

## AES (Advanced Encryption Standard)

a block cipher that operates on bytes and encrypts 128-bit, 168-bit, 192-bit, 224-bit, or 256-bit data blocks  
using a 128-bit, 192-bit, or 256-bit key

the standard AES in practice is AES-128, where both the data block and key are 128 bits in size  
uses several rounds of encryption

the entire block of data is encrypted in each of the rounds

depending on the size of the key used, the number of rounds performed varies

for a 128-bit key, there are 10 rounds

for a 192-bit key, there are 12 rounds

for a 256-bit key, there are 14 rounds

each round has a separate sub-key that is based on the Rijndael key schedule

a mathematical function that expands a key into a number of separate round keys

### background story

at the time, DES (Data Encryption Standard) had been broken

so there was a desperate need for AES

NIST announced an AES competition and issued a call for algorithm submissions

15 were submitted

5 made it to the finals

finalists?

Ron Rivest, IBM, etc

Rijndael, designed by two young Belgian cryptographers, won

named after Joan Daeman and Vincent Rijmen

later became AES

today, AES is the most-widely used encryption algorithm

NSA allows AES to encrypt top secret documents (if a 192-bit or larger key is used)

### AES working mechanism

each round (except the last one) has four layers:

1. byte substitution

2. row shift

3. column mix

4. key addition

(the last round does not have the column mix layer)

to begin, the data is arranged in a 4x4 matrix

e.g., "Sky is falling":

|   |   |   |   |   |
|---|---|---|---|---|
|   | 0 | 1 | 2 | 3 |
| 0 | S | i | a | n |
| 1 | k | s | l | g |
| 2 | y |   | l | # |
| 3 |   | f | i | # |

note that the blank cells contain a space

the final two # symbols are padded characters

padding?

when the data block is not 16 bytes long, it is padded by appending some values at the end  
the most basic form of padding is to append 0's at the end (we add #'s)

1. byte substitution (i.e., confusion)

16 bytes of input data (=128 bits)

each byte is substituted using a substitution box (S-box)

an S-box is just a constant matrix that substitutes bits for other bits

it is defined to be strong against numeric attacks (which makes the cipher stronger)

2. row shift (i.e., diffusion at an algorithmic level)

each row in the matrix above is shifted to the left by 0, 1, 2, and 3 respectively

the output for the matrix above after the row shift is:

|   | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | S | i | a | n |
| 1 | s | l | g | k |
| 2 | l | # | y |   |
| 3 | # |   | f | i |

3. column mix (i.e., diffusion)

diffuse the data so that even a single change in an input changes everything on the output

a different matrix is used to perform polynomial multiplication on the row shift matrix above:

|   | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | 2 | 3 | 1 | 1 |
| 1 | 1 | 2 | 3 | 1 |
| 2 | 1 | 1 | 2 | 3 |
| 3 | 3 | 1 | 1 | 2 |

note: each of the letters on the row shift matrix corresponds to some binary value

binary values are multiplied with the above matrix

a dot product

4. key addition

the output obtained after matrix polynomial multiplication is XOR'd with this round's sub-key

recall the Rijndael key schedule above for generating round keys

in general, for  $n$  rounds, to get the ciphertext:

the four layers are performed in all rounds 1 to  $n-1$

all but the column mix layer is performed in the final ( $n$ -th) round

security of AES

depends on confusion and diffusion

polynomial matrix multiplication diffuses the input at a great level