

Correction de l'exercice 24:

4. a. Les coordonnées de I et J dans le repère orthonormal de l'espace (A;B;E;D).

$I(1/2; 0; 1)$ et $J(1; 2/5; 1)$

b. Le triangle FIJ est-il rectangle en J ?:

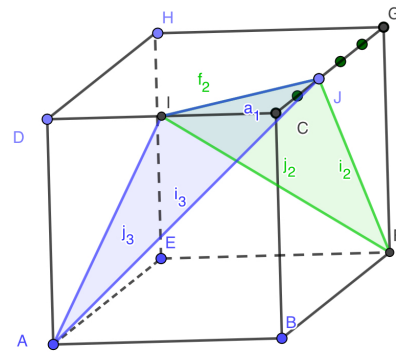
$$FI^2 = IJ^2 + JF^2$$

$$F(1; 1; 0)$$

$$\overrightarrow{IF}(1 - 1/2; 1 - 0; 0 - 1) = (1/2; 1; -1)$$

$$|\overrightarrow{IF}| = \sqrt{1^2 + (1/2)^2 + (-1)^2} = \sqrt{2 + 1/4} = \sqrt{9/4}$$

$$\overrightarrow{IJ}(1 - 1/2; 2/5 - 0; 1 - 1) = (1/2; 2/5; 0).$$



$$|\overrightarrow{IJ}| = \sqrt{(1/2)^2 + (2/5)^2 + 0} = \sqrt{1/4 + 4/25} = \sqrt{25/100 + 16/100} = \sqrt{41/100}$$

$$\overrightarrow{JF}(1 - 1; 1 - 2/5; 0 - 1) = (0; 3/5; -1)$$

$$|\overrightarrow{JF}| = \sqrt{0 + (3/5)^2 + (-1)^2} = \sqrt{9/25 + 1} = \sqrt{34/25}$$

$$FI^2 = 9/4; IJ^2 = 41/100; JF^2 = 34/25$$