Lab_1 Problem 1.3: Test Assumptions

QUESTION: For the four following questions, your task is to evaluate the assumptions for the given test. It is not enough to say that an assumption is met or not met; instead, present your evidence in the form of background knowledge, visualizations, and numerical summaries. If you produce a histogram as part of your evaluation, be sure to consider what the most appropriate bin width is. The test that we ask you to evaluate may or may not be the most appropriate test for the scenario. Because the goal of this task is to evaluate whether the data satisfies the assumptions necessary for the test to provide meaningful results, you do not need perform the test (you may perform the test, but we will not be marking for the test results).

1.3.1 World Happiness

QUESTION: The file datasets/Happiness_WHR.csv is subsetted from the World Happiness Report, a yearly publication that uses data from the Gallup World Poll surveys. The variable life ladder is a measure of happiness, described in the FAQ as follows: This is called the Cantril ladder: it asks respondents to think of a ladder, with the best possible life for them being a 10, and the worst possible life being a 0. They are then asked to rate their own current lives on that 0 to 10 scale. The rankings are from nationally representative samples, for the years 2018-2020. You would like to know whether people in countries with high GDP per capita (higher than the mean) are more happy or less happy than people in countries with low GDP (lower than the mean).

Solution

Test Assumptions for a Two Sample t-Test

- 1. Metric scale (In particular, the t-test is not valid for variables which only have an ordinal structure)
- 2. IID data
- 3. No major deviations from normality, considering the sample size (In particular, the t-test is invalid for highly skewed distributions when sample size is larger than 30. It may also be invalid for very highly skewed distributions at higher sample sizes)

Metric Scale

Upon evaluating the dataset happinees_WHR.csv, although the evaluation was on a scale of 1-10, the Cantril Ladder is an example of a Likert Scale meaning that we have a non-metric scale. In other words the values used in the dataset rely upon opinion (qualitative measurement) rather than a quantitative measurement. Therefore a two sample t-test fails on this assumption. View the query below to get an understanding of the happinees_WHR.csv dataset.

```
librarv(readr)
happiness_WHR <- read_csv("happiness_WHR.csv")</pre>
## Rows: 239 Columns: 11
## — Column specification
## Delimiter: ","
## chr (1): Country name
## dbl (10): year, Life Ladder, Log GDP per capita, Social support, Healthy
lif...
##
## Use `spec()` to retrieve the full column specification for this data.
## U Specify the column types or set `show_col_types = FALSE` to quiet this
message.
summary(happiness WHR)
##
   Country name
                                      Life Ladder
                                                      Log GDP per capita
                           year
##
   Length:239
                      Min.
                              :2019
                                      Min.
                                             :2.375
                                                      Min. : 6.966
                                      1st Qu.:4.971
                                                      1st Qu.: 8.827
## Class:character
                      1st Qu.:2019
## Mode :character
                      Median :2019
                                     Median :5.768
                                                      Median : 9.669
##
                      Mean
                              :2019
                                      Mean
                                             :5.678
                                                      Mean
                                                            : 9.584
##
                       3rd Qu.:2020
                                      3rd Qu.:6.428
                                                      3rd Qu.:10.527
##
                      Max.
                             :2020
                                      Max.
                                             :7.889
                                                      Max.
                                                            :11.648
##
                                                      NA's
                                                             :13
                    Healthy life expectancy at birth Freedom to make life
## Social support
choices
## Min.
           :0.4200
                    Min.
                            :48.70
                                                      Min.
                                                             :0.3850
## 1st Ou.:0.7590
                    1st Ou.:62.00
                                                      1st Qu.:0.7360
## Median :0.8480
                    Median :67.20
                                                      Median :0.8220
## Mean
           :0.8256
                    Mean
                            :65.84
                                                      Mean
                                                             :0.8038
##
   3rd Qu.:0.9175
                     3rd Qu.:70.45
                                                      3rd Ou.:0.8910
## Max.
          :0.9830
                    Max.
                            :77.10
                                                      Max.
                                                             :0.9700
##
                    NA's
                                                      NA's
                            :8
                                                             :2
                       Perceptions of corruption Positive affect Negative
##
      Generosity
affect
           :-0.28900
                      Min.
                              :0.0700
                                                Min.
                                                                  Min.
## Min.
                                                        :0.3220
:0.0830
## 1st Qu.:-0.11900
                      1st Qu.:0.6470
                                                1st Qu.:0.6450
                                                                  1st
Qu.:0.2250
## Median :-0.04500
                      Median :0.7780
                                                Median :0.7330
                                                                  Median
:0.2830
## Mean
           :-0.01524
                      Mean
                              :0.7168
                                                Mean
                                                        :0.7149
                                                                  Mean
:0.2891
## 3rd Qu.: 0.07400
                       3rd Qu.:0.8480
                                                 3rd Qu.:0.7900
                                                                  3rd
Ou.:0.3440
## Max.
           : 0.56100
                      Max.
                             :0.9630
                                                Max.
                                                        :0.8910
                                                                  Max.
:0.5320
                      NA's
                                                 NA's :2
## NA's
           :14
                              :14
                                                                  NA's
                                                                         :2
```

IID Data

Based on background knowledge, given that each country is fairly independent of one another. There are no apparent violates of independents, some examples being clustering of data, in geographical regions, school cohorts, or families, strategical interaction, like competition among sellers or imitation of a species, or autocorrelation were one time period may affect the next. The data also appears to be identically distributed as will be shown in the plots below. This assumption for the data is meet, but as stated previously, a t-test would not be a wise test to use for a non-metric statistical analysis.

No Major Deviations from Normality

This assumption would not be met if the distribution was highly skewed for distributions when the sample size is larger than 30. While our data is slightly left skewed, it does not meet the criteria for highly skewed data and therefore this assumption is meet. Please see the histograms below

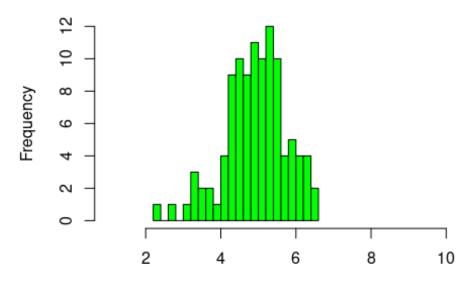
The steps taken here to create the histograms were to first separate the data based off of high and low GDP as done by splitting across the mean GDP of the given 239 countries.

```
m <- mean(happiness_WHR$`Log GDP per capita`, na.rm = TRUE)
h_GDP <- subset(happiness_WHR, subset = happiness_WHR$`Log GDP per capita` >
m)
l_GDP <- subset(happiness_WHR, subset = happiness_WHR$`Log GDP per capita` <
m)</pre>
```

Next, two histograms were made and show the left skewness of the distribution for high and low GDP countries.

```
hist(l_GDP$`Life Ladder`,
    main="Histogram for Happiness of Low GDP countries",
    xlab="Average Life Ladder Score per Country",
    col="green",
    xlim=c(1,10),
    breaks=15)
```

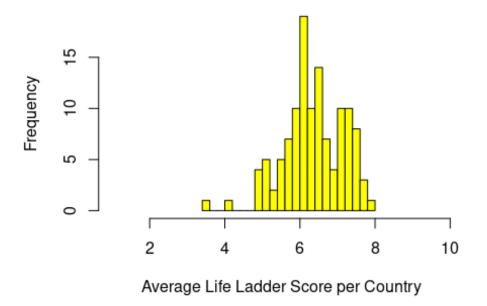
Histogram for Happiness of Low GDP countries



Average Life Ladder Score per Country

```
hist(h_GDP$`Life Ladder`,
    main="Histogram for Happiness of High GDP countries",
    xlab="Average Life Ladder Score per Country",
    col="yellow",
    xlim=c(1,10),
    breaks=20)
```

Histogram for Happiness of High GDP countries



Lastly, a simple unpaired t-test was run to see what the results would have been and given the p-value for this example, it would have been likely that the null hypothesis would have been rejected.

```
t.test(h_GDP$`Life Ladder`, l_GDP$`Life Ladder`)

##

## Welch Two Sample t-test

##

## data: h_GDP$`Life Ladder` and l_GDP$`Life Ladder`

## t = 13.251, df = 218.47, p-value < 2.2e-16

## alternative hypothesis: true difference in means is not equal to 0

## 95 percent confidence interval:

## 1.218086 1.643727

## sample estimates:

## mean of x mean of y

## 6.355488 4.924581</pre>
```

1.3.2: Legislators

QUESTION: The file datasets/legislators-current.csv is taken from the congress-legislators project on Github. You would like to test whether Democratic or Republican senators are older. List all assumptions for a Wilcoxon rank-sum test (using the Hypothesis of Comparisons). Then evaluate each assumption, presenting evidence based on your background knowledge, visualizations, and numerical summaries.

Solution

Test Assumptions for a Wilcoxon Rank-Sum Test (Hypothesis of Comparisons)

- 1. Ordinal Scale
- 2. IID Data

Null Hypothesis: The probability that a draw from *X* ranks higher than a draw from *Y* is the same as the probability that a draw from *Y* ranks higher than a draw from *X*.

$$P(X > Y) = P(X < Y)$$

Ordinal Scale

Based on background knowledge, ordinal scale measures data of categorical nature where ordered categories and the distances between the categories are not known. Since we are measuring age given by the birthday of each congressman in this analysis, and age would be considered a metric variable, this test would fail on this assumption and not be a viable option for statistical analysis. View a summary of the data below.

```
library(readr)
legislators current <- read csv("legislators-current.csv")</pre>
## Rows: 538 Columns: 34
## — Column specification
## Delimiter: "."
       (26): last name, first name, middle name, suffix, nickname,
## chr
full name, ...
         (6): district, senate class, cspan id, govtrack id, votesmart id,
## dbl
icps...
## lgl
         (1): washington post id
## date (1): birthday
##
## Use `spec()` to retrieve the full column specification for this data.
## I Specify the column types or set `show_col_types = FALSE` to quiet this
message.
summary(legislators current)
                                          middle name
##
    last name
                       first name
                                                                suffix
##
    Length:538
                       Length:538
                                          Length:538
                                                             Length:538
                                          Class :character
   Class :character
                       Class :character
                                                             Class :character
##
##
   Mode :character
                       Mode :character
                                          Mode :character
                                                             Mode :character
##
##
##
##
                        full name
                                             birthday
##
     nickname
                                                                  gender
```

## ##	Length:538 Class :character aracter	Length:538 Class :character	Min. :1933-06-09 1st Qu.:1953-03-30	•
		Mada ishanastan	Madian .1061 02 05	Mada
##	Mode :character	Mode :character	Median :1961-03-05	Mode
	aracter		Maria 1001 11 20	
##			Mean :1961-11-29	
##			3rd Qu.:1970-08-14	
##			Max. :1995-08-01	
##				
##	type	state		senate_class
##	Length:538	Length:538	Min. : 0.000 M	in. :1.00
##	Class :character	Class :character	1st Qu.: 3.000 1	st Qu.:1.00
##	Mode :character	Mode :character	Median : 6.000 M	edian :2.00
##			Mean : 9.984 M	ean :2.01
##			3rd Qu.:13.000 3	rd Qu.:3.00
##				ax. :3.00
##				A's :438
##	party	url	address	phone
##	Length:538	Length:538	Length:538	Length:538
##	Class :character		Class :character	
##	Mode :character	Mode :character	Mode :character	Mode :character
##	rioue .character	Houe .character	Houe .character	riode . Character
##				
##				
##				
	contact form	ncc unl	+,,;++,,,	facebook
## ##	contact_form	rss_url	twitter	
##			1 ana+h • F 2 0	
	Length:538	Length:538	Length:538	Length:538
##	Class :character	Class :character	Class :character	Class :character
## ##	_			_
## ## ##	Class :character	Class :character	Class :character	Class :character
## ## ## ##	Class :character	Class :character	Class :character	Class :character
## ## ## ##	Class :character	Class :character	Class :character	Class :character
## ## ## ## ##	Class :character Mode :character	Class :character Mode :character	Class :character Mode :character	Class :character Mode :character
## ## ## ##	Class :character Mode :character youtube	Class :character Mode :character youtube_id	Class :character Mode :character bioguide_id	Class :character Mode :character thomas_id
## ## ## ## ##	Class :character Mode :character youtube Length:538	Class :character Mode :character	Class :character Mode :character bioguide_id Length:538	Class :character Mode :character thomas_id Length:538
## ## ## ## ##	Class :character Mode :character youtube	Class :character Mode :character youtube_id	Class :character Mode :character bioguide_id	Class :character Mode :character thomas_id
## ## ## ## ## ##	Class :character Mode :character youtube Length:538	Class:character Mode:character youtube_id Length:538	Class :character Mode :character bioguide_id Length:538	Class :character Mode :character thomas_id Length:538
## ## ## ## ## ##	Class :character Mode :character youtube Length:538 Class :character	Class:character Mode:character youtube_id Length:538 Class:character	Class :character Mode :character bioguide_id Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character
## ## ## ## ## ## ##	Class :character Mode :character youtube Length:538 Class :character	Class:character Mode:character youtube_id Length:538 Class:character	Class :character Mode :character bioguide_id Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character
## ## ## ## ## ## ## ##	Class :character Mode :character youtube Length:538 Class :character	Class:character Mode:character youtube_id Length:538 Class:character	Class :character Mode :character bioguide_id Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character
## ## ## ## ## ## ## ## ## ##	Class :character Mode :character youtube Length:538 Class :character	Class:character Mode:character youtube_id Length:538 Class:character	Class :character Mode :character bioguide_id Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character
## ## ## ## ## ## ## ## ## ## ## ## ##	Class :character Mode :character youtube Length:538 Class :character Mode :character	Class :character Mode :character youtube_id Length:538 Class :character Mode :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character	Class :character Mode :character thomas_id Length:538 Class :character Mode :character
## ###################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id	Class :character Mode :character youtube_id Length:538 Class :character Mode :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id
######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538	Class:character Mode:character youtube_id Length:538 Class:character Mode:character lis_id Length:538	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id Min. : 260
######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538 Class :character	Class :character Mode :character youtube_id Length:538 Class :character Mode :character lis_id Length:538 Class :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id Min. : 260 1st Qu.: 45591
######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538	Class:character Mode:character youtube_id Length:538 Class:character Mode:character lis_id Length:538	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id Min. : 260 1st Qu.: 45591 Median : 79718
#######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538 Class :character	Class :character Mode :character youtube_id Length:538 Class :character Mode :character lis_id Length:538 Class :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id Min. : 260 1st Qu.: 45591 Median : 79718 Mean : 543374
#######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538 Class :character	Class :character Mode :character youtube_id Length:538 Class :character Mode :character lis_id Length:538 Class :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538 Class :character	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id Min. : 260 1st Qu.: 45591 Median : 79718 Mean : 543374 3rd Qu.:1003305
#######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538 Class :character	Class :character Mode :character youtube_id Length:538 Class :character Mode :character lis_id Length:538 Class :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538 Class :character	cspan_id Min. : 260 1st Qu.: 45591 Median : 79718 Mean : 543374 3rd Qu.:1003305 Max. :9275683
#######################################	Class :character Mode :character youtube Length:538 Class :character Mode :character opensecrets_id Length:538 Class :character	Class :character Mode :character youtube_id Length:538 Class :character Mode :character lis_id Length:538 Class :character Mode :character Mode :character	Class :character Mode :character bioguide_id Length:538 Class :character Mode :character fec_ids Length:538 Class :character Mode :character	Class :character Mode :character thomas_id Length:538 Class :character Mode :character cspan_id Min. : 260 1st Qu.: 45591 Median : 79718 Mean : 543374 3rd Qu.:1003305

```
## Min. :300018
                    Min. : 119
                                    Length:538
                                                      Mode:logical
                    1st Qu.: 22411
                                                      NA's:538
## 1st Qu.:412199
                                    Class :character
                    Median : 52964
                                    Mode :character
## Median :412570
## Mean
         :412042
                    Mean : 75411
   3rd Qu.:412772
                    3rd Qu.:133024
##
##
          :456862
   Max.
                    Max.
                           :188334
##
                    NA's
                           :62
##
      icpsr_id
                   wikipedia_id
## Min.
         :14066
                   Length:538
##
   1st Qu.:21106
                   Class :character
## Median :21564
                   Mode :character
## Mean
          :24264
##
   3rd Qu.:21972
## Max.
          :94659
## NA's
          :77
```

IID Data

For this assumption, each X_i has to be drawn from the same distribution, each Y_i has to be drawn from the same distribution, and all X_i and Y_i are mutually independent. There are no apparent violates of independents, some examples being clustering of data, in geographical regions, school cohorts, or families, strategical interaction, like competition among sellers or imitation of a species, or autocorrelation were one time period may affect the next. The data also appears to be identically distributed as will be shown in the plots below. This assumption for the data is meet, but as stated previously, the Hypothesis of Comparison version of the Wilcoxon Rank-Sum would not be a wise test to use for a metric statistical analysis.

For the analysis of this dataset, a simple extraction of the each congressmen's birthyear subtracted from the current year yields their age.

```
a <- as.POSIXct(legislators_current$birthday, format = "%Y-%m-%d")
year <- strtoi(format(a, format = "%Y"))
legislators_current$year = year
legislators_current$age <- 2021 - legislators_current$year</pre>
```

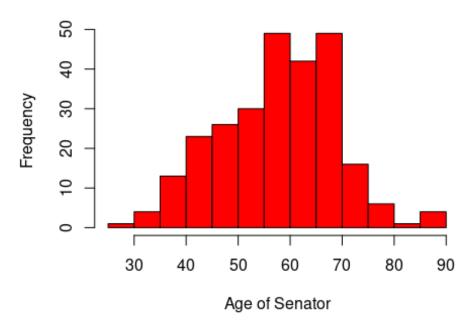
Next, subsetting the data by Republicans and Democrats in rep and dem respectively.

```
legislators_current$party[legislators_current$party == 'Independent'] = NA
rep <- subset(legislators_current, subset = legislators_current$party ==
"Republican")
dem <- subset(legislators_current, subset = legislators_current$party ==
"Democrat")</pre>
```

And finally, plotting the resulting of ages for Republicans and Democrats.

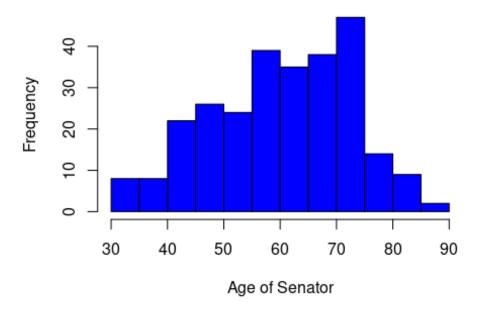
```
hist(rep$age,
    main="Histogram for Age of Republican Congressmen",
    xlab="Age of Senator",
    col="red",
    breaks=15)
```

Histogram for Age of Republican Congressmen



```
hist(dem$age,
    main="Histogram for Age of Democrat Congressmen",
    xlab="Age of Senator",
    col="blue",
    breaks=15)
```

Histogram for Age of Democrat Congressmen



And Finally below, I have the Wilcoxon Rank-Sum Test. I'm not sure how to make sure that I'm evaluting the Hypothesis of Comparison version, nevertheless, this version would not be the correct hypothesis test to run because of the failed assumption.

```
wilcox.test(rep$age, dem$age)
##
## Wilcoxon rank sum test with continuity correction
##
## data: rep$age and dem$age
## W = 31022, p-value = 0.006447
## alternative hypothesis: true location shift is not equal to 0
```

1.3.3 Wine and Health

QUESTION: The dataset wine can be accessed by installing the wooldridge package. install.packages("wooldridge") library(wooldridge) ?wine wine It contains observations of variables related to wine consumption for 21 countries. You would like to use this data to test whether countries have more deaths from heart disease or from liver disease. List all assumptions for a signed-rank test. Then evaluate each assumption, presenting evidence based on your background knowledge, visualizations, and numerical summaries.

Solution

Test Assumptions for Wilcoxon Signed-Rank Test

- 1. Metric Scale
- 2. IID Data
- 3. The distribution of the difference (X Y) is symmetric around the same mean.

Metric Sacle

Based on background knowledge, the X and Y measured here have to be measured on the same scale since we are using a paired test. For this question, both the liver and heart deaths are on the same scale of 100,000 deaths. This will be shown in the dataset below.

```
install.packages("wooldridge")
## Installing package into '/usr/local/lib/R/site-library'
## (as 'lib' is unspecified)
library(wooldridge)
?wine
wine
##
           country alcohol deaths heart liver
## 1
         Australia
                        2.5
                               785
                                      211
                                           15.3
           Austria
## 2
                        3.9
                               863
                                      167
                                          45.6
## 3
          Belg/Lux
                        2.9
                                      131 20.7
                               883
## 4
            Canada
                        2.4
                               793
                                      191
                                           16.4
## 5
                        2.9
                                      220 23.9
           Denmark
                               971
## 6
           Finland
                        0.8
                               970
                                      297
                                           19.0
## 7
            France
                        9.1
                               751
                                       71 37.9
## 8
           Iceland
                        0.8
                               743
                                      211
                                          11.2
                                            6.5
## 9
           Ireland
                        0.7
                              1000
                                      300
## 10
            Israel
                        0.6
                               834
                                      183
                                           13.7
                        7.9
## 11
             Italy
                               775
                                      107
                                          42.2
                                       36
## 12
                        1.5
                                           23.2
             Japan
                               680
## 13
       Netherlands
                        1.8
                               773
                                      167
                                            9.2
                        1.9
## 14
       New Zealand
                               916
                                      266
                                            7.7
## 15
            Norway
                        0.8
                               806
                                      227
                                          12.2
## 16
             Spain
                        6.5
                               724
                                       86 36.4
## 17
            Sweden
                        1.6
                               743
                                      207
                                           11.2
## 18
       Switzerland
                        5.8
                               693
                                      115
                                           20.3
## 19
                UK
                        1.3
                               941
                                      285
                                           10.3
## 20
                 US
                                      199
                                           22.1
                        1.2
                               926
## 21 West Germany
                        2.7
                               861
                                      172 36.7
```

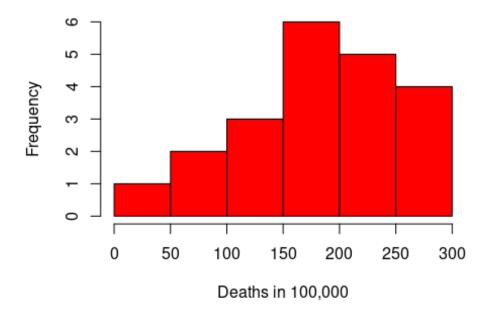
IID Data

Using background knowledge, each pair (X_i, Y_i) has to be drawn from the same distribution independently of all other pairs. Even though this is a small dataset, it appears to be independent due to each observation being a different country and the data also appears to

be identically distributed as will be shown in the plots below. In this case, There are no apparent violates of independents, some examples being clustering of data, in geographical regions, school cohorts, or families, strategical interaction, like competition among sellers or imitation of a species, or autocorrelation were one time period may affect the next. This assumption for the data is meet and thus far, the Wilcoxon Ranked-Summed Test appears to be a viable test.

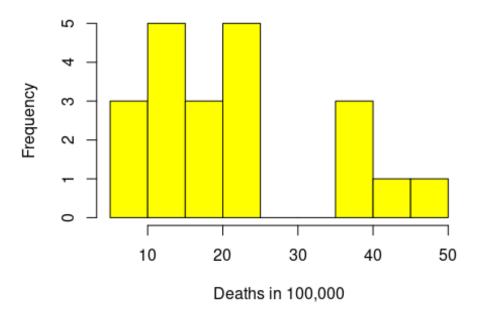
For the data visualization, two histograms of heart deaths and liver deaths were made in the plots below.

Histogram for Heart Deaths



```
hist(wine$liver,
    main="Histogram for Liver Deaths",
    xlab="Deaths in 100,000",
    col="yellow")
```

Histogram for Liver Deaths



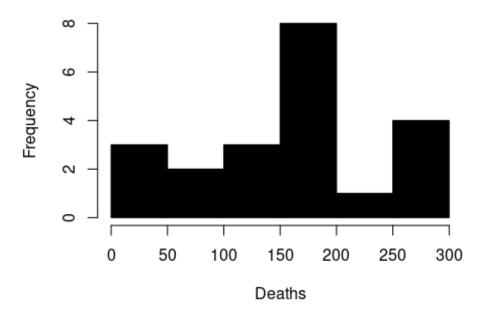
The Distribution of the difference (X - Y) is the Same Around Some Mean

Using the data visualization below, we have taken the difference of Heart and Liver deaths over the 21 different observations and take the difference of their means (162) as the point for the data to be symmetrical around. The data below shows that even with this small dataset it appears that the data meets this assumption being symmetrical around the mean of 162.

In conclusion, all of the assumptions have been met for this test and it appears to be a viable test to use for this dataset.

```
hist(wine$difference,
    main="Histogram for Heart - Liver Deaths",
    xlab="Deaths",
    col="black")
```

Histogram for Heart - Liver Deaths



The test was ran below to see what the results might be.

```
wilcox.test(wine$heart, wine$liver, paired=TRUE)
##
## Wilcoxon signed rank exact test
##
## data: wine$heart and wine$liver
## V = 231, p-value = 9.537e-07
## alternative hypothesis: true location shift is not equal to 0
```

1.3.4 Attitudes Towards Religion

QUESTION:The file datasets/GSS_religion is a subset of data from the 2004 General Social Survey (GSS). The variables prottemp and cathtemp are measurements of how a respondent feels towards protestants and towards Catholics, respectively. The GSS questions are phrased as follows: I'd like to get your feelings toward groups that are in the news these days. I will use something we call the feeling thermometer, and here is how it works: I'll read the names of a group and I'd like you to rate that group using the feeling thermometer. Ratings between 50 degrees and 100 degrees mean that you feel favorable and warm toward the group. Ratings between 0 degrees and 50 degrees mean that you don't feel favorable toward the group and that you don't care too much for that group. If we come to a group whose name you Don't recognize, you don't need to rate that group. Just tell me and we'll move on to the next one. If you do recognize the name, but you don't feel particularly warm or cold toward the group, you would rate the group at the 50 degree

mark. How would you rate this group using the thermometer? You would like to test whether the US population feels more positive towards Protestants or towards Catholics. List all assumptions for a paired t-test. Then evaluate each assumption, presenting evidence based on your background knowledge, visualizations, and numerical summaries.

Solution

Test Assumptions Paired t-Test:

- 1. Metric Scale
- 2. IID Data
- 3. No major deviations from normality, considering the sample size.

Null Hypothesis: The expectation of *X* equals the expectation of *Y*.

Metric Scale

Using background information, the t-test is not valid for variables which only have an ordinal structure. In this case, the feeling thermometer used to determines ones feelings towards Catholics or Protestants would fall under the Likert Scale and also be considered of ordinal structure. Therefore, the test would fail under this assumption. A summary of the given data is shown below as supporting evidence.

```
library(readr)
GSS <- read csv("GSS religion.csv")</pre>
## New names:
## * `` -> ...1
## Rows: 802 Columns: 5
## — Column specification
## Delimiter: "."
## dbl (5): ...1, year, id, prottemp, cathtemp
##
## Use `spec()` to retrieve the full column specification for this data.
## I Specify the column types or set `show col types = FALSE` to quiet this
message.
summary(GSS)
##
                       year
                                       id
                                                    prottemp
                   Min. :2004
                                 Min.
## Min.
        : 1.0
                                      :
                                            4.0
                                                  Min. : 0.00
## 1st Qu.:201.2
                   1st Qu.:2004
                                 1st Qu.: 728.8
                                                  1st Qu.: 50.00
## Median :401.5
                   Median :2004
                                 Median :1373.5
                                                  Median : 60.00
## Mean :401.5
                   Mean :2004
                                 Mean :1381.9
                                                 Mean : 65.56
                   3rd Qu.:2004
##
   3rd Qu.:601.8
                                 3rd Qu.:2053.5
                                                  3rd Qu.: 85.00
## Max. :802.0
                   Max. :2004
                                 Max. :2808.0
                                                 Max. :100.00
```

```
## cathtemp
## Min. : 0.00
## 1st Qu.: 50.00
## Median : 60.00
## Mean : 63.16
## 3rd Qu.: 85.00
## Max. :100.00
```

IID Data

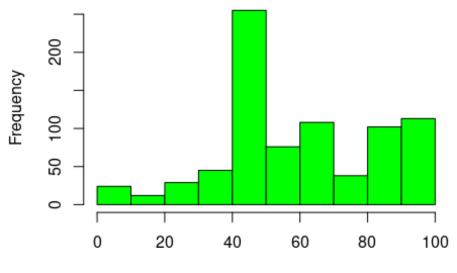
Making use of background knowledge, each pair of measurements (X_i, Y_i) is drawn from the same distribution, independently of all other pairs. This data appears to have paring, independence and identical distribution and does not violate. There are no apparent violates of independents, some examples being clustering of data, in geographical regions, school cohorts, or families, strategical interaction, like competition among sellers or imitation of a species, or autocorrelation were one time period may affect the next. The data also appears to be identically distributed as will be shown in the plots below. This assumption for the data is meet, but as stated previously, the Paired t-Test would not be a wise test to use for an ordinal scale statistical analysis.

No Major Deviations from Noramlity, Considering the Sample Size

Using background knowledge the t-test is invalid for highly skewed distributions when sample size is larger than 30. It may also be invalid for very highly skewed distributions at higher sample sizes. This does not appear to be the case as shown in the graphs below. This assumption for the data is meet, but as stated previously, the Paired t-Test would not be a wise test to use for an ordinal scale statistical analysis.

```
hist(GSS$cathtemp,
    main="Histogram for Temperature Measurments towards Catholics",
    xlab="Temp Measurement in Degrees",
    col="green")
```

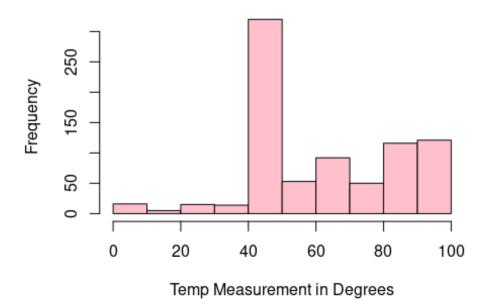
istogram for Temperature Measurments towards Catl



Temp Measurement in Degrees

```
hist(GSS$prottemp,
    main="Histogram for Temperature Measurments towards Protestant",
    xlab="Temp Measurement in Degrees",
    col="pink")
```

stogram for Temperature Measurments towards Prot



A Paired T-Test was run out of curiosity for the results.

```
t.test(GSS$prottemp, GSS$cathtemp, paired=TRUE)

##

## Paired t-test

##

## data: GSS$prottemp and GSS$cathtemp

## t = 2.9249, df = 801, p-value = 0.003543

## alternative hypothesis: true difference in means is not equal to 0

## 95 percent confidence interval:

## 0.7902444 4.0152419

## sample estimates:

## mean of the differences

## # 2.402743
```

In conclusion, through our analysis of the different scenarios where hypothesis tests could be run, the World Happiness statistical test would not be best evaluated with a Two-Sample T-Test, the Legislators problem would not be best evaluated with a hypothesis of comparisons version of the Wilcoxon Rank-Sum Test, the Wine and Health problem does fit all the assumptions for a Wilcoxon Signed-Rank Test and finally the Attitudes towards Religions problem does not fit the assumptions for a Paired T-Test.