: unordered_set<pair<ll,ll>, HASH> exists;

struct HASH{
  size_t operator()(const pair<ll,ll>&x)const{
    return hash<ll>()(((ll)x.first)^(((ll)x.second)<<32));
  }
};
```

10.4 exponential$_{n}otation$

```
// O(n) convert numbers to Exponential Notation
// (e.g 0102.150 -> 1.0215E2)
// only float numbers > 0
string exponential_notation(string s) {
    int firstPos = find_if(all(s), [&](char c) {
        return c != '0' && c != '.';
    }) - s.begin();
    int dotPos = find(all(s), '.') - s.begin();
    ll base = dotPos - (firstPos+(firstPos <= dotPos));
    s.erase(dotPos, 1);
    for (int i = 0; i < 2; i++) { //erase traveling zeros
        while (s.back() == '0') s.pop_back();
        reverse(all(s));
    }
    if (s.size() > 1) s.insert(1, ".");
    if (base != 0) s+= "E" + to_string(base);
    return s;
}
```

10.5 io-int128

```
__int128 read() {
    __int128 x = 0, f = 1;
    char ch = getchar();
    while (ch < '0' || ch > '9') {
        if (ch == '-') f = -1;
        ch = getchar();
    }
    while (ch >= '0' && ch <= '9') {
        x = x * 10 + ch - '0';
        ch = getchar();
    }
    return x * f;
}
void print(__int128 x) {
    if (x < 0) {
        putchar('-');
        x = -x;
    }
    if (x > 9) print(x / 10);
    putchar(x % 10 + '0');
}

void print(__int128 x) {
    if (x < 0) {
        cout << "-";
        x = -x;
    }
    if (x > 9) print(x / 10);
    cout << char((int)(x % 10) + '0');
}
```

10.6 macros

```
#define MP make_pair
#define MT make_tuple
#define PB push_back
#define F first
#define S second
#define all(x) (x).begin(), (x).end()
#define sortt(x) sort(all(x))
#define sortn(x, n) sort((x), (x) + (n));
#define SQ(a) ((a) * (a))
```

```
#define max3(a, b, c) max((a), max((b), (c)))
#define max4(a, b, c, d) max(max3(a, b, c), d)
#define min3(a, b, c) min((a), min((b), (c)))
#define min4(a, b, c, d) min(min3(a, b, c), d)
#define fastIO() cin.tie(0); ios::sync_with_stdio(0);

// loops
#define FOR(i, a, b) for (ll (i) = (a); (i) < (b); (i)++)
#define ROF(i, a, b) for (ll (i) = (a); (i) >= (b); (i)--)
#define REP(i, a, b) for (ll (i) = (a); (i) <= (b); (i)++)
#define EACH(a, x) for (auto &(a) : (x))

typedef long long ll;
typedef pair<int, int> pii;
typedef tuple<long long, long long, long long> tiii;
typedef pair<long long, long long> pll;
typedef unsigned long long ull;
typedef long double ld;
typedef vector<int> vi;
typedef vector<bool> vb;
typedef vector<ll> vl;
typedef vector<pll> vpll;
typedef vector<vl> vvl;
typedef vector<vi> vvi;
typedef vector<string> vs;
typedef vector<ld> vld;

template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;
template<class T> using pqg = priority_queue<T>;

const ld DINF=1e100;
const ld EPS = 1e-9;
const ld PI = acos(-1);
const ll infl = INT64_MAX;
const int inf = INT32_MAX;
const int dx[4]{1,0,-1,0}, dy[4]{0,1,0,-1};
const int MOD = 1e9 + 7;
```

10.7 multi$_o$set

```
#include <bits/stdc++.h>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/assoc_container.hpp>

using namespace __gnu_pbds;

struct multiordered_set {
    tree<ll,
        null_type,
        less_equal<ll>, // this is the trick
        rb_tree_tag,
        tree_order_statistics_node_update> oset;

    //this function inserts one more occurrence of (x) into the set.
    void insert(ll x) {
        oset.insert(x);
    }

    //this function checks weather the value (x) exists in the set or not.
    bool exists(ll x) {
        auto it = oset.upper_bound(x);
        if (it == oset.end()) {
            return false;
        }
        return *it == x;
    }

    //this function erases one occurrence of the value (x).
    void erase(ll x) {
        if (exists(x)) {
            oset.erase(oset.upper_bound(x));
        }
    }

    //this function returns the value at the index (idx)..(0 indexing).
    ll find_by_order(ll pos) {
        return *(oset.find_by_order(pos));
    }

    //this function returns the first index of the value (x)..(0
        indexing).
    int first_index(ll x) {
        if (!exists(x)) {
            return -1;
        }
        return (oset.order_of_key(x));
    }
```

```
    //this function returns the last index of the value (x)..(0 indexing).
    int last_index(ll x) {
        if (!exists(x)) {
            return -1;
        }
        if (find_by_order(size() -1) == x) {
            return size() - 1;
        }
        return first_index(*oset.lower_bound(x)) -1;
    }

    //this function returns the number of occurrences of the value (x).
    int count(ll x) {
        if (!exists(x)) {
            return -1;
        }
        return last_index(x) - first_index(x) + 1;
    }

    //this function clears all the elements from the set.
    void clear() {
        oset.clear();
    }

    //this function returns the size of the set.
    ll size() {
        return (ll)oset.size();
    }
};
```

10.8 oset

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

#define oset tree<ll, null_type,less<ll>,
    rb_tree_tag,tree_order_statistics_node_update>
//find_by_order(k) order_of_key(k)
```

10.9 pragmas

```
//#pragma GCC target("popcnt")
//It's worth noting that after adding __builtin_popcount() is replaced to
    corresponding machine instruction (look at the difference). In my
    test this maked x2 speed up. bitset::count() use __builtin_popcount()
    call in implementation, so it's also affected by this.
#pragma GCC target ("avx2")
#pragma GCC optimization ("O3")
#pragma GCC optimization ("unroll-loops")
#pragma GCC target("popcnt")
#pragma GCC target("avx,avx2,sse3,ssse3,sse4.1,sse4.2,tune=native")
#pragma GCC optimize(3)
#pragma GCC optimize("O3")
#pragma GCC optimize("inline")
#pragma GCC optimize("-fgcse")
#pragma GCC optimize("-fgcse-lm")
#pragma GCC optimize("-fipa-sra")
#pragma GCC optimize("-ftree-pre")
#pragma GCC optimize("-ftree-vrp")
#pragma GCC optimize("-fpeephole2")
#pragma GCC optimize("-fsched-spec")
#pragma GCC optimize("-falign-jumps")
#pragma GCC optimize("-falign-loops")
#pragma GCC optimize("-falign-labels")
#pragma GCC optimize("-fdevirtualize")
#pragma GCC optimize("-fcaller-saves")
#pragma GCC optimize("-fcrossjumping")
#pragma GCC optimize("-fthread-jumps")
#pragma GCC optimize("-freorder-blocks")
#pragma GCC optimize("-fschedule-insns")
#pragma GCC optimize("inline-functions")
#pragma GCC optimize("-ftree-tail-merge")
#pragma GCC optimize("-fschedule-insns2")
#pragma GCC optimize("-fstrict-aliasing")
#pragma GCC optimize("-falign-functions")
#pragma GCC optimize("-fcse-follow-jumps")
#pragma GCC optimize("-fsched-interblock")
#pragma GCC optimize("-fpartial-inlining")
#pragma GCC optimize("no-stack-protector")
#pragma GCC optimize("-freorder-functions")
#pragma GCC optimize("-findirect-inlining")
#pragma GCC optimize("-fhoist-adjacent-loads")
#pragma GCC optimize("-frerun-cse-after-loop")
#pragma GCC optimize("inline-small-functions")
#pragma GCC optimize("-finline-small-functions")
```

```
#pragma GCC optimize("-ftree-switch-conversion")
#pragma GCC optimize("-foptimize-sibling-calls")
#pragma GCC optimize("-fexpensive-optimizations")
#pragma GCC optimize("inline-functions-called-once")
#pragma GCC optimize("-fdelete-null-pointer-checks")
```

10.10 priority$_q ueue$

```
template<class T> using pql = priority_queue<T,vector<T>,greater<T>>;//
    less
template<class T> using pqg = priority_queue<T>; // greater
```

10.11 random

```
mt19937 mt_rng(chrono::steady_clock::now().time_since_epoch().count());
// also for ll exists mt19937_64
ll randint(ll a, ll b) {
    return uniform_int_distribution<ll>(a, b)(mt_rng);
}
```

10.12 util bultin functions

```
# Sum the values of a iterable
# Very important to put 0ll to avoid overflows
accumulate(v.begin(),v.end(),0ll)/n;
```