

## Assignment 2.

### Using OpenGL library for drawing planar curves.

1. In this example, the OpenGL begin/end paradigm (GL\_LINE\_STRIP) was used for drawing polygonal lines corresponding to:

1. the graph of the function:  $|\sin x| \cdot e^{-\sin x}, x \in [0, 8\pi]$  and
2. the graph of the Conchoid of Nicomedes:

$$x = a \pm b \cos t, y = a \tan t \pm b \sin t, t \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right).$$

2. As for assignment 1, add in the example program lines of code in order to draw the following graphs:

1. The graph of the function  $f(x) = \begin{cases} 1 & , x = 0 \\ \frac{d(x)}{x} & , 0 < x \leq 100 \end{cases}$ ,

where  $d(x)$  is the distance from  $x$  to the nearest integer.

2. The following curves are given by parametric equations (for each example, the values of various parameters, called  $a$ ,  $b$ , etc., can be found inside the images):

1. [The trisectrix of Longchamps](#):

$$x = \frac{a}{4 \cos^2 t - 3}, \quad y = \frac{a \tan t}{4 \cos^2 t - 3}, \quad t \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \setminus \left\{\pm \frac{\pi}{6}\right\}.$$

Hint: First, draw the graph of the trisectrix of Longchamps (please note

that the [image](#) is not the graph!). Use no scaling, use GL\_POINTS

and vary the ratio of arithmetic progression. Then overlap your

window on the image requested and notice some patterns, the geometric

objects etc. If your image has some/many pixels in the middle it is

still considered correct.

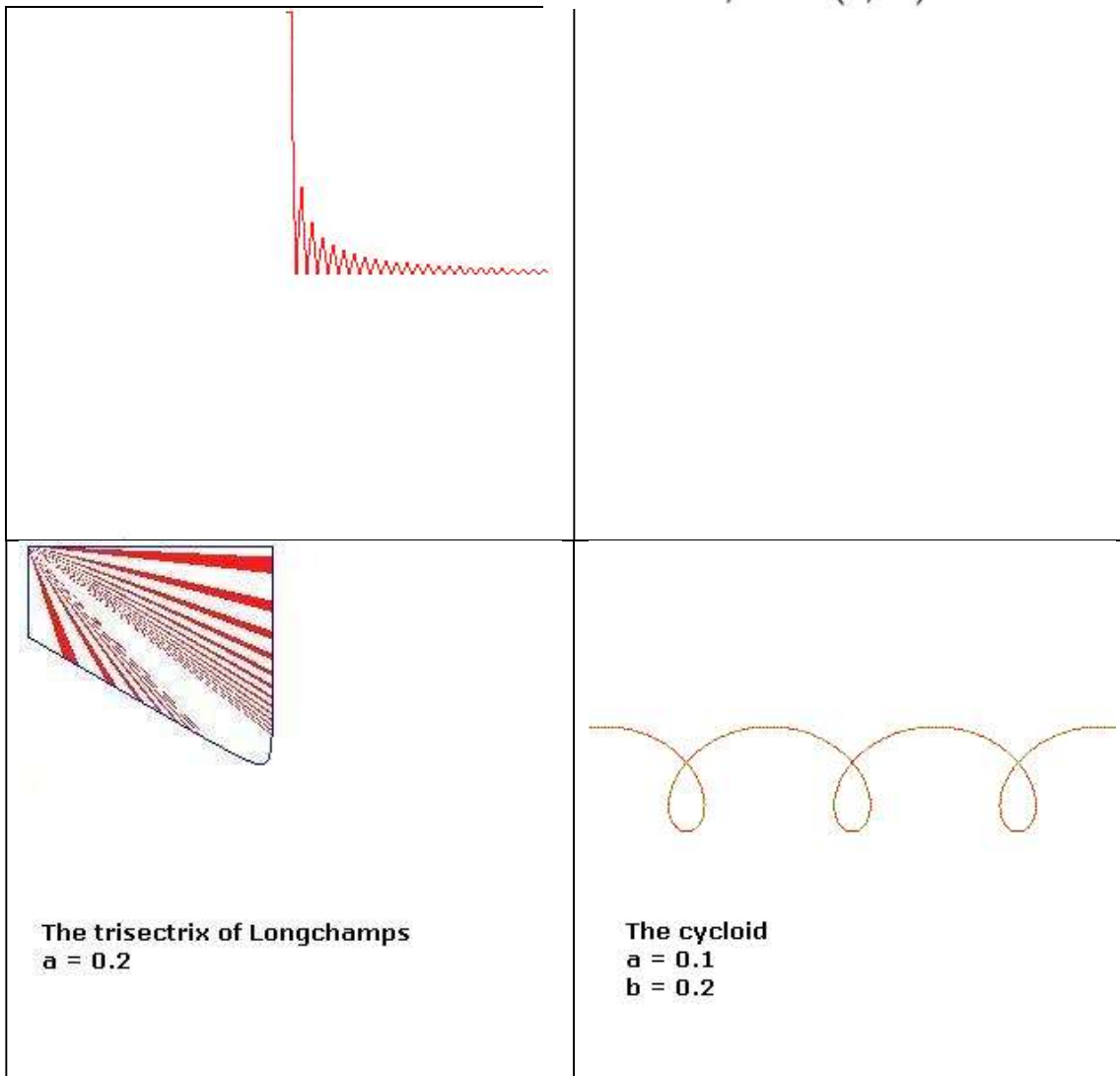
2. [The cycloid](#):

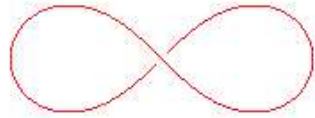
$$x = a \cdot t - b \sin t, \quad y = a - b \cos t, \quad t \in \mathbb{R}.$$

3. Some curves are specified by polar equations: the polar coordinates are  $(r, t)$ ,

where  $t \in [a, b]$  and  $r = f(t)$ . The polar coordinates  $(r, t)$  are transformed in cartesian coordinates as following  $x = r \cos t$  and  $y = r \sin t$ . Add in the example program lines of code in order to draw the following curves specified by polar equations:

1. [The lemniscate of Bernoulli](#):  $r = \pm a \cdot \sqrt{2 \cos 2t}$ ,  $t \in (-\frac{\pi}{4}, \frac{\pi}{4})$ ,
2. [The logarithmic spiral](#):  $r = a \cdot e^{1+t}$ ,  $t \in (0, \infty)$ .





**The lemniscate of Bernoulli**  
 **$a = 0.4$**



**The logarithmic spiral**  
 **$a = 0.02$**