

Multivariate comparative analysis using OUCH*!

Aaron King

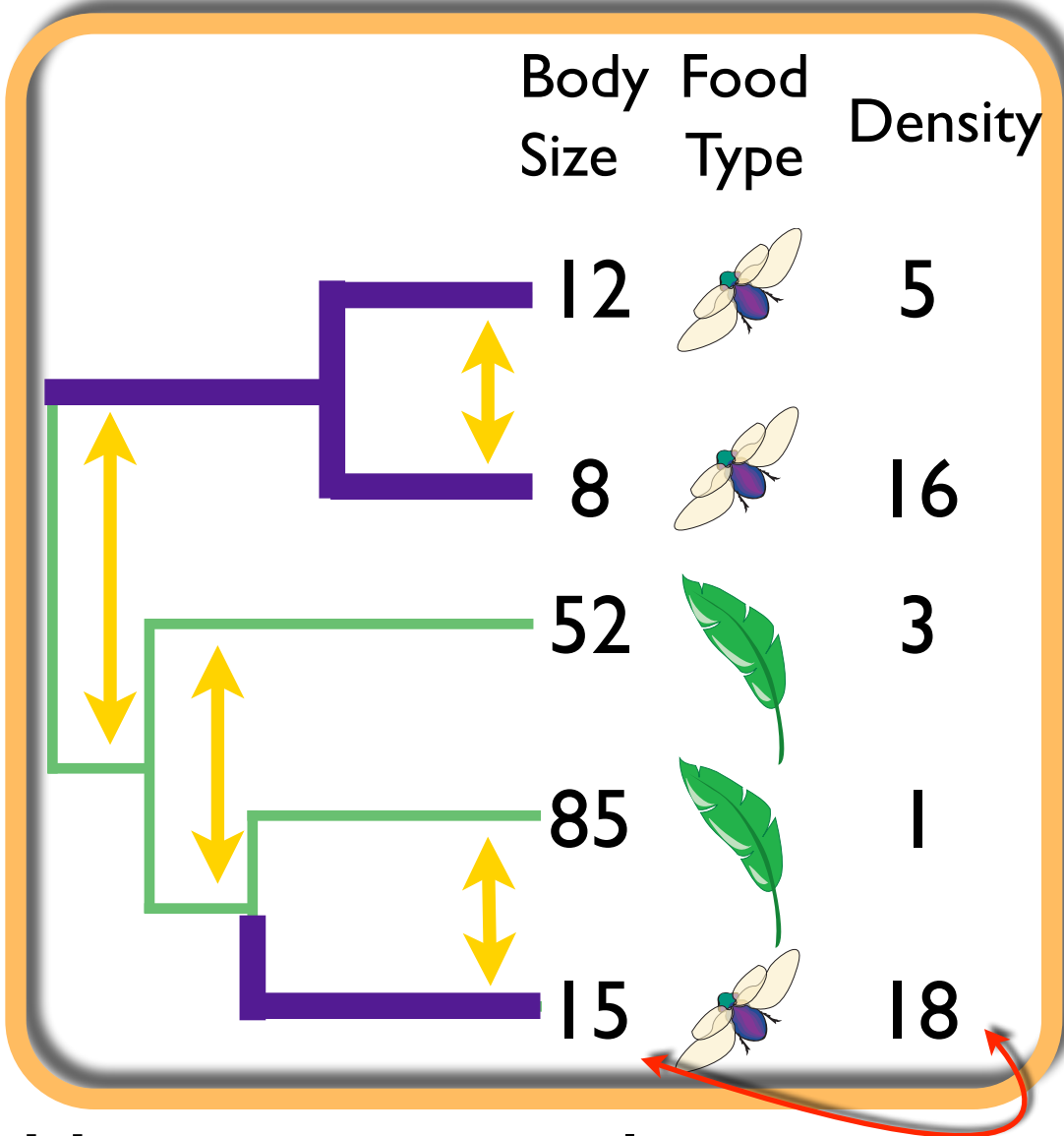
University of Michigan, Ecology & Evolutionary Biology

Marguerite Butler

University of Hawaii, Department of Zoology

(*Ornstein-Uhlenbeck for Comparative Hypotheses)



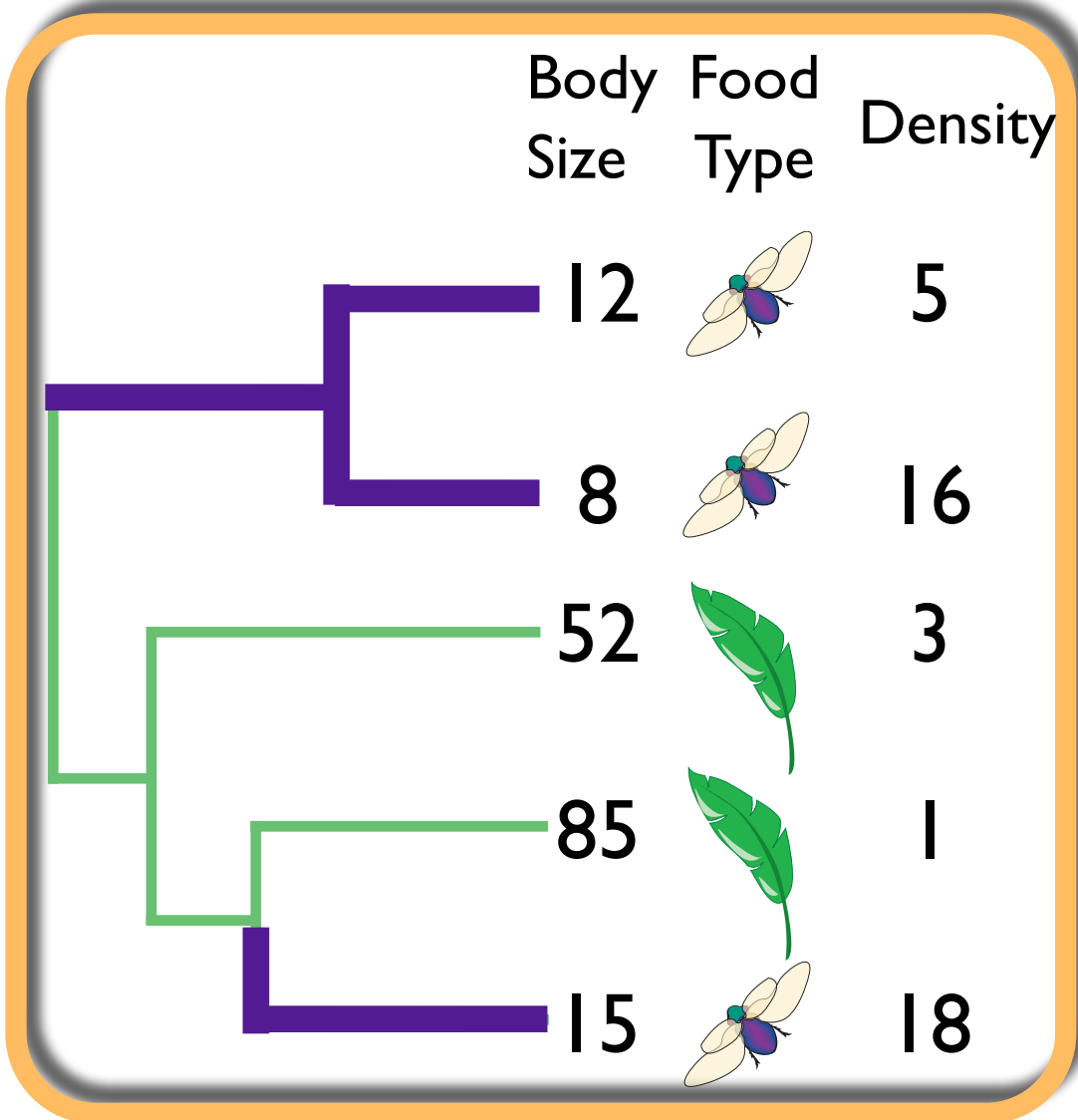


Previously, we developed an approach for comparative analysis which allows testing for alternative adaptive regimes

But...
only for one character

Uncovering evolutionary correlations is the most popular use of comparative methods

Here we develop a general modeling approach for multiple characters



Why study correlated evolution?

Helps us to understand patterns in diversity

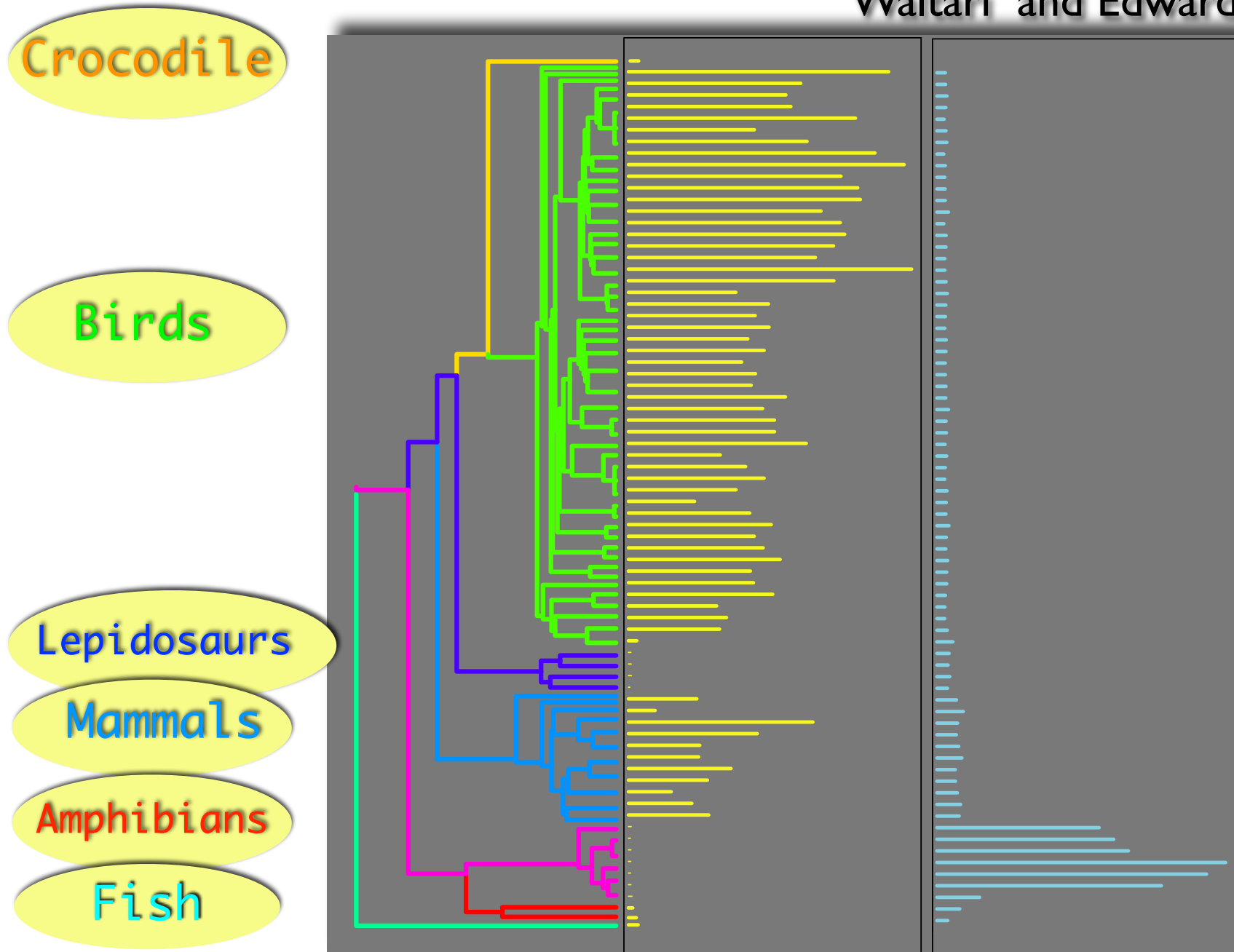
Reveals important functional relationships

Correlated selection can also prevent traits from reaching their individual optima

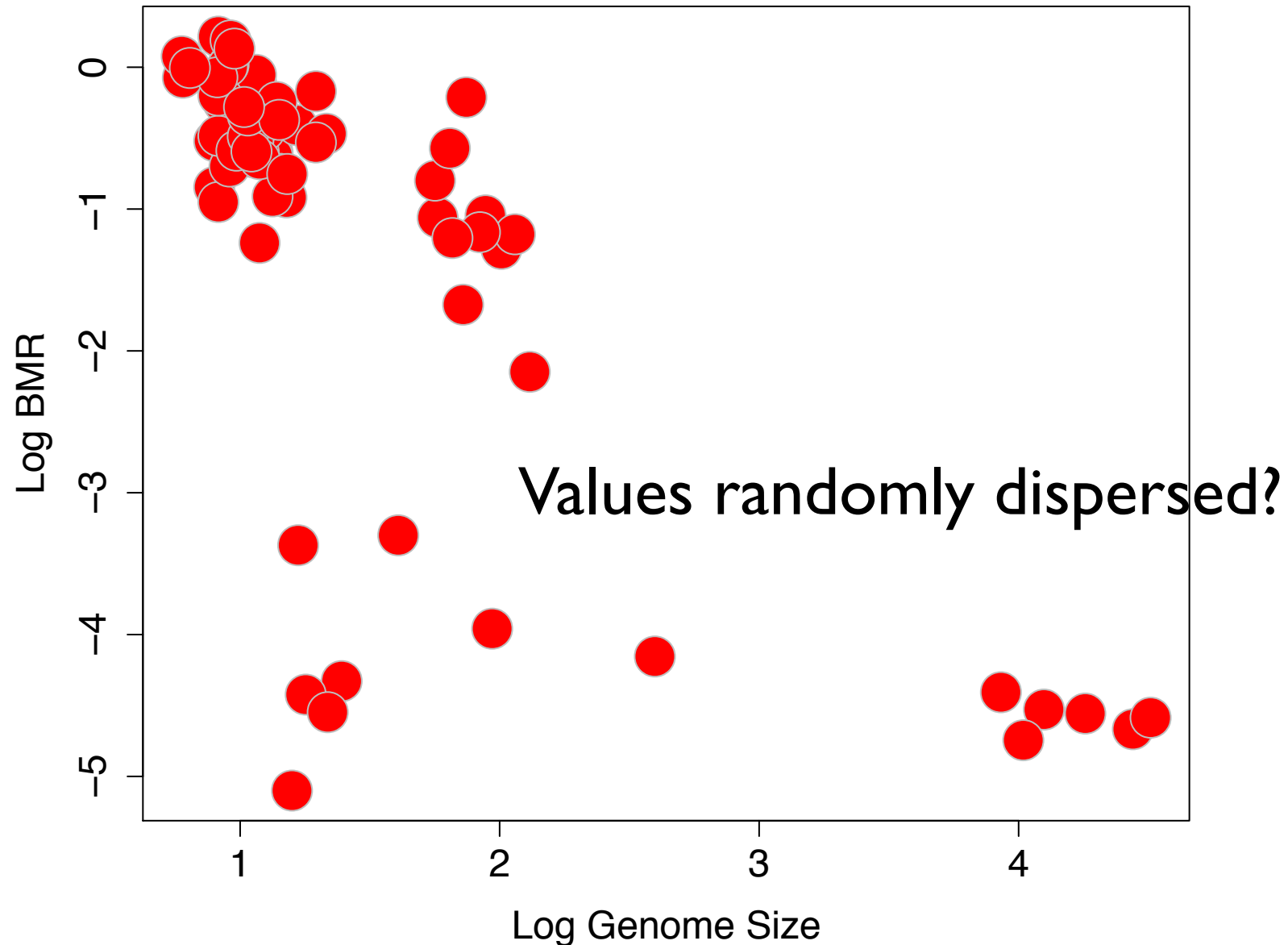
Here we develop a general modeling approach for multiple characters

Basal Metabolic Rate and Genome Size

Waltari and Edwards 2002

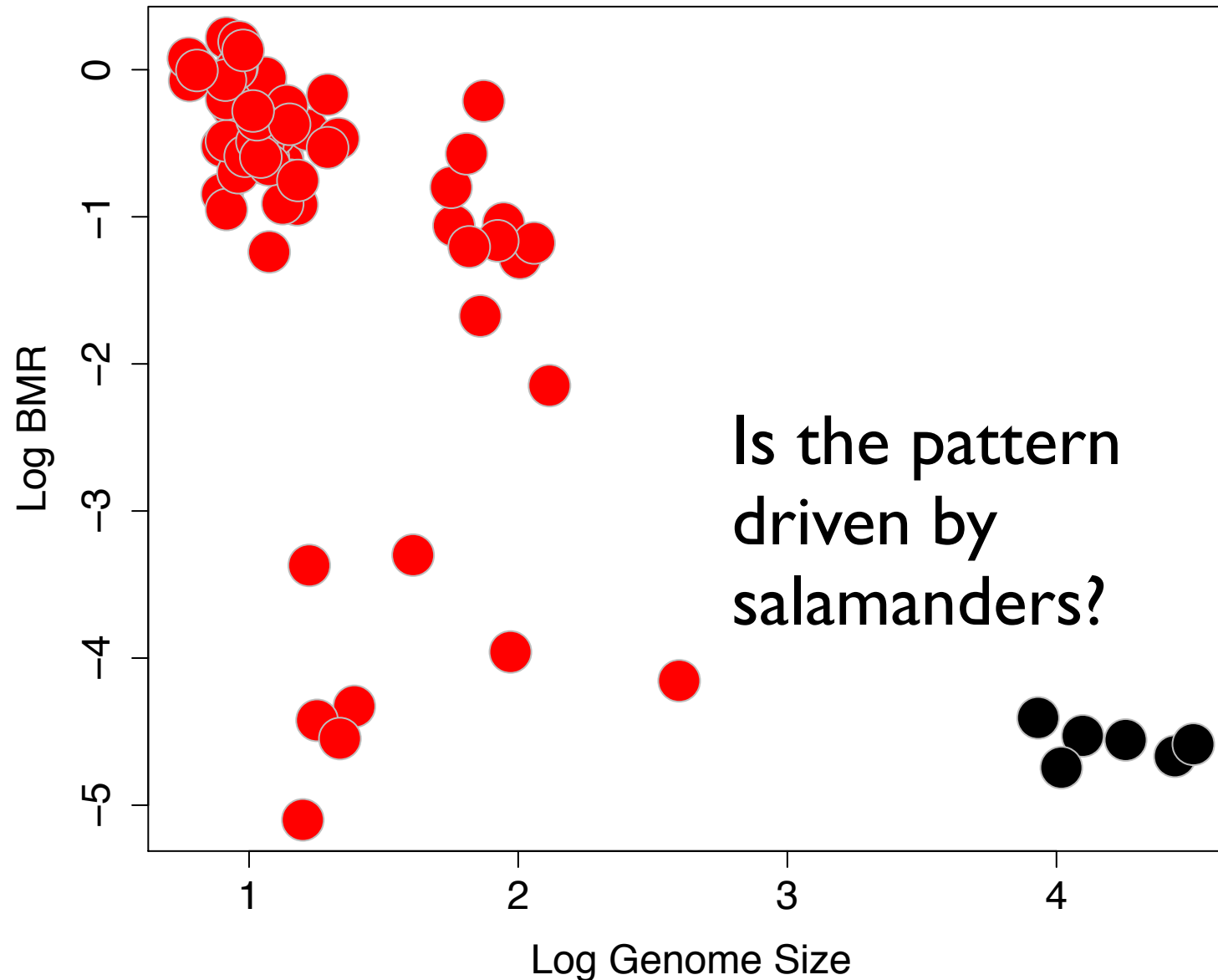


How do we explain the evolution of BMR and GS?
Are they linked? What is the relationship?

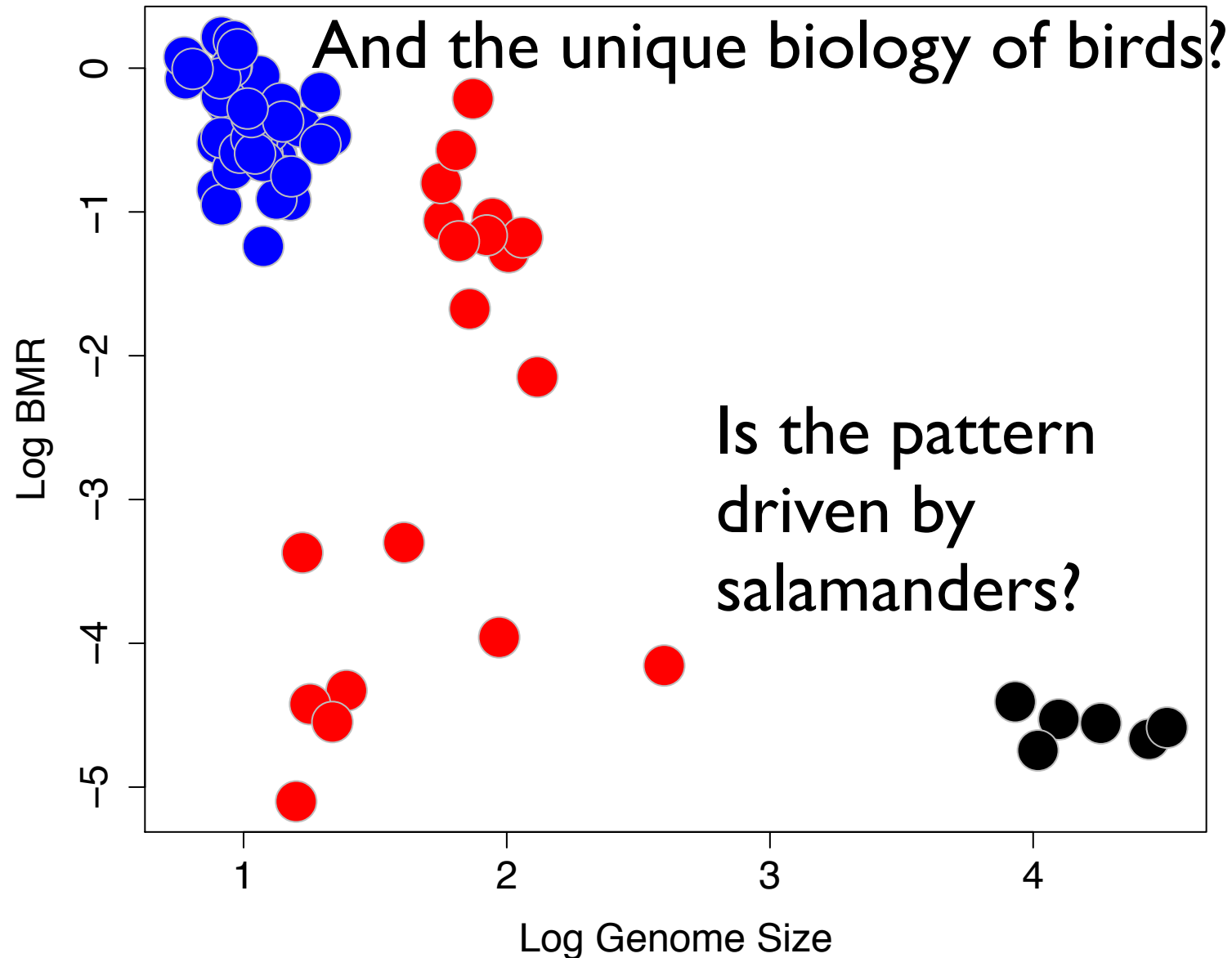


How do we explain the evolution of BMR and GS?

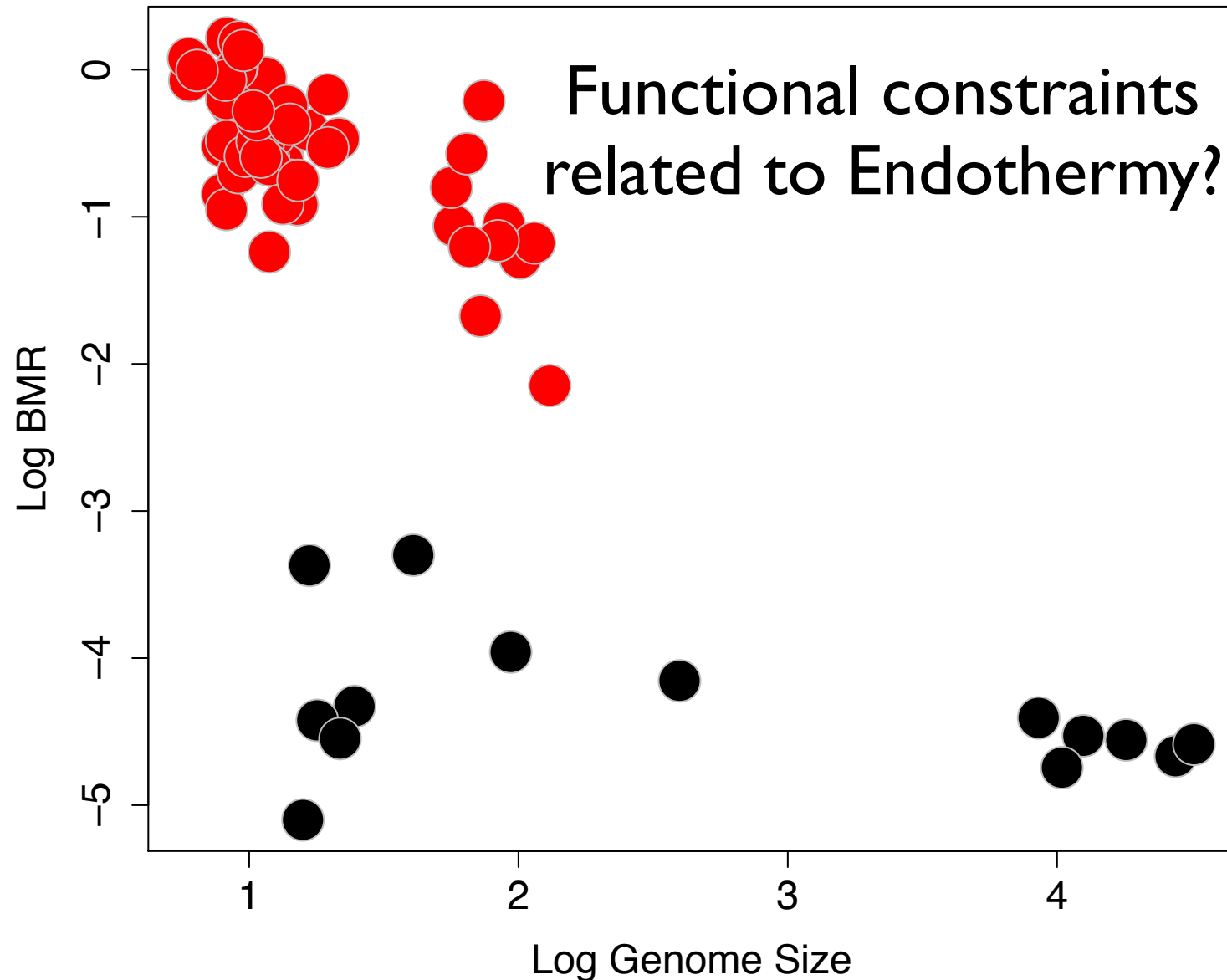
Are they linked? What is the relationship?



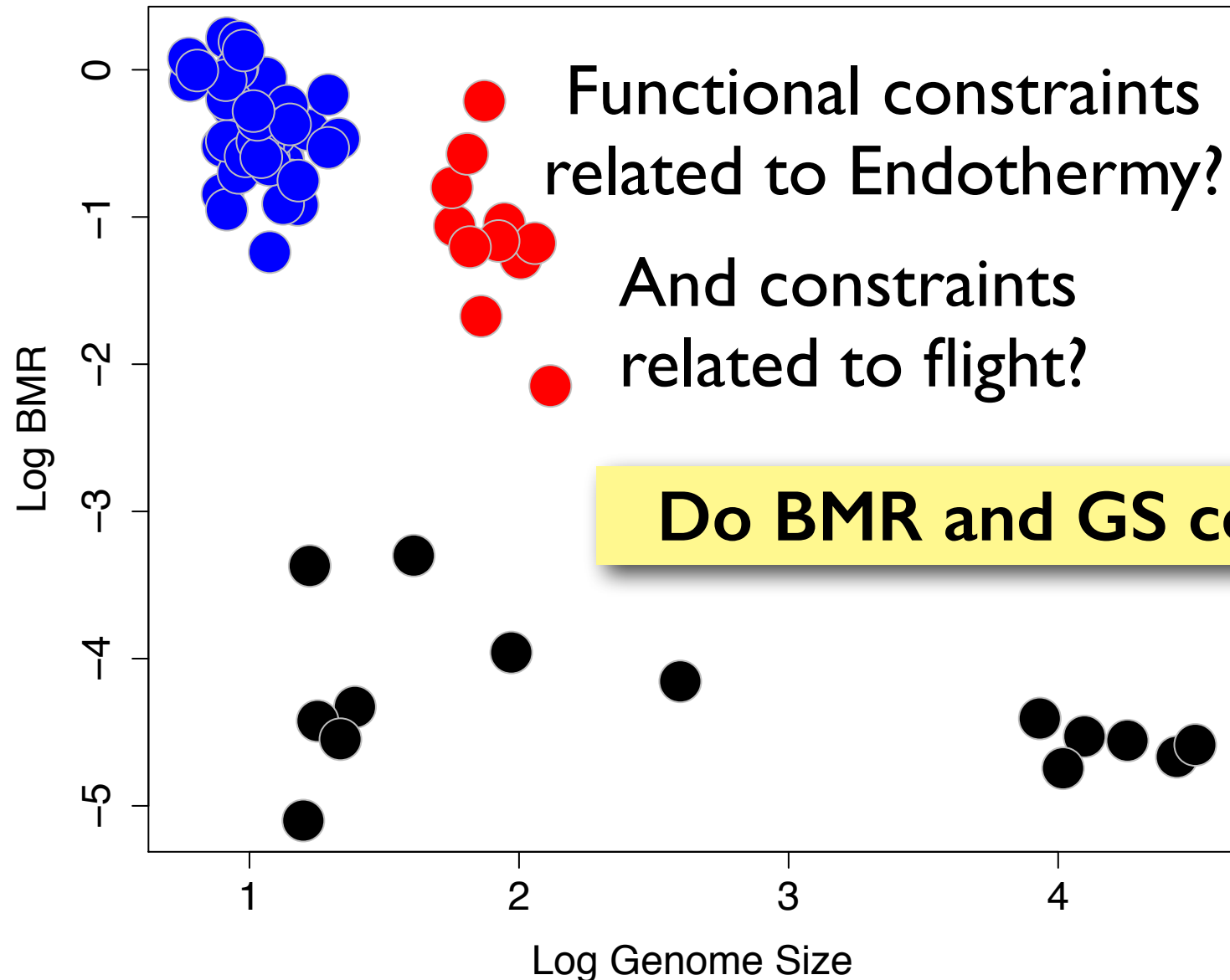
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How do we explain the evolution of BMR and GS?
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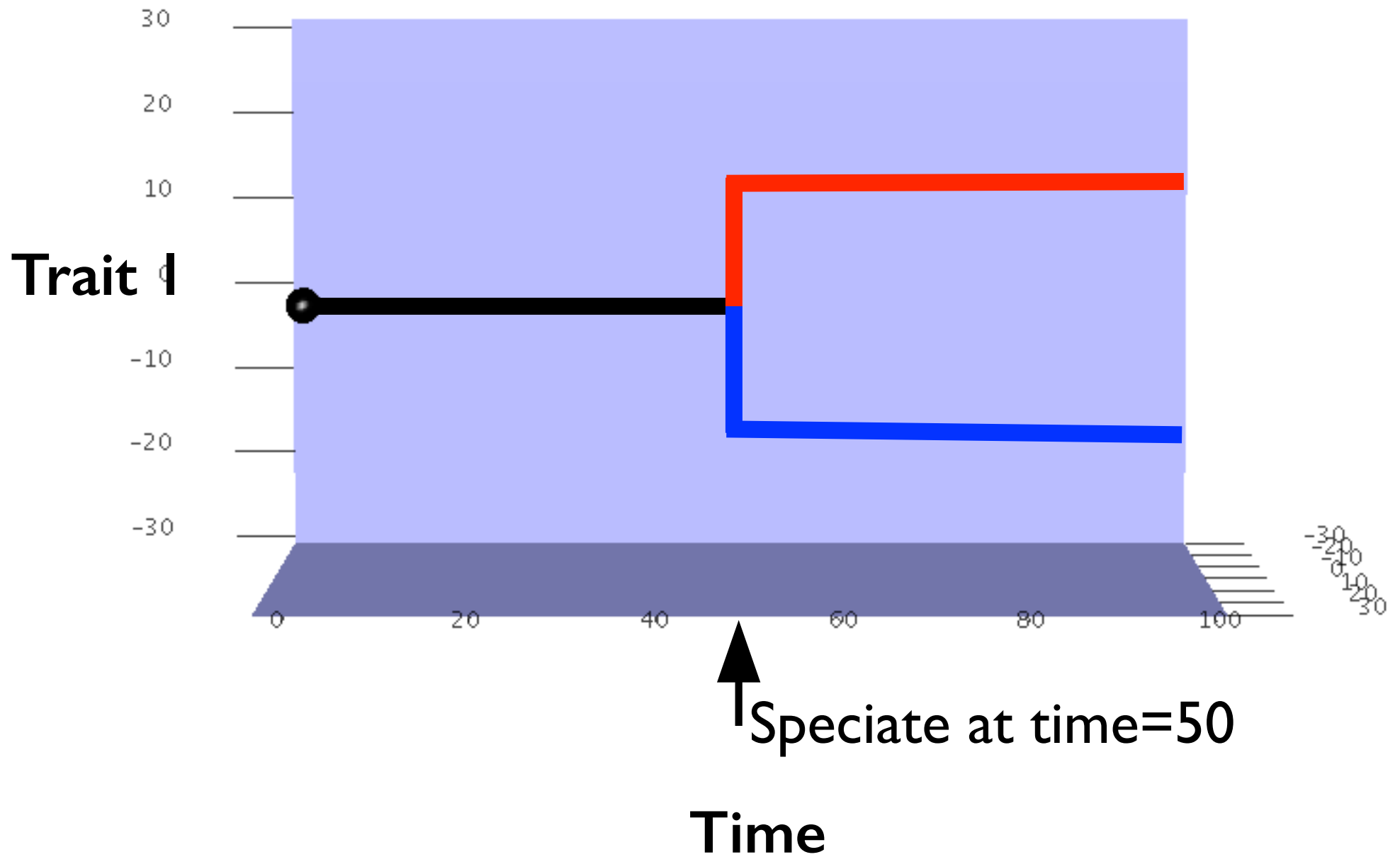


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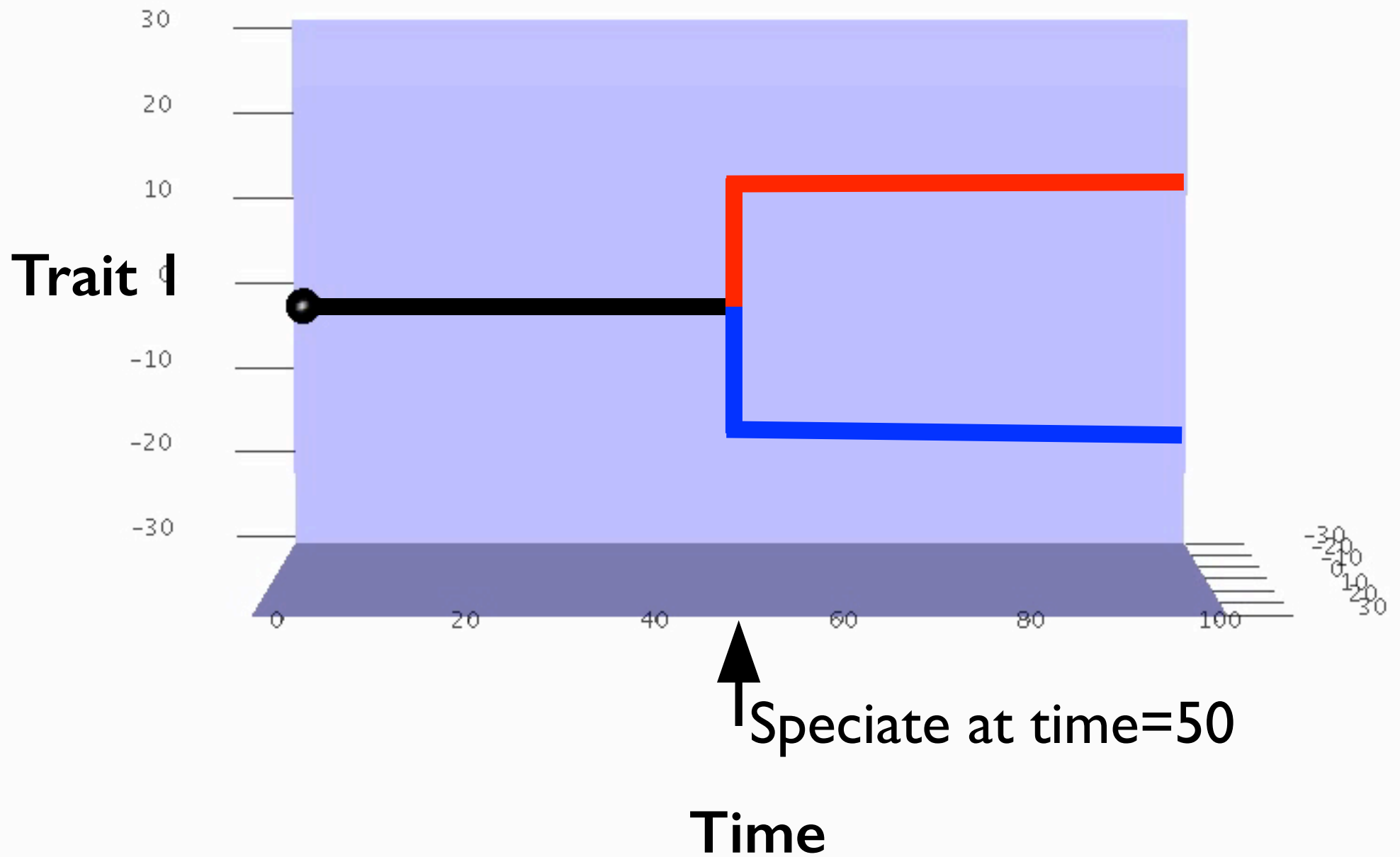


Illustrating the Model

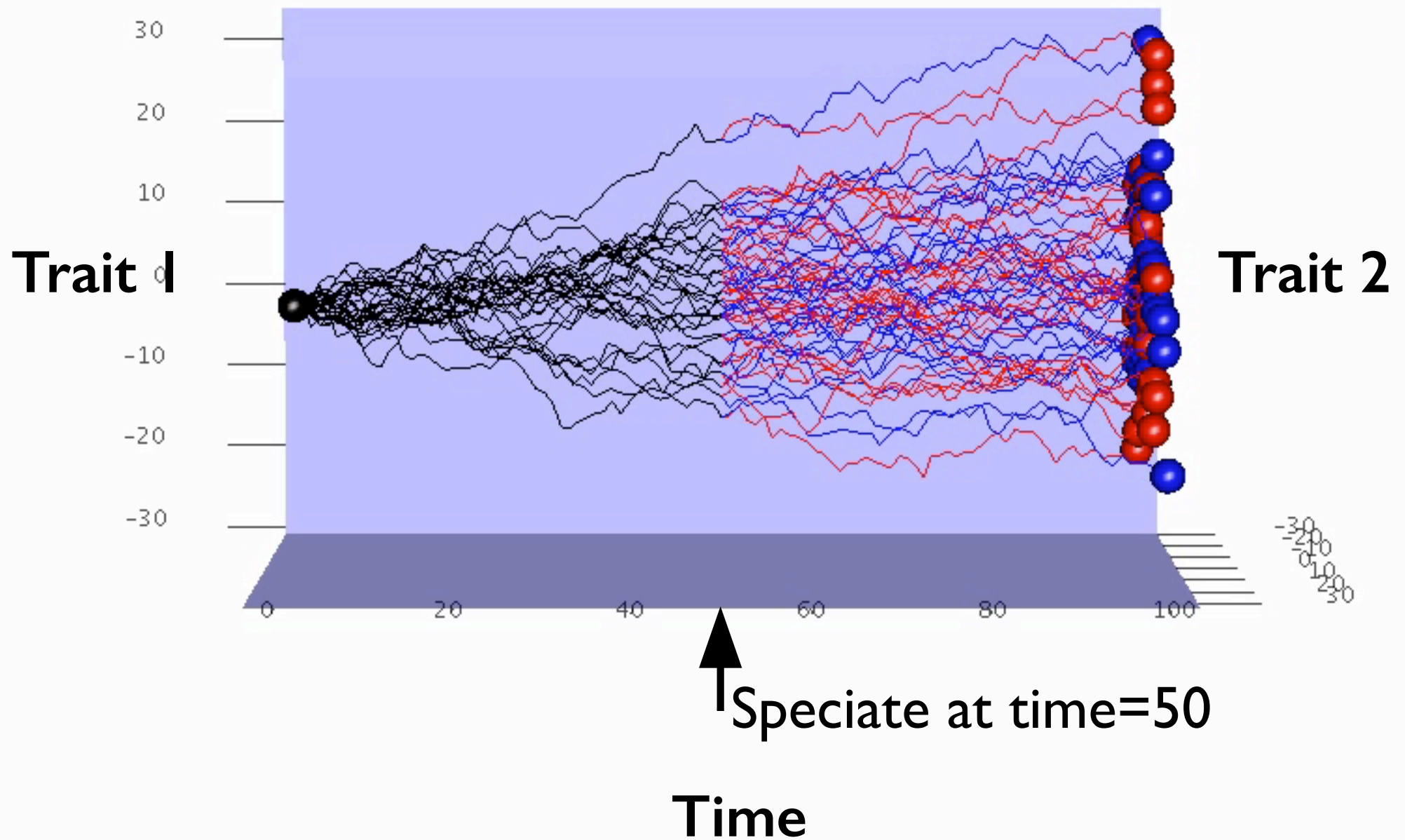
Brownian motion in 2D



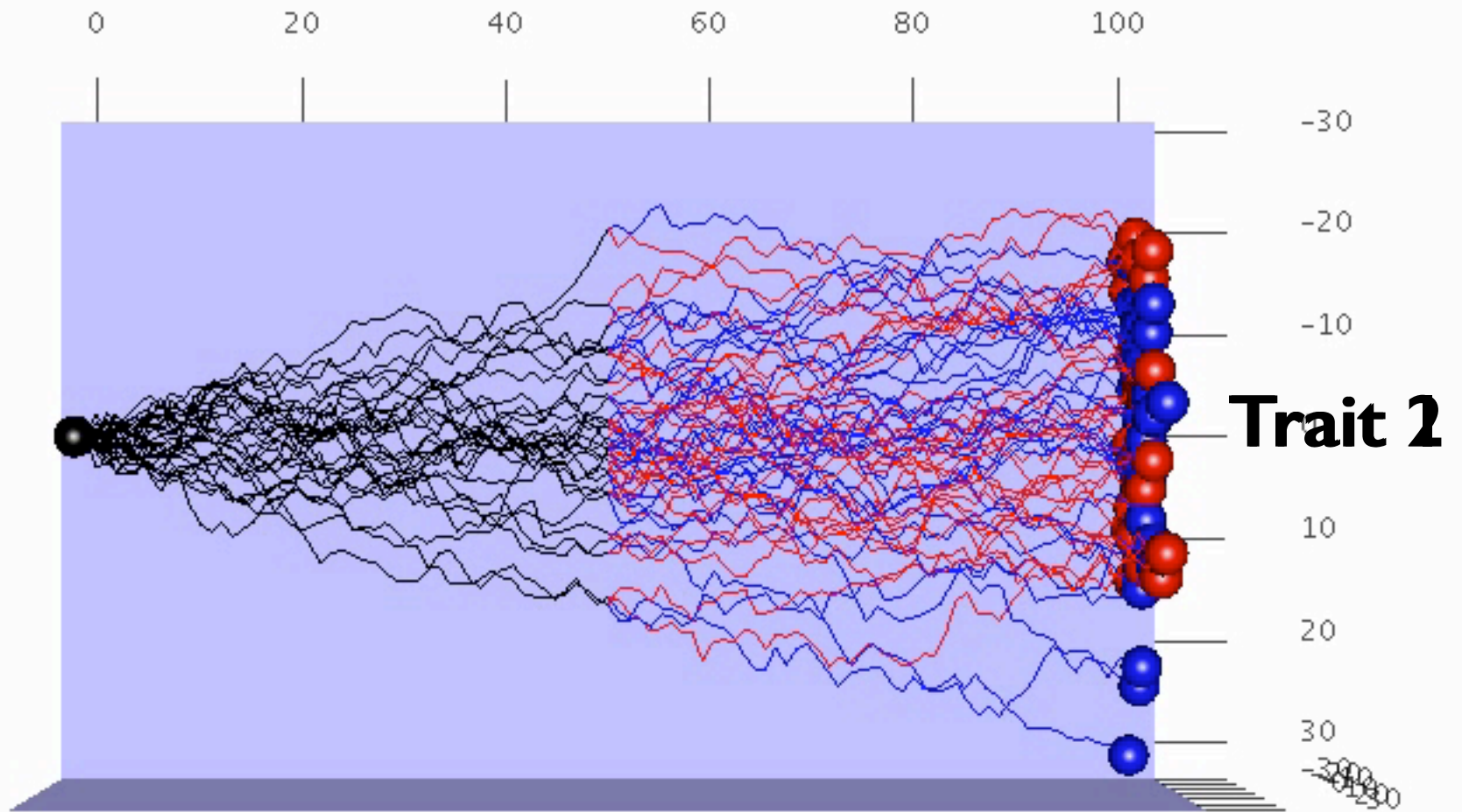
Brownian motion in 2D



Brownian motion in 2D

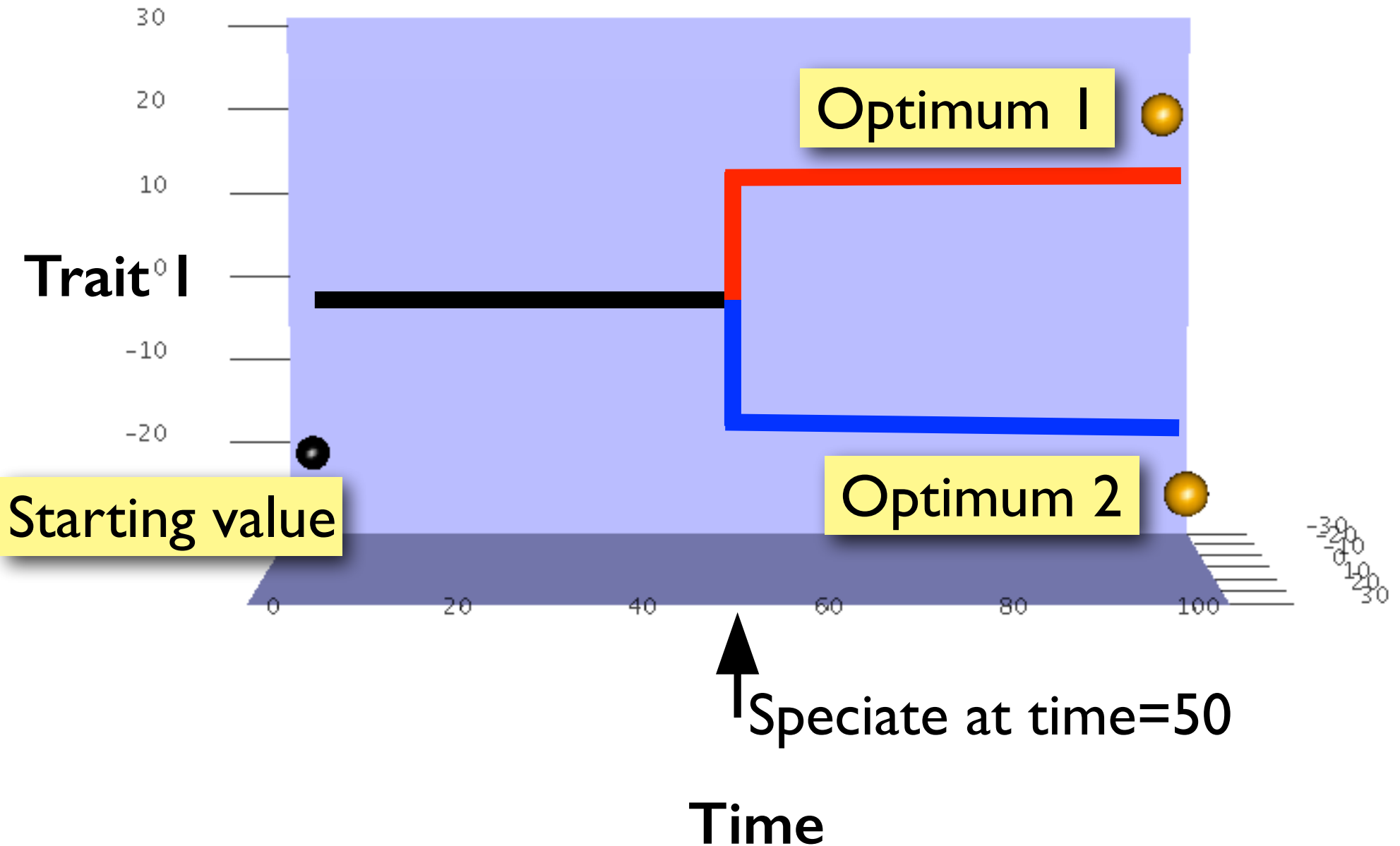


Brownian motion in 2D

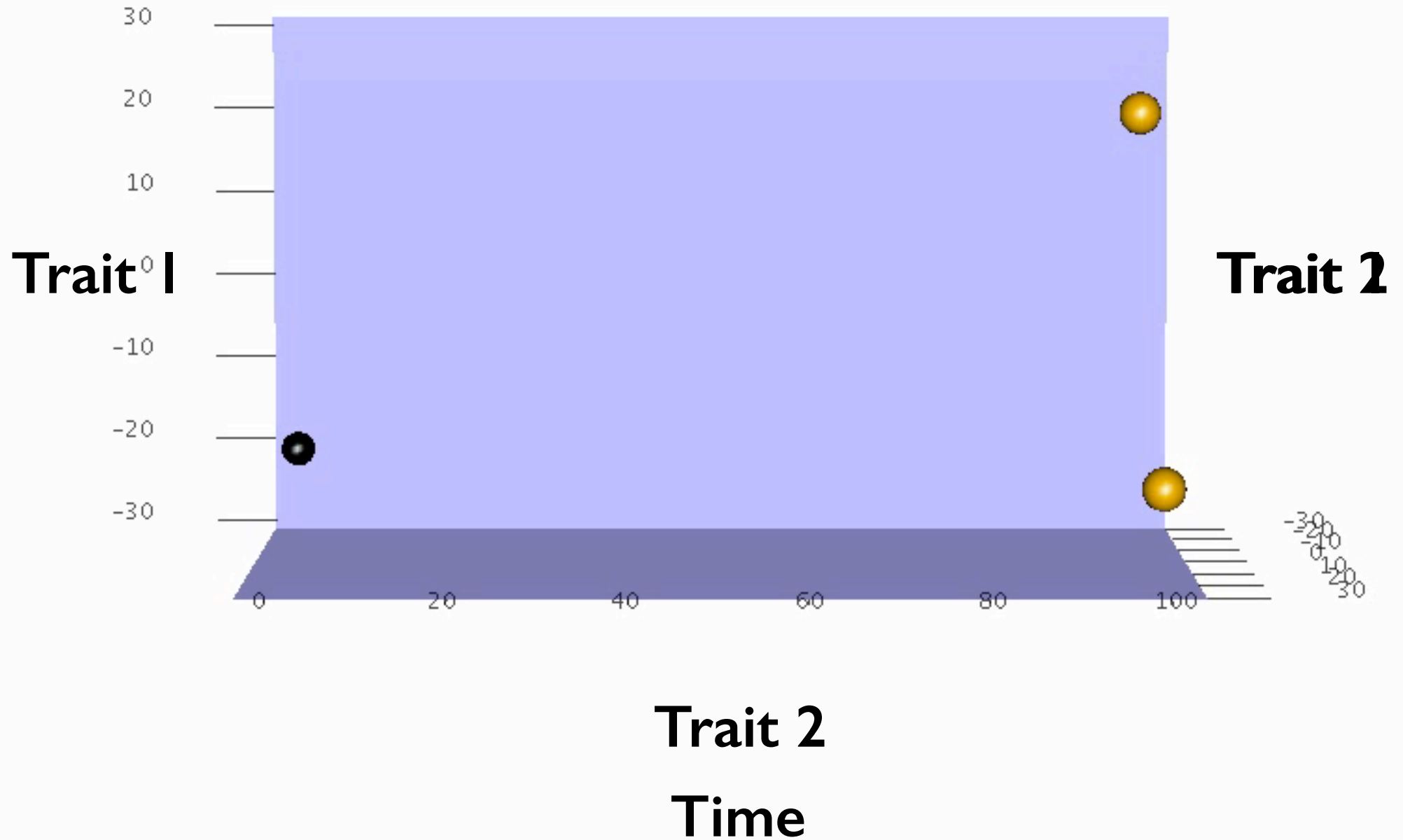


Trait 2
Time

Orstein-Uhlenbeck with strong selection



Orstein-Uhlenbeck with strong selection



With two traits,

$$dX(t) = \alpha (\theta - X(t)) dt + \sigma dB(t)$$

The alpha and sigma parameters become matrices

Superlinear
increase in
parameters
with more traits

$$\alpha = \begin{pmatrix} \alpha_{11} & \alpha_{12} \\ \alpha_{12} & \alpha_{22} \end{pmatrix}$$

$$\sigma = \begin{pmatrix} \sigma_{11} & 0 \\ \sigma_{12} & \sigma_{22} \end{pmatrix}$$

With diagonal terms being selection and drift as usual on trait 1 and trait 2

And off-diagonal terms for correlational effects (the effect of trait 1 on trait 2, and vice versa)



Illustrating the off-diagonal parameters

“Double
Univariate”

$$\alpha = \begin{pmatrix} \alpha_{11} & 0 \\ 0 & \alpha_{22} \end{pmatrix} \quad \sigma = \begin{pmatrix} \sigma_{11} & 0 \\ 0 & \sigma_{22} \end{pmatrix}$$

Correlated
“drift”

$$\alpha = \begin{pmatrix} \alpha_{11} & 0 \\ 0 & \alpha_{22} \end{pmatrix} \quad \sigma = \begin{pmatrix} \sigma_{11} & 0 \\ \sigma_{12} & \sigma_{22} \end{pmatrix}$$

Correlated
“selection”
+ “drift” 

$$\alpha = \begin{pmatrix} \alpha_{11} & \alpha_{12} \\ \alpha_{12} & \alpha_{22} \end{pmatrix} \quad \sigma = \begin{pmatrix} \sigma_{11} & 0 \\ \sigma_{12} & \sigma_{22} \end{pmatrix}$$

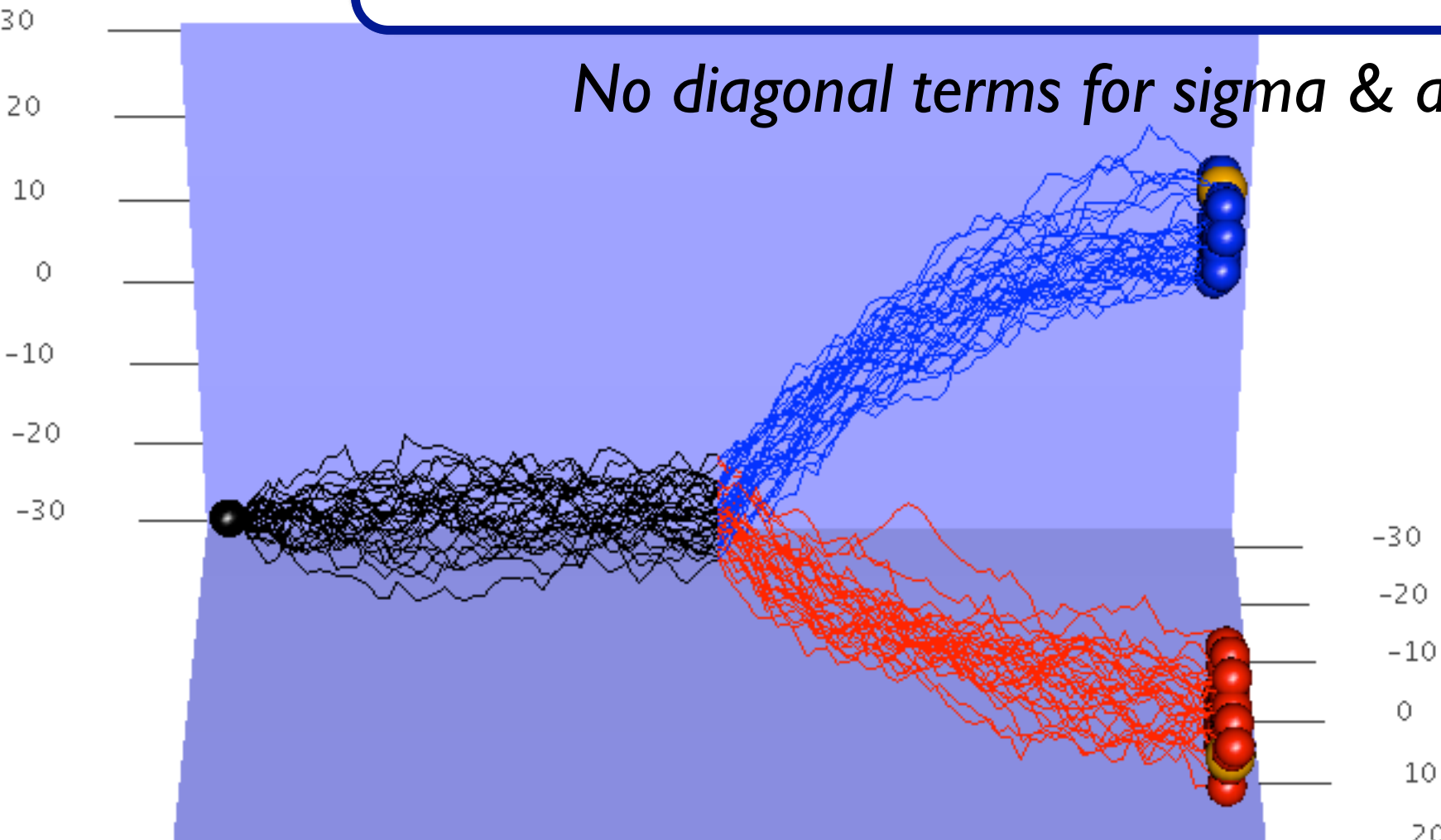
add off-diagonal sigma and alpha terms

Illustrating the off-diagonal parameters

“Double
Univariate”

$$\alpha = \begin{pmatrix} 4 & 0 \\ 0 & 4 \end{pmatrix} \quad \sigma = \begin{pmatrix} 10 & 0 \\ 0 & 10 \end{pmatrix}$$

No diagonal terms for sigma & alpha

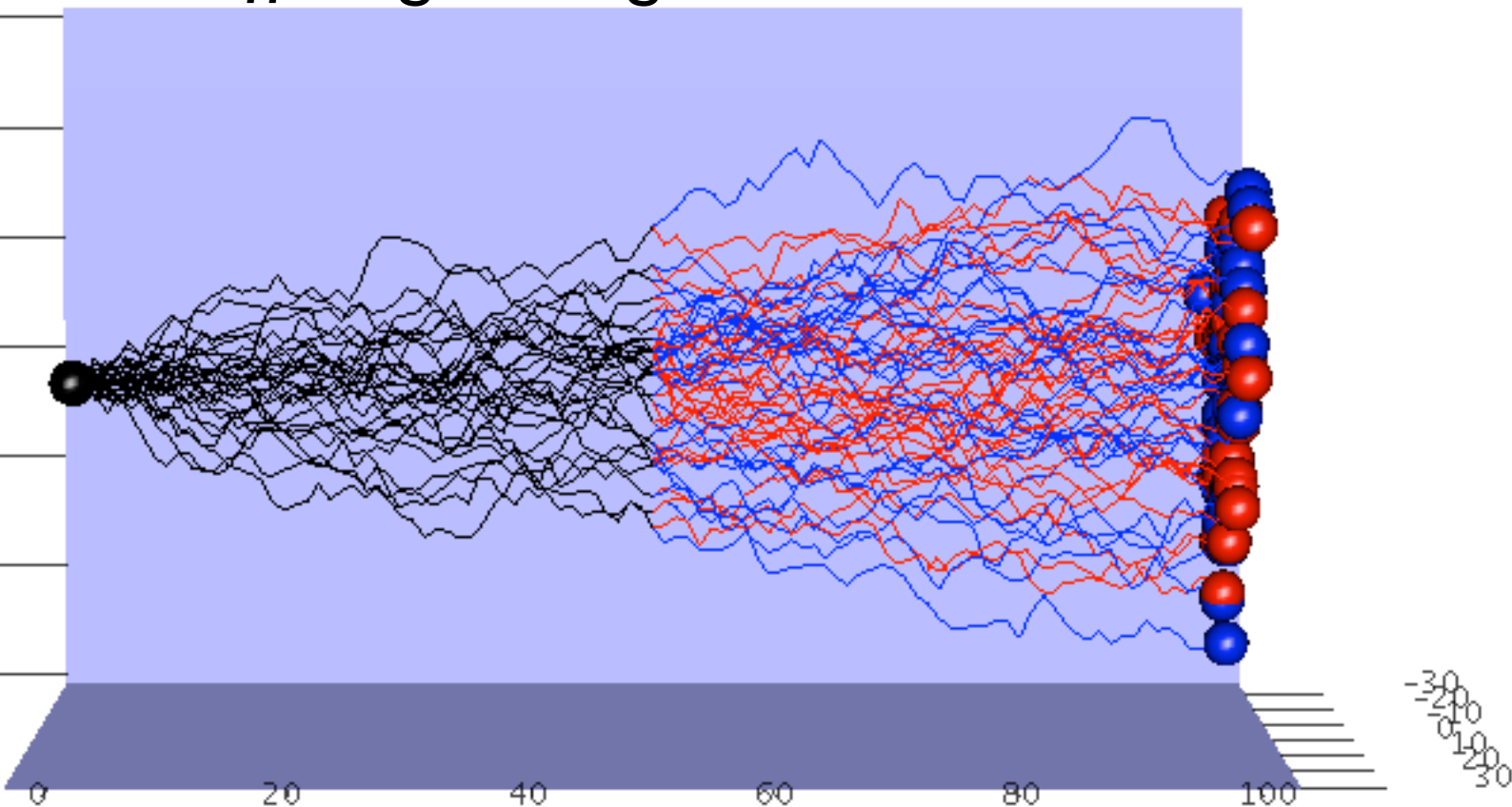


Illustrating the off-diagonal parameters

Correlated
“drift”

$$\alpha = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix} \quad \sigma = \begin{pmatrix} 10 & 0 \\ 5 & 10 \end{pmatrix}$$

add off-diagonal sigma term



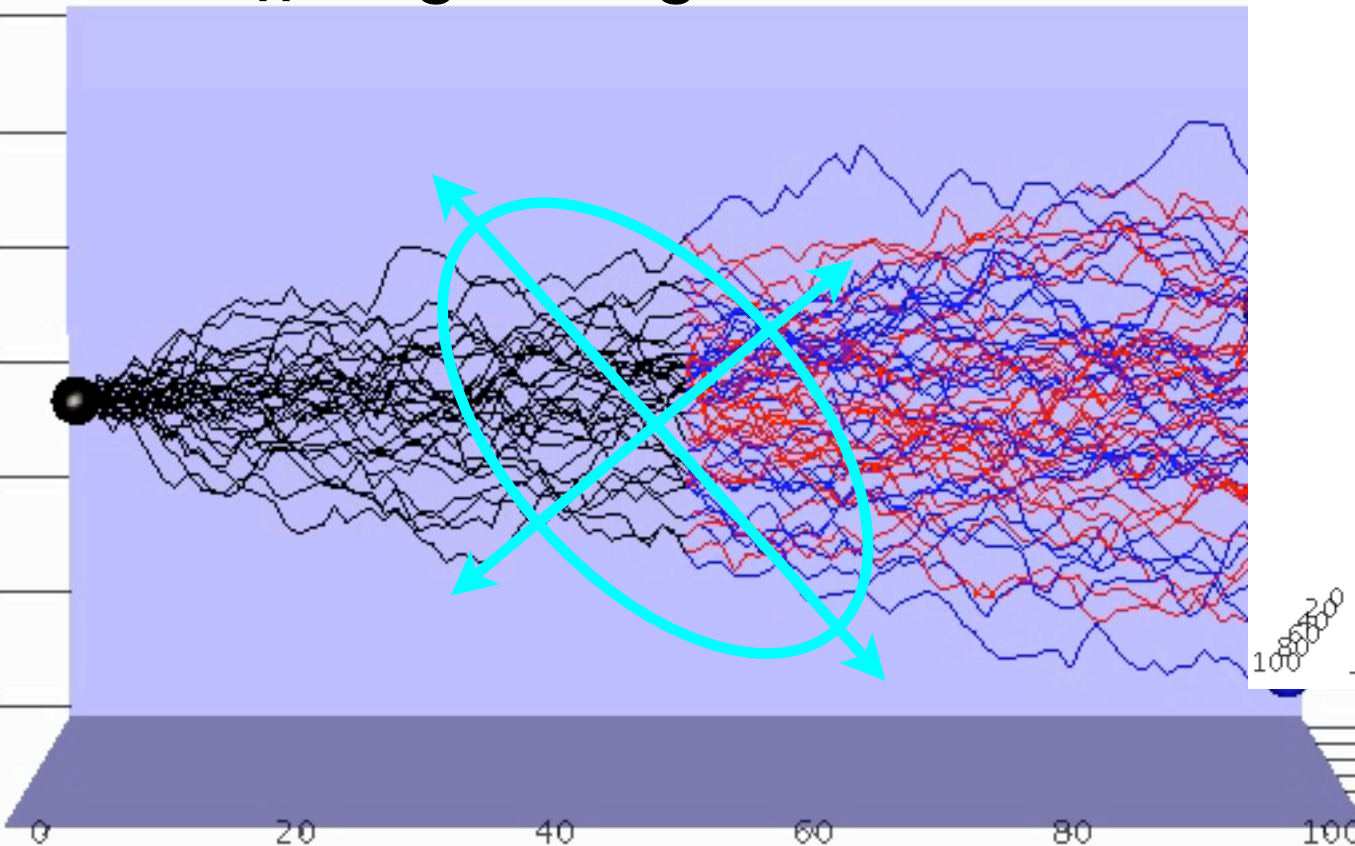
Illustrating the off-diagonal parameters

Correlated
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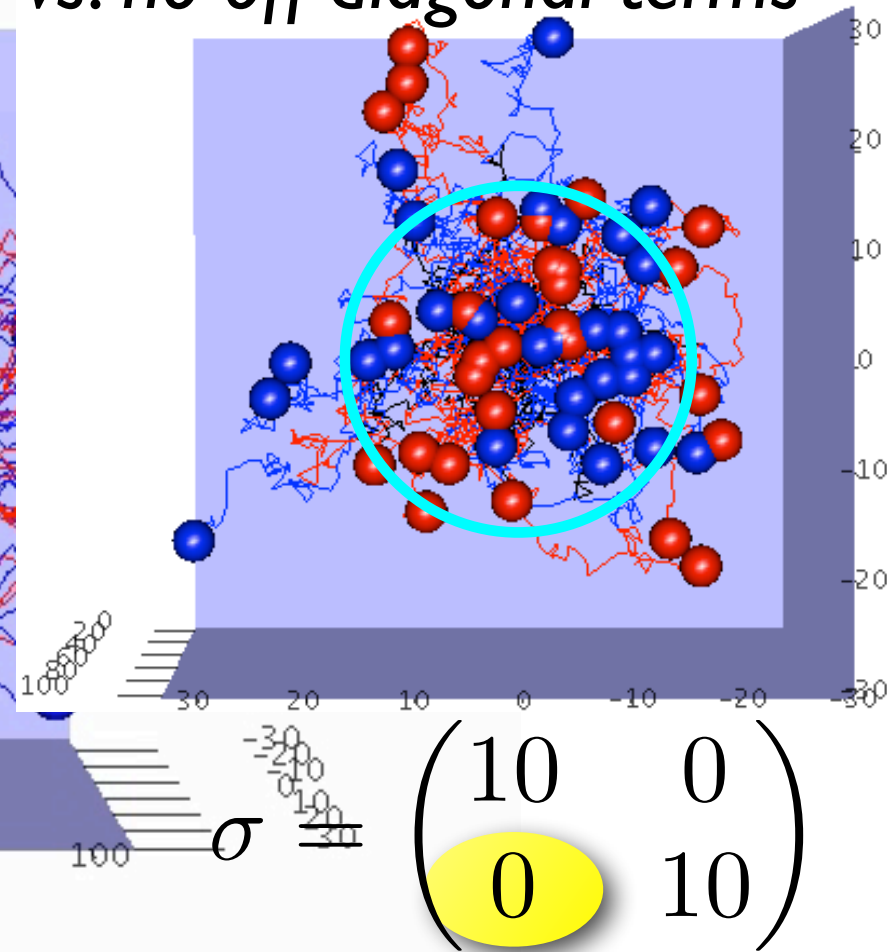
$$\alpha = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

$$\sigma = \begin{pmatrix} 10 & 0 \\ 5 & 10 \end{pmatrix}$$

add off-diagonal sigma term



vs. no off-diagonal terms



$$\sigma = \begin{pmatrix} 10 & 0 \\ 0 & 10 \end{pmatrix}$$

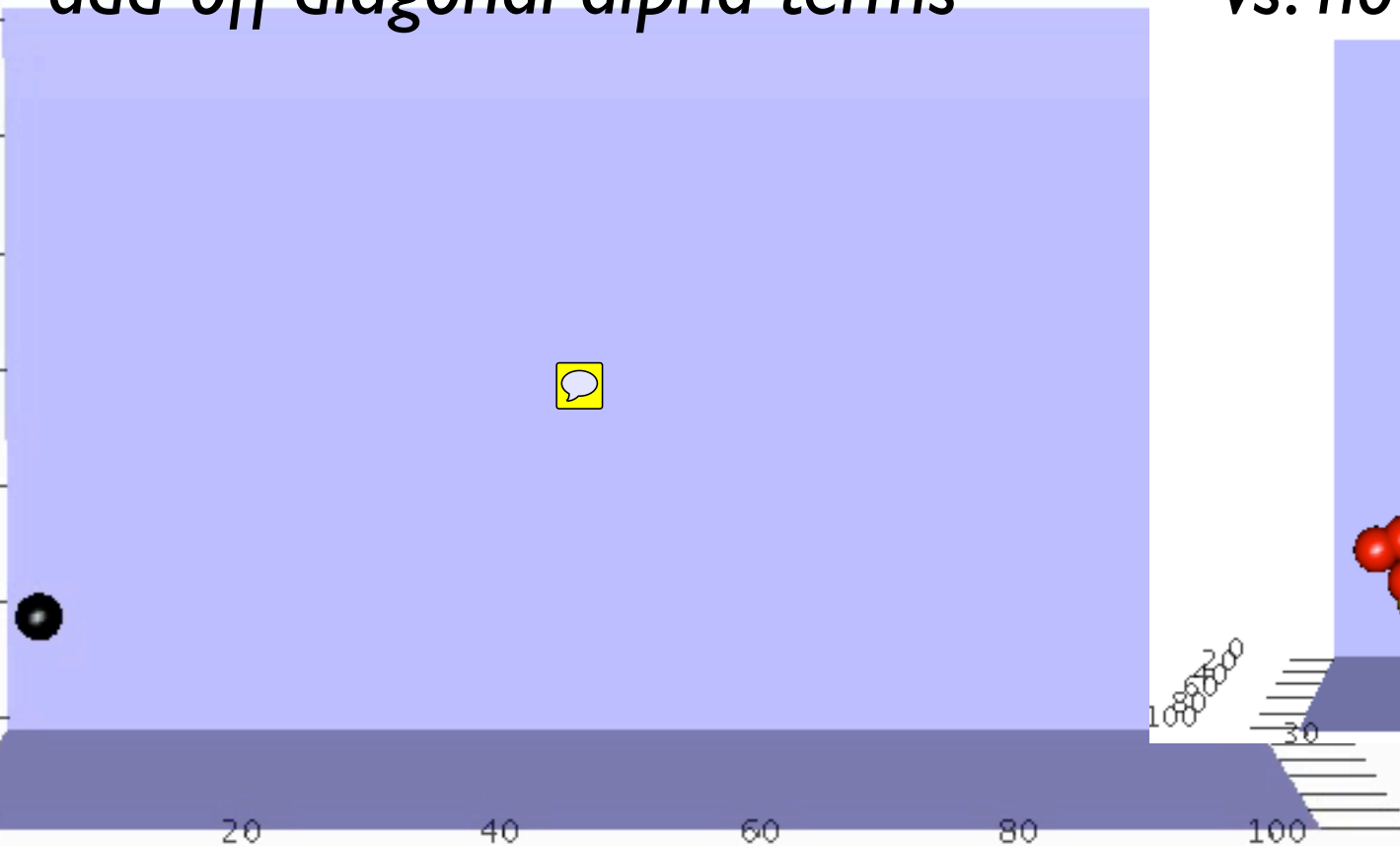
Illustrating the off-diagonal parameters

Correlated
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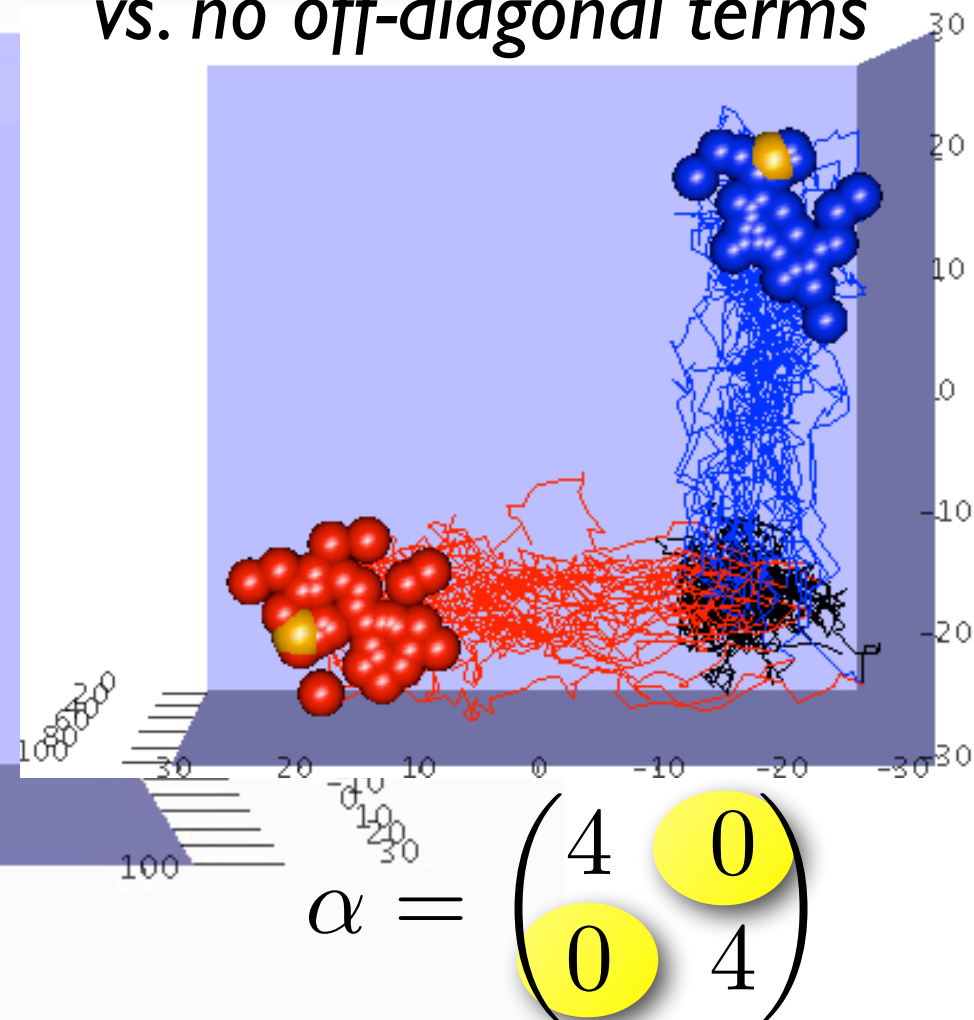
$$\alpha = \begin{pmatrix} 4 & 3 \\ 3 & 4 \end{pmatrix}$$

$$\sigma = \begin{pmatrix} 10 & 0 \\ 0 & 10 \end{pmatrix}$$

add off-diagonal alpha terms



vs. no off-diagonal terms

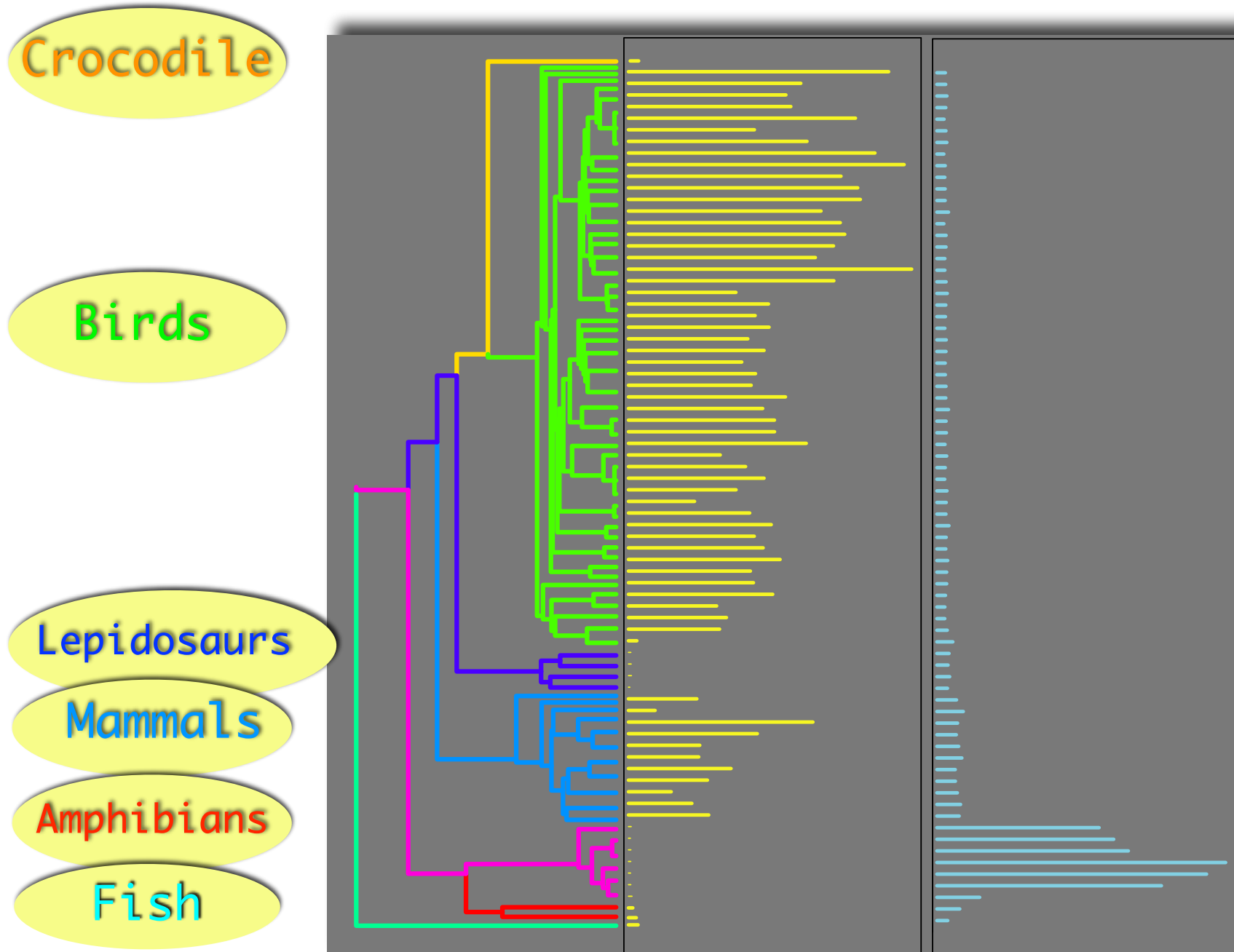


$$\alpha = \begin{pmatrix} 4 & 0 \\ 0 & 4 \end{pmatrix}$$

Back to our example

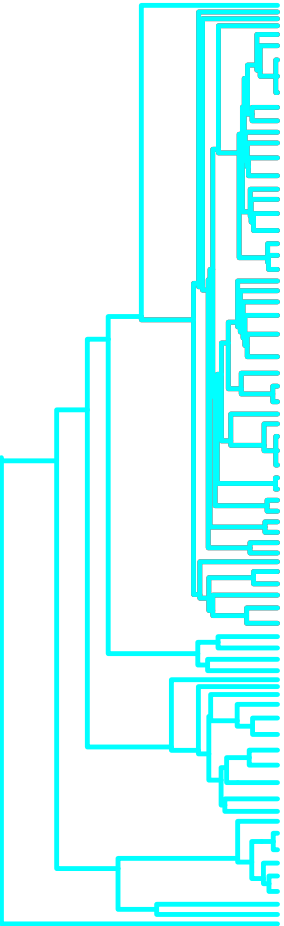
Basal Metabolic Rate and Genome Size

Waltari & Edwards 2002



Alternative Adaptive Regime Models

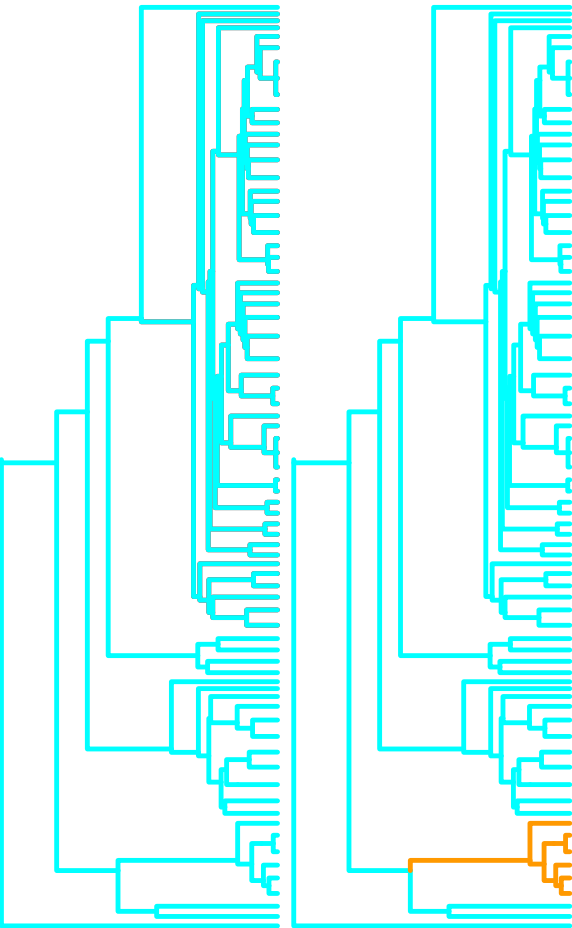
BM



Alternative Adaptive Regime Models

BM

Salamanders
Vertebrates

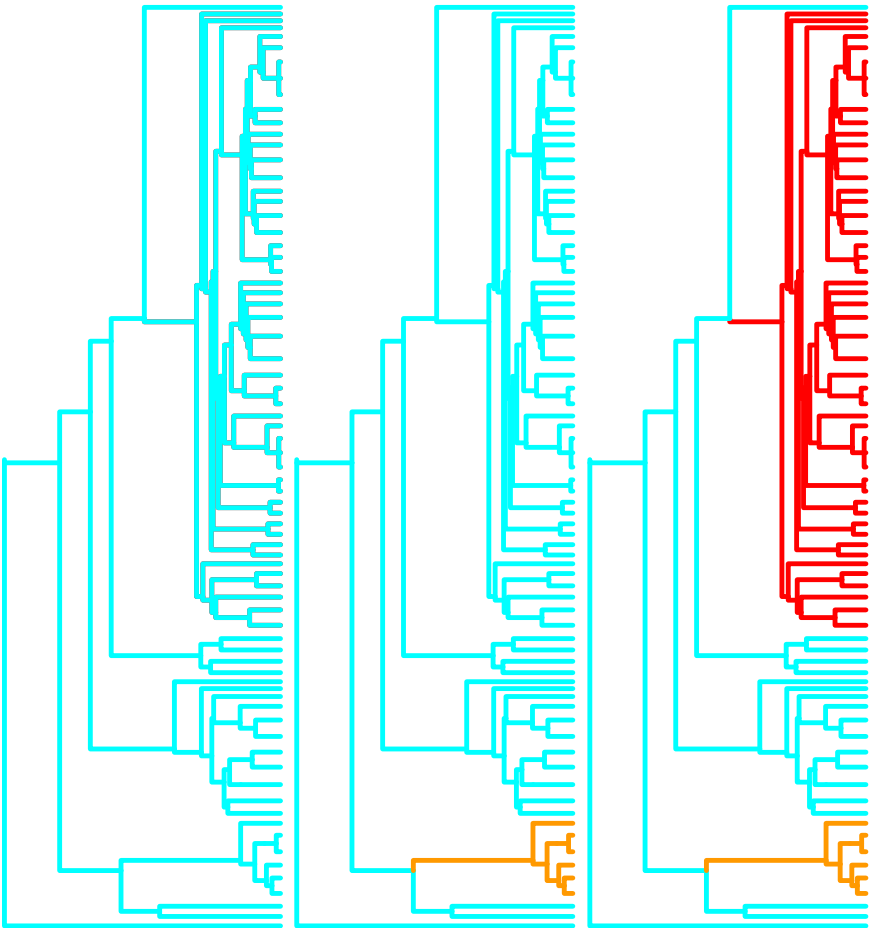


Alternative Adaptive Regime Models

BM

Salamanders
Vertebrates

Birds
Salamander
Vertebrates



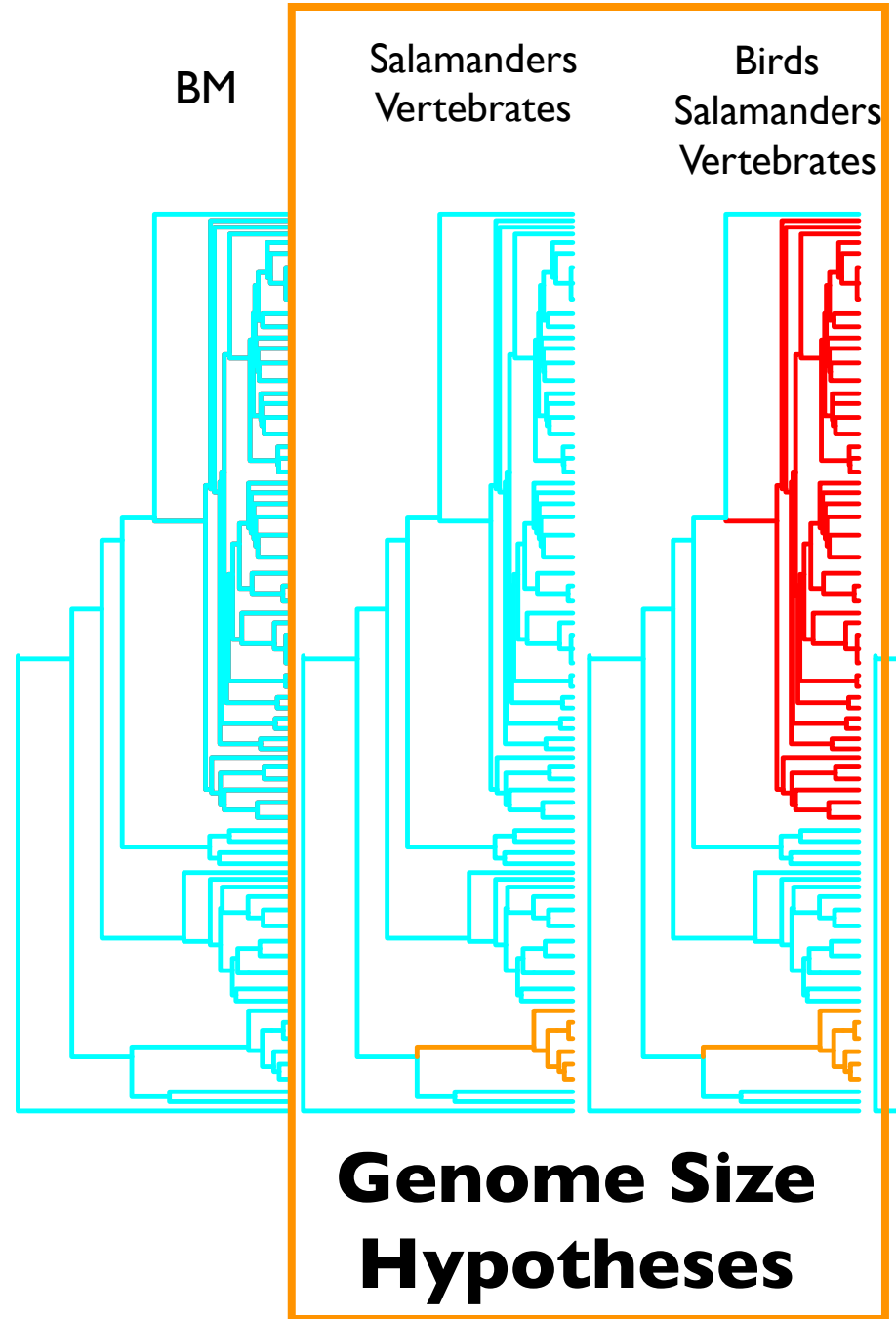
Alternative Adaptive Regime Models

BM

Salamanders
Vertebrates

Birds
Salamanders
Vertebrates

**Genome Size
Hypotheses**



Alternative Adaptive Regime Models

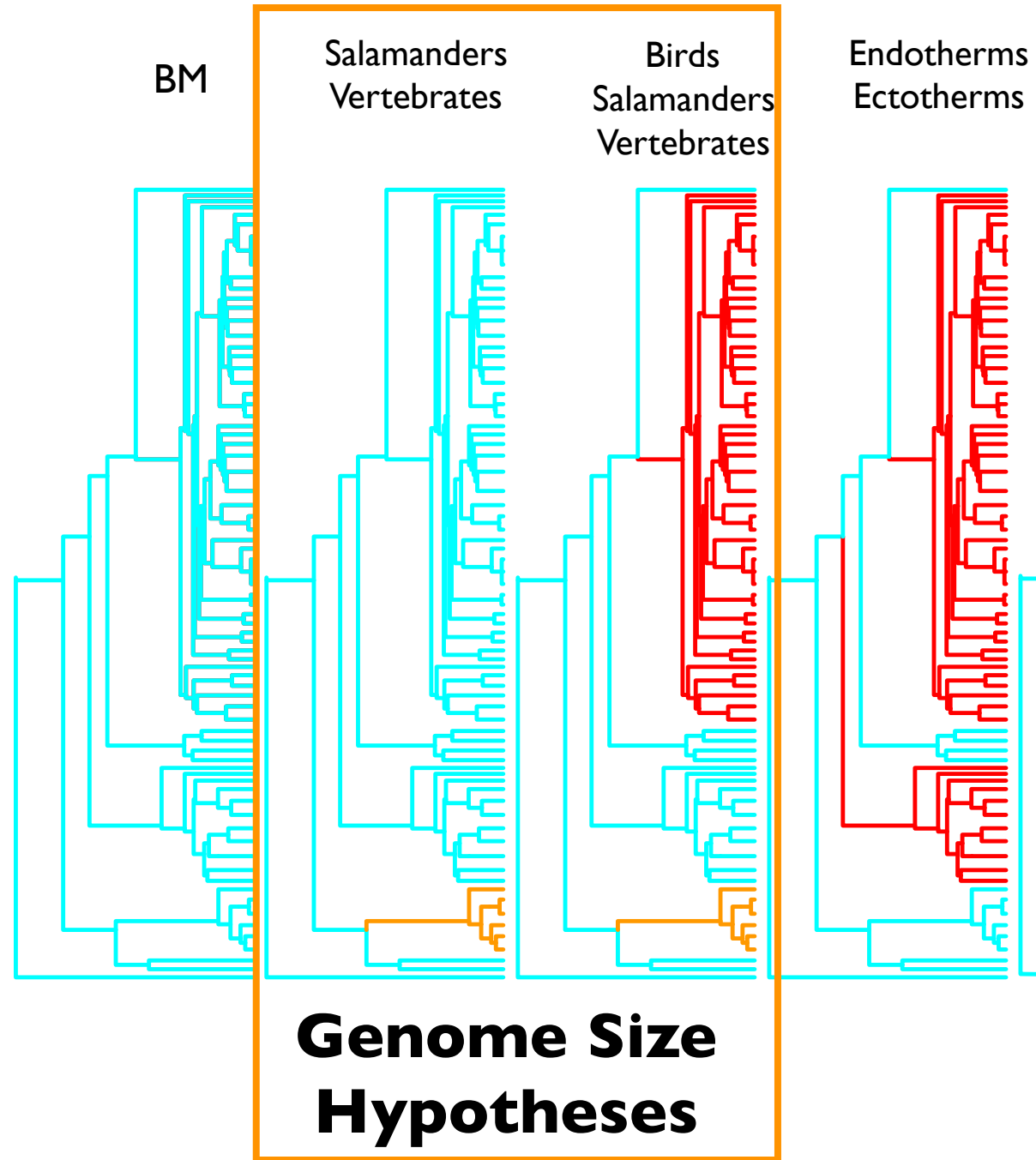
BM

Salamanders
Vertebrates

Birds
Salamanders
Vertebrates

Endotherms
Ectotherms

**Genome Size
Hypotheses**



Alternative Adaptive Regime Models

BM

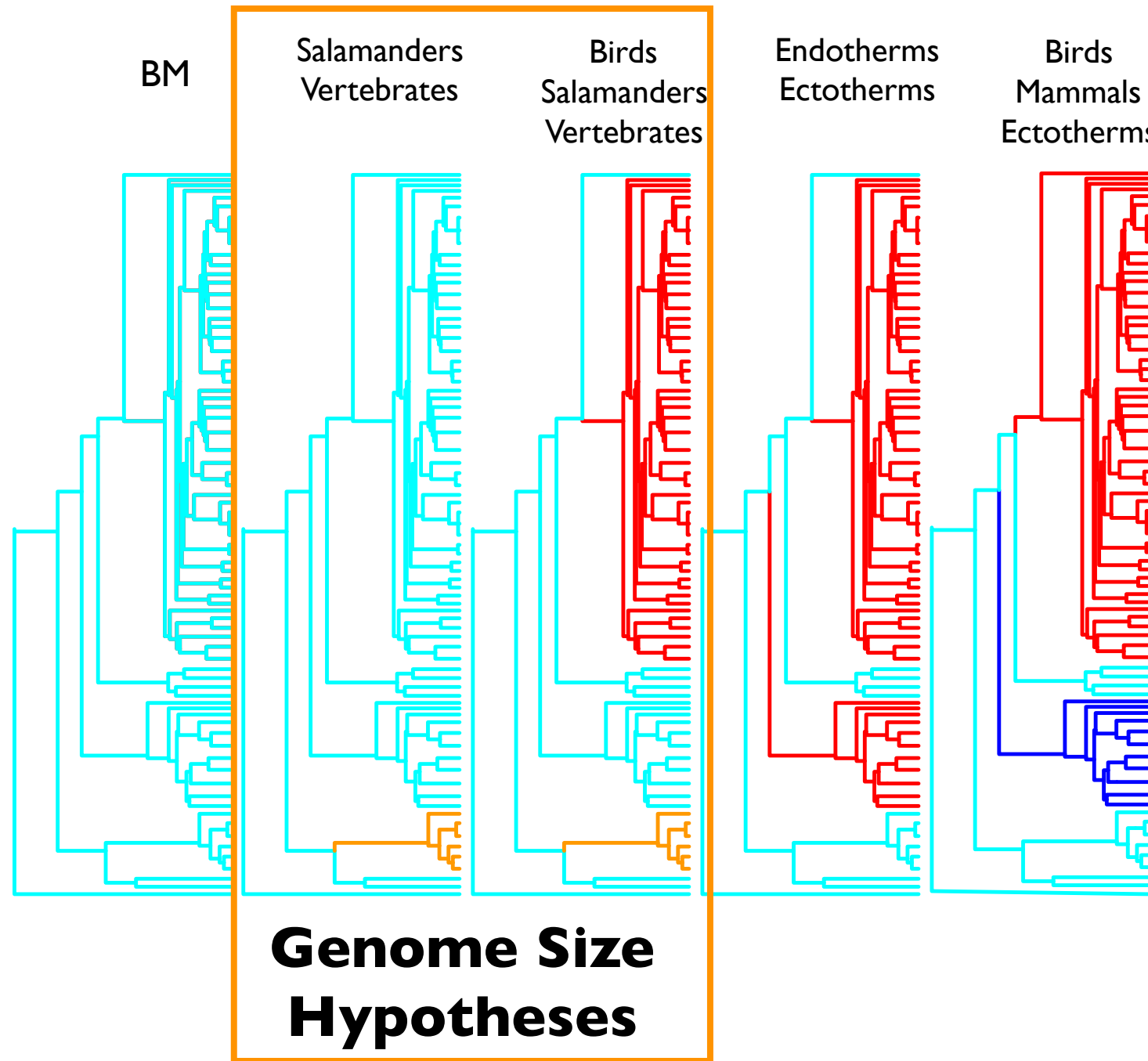
Salamanders
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Salamanders
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Birds
Mammals
Ectotherms

**Genome Size
Hypotheses**



Alternative Adaptive Regime Models

BM

Salamanders
Vertebrates

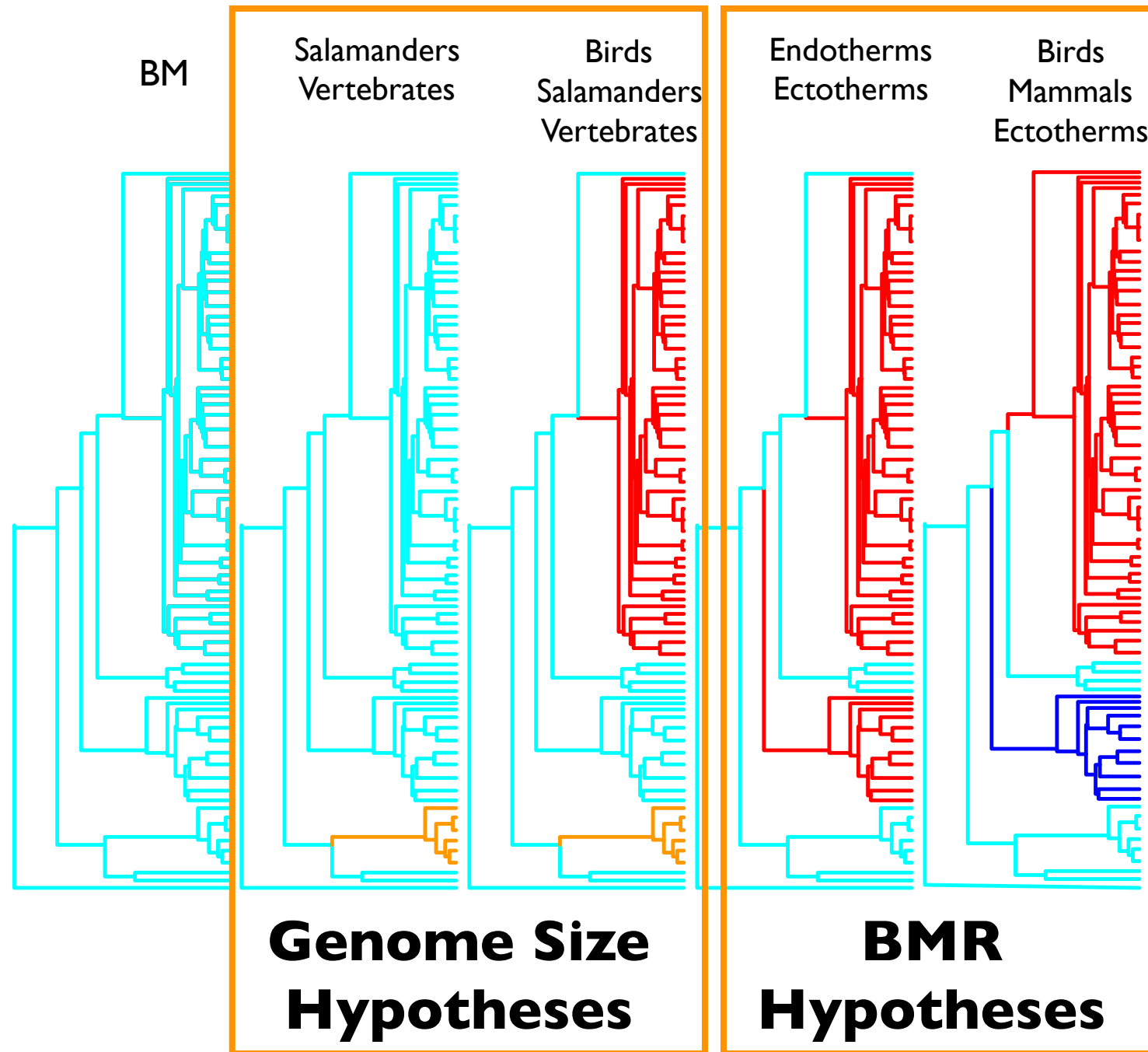
Birds
Salamanders
Vertebrates

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Birds
Mammals
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**Genome Size
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**BMR
Hypotheses**



Alternative Adaptive Regime Models

BM

Salamanders
Vertebrates

Birds
Salamanders
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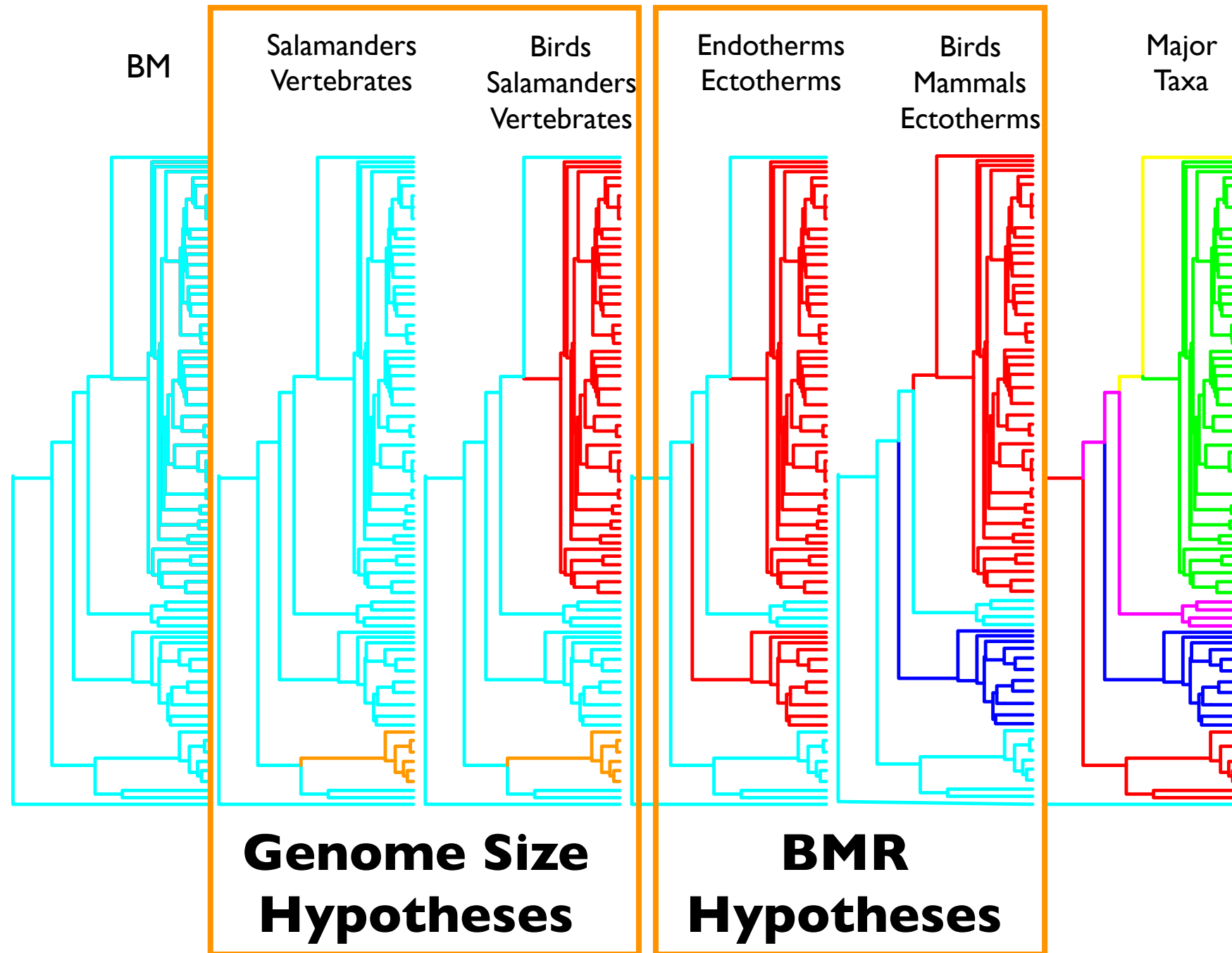
Endotherms
Ectotherms

Birds
Mammals
Ectotherms

Major
Taxa

**Genome Size
Hypotheses**

**BMR
Hypotheses**



Alternative Adaptive Regime Models

BM

Salamanders
Vertebrates

Birds
Salamanders
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Endotherms
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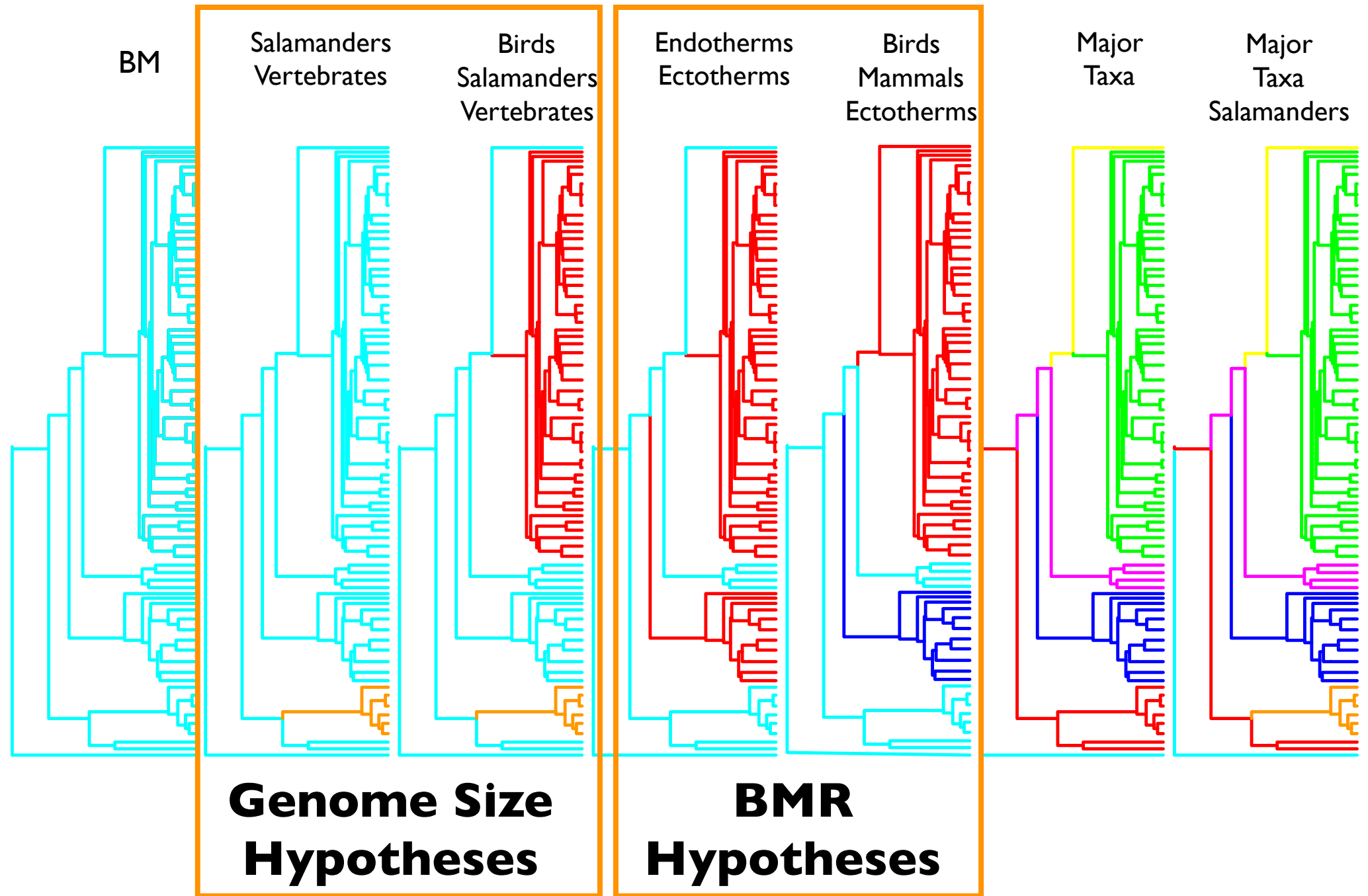
Birds
Mammals
Ectotherms

Major
Taxa

Major
Taxa
Salamanders

**Genome Size
Hypotheses**

**BMR
Hypotheses**



Alternative Adaptive Regime Models

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Vertebrates

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Salamanders
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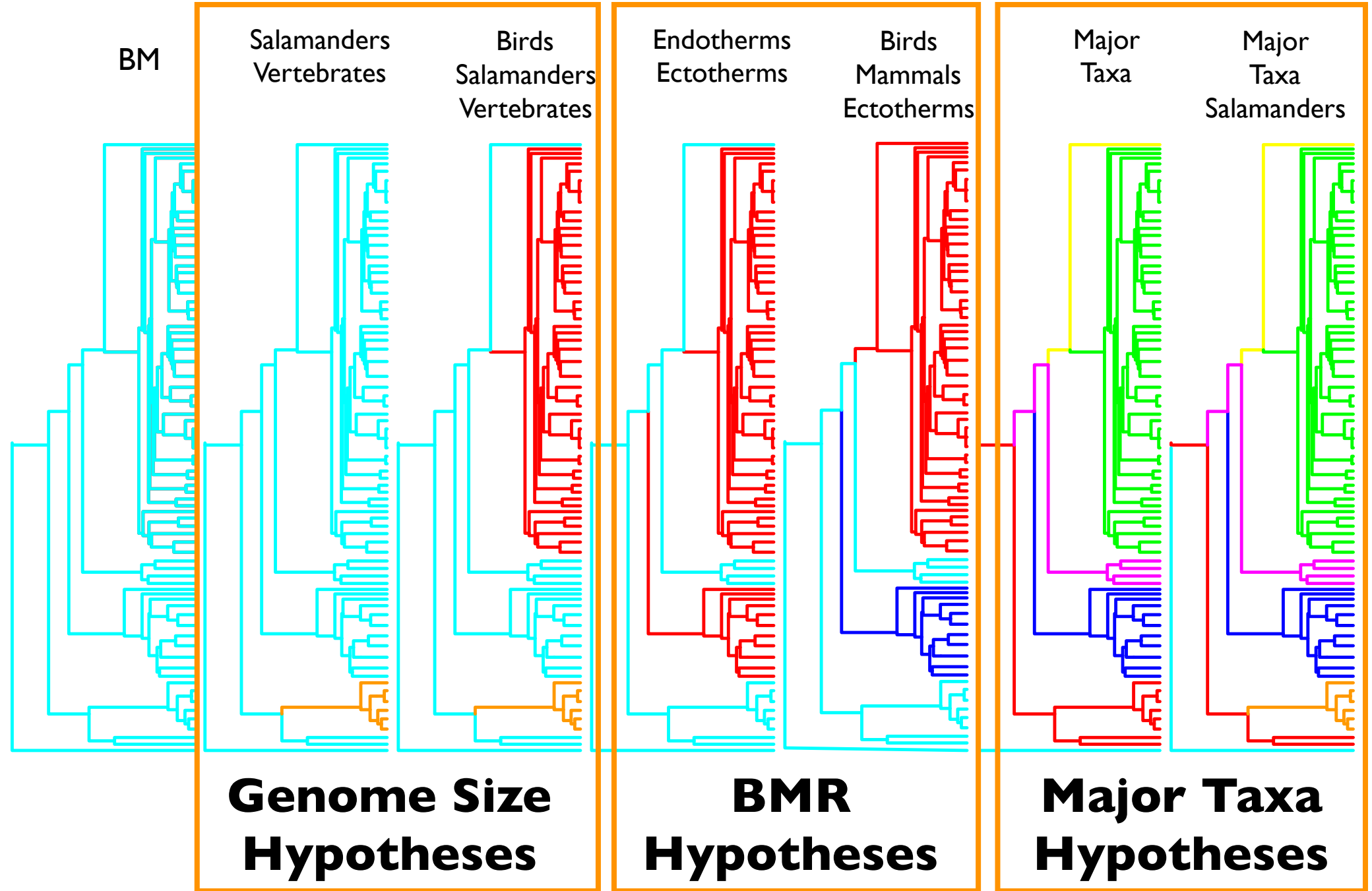
Major
Taxa

Major
Taxa
Salamanders

**Genome Size
Hypotheses**

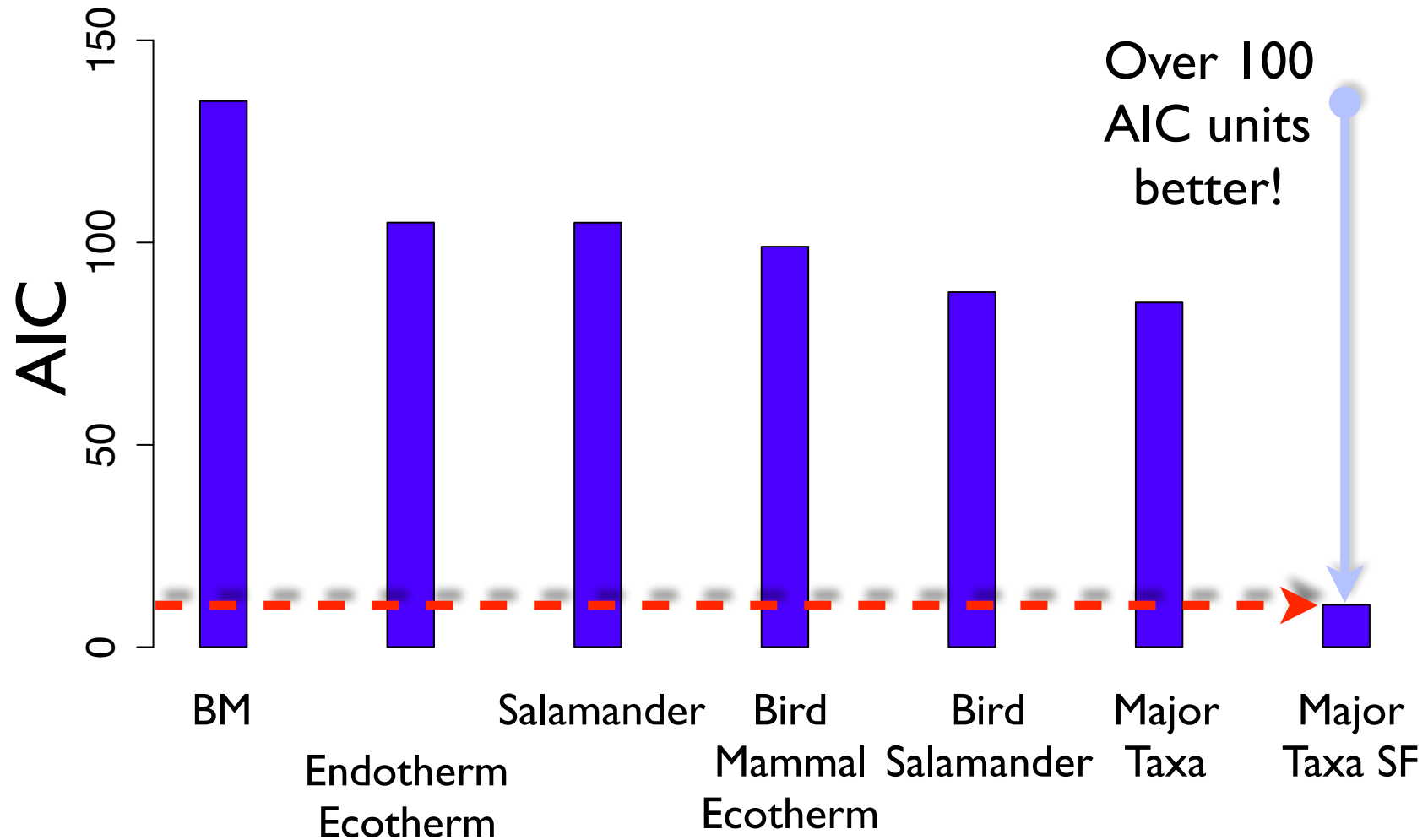
**BMR
Hypotheses**

**Major Taxa
Hypotheses**



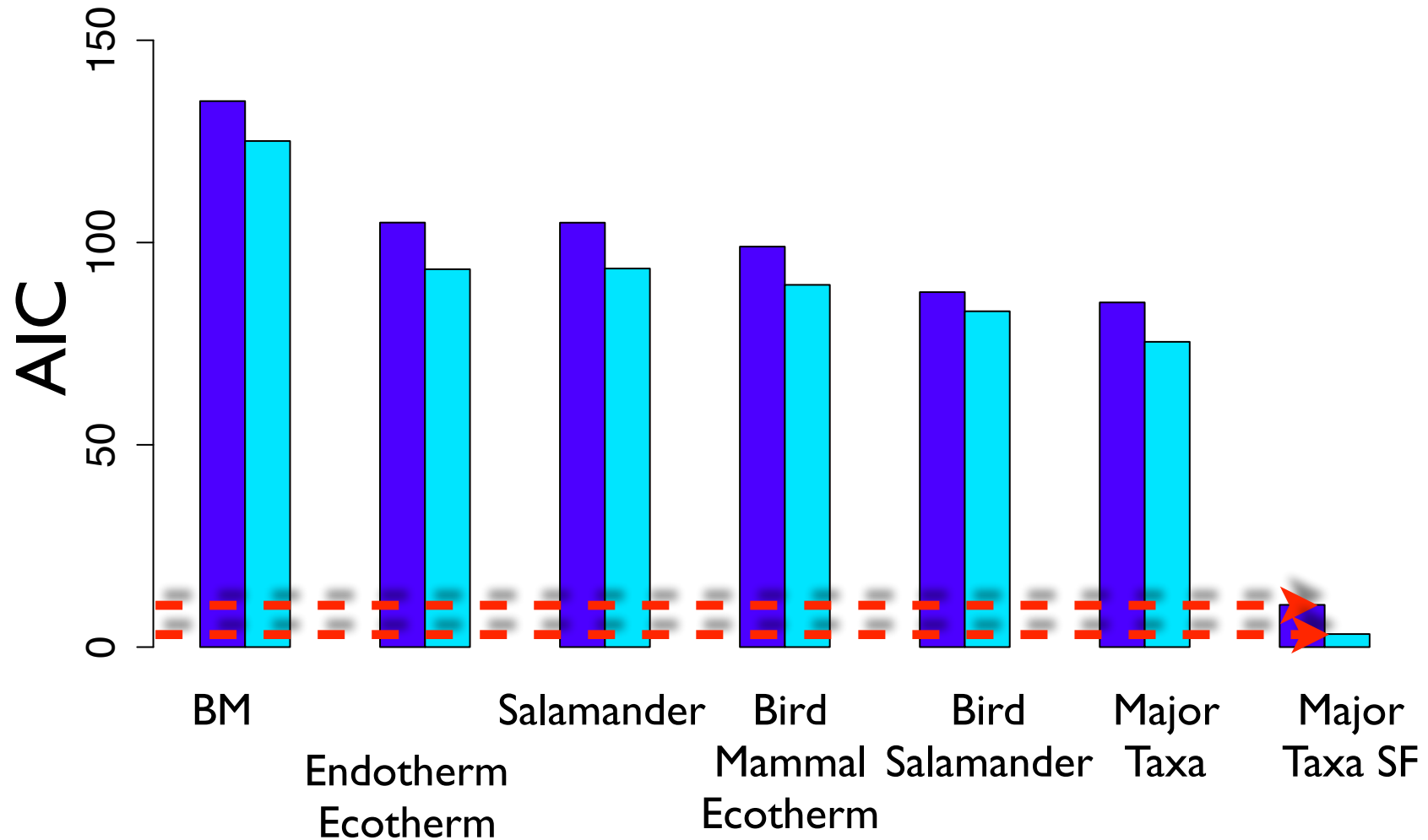
Separate adaptive regimes for each Major Taxon (splitting salamanders & frogs) was the Best Model

simplest bivariate model: no off-diagonal terms



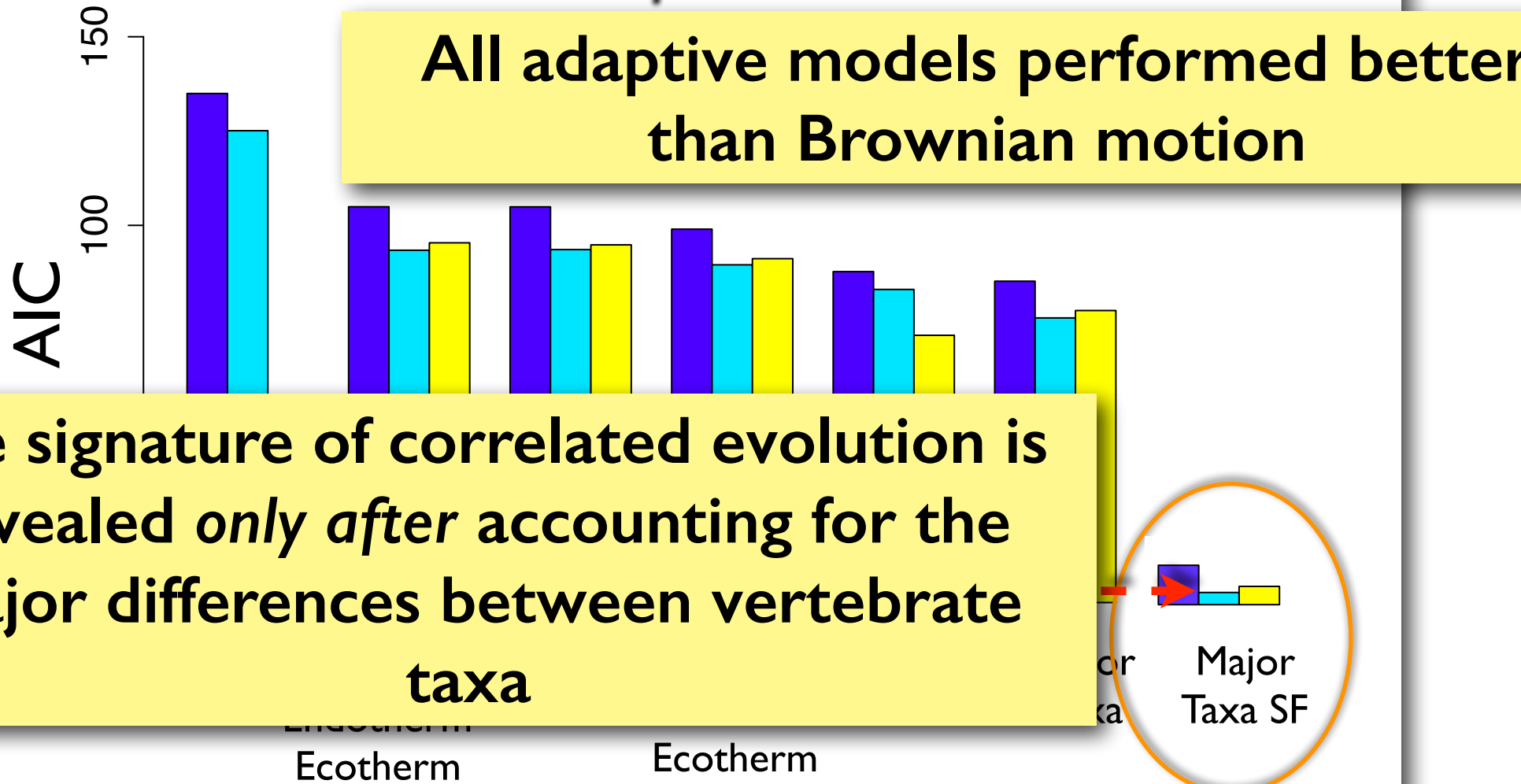
Separate adaptive regimes for each Major Taxon (splitting salamanders & frogs) was the Best Model

correlated drift: off-diagonal **sigmas** improve fit

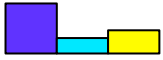


Separate adaptive regimes for each Major Taxon (splitting salamanders & frogs) was the Best Model

correlated drift: off-diagonal **sigmas** improve fit
but off-diagonal **alphas** do not



Results



Major
Taxa SF

Double
Univariate

$$\alpha = \begin{pmatrix} 38.1 & 0 \\ 0 & 4.7 \end{pmatrix} \quad \sigma = \begin{pmatrix} 1.2 & 0 \\ 0 & 1.0 \end{pmatrix}$$

Very strong selection, especially on Genome Size. Moderate drift.

Results



Major
Taxa SF

Off-diagonal sigmas improved the model

$$\alpha = \begin{pmatrix} 38.1 & 0 \\ 0 & 4.7 \end{pmatrix} \quad \sigma = \begin{pmatrix} 1.2 & 0 \\ 0 & 1.0 \end{pmatrix}$$

Correlated
“drift”

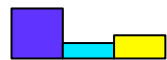
$$\alpha = \begin{pmatrix} 30.8 & 0 \\ 0 & 4.8 \end{pmatrix} \quad \sigma = \begin{pmatrix} 1.1 & 0 \\ -0.44 & 0.91 \end{pmatrix}$$

Correlated
“selection”
+ “drift”

$$\alpha = \begin{pmatrix} 33.5 & 1.5 \\ 1.5 & 4.8 \end{pmatrix} \quad \sigma = \begin{pmatrix} 1.1 & 0 \\ -0.35 & 0.93 \end{pmatrix}$$

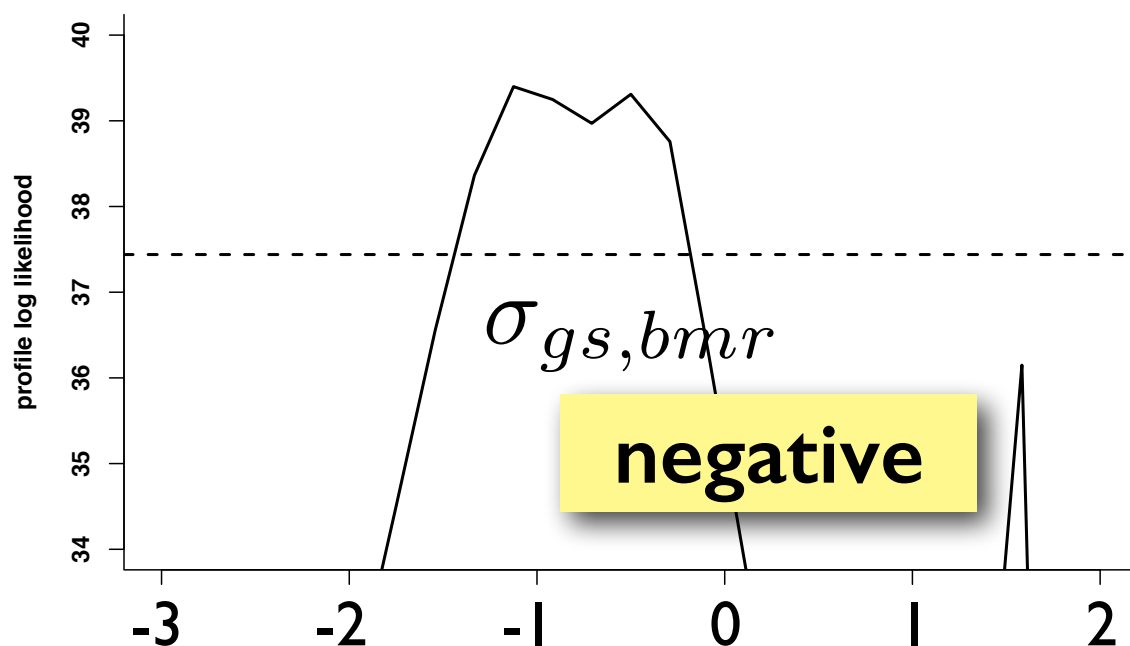
BUT off-diagonal alphas did not

Results



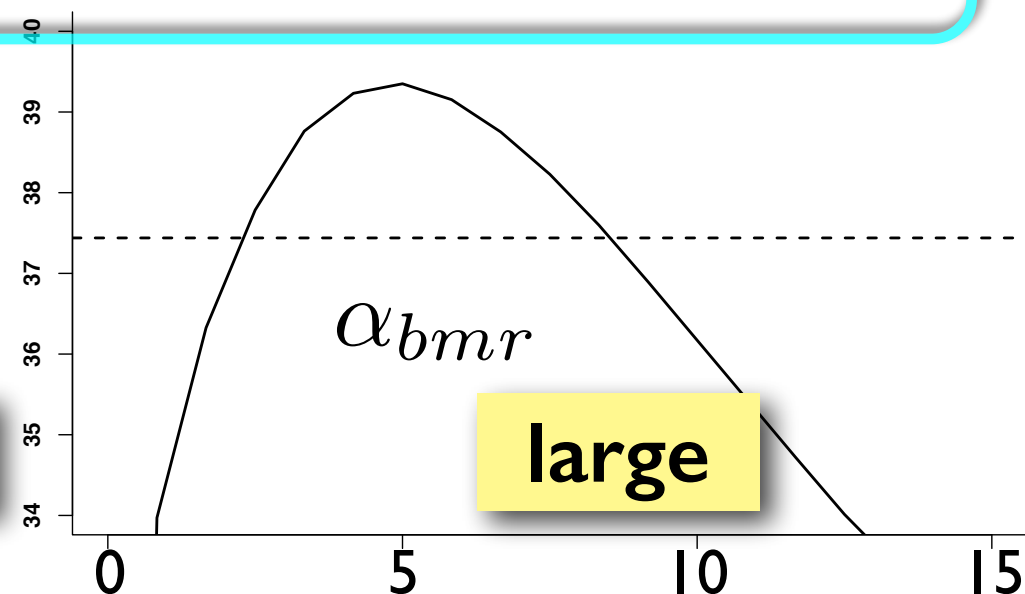
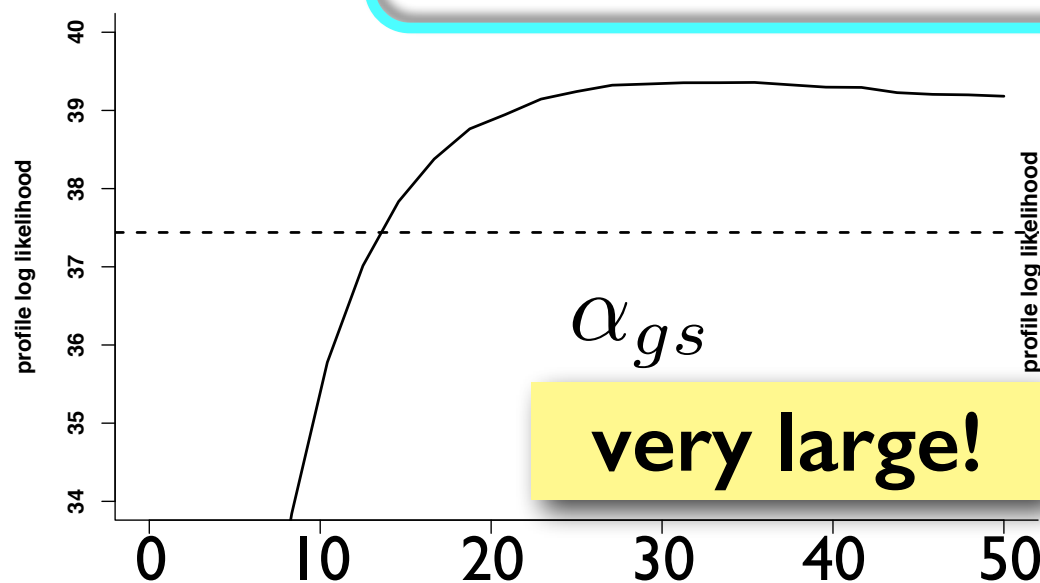
Major
Taxa SF

Profile Likelihoods for parameter estimates



Correlated
“drift”

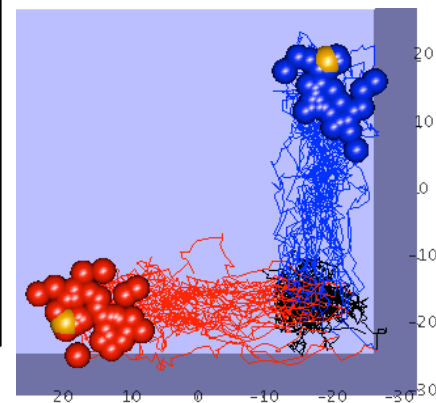
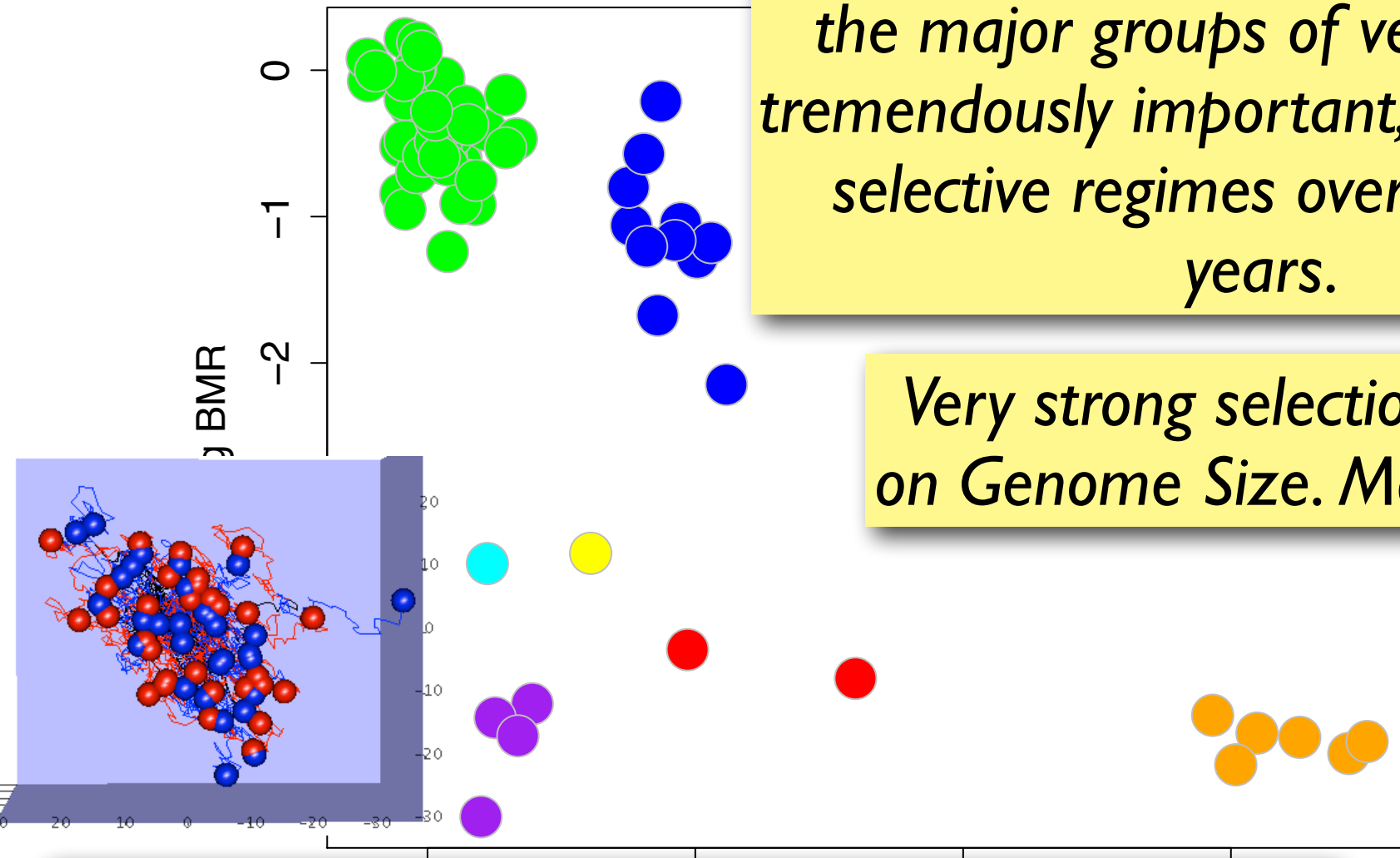
$$\alpha = \begin{pmatrix} 30.8 & 0 \\ 0 & 4.8 \end{pmatrix} \quad \sigma = \begin{pmatrix} 1.1 & 0 \\ -0.44 & 0.91 \end{pmatrix}$$



So... how to explain these data?

The stamp of history. The biology of the major groups of vertebrates is tremendously important, shaping their selective regimes over millions of years.

Very strong selection, especially on Genome Size. Moderate drift.



After accounting for major differences among taxa, strong signature of correlated evolution

But this looks like a lot of math.

I can already calculate statistically valid correlations.

What can modeling really do for me?

Only by being explicit can we see which elements of our evolutionary scenario are most important

selective
regimes

selection

drift

evolutionary correlation

Remember: Modeling is your friend.

What we are advocating is the method of multiple working hypotheses. the “best” model ?

it's about learning the most you can about your data

Some Papers

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National Science Foundation

Systematic Biology Panel (DEB 0515390 and DEB 0542360)



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ECOLOGY AND EVOLUTIONARY BIOLOGY



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